

Application of a Passive Velocity Field Controller on an underactuated quadcopter

by

Jonas Brami

Submitted in partial fulfilment of the requirements for the MSc Degree in
Computing of Imperial College London

August 31st 2022

Contents

1	Introduction	2	4	Implementation	9
2	Background and Literature Review	2	4.1	Simplistic Python implementation	9
2.1	Placing sensors using UAVs	2	4.2	Full Sensor Placement pipeline in ROS/Gazebo/Pixhawk 4	9
2.2	Current State of the art for UAM	2	4.2.1	Velocity Field ROS Node	10
2.3	Velocity field path-planning for single and multiple unmanned aerial vehicles	3	4.2.2	PVFC ROS Node	10
3	Design and Theory	4	4.2.3	PCL Object Segmentation Node	10
3.1	Designed velocity Field for planning task	4	4.2.4	Grasping arm Gazebo-ROS plugin	10
3.1.1	Sink field for reaching the target	5	5	Results, Evaluation and Experiments	11
3.1.2	Obstacle repulsive field	5	5.1	Compensation for drag	11
3.1.3	Spherical field to maintain desired force	5	5.1.1	Experience without drag compensation	11
3.1.4	Circular field for contour following	5	5.1.2	Experience with drag compensation	12
3.2	Quadcopter modeling	6	5.2	No drag forces	12
3.2.1	Platform	6	5.3	No drag forces with force wrench	13
3.2.2	Translational dynamics	6	5.4	Circular Field	13
3.3	Passive Velocity Field Control of Mechanical Manipulators	7	5.4.1	\bar{E} study	13
3.3.1	Velocity fields for planning	7	5.4.2	γ study	14
3.3.2	Passivity	7	5.4.3	force compensation study	14
3.3.3	Augmented dynamics	8	5.4.4	World with Wrench	15
3.3.4	Augmented velocity field	8	5.5	Potential sink Field	16
3.3.5	PVFC Control law	8	5.5.1	\bar{E} study	18
3.4	Compensation terms	9	5.5.2	force compensation study	19
			5.6	Sensor placement experiment	20
			6	Conclusion, Future Work	22

1. Introduction

The problem we aimed to solve during this project is the placement of a sensor on a specific target point on a surface using a fixed manipulator arm mounted on the top of an unmanned quadcopter.

A quacopter is an underactuated helicopter with four rotors. A robot is said to be underactuated when arbitrary configurations cannot be realized.

In the last ten years, research about UAV controls accelerated drastically with many applications in the civilian industry in a variety of areas.

Monitoring and sensing tasks are traditionally operated by human but can be complicated (require expert, highly trained technicians), expensive, and dangerous for the human operator (when the point of interest is hard to reach, the human manipulator may need special training and equipment to reach the point of interest). For example, big structures like bridges need to undergo regular inspections to ensure there are no cracks or other signs of structural fatigue.

Using UAVs for such tasks would not only reduce cost of maintenance of those structures, but also increase the security of both the human manipulator and the civilians using it.

Sensor placement on surfaces using UAVs is an active field of research and we will propose a solution based on velocity fields.

In this project we present an application of the Passive Velocity Field controller (PVFC) using Velocity field derived from the gradient of a potential or a shaping function; integrated with a depth camera for active obstacle avoidance and a grasping arm for sensor placement. We also provide an analysis of the controller behavior under multiple types of fields and controller parameters.

This project was done in 2 steps: The first one was the implementation of a Passive Velocity Field controller with simple quadcopter dynamics and physics on Python. The simplicity of this simulation has allowed us to easily debug the controller, verify that our implementation is behaving as expected, and get a high level understanding of the parameters of this controller. The second step was implementing the full Sensor Placement pipeline using ROS/Pixhawk 4/Gazebo. Robot Operating System is a platform to build robot application where task specific nodes interact together based on subscribing and advertising to topics. Gazebo is a simulator providing real world physics, a variety of plugins that we used to implement a grasping arm to simulate a Sensor Placement task. Pixhawk 4 is an open source autopilot software integrated

with ROS to provide seamless communication between our ROS controller and the quadcopter actuators. Those implementations will be further detailed in section 4.

This work would not have been possible without the initial implementations and huge help of my Project supervisor Brett Stephens !

2. Background and Literature Review

2.1. Placing sensors using UAVs

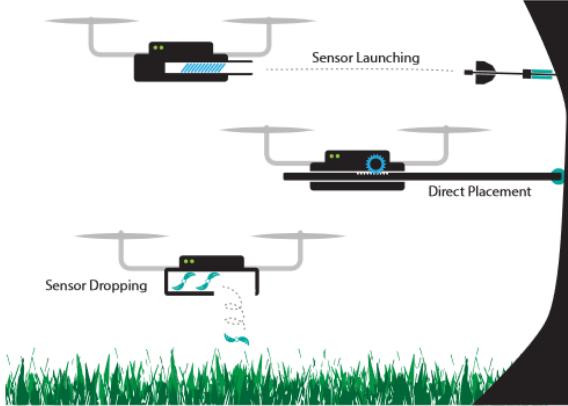
Diverse ways of placing sensors using UAVs have been explored in the past, including but not limited to:

- Direct Placement: Using a fixed arm manipulator on an UAV, we use the thrust of the UAV to provide enough pressure on the tip of the arm to place the sensor on the target point.
- Sensor Launching [2]: Using the energy stored in a spring, the UAV ejects the sensor at the desired velocity to reach and attach to the target (Unmanned Aerial Sensor Placement for Cluttered Environments). This strategy is very useful when it is not physically possible for a mounted arm to reach the target, however, it suffers from small payload capacity.
- Drop from flight: We simply drop the sensor above the target point. When target accuracy is not a priority and we are aiming at a non-vertical surface and there is no occlusion above the target, this sensor placement strategy is the most effective.

The characteristics of each one of mentioned methods are shown in figure 1. We decided to go through with the Direct Placement strategy because despite its simplicity, it provides good accuracy and is able to place a large variety of payloads.

2.2. Current State of the art for UAM

There exists 2 main approaches for controls of unmanned aerial manipulators: The first one is the centralized approach where we consider the manipulator and the UAV as a whole; whereas in the decentralized approach, the manipulator controls and UAV control are independent problems. In the case of the Sensor placement with a quadcopter, we use the centralized approach because the arm has no degree of freedom and the force exerted by the tip is coming from the thrust of the UAV. The centralized approach is often built on top of a model-based full state control loop optimized with LQR



	Direct [7]	Drop [2]	Launch ⁱ
Accuracy	$\pm 0.025 \text{ m}$	$\pm 4 \text{ m}$	$\pm 0.1 \text{ m}$
Safety distance	0 m	>10 m	4 m
Payload	1.85 kg	10 kg ⁱⁱ	0.65 kg
Sensor number	single	multiple	expandable

Figure 1: Different types of sensor placement from [2]

(Linear-quadratic regulator) around some desired state. In [6], the author present the current state of the research for UAMs. An UAM can be divided into 4 elements: the UAV floating base (in our case, a quadcopter), the robotic arm, a sensor/gripper attached to the end of the arm (in our case, a sensor will be attached to the end of the arm), diverse sensors on UAV to handle perception (the depth camera). While the state of the art approaches for UAV controllers are based on minimizing a state trajectory error, the planning strategy we will study next is based on velocity fields.

2.3. Velocity field path-planning for single and multiple unmanned aerial vehicles

In [2], the author presents a path-planning technique based on velocity fields generated from potentials solution of Laplace’s equation. Two different types of solution to potential V for the Laplace

$$\begin{aligned} \nabla^2 V &= 0 \\ \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} &= 0 \end{aligned} \quad (1)$$

equation are presented in this paper: Type 1 are irrotational solutions to generate sink and source fields and Type 2 solutions are used to build solenoidal fields.

$$V_1 = Q_1 \ln((x_1 - \tilde{x}_1)^2 + (x_2 - \tilde{x}_2)^2) \quad (2)$$

$$V_2 = Q_2 \arctan\left(\frac{(x_2 - \tilde{x}_2)}{(x_1 - \tilde{x}_1)}\right) \quad (3)$$

where (x_1, x_2) is the position of the UAV, $(\tilde{x}_1, \tilde{x}_2)$ is the position of the obstacle; V_1 and V_2 are respectively type 1 solution (source field) and type 2 solution (vortex field).

The author justifies the use of Laplace solution for building the velocity field for multiple reasons:

- The use of Laplace solution for potential guarantees the uniqueness of the minimum in the field. Specifically, the use of vortex function built from shaping function to circle around obstacle will ensure that only the goal point will be a minimum of the field and that the UAV will not get stuck at some local minimum. As the author states, we can do an analogy to a famous strategy to find the exit of a maze: by keeping a hand on a wall of the maze and walking while always touching the wall, we are ensured to find the end of the maze. This is far from being an optimal solution, however, it can guarantee that the goal will be reached. As a result, those solenoidal fields based on vortex function also provide active collision avoidance.
- Scalar shaping functions are at the base of these methodology because by crafting them to match the shape of the obstacles, we are able to generate corresponding vortex or repulsive functions for obstacles of any shape. Since those functions are defined for each obstacle, it would be easy to reevaluate the field after addition or removal of an obstacle.
- Finally, irrotational solutions of the Laplace equation allow us to enforce an exclusion radius around obstacles (source field) and to direct the UAV in direction of the target point (sink field). The exclusion radius is encoded using the amplitude Q_1 of the irrotational field.

We can leverage these both types of potentials to derive a velocity field that will guide the UAV to the contact point without colliding with the surface. For example, we could define the exclusion radius to be the distance between the centre of mass (CoM) of the quadcopter and its most distant part on the quadcopter.

We will present the field we previously described with illustrations. The field in figure 2 was drawn by computing the gradient of V_1 with $(\tilde{x}_1, \tilde{x}_2) = (0, 0)$.

The field in figure 3 is a sink field at $(0, 1)$, it is similar to the source field in figure 2 but with opposite sign.

The field in figure 4 has been generated by computing the gradient of the shaping function of a

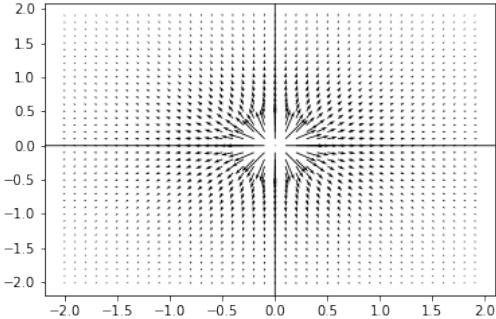


Figure 2: Simple Type 1 irrotational source

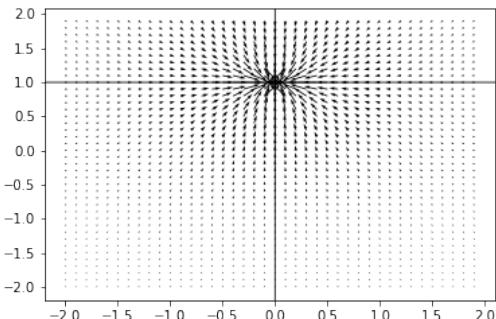


Figure 3: Simple Type 1 irrotational sink

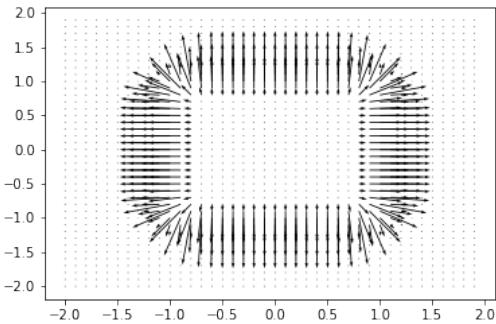


Figure 4: irrotational field from shaping function

superquadratic:

$$H = (x_1 - \tilde{x}_1)^n + (x_2 - \tilde{x}_2)^n \quad (4)$$

$$F = \frac{1}{1 + (\frac{1}{L} H^{\frac{1}{n}})^m} \quad (5)$$

As stated in [5], when $m \gg 1$, the edge of the shaping function gets thinner. Higher values of n result in more rectangular shapes whereas $n = 2$ describes the shaping function of an infinite cylinder.

Both these fields are type 1 irrotational solu-

tions of the Laplace equation.

By adding the irrotational sink from figure 3 and the irrotational field from shaping function in figure 4 we obtain a good representation in figure 5 of what the velocity field will look like when close to the target point.

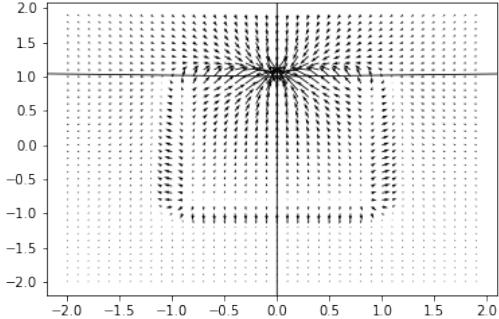


Figure 5: irrotational field from shaping function with sink

The shaping function is mainly used to generate a vortex field around an obstacle, as explained in the paper. It is given by:

$$v_2 = -\frac{\partial F}{\partial x_2} e_1 + \frac{\partial F}{\partial x_1} e_2 \quad (6)$$

Here, e_1 and e_2 are an orthonormal basis.

We can see in figure 6 an example of vortex field around a superquadric.

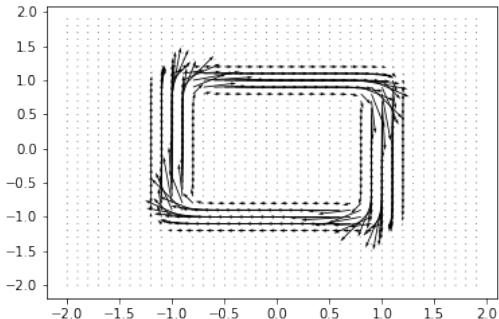


Figure 6: Solenoidal field from shaping function

3. Design and Theory

3.1. Designed velocity Field for planning task

A velocity field is a function taking as input a state, q and returns a 3-dimensional desired velocity vector (u, v, w) .

It describes a path (a function of position) as opposed to a trajectory (function of position and time).

3.1.1. Sink field for reaching the target

In [5], the author chose to apply a logarithmic function on the distance between the current position and the goal position as a potential for the sink field. However, we observed that using such a potential does not allow the robot to safely approach the goal point since when the distance approaches 0, the logarithmic function diverges. As a result, we decided to simply use the distance as a potential function. This will allow us to smoothly decrease the velocity of the UAV when approaching the desired goal point.

3.1.2. Obstacle repulsive field

In our current solution, because of the simplicity of the environment and the convexity of the obstacles, we are only using the type 1 solution described in [5], we only have a repulsive field normal to the surface of the obstacle.

3.1.3. Spherical field to maintain desired force

When contact has been made, we suppose that the surface static friction coefficient is high enough to maintain the contact. Since the arm has a fixed size and does not move, this section will describe a velocity field on the surface of a sphere around the target point with a radius defined by the distance between the CoM of the quadcopter and the tip of the arm.

First we need to compute the feasible position of the CoM to apply the desired force. We know that this position is unique because there is only one vertically stable pitch for a given desired force amplitude. The quadcopter needs to pitch to have a forward velocity because the quadcopter is underactuated.

We can generate the velocity field on the surface of the sphere to point on the tangent direction of the sphere in the direction of the stable pitch position. This field will have an amplitude proportional to the distance from this point. The planning strategy we described would also allow us to easily define a desirable range for the yaw angle depending on the type of sensor and on the friction coefficient of the target surface. Finally, we use a Passive Velocity Field Controller [4] to follow this field to minimize the loss of kinetic energy to the environment when interacting with the surface. Now we are going to describe how the spherical field is computed. Let us recall that the cartesian to spherical coordinate change of variable is defined as

$$r = \sqrt{x^2 + y^2 + z^2}$$

$$\theta = \arccos\left(\frac{z}{r}\right)$$

$$\phi = \begin{cases} \arctan\left(\frac{y}{x}\right), & \text{if } x > 0, \\ \arctan\left(\frac{y}{x}\right) + \pi, & \text{if } x < 0 \text{ and } y \geq 0, \\ \arctan\left(\frac{y}{x}\right) - \pi, & \text{if } x < 0 \text{ and } y < 0, \\ \pi/2, & \text{if } x = 0 \text{ and } y > 0, \\ -\pi/2, & \text{if } x = 0 \text{ and } y < 0, \\ \text{not defined}, & \text{if } x = 0 \text{ and } y = 0 \end{cases} \quad (7)$$

The jacobian defining the curvature of the sphere at each point for this transformation is

$$J = \begin{bmatrix} \sin(\theta) \cos(\phi) & \cos(\theta) \cos(\phi) & -\sin(\phi) \\ \sin(\theta) \sin(\phi) & \cos(\theta) \sin(\phi) & \cos(\phi) \\ \cos(\theta) & -\sin(\theta) & 0 \end{bmatrix} \quad (8)$$

Figure 7 represents an example of such a field where the red point is the optimal position to apply the pressure, the blue arrows are the velocity field vectors and the center of the sphere is the point where the force is applied

3.1.4. Circular field for contour following

This field is based on the methodology explained in [1]. We used it to build intuition, debug and analyze the controller. The author explains how to encode a contour \mathcal{C} into a desired velocity field v_d . The field is given by:

$$v_d(p) = l(\alpha \hat{t} + \|Q - p\| \hat{n}) \quad (9)$$

- $p \in \mathbb{R}_3$ is the current position
- Q is the closest point from p on \mathcal{C}
- $l, \alpha \in \mathbb{R}_{\geq 0}$ are scaling constants
- \hat{t} is a unitary tangent vector to \mathcal{C} at Q
- \hat{n} is a unitary normal vector to \mathcal{C} going from p to Q

From there it is straightforward how to implement a circular velocity field with a radius of 1 and centered at the origin in the following way:

$$Q = \frac{p}{\sqrt{p_x^2 + p_y^2}} \quad (10)$$

$$\theta = \arctan(Q_y, Q_x) \quad (11)$$

$$\hat{t} = (-\sin \theta, \cos \theta, 0) \quad (12)$$

$$\hat{n} = \frac{Q - p}{\|Q - p\|} \quad (13)$$

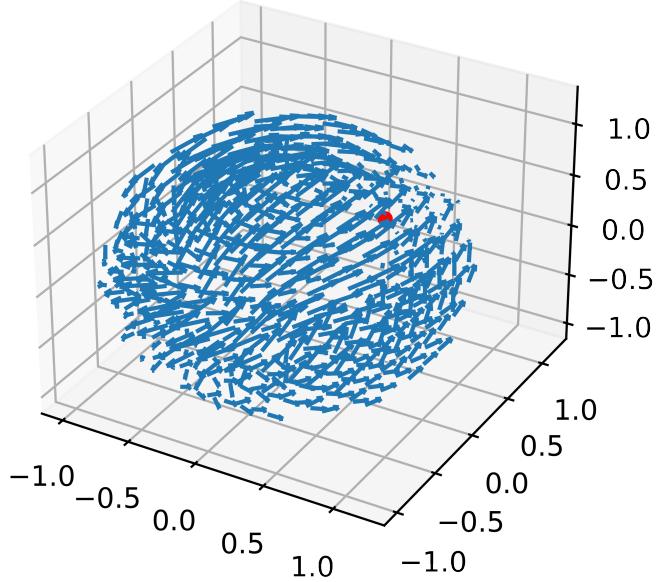


Figure 7: Spherical contact field

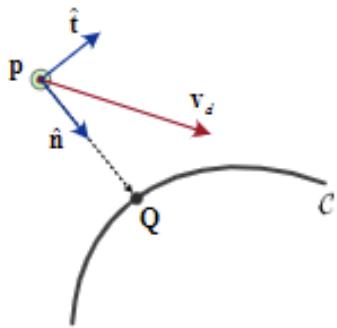


Figure 8: field construction from [1]

3.2. Quadcopter modeling

3.2.1. Platform

Similarly to the platform used in "An Aerial Parallel Manipulator with Shared Compliance", our system is composed of two subsystems: The underactuated quadrotor base (for which we have software in the loop integration given by PX4) and the fixed manipulator arm above the center of mass of the quad. This system is underactuated because in the base frame of this quad, the only thrust direction for the quadcopter is in the z axis in the frame of the base of the quad, the rotors cannot move relative to the base of the quad. Therefore, the IRIS

model control inputs are a quaternion vector and a thrust amplitude. However, the output of the passive controller for the non-augmented translational domain is a thrust vector $\Lambda \in \mathbb{R}_3$, therefore we will need to convert this desired thrust to the desired format. In addition to the fixed manipulator arm, a depth camera is mounted on the quad base. We use the depth camera model provided by Pixhawk 4 with IRIS that simulates an intel realsense r200. We use the transform provided in the PX4 obstacle avoidance package to transform from the frame of the camera to the frame of the quadcopter base, and we use the PX4 odometry information to transform from the base to the ground gazebo frame.

3.2.2. Translational dynamics

The dynamics that we take into account in our passive control strategy are only in the translational domain. The passive velocity field controller output is a thrust vector and PX4 translates this desired thrust into actual angular velocities for each one of the rotors $\Omega = (\bar{\omega}_1, \bar{\omega}_2, \bar{\omega}_3, \bar{\omega}_4)$. PVFC only acts on the translational level and not at the rotational level and has no knowledge or control about the speed of those rotors and therefore the passivity of this controller is only at the translational level. This quadcopter is an underactuated sys-

tem because for a given translational velocity, only a subset of attitudes are feasible. As a result, it is not possible to control all 6 degrees of freedom independantly (3 translational, 3 rotational).

3.3. Passive Velocity Field Control of Mechanical Manipulators

In [4], the author explains the advantages of encoding a contour following task using velocity fields. They later present the passive velocity field controller whose objective is to "maintain an energetically passive relationship between the manipulator under closed loop control and its physical environment, while causing the manipulator to perform the desired task." We will explain each one of those arguments and relate them to our sensor placement task.

3.3.1. Velocity fields for planning

The classical approach to do planning is to encode the task into a timed trajectory $Q : \mathbb{R}_{\geq 0} \rightarrow G$ where G is the n-dimensional configuration manifold for the manipulator and uses a controller to minimize the state trajectory error. Using this strategy, the objective of the controller is to minimize the deviation between $q(t)$ and $Q(t)$ where $q : \mathbb{R}_{\geq 0} \rightarrow G$ is the actual coordinate representation of the manipulator. This strategy could be fine if the manipulator was able to never deviate from the timed trajectory defined by Q . However, if deviation occurs for example, when external forces are applied to the robot, a side effect of this minimization strategy called radial reduction can occur.

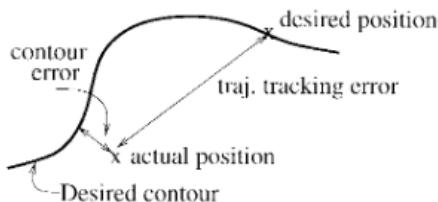


Figure 9: radial reduction from [4]

The author argues that if following the path of the desired trajectory is more important than the timing in which the manipulator follows this trajectory, a strategy based on velocity field is more appropriate because the velocity of the manipulator will only depend on its current position and will be time invariant. For the sensor placement task, using a timed trajectory strategy with deviation minimization to reach the contact point may lead the UAV to collide with an obstacle. With our strategy based on potential velocity field, the UAV will not try to shortcut the desired path in

case of deviation. The author defines an α error such that:

$$e_\alpha = \dot{q} - \alpha V \quad (14)$$

One of the most important priorities of PVFC is that when no external forces are applied on the robot, there is a positive α such that

$$\lim_{t \rightarrow \infty} e_\alpha = 0 \quad (15)$$

In other words, PVFC does not seek to exactly match the desired velocity field but just an α scaled version of it. The α we are going to converge to is a function of the energy in the augmented system and the energy in the desired velocity field.

3.3.2. Passivity

The controller presented in this paper is based on energy control theory and allows energy transfer between the environement and the augmented system. Passivity allows dissipation from the energy input to the system into the augmented system. To present this concept, the author first defines the notion of a passive dynamic system:

A dynamic system with input $u \in U$ and output $y \in Y$ is passive with respect to the supply rate $s : U \times Y \rightarrow \mathbb{R}$, if for any $u : \mathbb{R}_{\geq 0} \rightarrow U$ and for any $t \geq 0$ the following relation is satisfied:

$$\exists c \in \mathbb{R}$$

$$\int_0^t s(u(\tau), y(\tau)) d\tau \geq -c^2 \quad (16)$$

Let us remember that the work W and power P of a force F on a point mass object with velocity v are defined as

$$P = F \cdot v \quad (17)$$

$$W = \int_0^t P dt \quad (18)$$

Therefore the supply rate $s(\tau_{tot}, \dot{q}) = \tau_{tot}^T \dot{q}$ can be seen as the total mechanical power input. Here the input τ_{tot} is the total force exerted on the manipulator and the output \dot{q} is the velocity of the manipulator.

When considering a feedback system interacting with the environement shown in figure 10, we can decompose $\tau_{tot} = \tau_e + \tau$ (where τ and τ_e are respectively the forces generated by the actuators and the external forces, for example the contact force when touching a surface), we can derive the power generated by external forces as $s(\tau_e \dot{q}) = \tau_e^T \dot{q}$. As explained in the paper, a system defined by this supply rate is not passive because obstacles may bring the manipulator to a complete stop for an unbounded amount of time and this loss

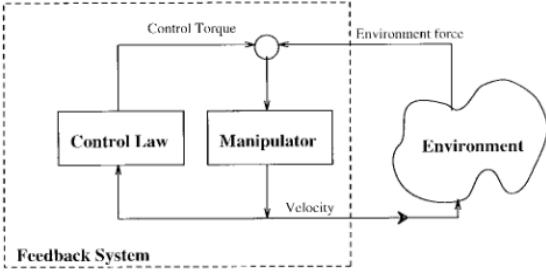


Figure 10: PVFC loop [4]

of kinetic energy cannot be bounded. As a result, the passivity relation

$$\int_0^t \tau_e^T \dot{q} d\tau \geq -c^2 \quad (19)$$

is not valid here because the l.h.s represents the total amount of energy lost to the environment and, as stated before, it cannot be bounded. This issue motivates the introduction of an augmented system: a fictitious flywheel is added to the system that acts as an energy storage element. The dimensionality of the manifold is then increased by one to include the state of the flywheel and this augmented state will be noted as

$$\bar{q} = [q, q_{\text{fly}}] \quad (20)$$

$$\bar{V} = [V, V_{\text{fly}}] \quad (21)$$

Using such passive and dissipative systems enables safe interaction between the robot and its environment since the total kinetical energy of the system is bounded by the system initial kinetic energy and energy input from the environment.

3.3.3. Augmented dynamics

Let us now describe the dynamics of the augmented system

$$\bar{M}(\bar{q}) \ddot{\bar{q}} + \bar{C}(\bar{q}, \dot{\bar{q}}) \dot{\bar{q}} = \bar{\tau} + \bar{\tau}_e \quad (22)$$

The mass matrix of the augmented system is defined such that:

$$\bar{M}(q) = \begin{bmatrix} M(q) & 0 \\ 0 & m_{\text{fly}} \end{bmatrix} \quad (23)$$

$$M(q) = \begin{bmatrix} m_b & 0 & 0 \\ 0 & m_b & 0 \\ 0 & 0 & m_b \end{bmatrix} \quad (24)$$

The Coriolis Matrix of the augmented system is defined such that:

$$\bar{C}(\bar{q}, \dot{\bar{q}}) = \begin{bmatrix} C(q, \dot{q}) & 0 \\ 0 & 0 \end{bmatrix} \quad (25)$$

C is built using the Levi–Civita connection described in [3].

3.3.4. Augmented velocity field

Now let us define the augmented field for the flywheel. The motivation for introducing an augmented system is to allow energy transfer between the quadcopter actuators and the flywheel such that the total kinetic energy in the system remains constant. This property is enforced in the definition of the desired velocity field.

First let us define \bar{E} to be the total desired energy of the augmented system following the desired velocity field. \bar{E} can be written as a sum of the flywheel desired kinetic energy K_{fly_d} and the quad desired kinetic energy K_{quad_d} :

$$\bar{E} = K_{\text{fly}_d} + K_{\text{quad}_d} \quad (26)$$

Given a desired velocity field V we have:

$$K_{\text{quad}_d}(q) = V(q)^T \frac{1}{2} M(q) V(q) \quad (27)$$

Since

$$K_{\text{fly}_d} = \frac{1}{2} m_{\text{fly}} V_{\text{fly}}^2 \quad (28)$$

We can derive V_{fly} in function of $K_{\text{quad}_d}(q)$ and \bar{E} :

$$V_{\text{fly}}(q) = \sqrt{\frac{2}{m_{\text{fly}}} (\bar{E} - K_{\text{quad}_d}(q))} \quad (29)$$

3.3.5. PVFC Control law

To define the PVFC control law, the author defines the following quantities

$$\bar{p}(\bar{q}, \dot{\bar{q}}) = \bar{M}(\bar{q}) \dot{\bar{q}} \quad (30)$$

$$\bar{P}(\bar{q}) = \bar{M}(\bar{q}) \bar{V}(\bar{q}) \quad (31)$$

$$\bar{w}(\bar{q}, \dot{\bar{q}}) = \bar{M}(\bar{q}) \dot{\bar{V}} + \bar{C}(\bar{q}, \dot{\bar{q}}) \quad (32)$$

The equation 30 can be seen as the actual momentum of the augmented system, the equation 31 can be seen as the desired momentum of the augmented system and 32 is the desired dynamics (desired force applied on) of the augmented system.

From there the author derived the two terms of the coupling control law:

$$\bar{\tau}_c = \frac{1}{2\bar{E}} (\bar{w} \bar{P}^T - \bar{P} \bar{w}^T) \dot{\bar{q}} \quad (33)$$

$$\bar{\tau}_f = \gamma (\bar{P} \bar{p}^T - \bar{p} \bar{P}^T) \dot{\bar{q}} \quad (34)$$

$$(35)$$

the $\bar{\tau}_f$ term is the feedback term, while $\bar{\tau}_c$ is the term enforcing passivity and allowing to dissipate external forces work into the quadcopter. The anti-symmetric structure of the matrices multiplying $\dot{\bar{q}}$ is key to proving that the derivative of the kinetic energy in the augmented system is:

$$\frac{d}{dt} k(\bar{q}, \dot{\bar{q}}) = \tau_e^T(t) \dot{q}(t) \quad (36)$$

This is done by introducing the concepts of compatibility between a metric defining an inner product and an affine connection. It is shown in [3] that the compatibility between the Levi-Civita connection with the metric defined by M has a direct link between anti-symmetry of the matrices in the control coupling law, passivity and energy conservation.

From equations 36 and 16, the passivity of the system with respect to external forces is straightforward.

3.4. Compensation terms

When using PVFC with the quadcopter dynamics, it is important to model the effect of drag and gravity on the robot to be able to compensate for them. If those forces are not taken into account, the robot total mechanical energy will decrease until it arrives to a complete stop. Therefore, to ensure the robot will continue to follow the desired velocity field, we have to introduce compensation terms for gravity and air drag. For simplicity, we chose to model drag as a linear function of the velocity. This worked for our proof of concept but this method shows its limits when running the simulation for a greater amount of time because not only drag is not exactly proportional to the speed, but we have no straightforward way of estimating those drag coefficients. Setting them too high will make our control output diverge but setting it too low will make the quad stop following the desired velocity field.

4. Implementation

As was stated in the introduction, we have two main implementations:

4.1. Simplistic Python implementation

The Python implementation uses simplistic quadcopter dynamics only defined by:

- Quad mass: m_b
- Moments of inertia: I_{xx}, I_{yy}, I_{zz}
- drag coefficient: A_x, A_y, A_z
- PD attitude gains: $K_{\phi_p}, K_{\phi_d}, K_{\psi_p}, K_{\psi_d}, K_{\theta_p}, K_{\theta_d}$. ϕ is the roll angle, θ is the pitch angle and ψ is the yaw angle.

In this subsection, we will consider $q \in \mathbb{R}_6$ to be the rotational and translational states: $q(t) = (x(t), y(t), z(t), \phi(t), \theta(t), \psi(t))$ and $\dot{q}(t) = \frac{dq}{dt} = (\dot{x}(t), \dot{y}(t), \dot{z}(t), \dot{\phi}(t), \dot{\theta}(t), \dot{\psi}(t))$

It should be noted that the drag coefficients here are used both by the PVFC controller and

the dynamics of our system. In opposition to the Gazebo implementation, the drag experienced by the quad in the python implementation is also defined by those drag coefficients. When running in Gazebo, the IRIS model has a real world drag that we do not control.

We use ODEint to evolve the state (q, \dot{q}, \ddot{q}) of the system by doing the following on each time step:

- First we compute the current Mass Matrix M , Coriolis Matrix C , Control Matrix B , gravity Matrix G . Since the mass of the system is constant, the translational parts of M and G are constants. Therefore, the only changes we have to take into account are for C and B .
- Then we pass to the PVFC controller those dynamics together with the desired velocity field and compute a desired thrust vector.
- Given a desired cartesian thrust vector $\tau_{desired} \in \mathbb{R}_3$, we can decompose it into euler coordinate $(\alpha, \tau_{\phi_{desired}}, \tau_{\theta_{desired}}, \tau_{\psi_{desired}})$.
- The quad uses a simple attitude PD to compute the final thrust $\tau(t) = (\tau_{\phi}(t), \tau_{\theta}(t), \tau_{\psi}(t))$ in euler coordinate :

$$\begin{aligned}\tau_{\phi}(t) &= I_{xx}(K_{\phi_d}(\dot{\phi}_{desired} - \dot{\phi}(t)) + K_{\phi_p}(\phi_{desired} - \phi(t))) \\ \tau_{\theta}(t) &= I_{yy}(K_{\theta_d}(\dot{\theta}_{desired} - \dot{\theta}(t)) + K_{\theta_p}(\theta_{desired} - \theta(t))) \\ \tau_{\psi}(t) &= I_{zz}(K_{\psi_d}(\dot{\psi}_{desired} - \dot{\psi}(t)) + K_{\psi_p}(\psi_{desired} - \psi(t)))\end{aligned}\quad (37)$$

- By multiplying the final euler thrust by the control matrix, we can obtain the new state of the quadcopter

It is important to notice that the big difference between the python implementation and the ROS/Gazebo/PX4 that we will later detail is that we do not explicitly use a PD attitude gains in the latter. The PX4 firmware of the IRIS model has its own low level attitude controller.

The desired velocity fields are computed using Sympy (A Python library for symbolic calculations) for easy field and field gradient computation. Since most fields we used are derived from potential functions, we can easily obtain the field and field jacobian required by PVFC by symbolically differentiating their potentials or shaping functions.

4.2. Full Sensor Placement pipeline in ROS/Gazebo/Pixhawk 4

In this implementation, we are using a real world quadrotor called IRIS quad provided in the Pixhawk 4 SITL package. The dynamics are evolved

and computed by Gazebo. The implementation is divided in 2 ROS Nodes, 1 ROS-PCL Node, 1 Gazebo-ROS plugin, and 1 Pixhawk 4/MAVROS node. A diagram of the implementation is shown in figure 11.

4.2.1. Velocity Field ROS Node

This node subscribes to the mavros odometry topic, computes the velocity field at the current position and publishes the desired field and field gradient. We implemented all the velocity field using the symbolic math library SymEngine so that all gradient computations from potential or shaping function would be done automatically. In addition, this node is implementing a state machine such that in each state, a specific field is being used. Specifically, the first state gives a sink to get altitude, the second state is a sink field to approach the target, the third state represents the contact phase with the wall (the node subscribes to a topic called "grasping" to know if the grasping arm is currently activated). It starts when an engagement signal is received from the grasping arm and it finishes when a disengagement signal is received from the grasping arm. The last state is to get away from the wall and land, we use a sink field to implement it. We implemented an obstacle avoidance system for generic superquadratic obstacles, upon obstacle detection, we compute the avoidance field for this obstacle from the appropriate shaping function, an irrotational field is generated to avoid the obstacle. This node subscribes to an obstacle topic to know when new obstacles have been detected.

4.2.2. PVFC ROS Node

This node subscribes to the desired velocity field and to the MAVROS odometry and publishes a thrust vector on the MAVROS attitude topic computed by the PVFC controller. The output of the passive velocity field controller is a 4-dimensional vector containing the desired thrust to be applied in each direction (x, y, z, fly) including the thrust to be applied on the fictitious flywheel. However, the input control for the IRIS model needs a desired attitude and thrust amplitude. Therefore, after obtaining the desired (cartesian) thrust vector from PVFC, we convert it to desired euler angles with desired amplitude ($\alpha, roll, pitch, yaw$). We can then convert this pose to quaternion and publish it to the attitude topic of the IRIS quad. It should be noted that the thrust amplitude expected by the IRIS attitude control is not in Newtons but is a scalar between 0 and 1. As a result, we had to experimentally calibrate a thrust slope and thrust intercept (affine transformation) to map the desired PVFC thrust amplitude to a scaled thrust amplitude.

4.2.3. PCL Object Segmentation Node

This node reuses the code of a PCL tutorial performing cylinder segmentation on point cloud data(cite). We added a ROS integration to the velocity field topic the position of the detected object and also we implemented the transforms from camera point of view to FCU (Flying control unit) frame, and from FCU frame to world frame. It works in the following way:

- Use a PCL passthrough filter to remove Nan datapoints and the scene background
- Use the PCL NormalEstimation class to estimate the normals of the cleaned pointcloud scene. This is done using KdTree based methods for increased robustness against noise in the measurements. KdTrees are data structures used in Computer Science that are very efficient for nearest neighbour search
- Perform plane model segmentation on the extracted normals using RANSAC and filter out the planar inliers
- After the last step, we should have a clean normals containing only cylinders normals, we can now use the SACSegmentationFromNormals class of PCL to extract the coefficient of the cylinder and its position in the frame of the camera
- If a cylinder was detected, we transform the position of the cylinder from the depth camera frame to the gazebo world frame and we publish it to the cylinder topic for the velocity field node to update the desired velocity field

4.2.4. Grasping arm Gazebo-ROS plugin

This node reuses the code of the vacuum arm of Gazebo, but it was modified so that could be "attached" to the moving IRIS model and fixed to a wall in Gazebo.

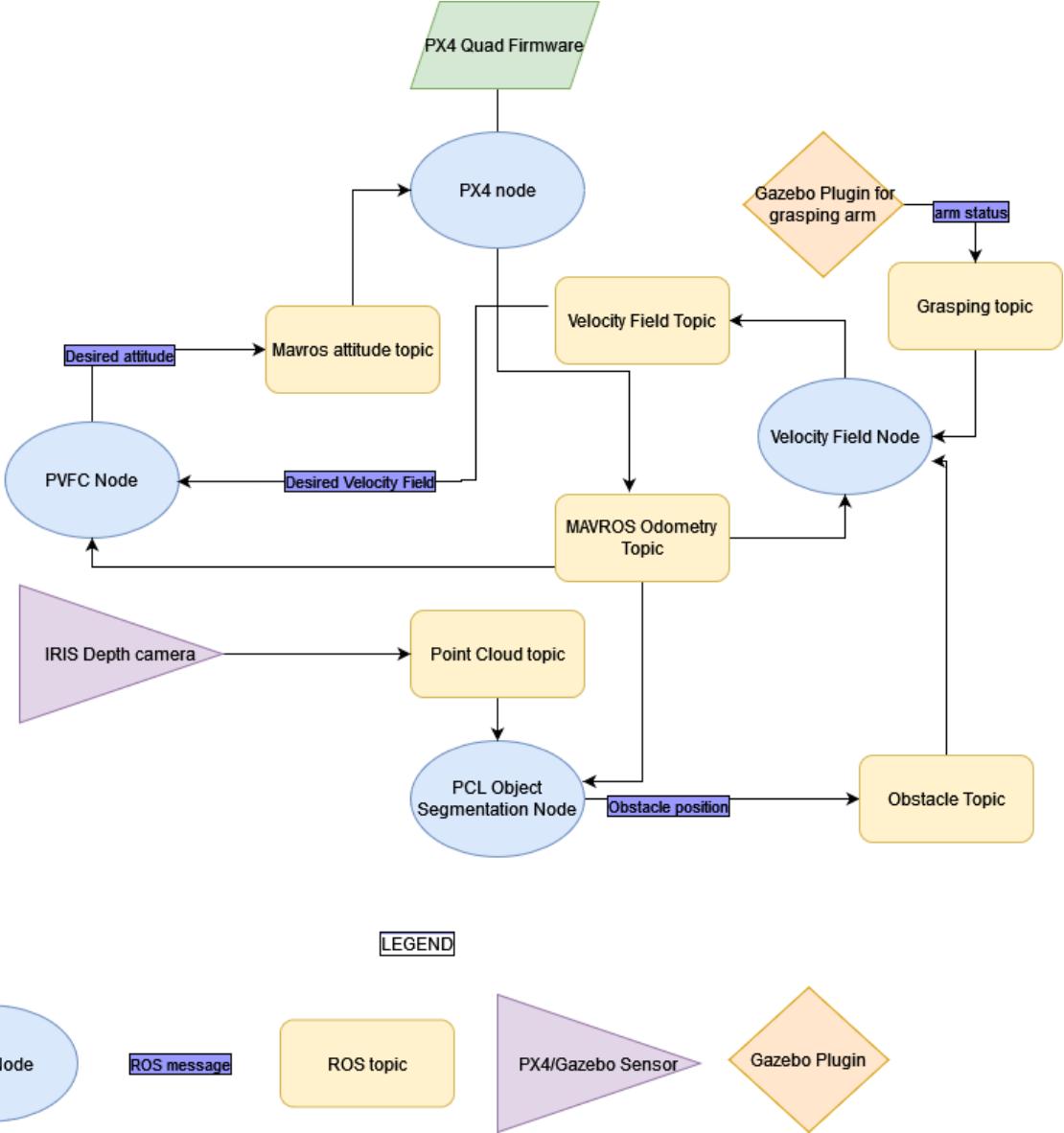


Figure 11: implementation diagram

5. Results, Evaluation and Experiments

In this section, we will discuss the results obtained in multiple conditions. Those data were recorded using ROSBag and were parsed using the ROSBag python module. ROSbag is a program included with RORS, it is used to store and replay the messages published on ROS topics by ROS node. We provide a jupyter notebook in the repository that facilitates drawing all the relevant graphs with a convenient way of storing all the parsed bags inside a pickle file.

5.1. Compensation for drag

In the first experiment, we will justify the need for an air drag compensation term. The velocity field we use in the circular velocity field is based on [5].

5.1.1. Experience without drag compensation

On the both of figure 12, we can see the trajectory of the quadcopter, the left scatter plot of the trajectory is colored according to the translational velocity of the quadcopter while the right scatter plot is colored according to the angular velocity of the fictitious flywheel. On both subplots, the quiver plot represents the desired velocity field. We can see that when we do not introduce a drag force compensation, the quad translational velocity goes to zero. This is explained by the fact by the quadcopter thrust given by PVFC has a too low amplitude to compensate the drag force and consequently the quad decelerates. The amplitude of the flywheel velocity is not affected by this drag because we defined a perfect no friction flywheel.

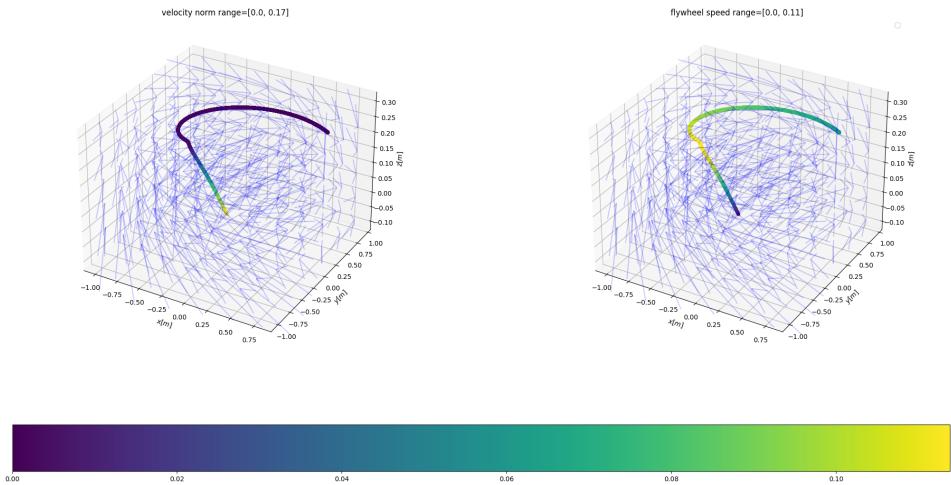


Figure 12: trajectory and mechanical energy without force compensation

These subplots are useful to observe how energy is being transferred between the fictitious flywheel and the quadcopter. We can see that as expected from equation 29, the faster the quad is going the slower the fictitious flywheel is spinning.

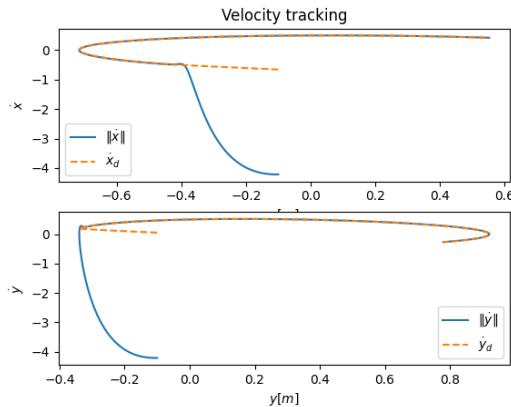


Figure 13: Trajectory tracking without force compensation

Despite the total stop, we can see from the figure 13 that the field is accurately followed.

5.1.2. Experience with drag compensation

This experiment is the same as the last one except that we add to the desired PVFC thrust output the compensation term $\tau_{comp} = C \cdot \dot{q}$ where C is current translational coriolis matrix and \dot{q} is the current translational velocity of the quadcopter. We can see in figure 14 that introducing this force compensation allows the quad to continue moving

despite drag forces. However, using such compensation slightly decreases the precision of the velocity field tracking (figure 15). It is not clear why this is happening.

5.2. No drag forces

In this second experiment, we remove the drag forces from the dynamics (we set the drag coefficients to 0). We can see in the figure 16 that when far away from the desired path, the translational speed of the quadcopter is high while the rotation speed of the flywheel is low. This is happening because of the way the velocity field is constructed in equation 9, the magnitude of the tangential component is constant but the magnitude of the normal component is proportional to the distance between the quad and the closest point in the circle. We can observe how energy is being traded between the quad and the flywheel when the quad approaches the desired path. It should also be noted that the desired path is exactly followed in opposition to the last experiment with drag compensation (see figure 17). We explained in section 3 that PVFC has interesting properties regarding the velocity tracking error (eq 14). In [4], the author explains that when no external forces are applied on the quadcopter, α should approach the square root of $\beta^2 = \frac{\text{augmented mechanical energy}}{\text{augmented desired mechanical energy}}$. In addition, when α approaches β , the α error should approach 0.

By design, the augmented desired mechanical energy of the system is always equal to \bar{E} , and we compute the augmented mechanical energy given by:

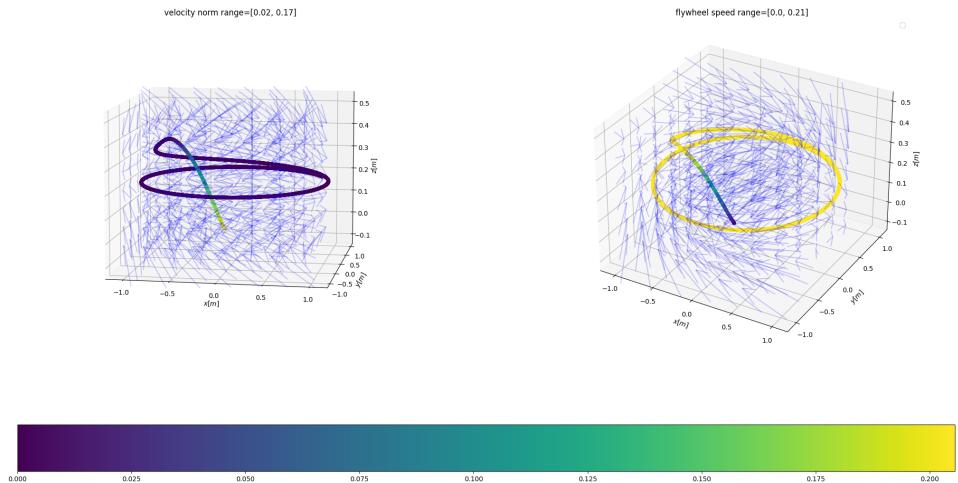


Figure 14: trajectory and mechanical energy with force compensation

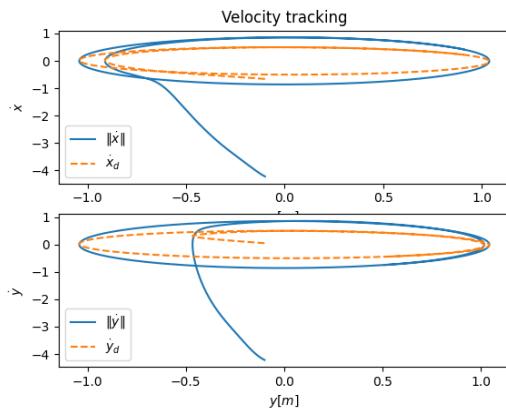


Figure 15: Trajectory tracking with force compensation

$$\frac{1}{2}m_b\|\dot{q}\|^2 + \frac{1}{2}m_{fly}\|\dot{q}_{fly}\|^2.$$

We successfully reproduced the results of [4] for the β error on a circular velocity field. We can see in figure 18 that β converges and the β error converges to 0.

5.3. No drag forces with force wrench

The third experiment is done in 3 phases: In the first one we let the quad follow the circular field for 120 seconds, then we apply an external force on the quad in the $-\hat{y}$ direction for 10 seconds, and finally we let the quad follow the desired field for 120 seconds. The passivity properties of PVFC are well shown in figure 19. We can see how the quadcopter is trading energy with the environment and

dissipating the work of the wrench inside the augmented system. This experiment also exemplifies well the advantage of using velocity field instead of a traditional trajectory following based controller: The radial reduction that could have occurred in figure 20 could have been a big issue in a task such as contour following where following the contour is more important than following a trajectory. In the contrary, figure 20 shows that when external forces are applied, we are able to go back to the desired circular path without radial reduction. In addition, we can observe what happens to the β error when wrench is applied: We can see in figure 21 that the β error converges to 0 before a wrench is applied, then during the second phase, we can see a spike for both β and β error when a wrench is applied. This is expected since the wrench increases mechanical energy in the system. We can see how PVFC dissipates the external force and makes the β error converge to 0 when no external force is applied in the last phase.

Now we are going to show experiments done on the Gazebo simulation. In the scatter trajectory plot that we will see in the following experiment, the color represents the velocity of the flywheel.

5.4. Circular Field

This subsection contains graphs and experiment with the circular field planner.

5.4.1. \bar{E} study

In this subsubsection, we try to gain intuition about the \bar{E} parameter of the controller with the circular velocity field. Let us remember that \bar{E} is the

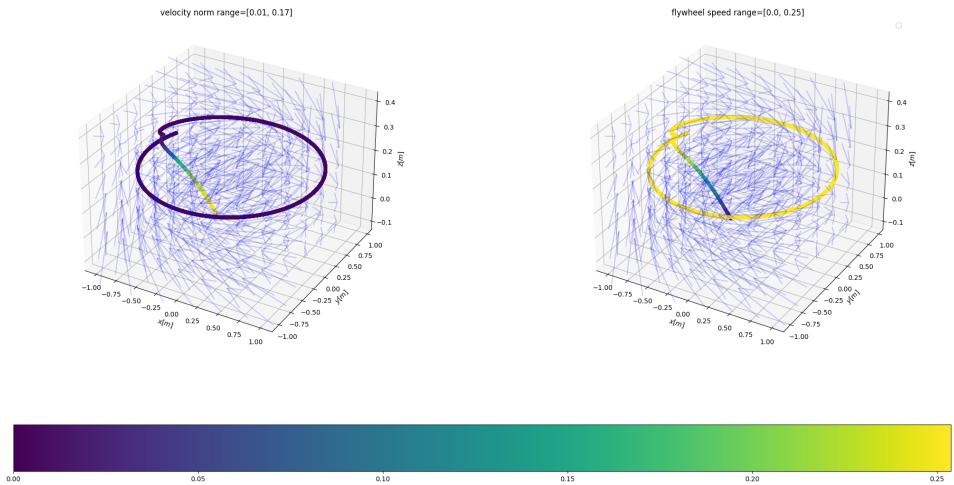


Figure 16: trajectory and mechanical energy without drag

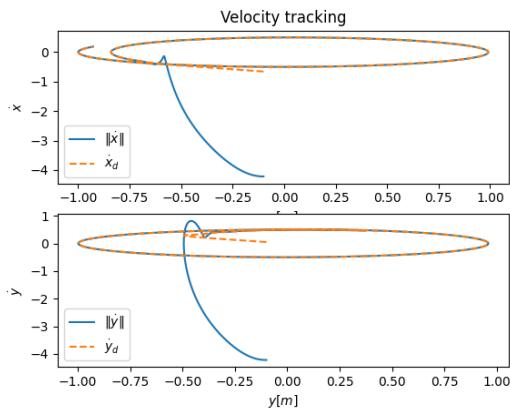


Figure 17: Trajectory tracking without drag

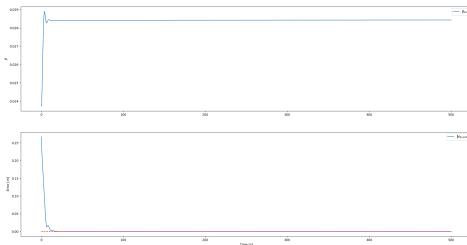


Figure 18: Beta error without drag

(desired) energy reservoir of the system such that the desired total mechanical of the system (meaning, the desired kinetic energy in the flywheel plus the desired kinetic energy coming from the desired translational velocity of the quadcopter). \bar{E} is used

in 2 places: The first is in the velocity field code where the flywheel velocity field is computed according to equation 29, the second one when computing τ_c in the coupling control law 33. We can see in figures 22 and 23 that the velocity of the quadcopter with the lowest \bar{E} is the highest. This is very counterintuitive since \bar{E} represents the total available mechanical energy in the desired velocity field.

5.4.2. γ study

The γ parameter of PVFC controls the amplitude of the feedback term of the PVFC control law 34. We would expect to follow the desired velocity field more accurately when γ is higher. As we can see in figure 24, the circles are drawn more accurately for $\gamma = 0.5$. When the field is not smooth enough, increasing gamma may cause instability because the desired attitude will change faster according to the direction of the desired velocity field and if those changes are too fast, the quad may turn over on its back and fall to the ground. This root cause of this problem is the underactuation of the quad and its lack of stability for high pitches. We can also see from figure 26 that the higher the γ the lower the β error. This is expected as higher gamma means faster convergence to the desired velocity field.

5.4.3. force compensation study

As we previously explained, the force compensation is essential when drag forces are in presence. It is important to remember that in the Python implementation, the dynamics of the drag forces are

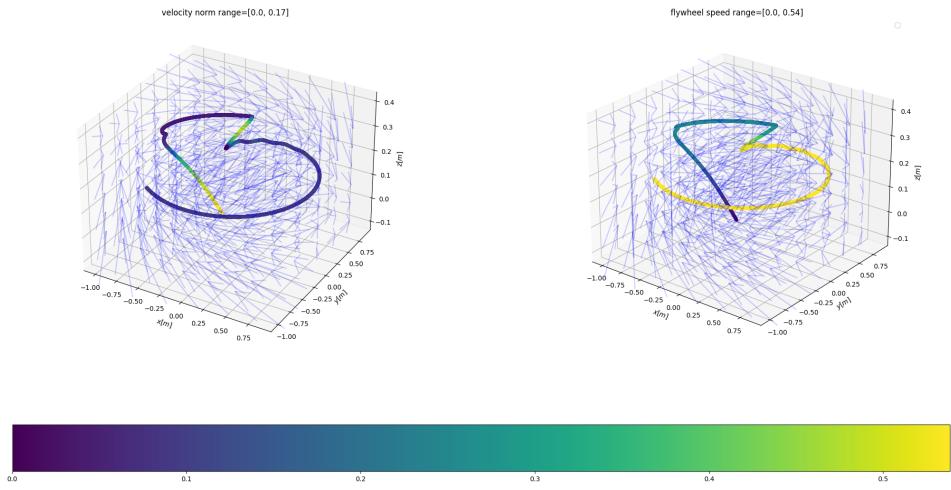


Figure 19: trajectory and mechanical energy without drag and with wrench - Python POC

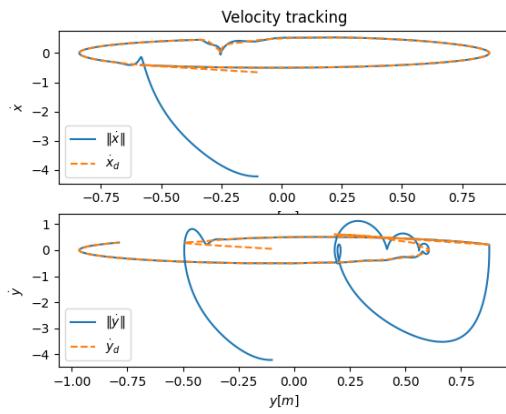


Figure 20: Trajectory tracking without drag with wrench - Python POC

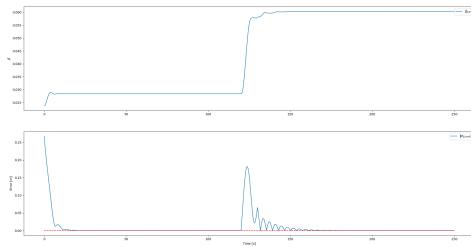


Figure 21: Beta error without drag with wrench

linear with respect to the speed of the quadcopter but in Gazebo, the drag forces are more complex and not linear to the velocity of the moving body. Therefore, it is hard to find the right linear drag

coefficient that will approximate the Gazebo drag force on the IRIS model. We can see how essential is this compensation term in the figures 28 and 27, without drag force compensation, the trajectory is not circular at all and the mechanical energy in the system goes to 0.

5.4.4. World with Wrench

In the above Gazebo experiments, no external force (except drag) was applied on the system. We present here an experiment where a force wrench was applied on the quadcopter during 5 seconds. We will compare it with an experiment in the same conditions but without force wrench applied. We can see in figure 20 that the wrench is injecting energy into the augmented system and that PVFC performs much better in term of velocity field tracking when it is dissipating this external work inside the augmented system. This experience also motivates injecting an initial energy into the system. However, it is hard to finetune the linear drag coefficient together with the amount of injected energy. We could not run the wrench experiment for more than 100 seconds because the quad crashes. We can see one of the reasons why the crash occurs in figure 30: The velocity of the flywheel is diverging, and the translational velocity of the quadcopter is also increasing. This experiments shows that it is crucial to carefully select the linear drag terms because we might lose the passivity properties of the controller when it is too high. This experiments also shows how robust the controller is for passive contour following when external forces are applied on the quadcopter. A [video](#) of this experiment is

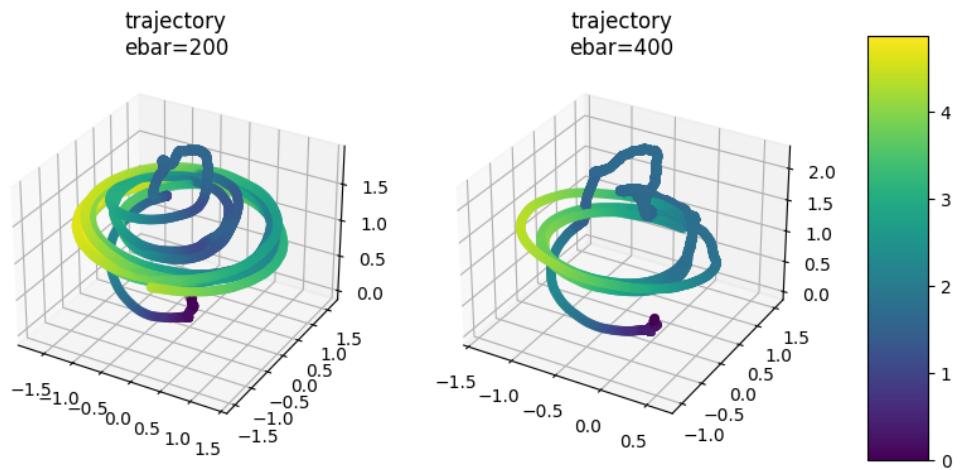


Figure 22: circular field trajectory Gazebo - \bar{E} experiment

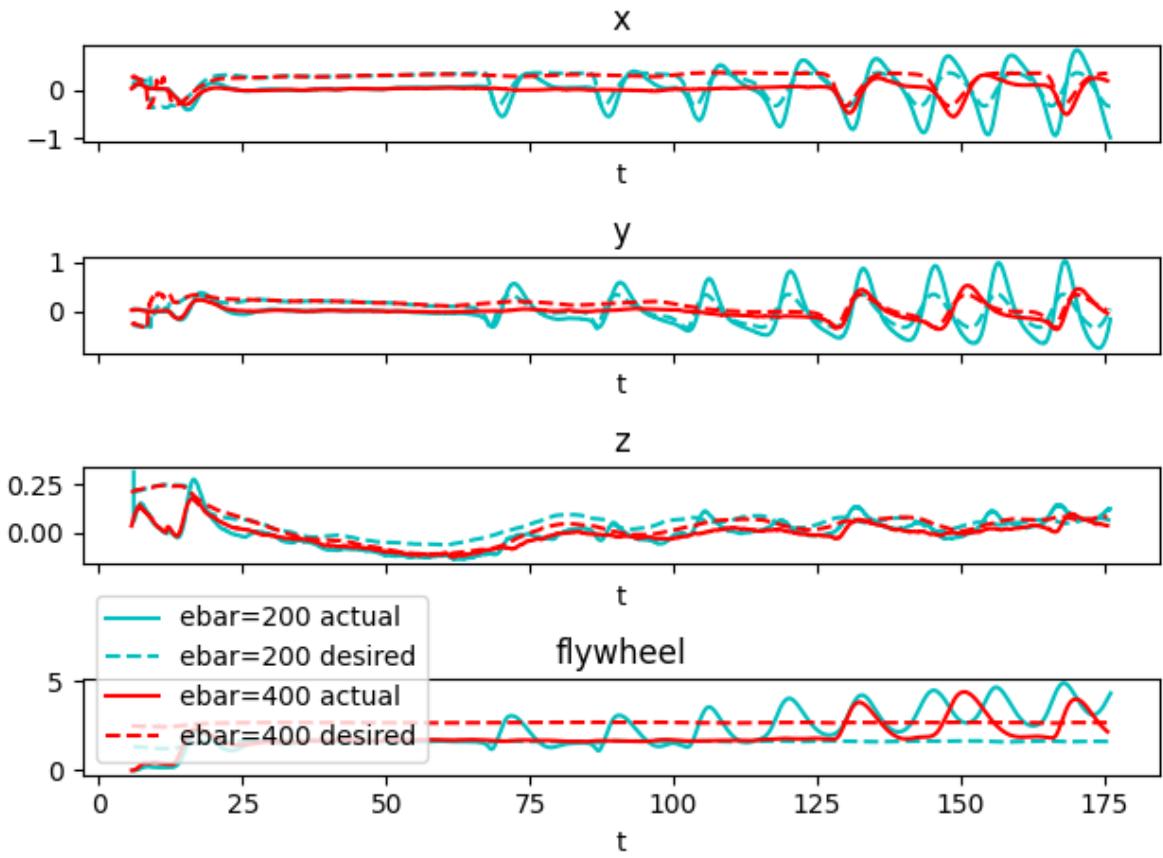


Figure 23: circular field velocity comparison Gazebo - \bar{E} experiment

available on Youtube

5.5. Potential sink Field

In the following experiment, we will study the behavior of PVFC when the desired velocity field is

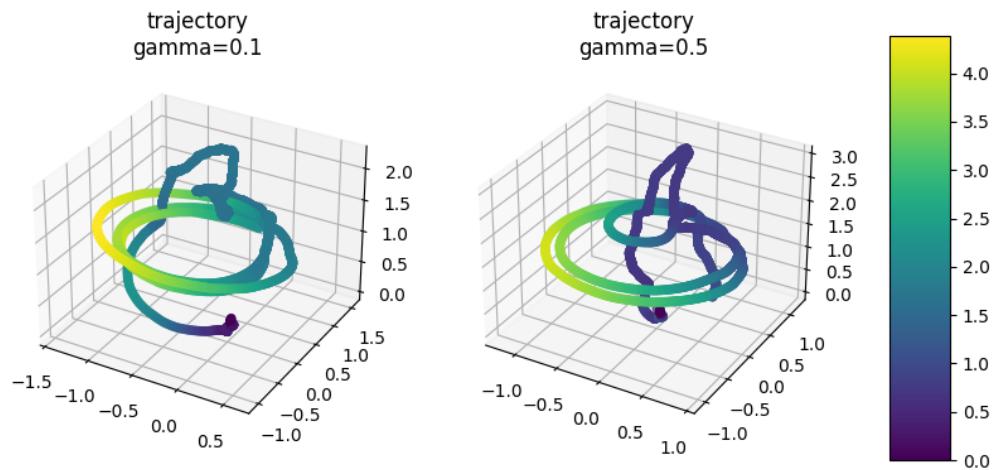


Figure 24: circular field trajectory Gazebo - γ experiment

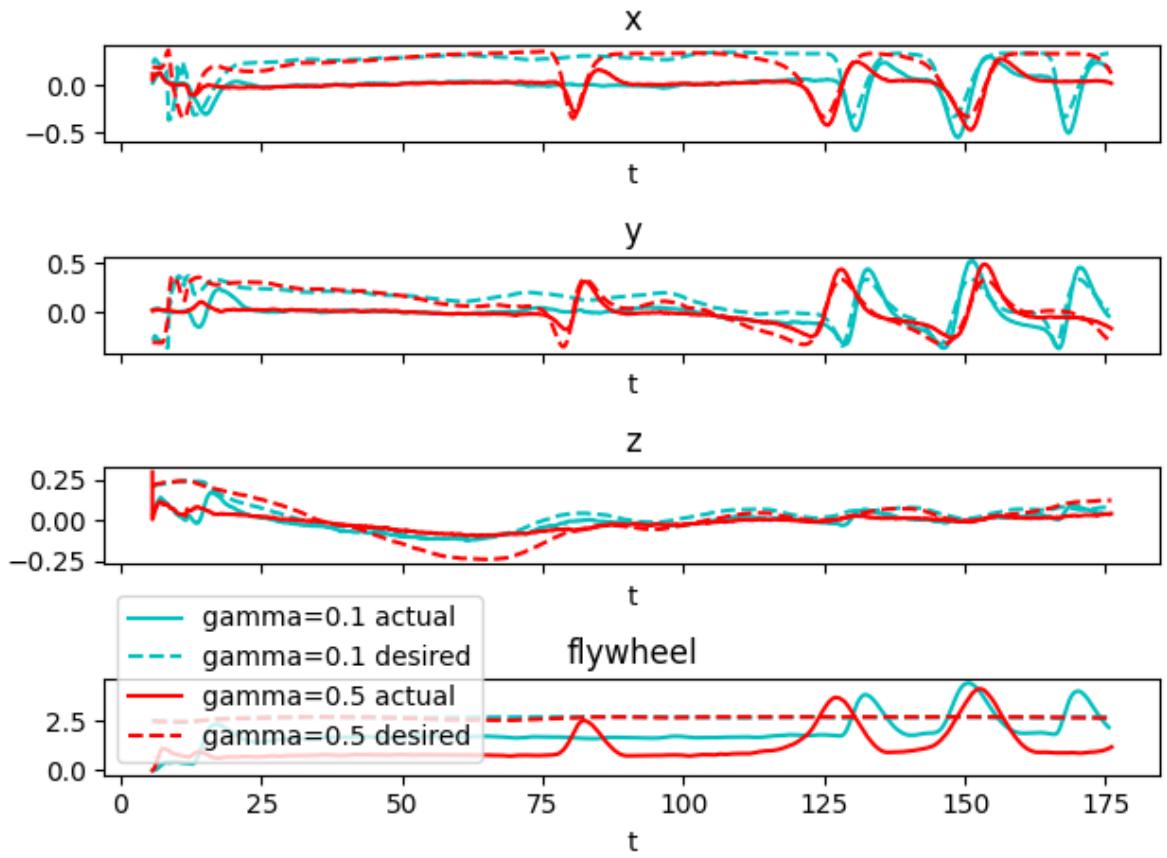


Figure 25: circular field velocity comparison Gazebo - γ experiment

the sink potential field described in section 3. In this section, PVFC will be under the regime of 2 successive potential sink field: The first one is a

sink at point $(0, 0, 0.5)$ (only $+z$) to gain altitude and the second one is a sink at point $(5, 0, 0.5)$ to reach the desired target point. It should be

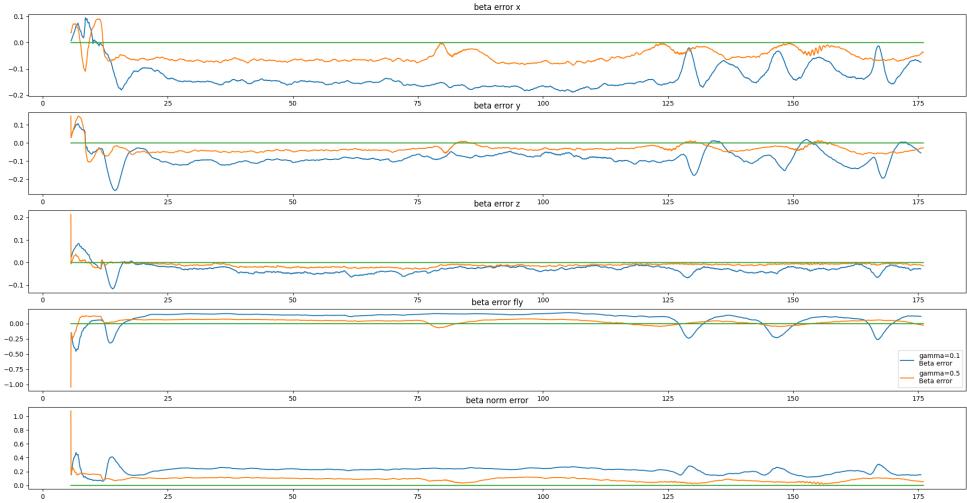


Figure 26: circular field β error Gazebo - γ experiment

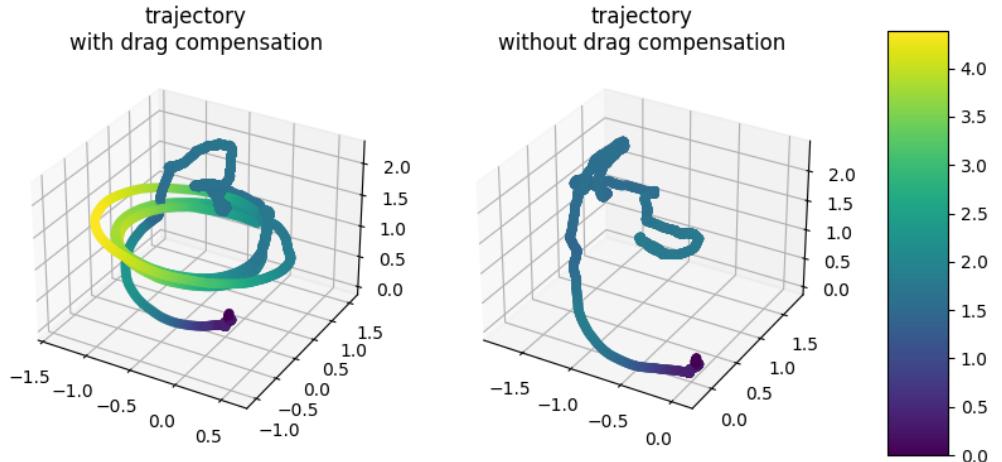


Figure 27: circular field trajectory Gazebo - drag compensation experiment

noted that the linear force compensation had to be increased in the potential sink experiments to accurately follow the desired field. This may be caused by the decreasing norm of the potential field when approaching the desired target point while the norm of the circular field is only affected by the distance from the quad to the closest point on the circle.

5.5.1. \bar{E} study

We can see that the trajectory in the \hat{x} and \hat{y} axis are more stable around the desired state when

$\bar{E} = 200$. However, if we set \bar{E} to be too small, the desired speed of the flywheel (29) may not be a real number which will cause the controller to stop working. Therefore, it is important to finetune this parameter according to the desired velocity field such that it would be the minimum necessary to have a real flywheel desired velocity. It should also be noted that the spike in the β error when switching field is higher when \bar{E} is small (see figure 32)

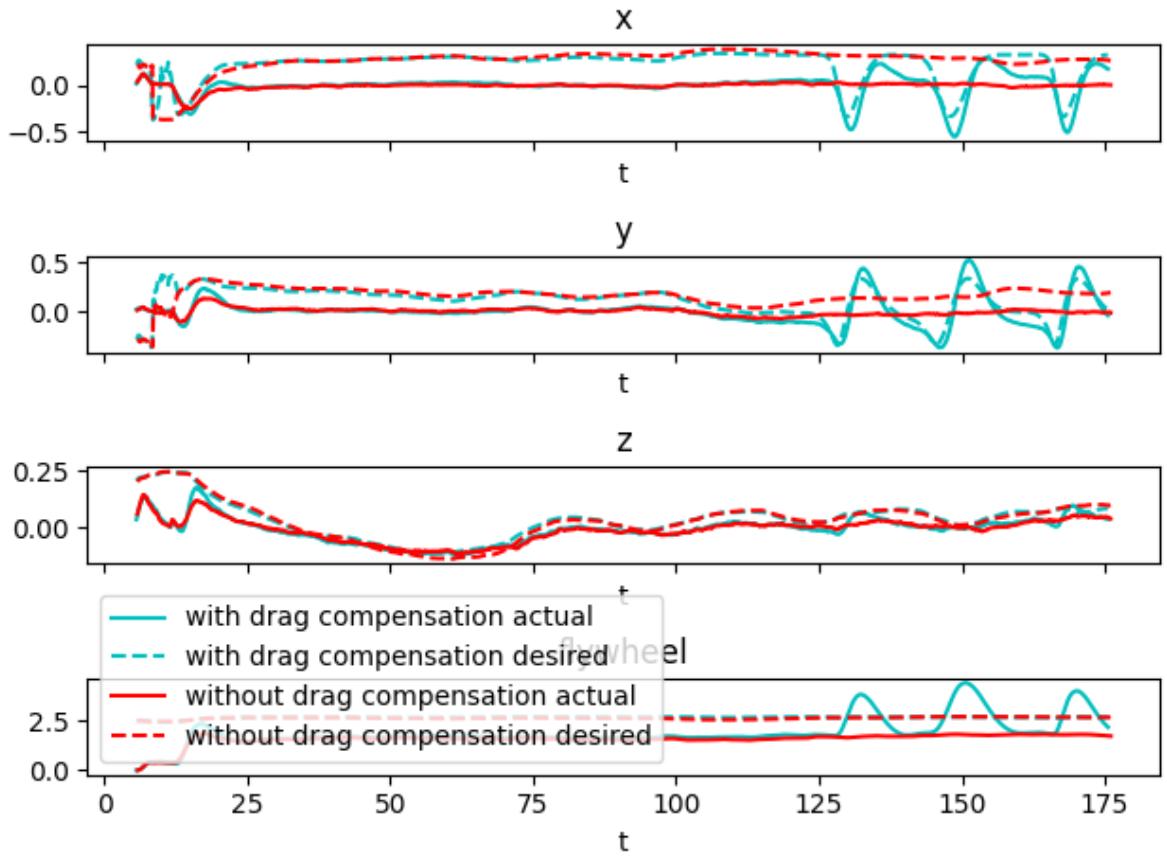


Figure 28: circular field velocity comparison Gazebo - drag compensation experiment

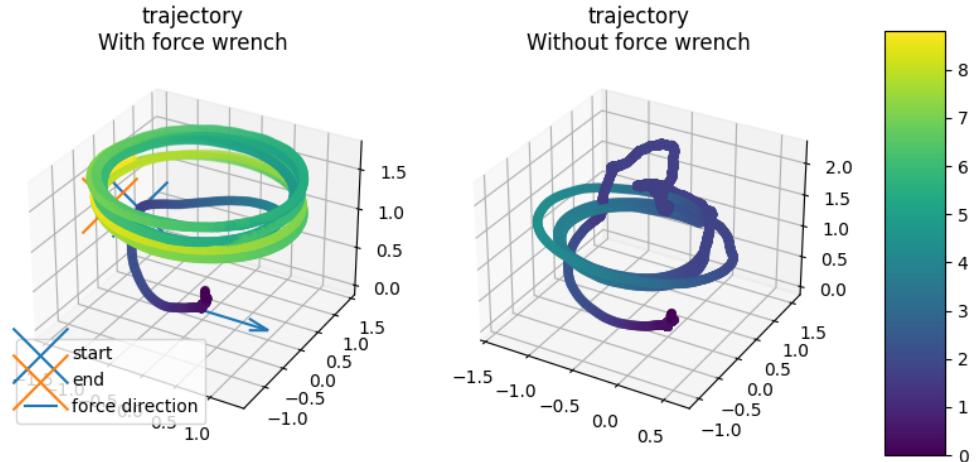


Figure 29: circular field trajectory Gazebo - Wrench experiment

5.5.2. force compensation study

Similarly to our circular field experiment, here to the drag compensation term is essential to prop-

erly follow the desired velocity field. We can see that when no drag compensation is used, the augmented quadcopter system lose all of its mechani-

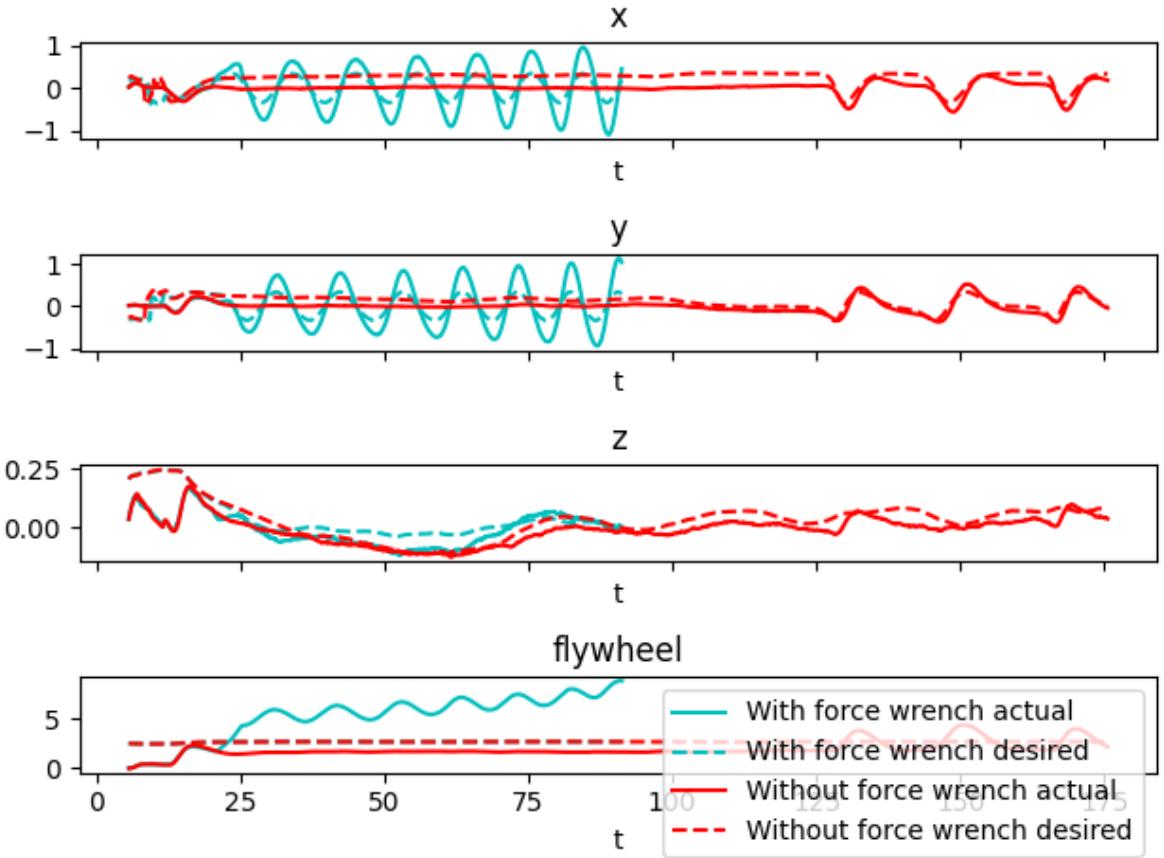


Figure 30: circular field velocity comparison Gazebo - Wrench experiment

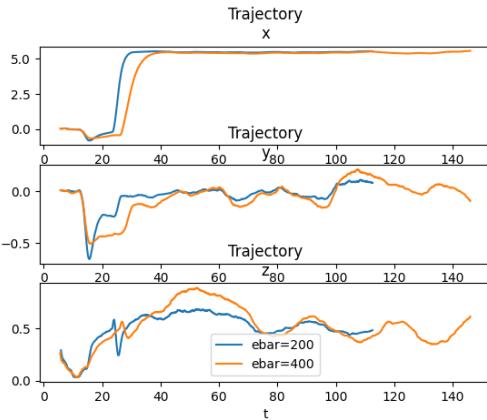


Figure 31: potential field velocity 2d trajectory comparison Gazebo - ebar experiment

cal energy and is unable to follow the desired potential field (see figure 33)

5.6. Sensor placement experiment

The sensor placement experiment starts in a similar way than the potential experience. There is an obstacle with the shape of a cylinder positioned at

$(2, 0)$ with a radius of 0.2 meters and a height of 3. In addition there is a wall spanning along the \hat{y}, \hat{z} plane positioned at $x = 5$. This experiment is taking place in 4 phases:

1. take off following the sink field at $(0, 0, 0.5)$ to gain altitude, when the desired altitude was reached, we switch to the next phase
2. Following the sink field with sink point at $(5, 0, 0.5)$, this is to reach the wall. While following this field, the obstacle will be encountered by the quadcopter and the PCL node will signal to the velocity field node the new obstacle. Upon this signal, the velocity field adds a repulsive field to the current sink field.
3. When the wall has been reached and contact was made between the arm and the wall, the modified grasping arm plugin from gazebo will activate for 10 seconds.
4. After the grasping arm disengages, a signal is sent to the velocity field node to update the sink field with a sink point on the floor close to the wall.

A state machine is implemented in the velocity

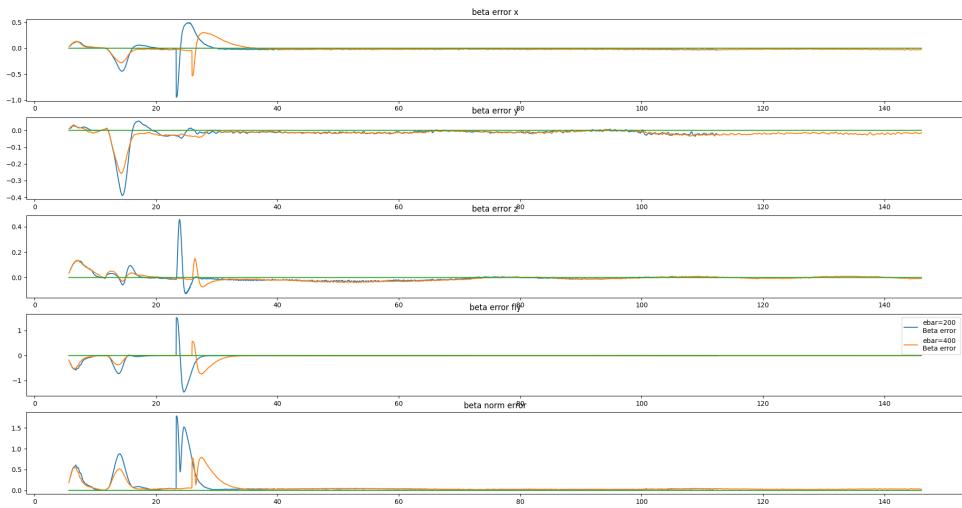


Figure 32: potential field β error Gazebo - \bar{E} experiment

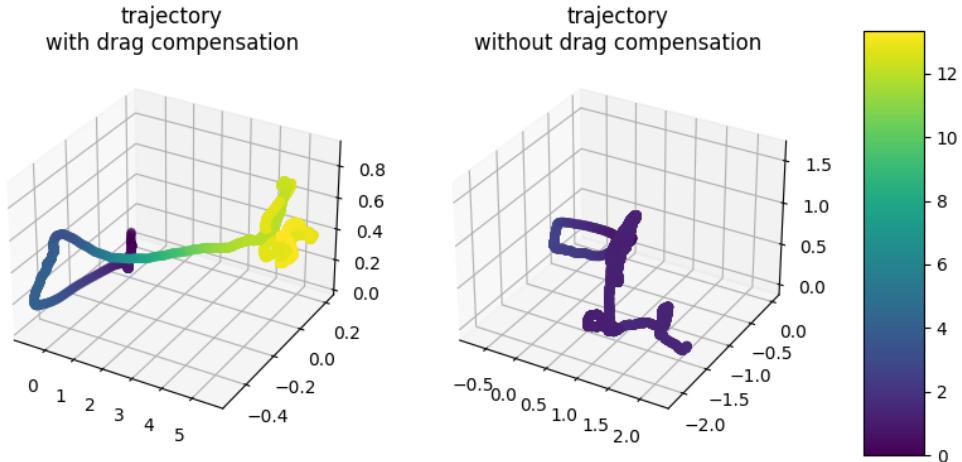


Figure 33: circular field trajectory Gazebo - drag compensation experiment

field node to switch and chose the right velocity field for each step. A [video](#) of this Gazebo experiment was published to Youtube. (Please watch with subtitles) Let us analyse the beta error and trajectory of this experiment. We can see in figure 34 that the flywheel energy is state when reaching the wall and increasing when contact is made. This is because of the passivity of PVFC dissipating the work of the wall inside the augmented system. The β error in figure 35 is spiking at each field update, the spike at $t = 10s$ is due to the change from take off field to approach field (the field to reach the

wall). The spike at $t = 30s$ is due to the added cylinder repulsive field to the approach field. The spike at $t = 45s$ is due to the contact with the wall. Between $t = 45s$ and $t = 55s$, the β error norm is unable to decrease because of the work from the wall on the tip of the arm. The small spike at $t = 75s$ is due to the quad landing causing work from the floor on the quad.

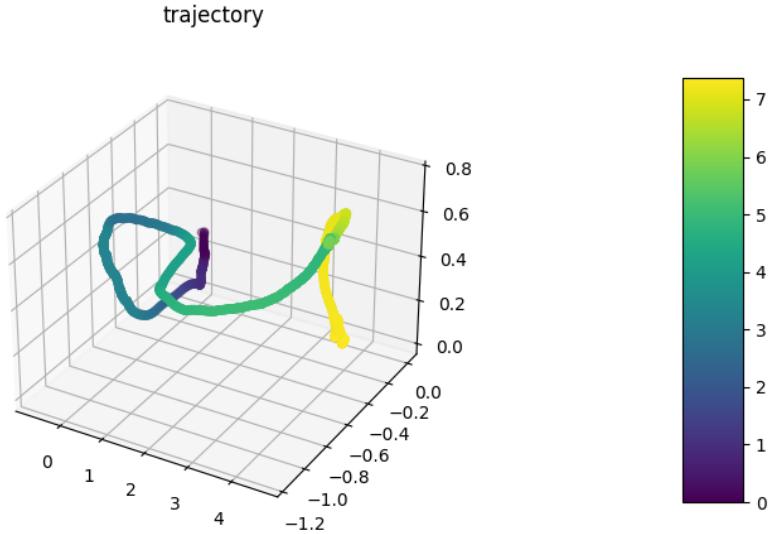


Figure 34: Sensor placement trajectory Gazebo

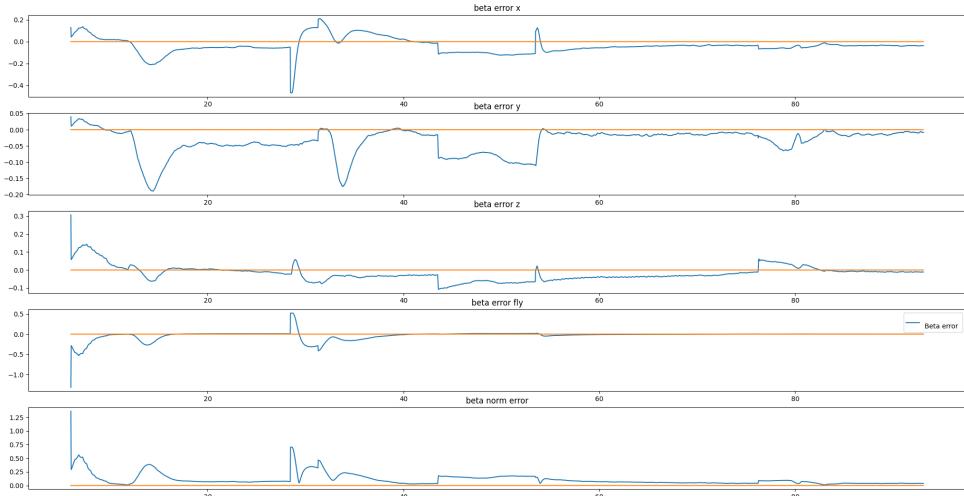


Figure 35: Sensor placement β error Gazebo

6. Conclusion, Future Work

In this project, we presented an application of a passive velocity field controller to the sensor placement task with a grasping arm mounted on a quadcopter integrated with a depth camera for active obstacle avoidance. We first implemented a simple passive velocity controller with simple dynamics on Python using Sympy to symbolically derive and evaluate the dynamics and velocity fields. This implementation allowed us to reproduce results from the PVFC paper [4]. Then we implemented the full pipeline of sensor placement using ROS, PX4,

Gazebo and PCL and explained the different field

Because of lack of time, we did not have time to improve the implementation but many steps could have been done to make it more robust. First, the linear approximation for the drag coefficient we used seems to be task specific and may need to be updated during flight. Therefore, another controller could be used to tune the linear drag coefficient according to the total mechanical energy in the augmented system.

In addition, we often struggled to choose a value for

the gains parameter of PVFC \bar{E} and γ . Multiple strategies could be used to solve this problem such as sampling the velocity field to know the minimum \bar{E} required such that the flywheel velocity never becomes an imaginary number.

It would be also possible to think about an evolutionary algorithm based solution for finding the best gains for the task. For example, in the case of a contour following task, a fitness function could be defined as a function of the path tracking accuracy. Another improvement could be to generalize the superquadratic detection spectrum to be able to detect any kind of superquadratic.

It would also be possible to switch to a solenoidal field in case the quad is stuck at the local minimum in the velocity field.

Finally, we hardcoded the yaw angle of the quad for all experiments but the depth camera has a limited field of view, to always be able to detect obstacle in the direction of movement, it would be necessary to set the desired yaw angle to be in the direction of the desired velocity field.

References

- ¹H. J. Asl and T. Narikiyo, «An assistive control strategy for rehabilitation robots using velocity field and force field», in 2019 IEEE 16th International Conference on Rehabilitation Robotics (ICORR) (IEEE, 2019), pp. 790–795.
- ²A. Farinha, R. Zufferey, P. Zheng, S. F. Armanini, and M. Kovac, «Unmanned aerial sensor placement for cluttered environments», IEEE Robotics and Automation Letters **5**, 6623–6630 (2020).
- ³P. Y. Li and R. Horowitz, «Passive velocity field control (pvfc). part i. geometry and robustness», IEEE Transactions on Automatic Control **46**, 1346–1359 (2001).
- ⁴P. Y. Li and R. Horowitz, «Passive velocity field control of mechanical manipulators», IEEE Transactions on robotics and automation **15**, 751–763 (1999).
- ⁵C. McInnes, «Velocity field path-planning for single and multiple unmanned aerial vehicles», The Aeronautical Journal **107**, 419–426 (2003).
- ⁶F. Ruggiero, V. Lippiello, and A. Ollero, «Aerial manipulation: A literature review», IEEE Robotics and Automation Letters **3**, 1957–1964 (2018).