

---

---

# Sound control in windy weather

---

---

Master Thesis  
Jonas Buchholdt

Aalborg University  
Electronic Engineering and IT

Copyright © Jonas Buchholdt, Electronic Engineering and IT P10, Aalborg University 2019

This report is compiled in L<sup>A</sup>T<sub>E</sub>X. Additionally Mathworks MATLAB<sup>®</sup> , Inkscape, and Xfig are used to draw figures and charts.



**AALBORG UNIVERSITY**  
STUDENT REPORT

**Electronic Engineering and IT**  
Aalborg University  
<http://www.aau.dk>

**Title:**

Sound control in windy weather

**Abstract:**

Will come later
-----------------

**Theme:**

Signal Processing and Acoustics

**Project Period:**

MSc, 10th Semester 2019

**Project Group:**

Jonas Buchholdt

**Participants:**

Jonas Buchholdt

**Supervisor:**

Sofus Birkedal Nielsen

**Number of Pages:** 57

**Date of Completion:**

?<sup>th</sup> June 2019

*The content of this report is freely available, but publication may only be pursued with reference.*



# Preface

This report is composed by Jonas Buchholdt during the 10th semester of Electronic Engineering and IT at Aalborg University. The general purpose of the report is *Signal Processing and Acoustics* .

For citations, the report employs the Harvard method. If citations are not present by figures or tables, these have been made by the authors of the report. Units are indicated according to the SI standard.

Aalborg University, March 15, 2019

*Jonas Buchholdt*  
<Jbuchh13@student.aau.dk>

# Contents

<b>Preface</b>	<b>v</b>
<b>Glossary</b>	<b>1</b>
<b>1 Introduction</b>	<b>3</b>
<b>I Problem Analysis and Requirements</b>	<b>5</b>
<b>2 Analysis of sound propogation in outdoor venue</b>	<b>7</b>
2.1 Live venue sound challenges . . . . .	7
2.2 Ideal geometric spreading loss . . . . .	10
2.3 Homogeneous atmospheric conditions . . . . .	11
2.4 Inhomogeneous atmospheric conditions . . . . .	19
2.5 sound pressure level doing a concert . . . . .	26
<b>3 Summary of Problem Analysis</b>	<b>27</b>
<b>4 Problem statement</b>	<b>31</b>
4.1 Deimitation . . . . .	31
<b>II Test Design</b>	<b>33</b>
<b>5 Design</b>	<b>35</b>
<b>III Results</b>	<b>37</b>
<b>6 Results</b>	<b>39</b>
<b>7 Discussion and conclusion</b>	<b>41</b>
7.1 Conclusion . . . . .	41
<b>IV Appendix</b>	<b>43</b>
<b>A cross wind effect on line source array</b>	<b>45</b>
<b>B cross wind effect on line source array</b>	<b>51</b>
<b>Bibliography</b>	<b>55</b>

# Glossary

**FDTD** Finite-Difference Time-Domain. 15

**FOH** Front Of House. 9, 26

**PA** Public Address System. 7, 8

**SPL** Sound Pressure Level. 7, 8, 9, 10, 11, 12, 16, 17, 20, 23, 24, 25, 26, 27, 28, 29, 47, 52





# Chapter 1

## Introduction

Coming later



## Part I

# Problem Analysis and Requirements



## Chapter 2

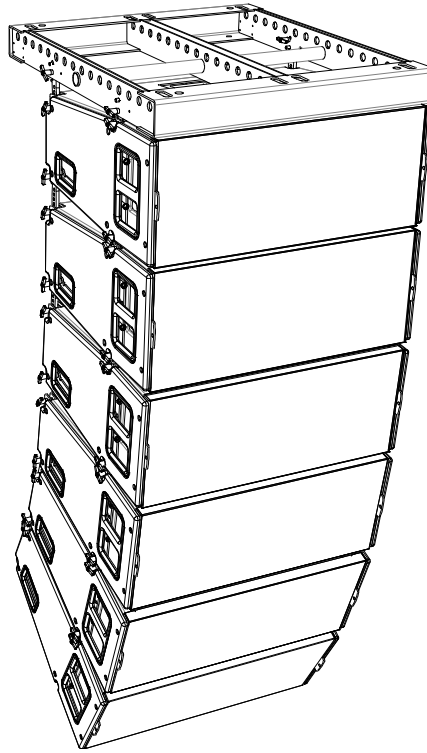
# Analysis of sound propagation in outdoor venue

### 2.1 Live venue sound challenges

This section explores the challenges of producing sound in an outdoor environment. The challenge of producing a good sound experience for the audience highly depend on the calibration method and the atmosphere condition. It is well known that acoustically wave propagation is strongly affected by the inhomogeneous atmosphere doing the outdoor sound propagation. This inhomogeneous atmosphere shifts the calibration of the sound system which affects the intelligibility. In section 2.1.1 an overview of high Sound Pressure Level (SPL) Public Address System (PA) system is discussed.

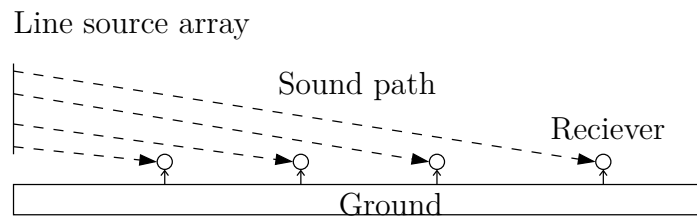
#### 2.1.1 Acoustics as live venue

An outdoor PA system is an essential sound reinforcement concept today. It is used to address information, music or just entertainment where the number of audiences is large, sometimes more than 10.000 audiences. The number of the audience makes it difficult to address the information to a large number of the audience without the reinforcement of the information. The reinforcement is nearly always done from a stage with a sizeable PA system and sometimes delay unit in the middle of the audience area. The stage lifts the artist while the PA system is designed to cover the audience area with sound. The optimal PA system covers the area with a linear frequency spectrum in the audible frequency range with a homogeneous SPL. Today, the used speaker is a line source array flown in both side of the stage and is therefore only close to the audience in front of the stage. The line source array is an array of small identically wide speakers attached to each other, to form a vertical line of speakers. An example of a line source array is shown in Figure 2.1



**Figure 2.1:** The figure shows an illustration of a KUDO line source array from L-Acoustics [L-Acoustics]

Every speaker or a small group of the line source array can be controlled individually, both in sound coverage area angle and SPL. The benefit of using the line source array design is that the coupling between the speaker makes a line acting source. With an optimised control system of the line source array, the audience area can be covered with sound such that all audience can hear the information without damage the ear of the frontal audience. An optimised line source array has, for example, an optimised main lobe such that the lower part of the main lobe lays flat along the audience area. The following Figure 2.2 shows a graphical illustration of the outdoor PA venue concept.



**Figure 2.2:** The figure illustrate the concept of outdoor PA venue

As shown in Figure 2.2, the distances from one element in the line source array to the receiving audience dependent on the audience position. The distance indicates that the signal to every line source element has to be set individually to cover the audience area with a homogeneous SPL. The individual control of the source is necessary because of the wave amplitude decay with distances. This phenomena is addressed in section 2.2. The adjustment is not as simple as just supply the upper speaker with more power. A sound wave is a mechanical movement of the particle in the air, which condensate and compression the air molecule, then low pressure and high pressure respectively. The movement of the molecule depends on the medium, and in this thesis, the medium is limited to air. The SPL is the pressure deviation of the instantaneous atmospheric pressure. The atmospheric pressure, therefore, set a lower bound on the condensation while very high pressure changes the speed of sound and distort the wave as it propagates. To ensuring that the information is communicated to the audience without distortion, the limitation is addressed in section 2.3.3. The medium in the air is not constant and varies over time regarding pressure, wind, humidity and temperature. The analysis starts with the experience for live concert of the author in section 2.1.2, next section 2.3 address the impact of homogeneous atmospheric effect on sound propagation. Then section 2.3 address the impact of inhomogeneous atmospheric effect on sound propagation.

### 2.1.2 Author experience of live concert

The Author of the thesis has experience with live concert both as an audience and as a sound engineer. The aspect of being the sound engineer and an audience to a live concert is very different. As a sound engineer, the area for controlling the sound is a secured area with a tent as protection. The tent roof often shadows for the high frequency, and the walls make standing waves of the low frequency because the distance between parallel tent walls fits with the wavelength for the low frequency. The sound engineer control area is defined as the Front Of House (FOH). The FOH is often equipped with an additional speaker, and the sound engineer does not fully know how it sounds outside the FOH, but base there mixes on experience. The aspect of being an audience depends on where the audience is regarding the stage. In close hand to the stage the SPL is high and often to high especially in the low frequency. The low frequency is often made as a vertical array at the ground or two end-fire arrays and shall be able to exhibit all audience by an audible low frequency spectrum typically from 25 Hz but one company extends down to 13 Hz. Therefore the SPL just in front of the subwoofer has a very high SPL. This position is not comfortable to be at in longer period, and the high SPL mask the higher frequency. The optimal audience position is in the centre of the stage and not as long from the stage as the delay towers. The average SPL is often less than 102 dB SPL since the sound engineer try to keep a maximum average SPL at 102 dB SPL just in front of the FOH. Moreover, it is the stereo sweet spot. This position is the only position where the stereo image is optimal. The stereo perspective problem is a hot topic nowadays, both L-Acoustics [L-Acoustics, 2019] and D&B Audiotechnik

[d&b audiotechnik, 2019] have made there own solution to the problem. The idea is to fly many small line source array above the stage and assign every musician to there own line source array. The concept minimises the interference between two line source array playing the same mono signal. Between the delay line towers, the low frequency spectrum is still sharp and audible but something happens to the high frequency. Often the high frequency disappears for a few seconds and gets back — this phenomenon altering through the full concert. Behind the delay towers, the line source array in the delay tower reproduces the sound such that the audience in the back also gets the high frequency spectrum. The question is why does the high frequency disappear for a short period when the low frequency does not? This thesis focus on answer this question.

## 2.2 Ideal geometric spreading loss

When a line source generates a sound wave, the wave field exhibits two fundamental difference spatially directive regions, near-field and far-field. In near-field, the wave propagates as a cylindrical wave wherein the far-field the wave propagates as a spherical wave. When the wave propagates as a cylindrical wave, the wave propagates only in the horizontal plane, and therefore the attenuation is 3 dB SPL per doubling of distance. For a spherical wave propagation, the wave propagates in all direction. Therefore the attenuation is 6 dB SPL per doubling of distance. The near-field and far-field attenuation are based on non-absorption homogeneous atmospheric conditions. The border between the near-field and far-field depends on the hight of the array and the frequency. The distance can be calculated with Fresnel formula Equation 2.1, where the wavelength  $\lambda$  is approximated to  $\frac{1}{3f}$  [Bauman et al., 2001]

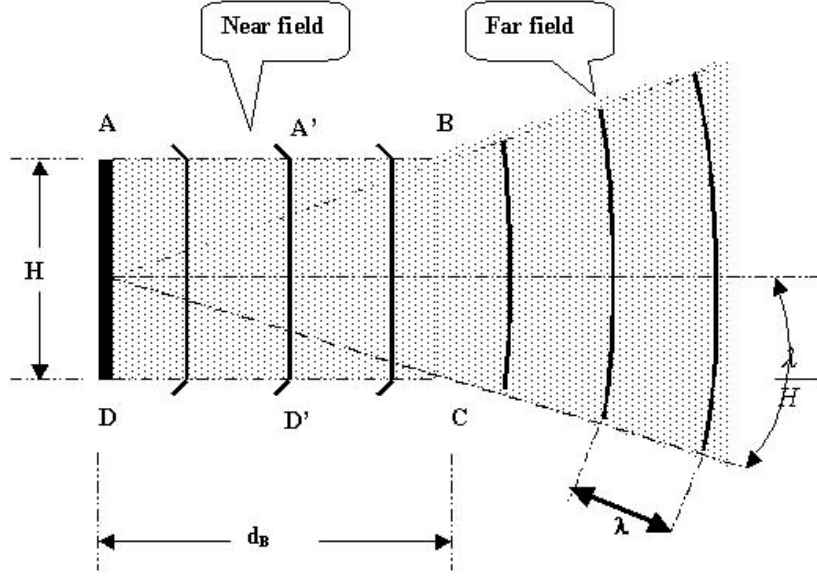
$$d_B = \frac{3}{2} f \cdot H^2 \sqrt{1 - \frac{1}{(3f \cdot H)}} \quad (2.1)$$

Where:

$d_B$ is is the distance from the array to the end of near field	[m]
$f$ is the frequency	[kHz]
$H$ is the hight of the array	[m]

In equation Equation 2.1 it can be calculated that less than 80 Hz radiate directly intro spherical wave on the exit of the speaker no matter the hight of the line source array. The following Figure 2.3 shows a horizontal cut of the near-field, far-field from a line source array.





**Figure 2.3:** The figure shows horizontal cut of a SPL radiation pattern of a line source array [Bauman et al., 2001].

As seen in Figure 2.3, the wave propagating as a plane cylindrical wave in the near-field, where the coverage area for every double of distance is twice as big. Since the coverage area is twice as big, the SPL is the half for the doubled distance. When the wave excites distance  $d_B$ , the wave propagates into far-field where the coverage area is four times higher while travelling the double of distance and therefore the SPL is four times less. In far-field, the wave propagates as a spherical sound source

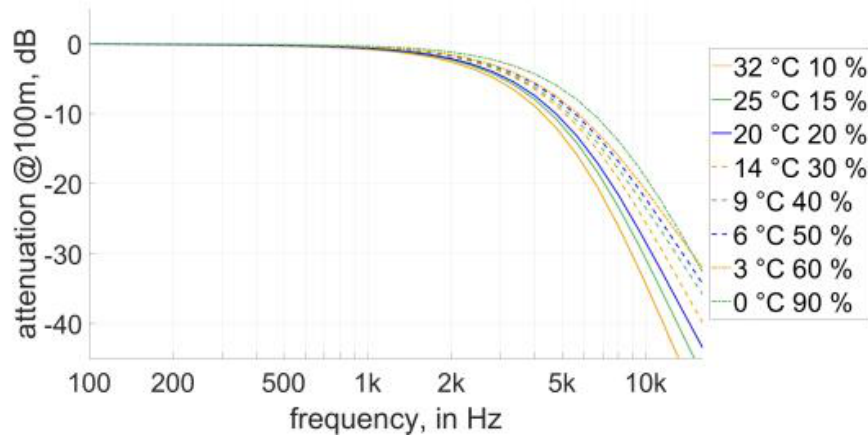
## 2.3 Homogeneous atmospheric conditions

This section aims to analyse the sound wave propagation in homogeneous atmospheric conditions. It is well known that the sound wave propagation is highly depending on the atmospheric conditions. The propagation depends on the atmospheric pressure, wind, temperature and humidity, where the two latter moreover is frequency dependent. The attenuation difference in frequency for temperature and humidity can be above 80 dB SPL [Corteel et al., 2017]. The following sections introduce a brief discussion of homogeneous atmospheric conditions effect on sound propagation.

### 2.3.1 Humidity and temperature impact

The temperature and humidity have three impacts on wave propagation from a line source array, directionality of the speaker, the speed of sound and a lowpass effect. The following description starts with the latter.

**Lowpass effect** The effect of humidity and temperature on wave propagation act as a lowpass filter while the wave propagates. The low frequency remains without any additional attenuation where the high frequency highly depends on the atmospheric condition. In other words, attenuation in the high frequency range does not only depends on the spreading loss but also temperature and humidity. Therefore, for long distance, the atmospheric conditions have a high influence on the frequency spectrum delivered to the audience. Humidity and temperature attenuation are already well studied and standardised. Standard [ISO 9613-1:1993] gives an overview of calculating the SPL attenuation concerning the frequency, distance, temperature and humidity. The article [Corteel et al., 2017] gives some examples of attenuation at a distance of 100 m. The article shows that if humidity increases proportionally to the temperature, the lowpass effect is small. If the change in temperature and humidity is the opposite of each other, for example, high temperature but dry, the attenuation in high frequency is significant. The following Figure 2.4 shows the worst-case scenario from [Corteel et al., 2017].

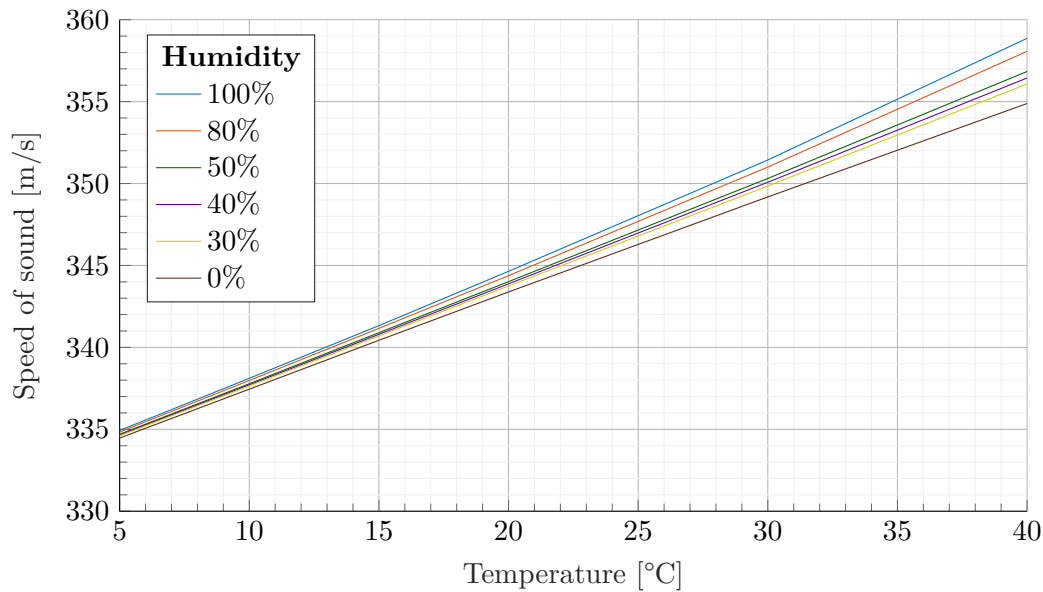


**Figure 2.4:** The graph shows the attenuation in dB with respect to frequency, humidity and temperature [Corteel et al., 2017].

As shown in Figure 2.4 the attenuation in the high frequency is significant and excite 30 dB SPL within the audible frequency range. The attenuation is such markedly that applying more power does not cover the attenuation without an extreme high-pressure driver. That driver might be possible to design in theory but not in practice. Extreme high-pressure drivers introduce high distortion as is explained in section 2.3.3

**Speed of sound** The second consequence is the speed of sound. At temperature range from 0 °C to 40 °C the speed of sound with respect to humidity change is sparse and mostly only depend on temperature change. At 0 % humidity, the speed of sound increases with 0.6 m/s for every increasing degree °C. At humidity higher

that 0 % the speed of sound increase with respect to humidity, depends on temperature. At 0 °C the speed of sound increases with approximately 0.8 m/s when the humidity raises from 0 % to 100 %. At 30 °C the speed of sound increases with approximately 2.7 m/s when the humidity raises from 0 % to 100 % [Wong and Embleton, 1985] [Bohn, 1987]. The wave propagation speed start at 331.5 m/s at 0 °C and 0 % humidity. The following Figure 2.5 shows the speed of sound with respect to humidity and temperature.



**Figure 2.5:** The figure shows the increase of sound speed with respect to humidity and temperature [Bohn, 1987]

As seen in Figure 2.5, the effect of humidity is negligible compared to the effect of temperature changes, but as the temperature increases the humidity gets significant. At a temperature of 40 °C the speed of sound is changed 4 m/s from 0 % humidity to 100 %

**Directivity** The directivity of a line source array in the mid and high frequency is always controlled mechanically by a horn because the wavelength is short compared to the size of the speaker. At low frequency, the wavelength is too long to be controlled mechanically by a horn. Therefore the directional pattern is controlled via cancellation from a backwards pointing speaker. The directivity of both the subwoofer and the high frequency driver suffers from temperature increased. At the high frequency, the main lobe gets narrower when the mechanical horn gets warmer, and the effect is notable when the sun directly heats up the horn. The resend that the temperature of the building horn affect the directivity of the high frequency is

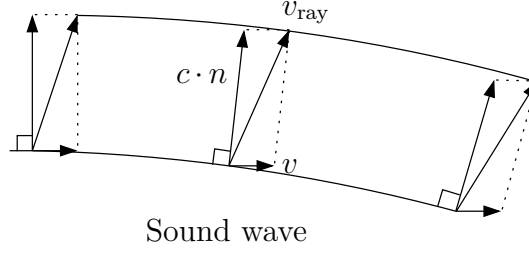
that the warm horn surface heats the air at the mouth of the horn. Since the temperature increases, the wavelength gets shorter. Therefore the main lobe of the high frequency gets narrower [Levine et al., 2018]. The directivity of the low frequency is affected as in the high frequency with the temperature increase. The difference is not as significant as in the high frequency since there is no surface heat. The directivity is then not affected due to the sunlight, but only the temperature is increasing and decreasing. As in the high frequency temperature differences change the wavelength, and then the length between the speaker in a cardioid subwoofer does not match the optimised distance between the speaker any more.

### 2.3.2 Wind impact

The wind impact is depending on the angle of the wind direction with respect to the direction of sound propagation. A homogeneous wind is a laminar wind flown with the same homogeneous speed. The following analysis assumes homogeneous laminar wind flow from one direction. The analysis is of both oblique wind and parallel wind with respect to the frontal direction of the speaker line source array. The analysis starts with the latter.

**Parallel to sound propagation** When the wind flows in the same direction as the sound wave propagation, the wind flow in m/s is an addition to the speed of sound. When the wind flows in the opposite direction, it is a negative addition. In other cases, the influence is complicated since the wind deflect the sound waves.

**oblique- and crosswind** The effect of oblique- and crosswind on sound wave propagation is rarely studied, and the effect on high frequency seems to be unclear. Few author have addressed the problem in a simulation of traffic noise and by practical experience [de Oliveira, 2012], [Hornikx and Renterghem, 2017], [Ballou, 2008]. They found that the crosswind effect might refract the wave in the wind direction over distances. Furthermore, they found that the effect is not linear in frequency. The author of [Ballou, 2008] indicates that the frequency dependency might be due to the directionality of the high frequency drivers. The author of [Ostashev et al., 2005] has simulated the homogeneous crosswind effect on a omnidirectional source at 100 Hz. The author of [Prospathopoulos and Voutsinas, 2007] implemented a ray tracing method with a vector based interpolation as shown in Figure 2.6.



**Figure 2.6:** The figure shows a geometrical calculation scheme of calculate the resulting wave direction at crosswind [Prospathopoulos and Voutsinas, 2007], [Ostashev et al., 2005]

Where:

$c$	is the speed of sound	[m/s]
$n$	is the normal unit vector	[m]
$v$	is the speed of wind	[m/s]
$v_{ray}$	is the resulting sound ray	[m]

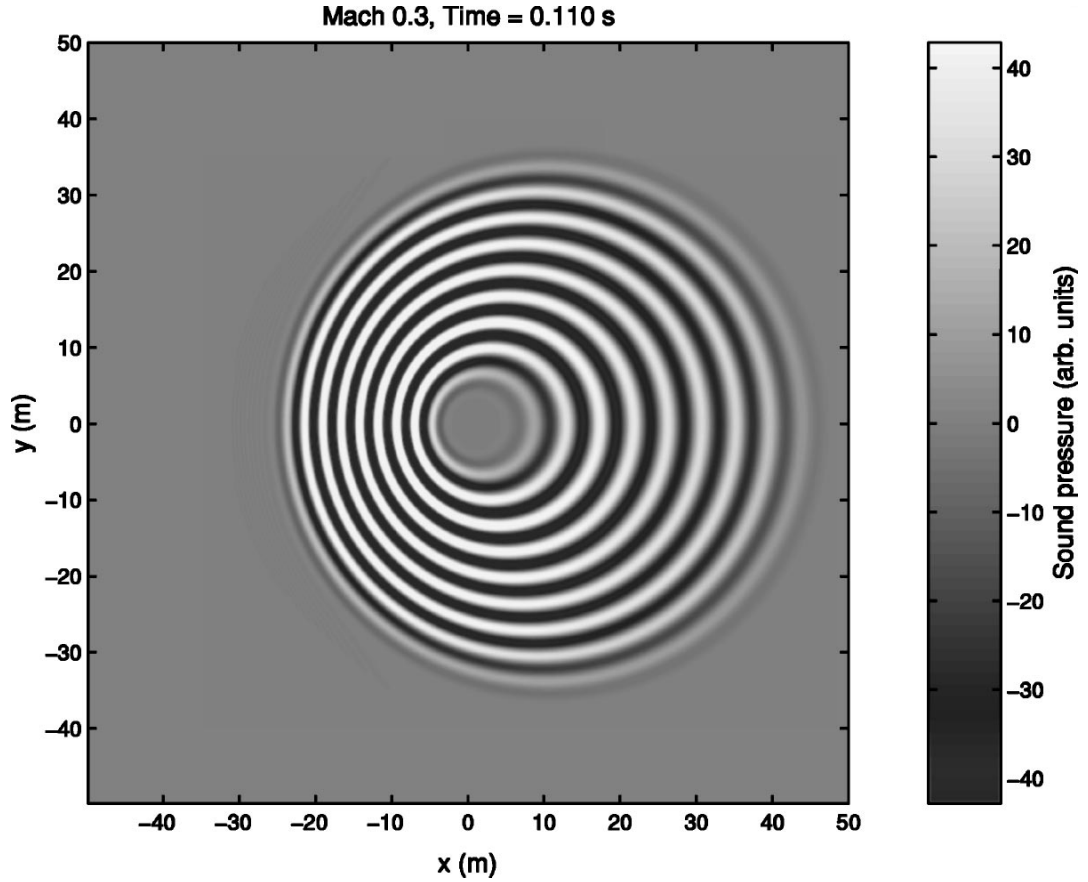
As it is seen in Figure 2.6 the ray vector  $v_{ray}$  is an addition of the sound speed vector  $c \cdot n$  and the speed of wind  $v$ . The wave speed and wave length therefore depend on the speed of wind and the angle between the wind and the sound propagation. The following Equation 2.2 calculate the speed of sound with respect to the angle and wind

$$c_r = c + \|v\|_2 \cdot \sin(\theta) = \|c \cdot n + v\|_2 = \|v_{ray}\|_2 \quad (2.2)$$

Where:

$\theta$	is the angle of the wave with respect to the wind	[°]
$c_r$	is the resulting speed of sound	[m/s]

As the wave propagating, the resulting  $v_{ray}$  increases in the direction of the wind. The article [Ostashev et al., 2005] simulates the effect of crosswind in a Finite-Difference Time-Domain (FDTD) simulation with a wind speed of 102.9 m/s. For the acceptable condition to a concert the wind speed is less than 20 m/s otherwise, the concert is stopped for safety. The following simulation Figure 2.7 shows the simulation result from [Ostashev et al., 2005]. The source is an omnidirectional 100 Hz spherical source while the wind has a constant uniform wind speed from left. The simulation is done in two dimensions.



**Figure 2.7:** The figure shows a simulation of a 100 Hz omnidirectional source with a uniform constant wind speed from left with speed of 102.9 m/s [Ostashev et al., 2005].

It is seen in Figure 2.7 that the crosswind do not affect the direction of the wave from a low frequency spherical source. It only affects the time of arrival to the audience.

### 2.3.3 Pressure impact

The influence of atmospheric pressure change is low compared to the effect of wind, humidity and temperature. The average attenuation from 4.0 kHz to 16.0 kHz with fixed temperature was 2 dB SPL while going from 54.02 kPa to 101.33 kPa. The atmospheric pressure then only have a negligibility influence on sound propagation and is generally not frequency dependent.

Beside the small impact of pressure difference in the atmosphere, the high pressure generated by the speaker does have a tremendous influence on the sound propagation. There are two main places in the propagation way that can produce distortion concerning the pressure. The design of the high frequency horn [Czerwinski et al., 1999],

the port design of the low frequency driver [Vanderkooy, 1998] and the influence of the sound path. The following description starts with the latter.

**Sound path** In the sound path, two main factors cause distortion in the wave propagating. As described in ... a sound wave is condensation and compresses the air particle. The air medium has a lower limit that cannot be less than a vacuum. Therefore the higher bound of SPL is depending on the atmospheric pressure. As an example, at 54.02 kPa the highest SPL before distortion caused by vacuum is 188.6 dB SPL and at 101.33 kPa the highest SPL before distortion caused by vacuum is 194.1 dB SPL.

There is therefore a higher limit determined by the atmospheric pressure to vacuum, but this is not the only limit for distortion. Very high pressure in the comparison also distorts the sound. At the comparison seriously signal deterioration occurs if the amplitude is high. The distortion of the comparison is explained by the lack of linear dependency between the particle velocity and the SPL in a sound wave. The SPL increases more than the density of the sound wave which causes the condensation of the sound wave to be stiffer and therefore propagate faster than in the condensation of the wave. This effect causes that the speed of sound to travel faster in the compression and slower in the condensation and produce harmonic distortion. The harmonic distortion is by this effect is even present in SPL less than 120 dB SPL [Czerwinski et al., 1999]. The effect is that the sine wave transforms to a sawtooth as it propagates which transfers energy to the harmonic of the propagation wave. The distortion is not only SPL dependent, but also depends on the frequency. The higher the frequency is the faster the sinusoid transforms into a sawtooth and therefore the distortion increases with frequency for similar SPL. The harmonic distortion of the fundamental sinusoid is frequencies that are the double, second order and the third order harmonic. Those frequencies are higher than the fundamental frequency and therefore as explained in section 2.3.1 have a higher attenuation with respect to the distance. In most cases the attenuation is not as high as the increase of the harmonic distortion and therefore the distortion of the wave propagation is not compensated by the viscous losses but does that the distortion is not as drastic as it would have been without viscous losses [Czerwinski et al., 1999]. The distortion made by air propagation is much less than the distortion in the mouth of the speaker which leads to the next distortion problem produced by high pressure [Czerwinski et al., 1999].

**Driver throat and mouth design** High pressure in both horn phase plug, sealed enclosures and vented enclosures or reflex enclosures for low frequency driver cabinets produce distortion as they act as nonlinear components. The latter produce distortion because high pressure makes air turbulence in the vent. By the optimal design the distortion of turbulent flow can be kept low [Roozen et al., 1998]. The turbulence phenomena does not only cause in the mouth of the low frequency driver, it also occurs in the phase plug of the compression driver if the SPL is high [Czer-

winski et al., 1999]. The distortion depends on the air's moving mass, the stiffness and the viscous losses on the diaphragm displacement and the SPL. As the air in the high frequency driver compression it becomes heavier, stiffer and thicker which make nonlinear wave propagation. It typically occurs when the compression chamber exceeds approximately 170 dB SPL. At higher level the particle velocity resistance to the air flow increases and the laminar air flow turns into turbulent air flow. The distortion is also depending on the length of the horn and the expansion rate of the horn flare. To keep the distortion as low as possible for the high frequency driver the displacement of the diaphragm should be kept significantly lower than the height of the compression chamber [Voishvillo, 2004]. Therefore, to keep the displacement of the high frequency driver as low as possible, the frequency range should be limited as high as possible since the displacement gets lower as the frequency increases.

### 2.3.4 Ground absorption and reflection

In a concert area, ground absorption and reflection is complex because there are two very different situations. Before the concert the area is a locally plan area often with mown grass and with ground reflection. An example of frequency response in the height of an audience or measurement microphone is given in [Piercy et al., 1977] where it is seen that the ground reflection does have a high effect while playing over mown grass. A measurement in Appendix A and Appendix B is also performed where the ground reflection clearly has a big influence on the received frequency response. During the concert the interesting part is not such ground reflection effect but the audience reflection or absorption. The area along the concert is packed by audience, and is therefore not easy to calculate. The absorption and reflection in an outside concert area with audience is rarely studied but absorption for the audience inside a concert hall have been highly studied [Beranek, 2006]. The absorption of the audience is found to be high in all measured concert hall from 1.0 kHz octave band and upwards to the highest measured octave band in [Beranek, 2006]. The average absorption  $a_{\text{sabine}}$  coefficient is calculated to be above 0.80. The method and result can be found in [Beranek, 2006]. The reflection in the high frequency in the audience area during concert is therefore assumed to be very low. At low frequency the article [Beranek, 2006] indicates that the absorption decays with frequency beneath 250 Hz, but the octave band for low frequency driver is 31.5 Hz but is not measured by [Beranek, 2006]. The low frequency absorption at 31.5 Hz octave band is therefore assumed to be low even in the normal position of the low frequency driver. They are often situated in front of the stage on a line or in end fire settings, often with a maximum distance of half the wavelength from acoustical center to acoustical center. The distance between the low frequency driver is determined by the half wavelength of the highest frequency, such that they radiate a plan wave [Bauman et al., 2001]. Higher distance between acoustical center will cause interference in the low frequency in the audience area.



### 2.3.5 Homogeneous speed equation

The following Equation 2.3 calculate the speed of sound based on homogeneous temperature and wind speed.

$$c = c_0 \sqrt{1 + t/t_0} + u \cdot \sin(\theta) \quad (2.3)$$

Where:

$c$	is the resulting speed of sound	[m/s]
$u$	is the speed of wind	[m/s]
$c_0$	is the speed of sound at 0 °C	[m/s]
$t$	is the temperature	[°C]
$t_0$	is the temperature at 0 °C (273.15)	[K]
$\theta$	is the angle of wind with respect to the wave propagation	[°]

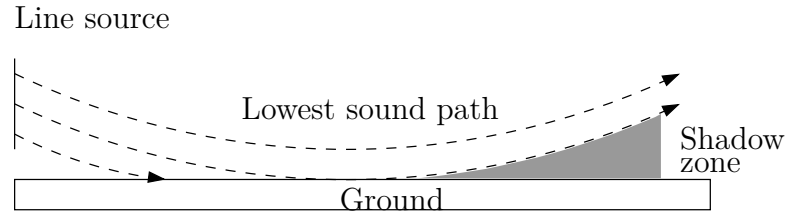
## 2.4 Inhomogeneous atmospheric conditions

The aim of this section is to analyse the sound wave propagation in inhomogeneous atmospheric conditions. In an inhomogeneous atmosphere, the pressure and speed is a function of position. By this fact, the modelling of a sound wave is very complex and depend on various variables such as temperature and wind speed. The following sections give a short introduction to the effect of inhomogeneous atmospheric conditions.

### 2.4.1 Atmospheric refraction

When the wind speed, the temperature and humidity is assumed to be homogeneous in the sound field, the sound is travelling in a straight path. Often this is not true, the wind speed increases logarithmically with the height from the ground to the geostrophic wind [Yang, 2016] in the free troposphere [Rossing, 2014] and the temperature and humidity are inhomogeneous. The geostrophic wind in the free troposphere is located in a height from approximately 1 km above the ground [Rossing, 2014], [Association, 2003]. The inhomogeneous atmospheric condition makes the speed of sound to depend on the height from the ground. This results in a curved sound path and is called as atmospheric refraction. For small distances, the atmospheric refraction has a sparse effect on the sound travelling path, because the speed of sound is much faster than the speed of the wind and the temperature change. Generally distance up to 50 m is often assumed to have no significant refraction effect [de Oliveira, 2012]. For distances larger than 50 m the refraction is assumed to have a significant influence, especially when the sound source and the receiver are close to the ground. Refraction is frequency and distance dependent and is measured in dB excess attenuation. The means of excess attenuation is that only the effect of wind or temperature is considered, all other atmospheric effect is excluded. A

measurement is given in [Piercy et al., 1977] for a point source where the wind speed is 5 m/s. At a distance of 110 m, it is observed that frequency above 400 Hz is refracting where frequency below is rarely effected of refraction. Moreover, at a distance of 615 m the refraction is present in the full measured frequency range from 50 Hz to 3.2 kHz. In the perspective of live concert the intersting distance is the 110 m from the line source array to the audience rather than the 615 m. Both the downwards and upwards refraction is intersting. In the upwards refraction the audience might be in the shadow zone where for the downwards refraction the high frequency reflection from the ground is asumed to be low when the concert area is full of audience. Therefore the high frequency is refracted down into the frontal audience and no reflection of the high frequency propagate to the back part of the audience. The following Figure 2.8 display the phenomena of upwards refraction.



**Figure 2.8:** The figure illustrate the shadow zone occur from a upwards refraction. A line source speaker array contains of many couplet point sources. Every lowest sound path dashed line indicate the lower directional angle of one poins source in the line source array.

The following description is based on the distance of 110 m and upwards refraction. As explained in [Piercy et al., 1977] the refraction at a distance of 110 m is highly frequency dependent. At frequency below 400 Hz the effect is sparse but above the effect is high and may result in 20 dB SPL attenuation at the audience. The reason that the refraction is frequency dependent is that the scale of the wind gradient and temperature gradient close to the ground is small compare to the wavelength of the low frequency [Piercy et al., 1977]. This theory does not follows the shell's law. Shell's law describe the refraction as a layer change in the medium of propagation. Shell's law of refraction is defined as Equation 2.4

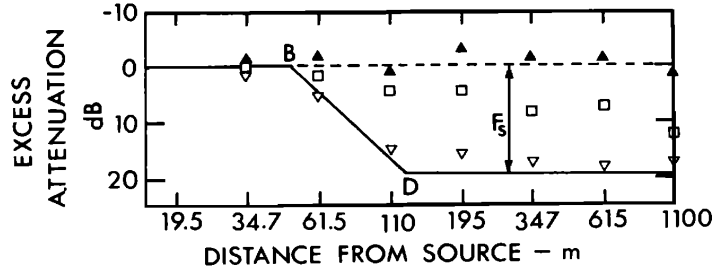
$$\frac{\cos(a_1)}{c_1} = \frac{\cos(a_2)}{c_2} \quad (2.4)$$

Where:

$a_1$	is the input angle in the horizontal plan	[°]
$c_1$	is the sound of speed in the medium of arrival	[m/s]
$a_2$	is the output angle in the horizontal plan	[°]
$c_2$	is the sound of speed in the medium of destination	[m/s]

As it can be seen in shell's law Equation 2.4 the frequency dependency is not a factor and ether shell's law is only a approximation or the frequency dependency does

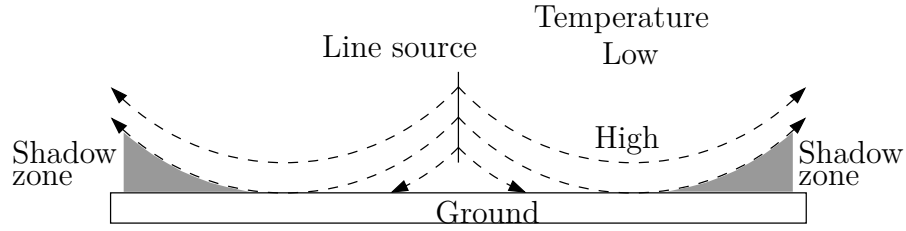
not appear from only laminar wind flow profile. The article [Piercy et al., 1977] only explored frequency up to 3.2 kHz but since the refraction depends on the wavelength, the distance of refraction wave might be much smaller for high frequency. The attenuation with respect to refraction seems to have a saddle attenuation at 20 dB SPL. A measurement in [Piercy et al., 1977] shows the attenuation for the center frequency of 1.2 kHz with  $1/3$  octave band filtered airplane noise. The measurement is interesting with respect to a concert area and is therefore shown in Figure 2.9



**Figure 2.9:** Excess attenuation measured for aircraft noise in the 1.2 kHz  $1/3$  octave band for the ground-to-ground configuration. The vector component of the wind velocity in the direction of propagation for ▲ is 5 m/s, □ is 0 m/s, and ▽ is -5 m/s. The temperature profile is neutral.  $F_s$  is the shielding factor, B is the shadow boundary [Piercy et al., 1977]

The following two paragraphs explain the difference between wind refraction and temperature refraction.

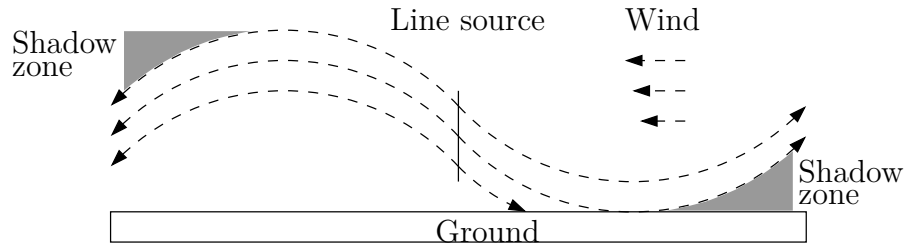
**Temperature** Temperature decreases with respect to height at day time and increases at the night time. The increase or decrease can usually be approximated as a logarithmic function. In the day time, the sun heats the ground even at a cloudy day, and the concert area is full of audience. Therefore, the earth and audience radiate warm air, which makes the temperature at a low height warmer than the temperature at higher height. This phenomenon is named lapse where the upper site is defined as inversion. As explained in section 2.3.1, the speed of sound depends on the temperature. Therefore, at day time, the speed of sound in this situation decays with respect to height. The speed change can be modeled as a change of layer for a plan wave. The output angle of the layer change follows the shell's law. Therefore when the temperature profile is logarithmic the layer change is a function of height and changes the wave direction. The wave direction of the described weather condition results in an upwards refraction. Since the temperature is a scalar quantity uniformly over large area and a function of height, an identical temperature profile is applicable all around the sound source. Therefore the upwards refraction is uniform all along the speaker in the horizontal plane. The following Figure 2.10 illustrates the phenomena where the temperature decays with respect to height.



**Figure 2.10:** Wave refraction in inhomogeneous temperature with lapse profile

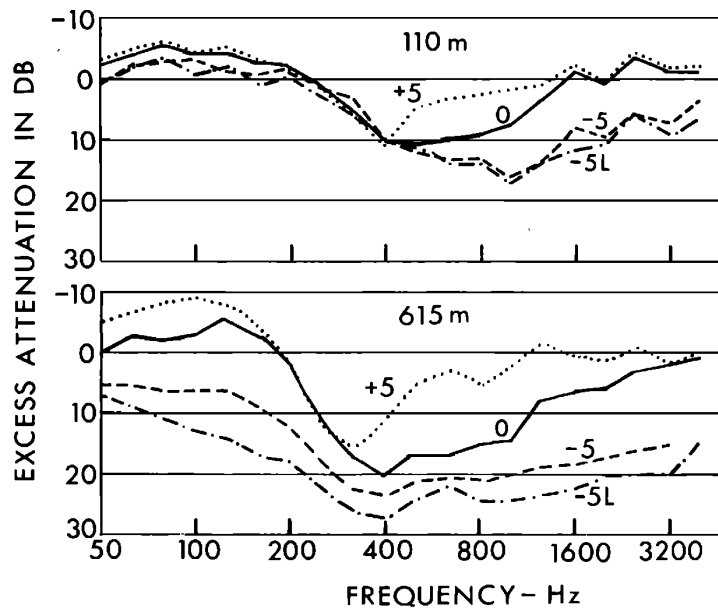
When the temperature profile is reversed, the refraction will be downwards.

**Wind** With respect to the wind speed, a concert area is often a protected area with for example barrier, stage and building. This blockage and the ground friction slows down the wind speed near the ground. Moreover, from nature itself, the wind speed is often logarithmically increased with respect to the height. When the wave is propagation in the same direction as the wind, the atmospheric refraction refracts the sound wave downwards. When the wave propagates against the wind, the atmospheric refraction refracts the sound wave upwards. The following Figure 2.11 shows the phenomena when the wave propagates against the wind.



**Figure 2.11:** Wave refraction in inhomogeneous logarithmically increasing wind profile where the wind gradient points towards left

As shown in Figure 2.8 the refraction is upwards when the wind flows in the opposite direction as the wave propagation. Behind the line array source, the refraction is downwards and is therefore different than for temperature refraction. The refraction of wind is the most dominant at a distance of 110 m. The following Figure 2.12 shows an excess attenuation plot of both inhomogeneous wind and lapse temperature profile.

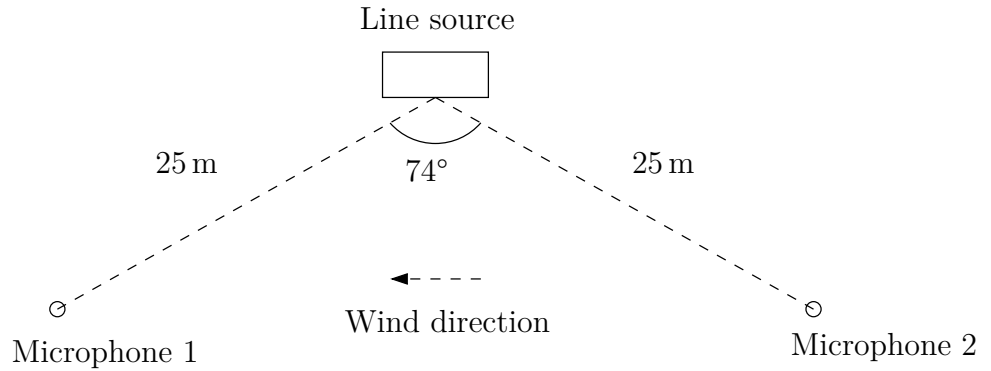


**Figure 2.12:** Observed attenuation of aircraft noise in a ground-to-ground configuration under a variety of weather conditions. Calculated losses from atmospheric absorption and spherical spreading have been subtracted from the attenuation measured in  $1/3$  octave bands for distances of 110 m and 615 m. The numbers on the curves indicate the vector component of the wind velocity in the direction of propagation in m/s. All curves are for neutral conditions of temperature except for those marked L, which are for lapse. [Piercy et al., 1977]

It can be seen in Figure 2.12 that the refraction effect at a distance of 110 m starts at 400 Hz. The reason that sound enters the shadow zone is not fully understood, but one theory is that the shadow boundary wave is diffuse and therefore significant amount of sound energy enters the shadow zone in turbulent weather. In a non turbulent atmosphere condition the SPL inside the shadow zone is attenuated well more than 30 dB SPL. Close to the ground the atmosphere condition is always turbulent because of ground friction. The turbulence wind diffuses the sound wave and change the direction of propagation. The wave that enter the shadow zone can be considered as creeping wave in turbulent scenario. The creeping wave will by them self also refract and therefore be parallel to the the other refraction waves. [Embleton, 1996]

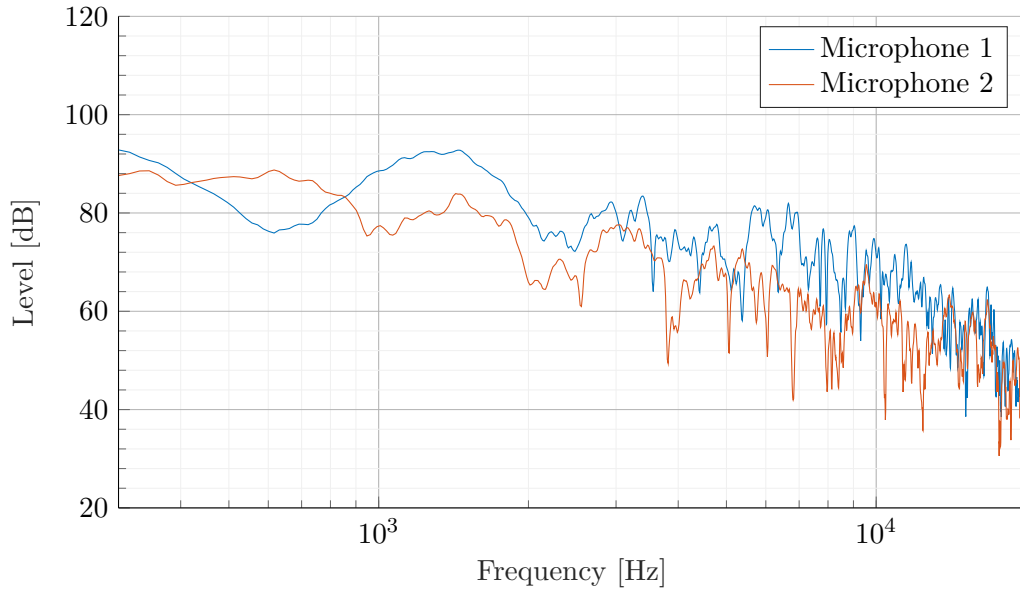
**Oblique- and crosswind** The effect of oblique- and crosswind on acoustical wave propagation in inhomogeneous atmospheric conditions are rarely studied. The author in [Piercy et al., 1977] explain that the refraction is directly zero when crosswind is present, and increase progressive as the direction of propagation deviate from the angle of crosswind.

Since the effect of crosswind on a line source array speaker is rarely studied, a measurement in windy condition is preformed. The measurement is done over mown grass in a large open area used for football. The used measurement technique is done according to [Gunness, 2001] where more than one impulse response is measured and the mean is calculated by align the impulse response in time. The wind was considered as strong for outdoor concert. The wind speed was measured to 14 m/s doing the full measurement. The measurement was done with a four element line source array one meter above the ground. There was used two microphone, where both was situated 23 m from the speaker, beyond the limiting high frequency directional angle of the speaker. The speaker was placed to propagate in direct crosswind and the microphone was placed on both side of the speaker as shown in Figure 2.13



**Figure 2.13:** The figure shows the microphone position versus the position of the line source

The measurement was done according to the description in Appendix A. The measurement was preformed in to step, two measurement within the speaker high frequency directional angle and three outside the speaker high frequency directional angle. The first measurement is shown in Figure 2.14. The other four measurement result can be seen in Appendix A and Appendix B. They show same tendency but the difference between the measurement is more drastical in the measurement outside the high frequency directional angle.



**Figure 2.14:** The graph shows the first transfer function measurement within the high frequency directional angle. The  $L_{eq,5}$  SPL different between the microphones is 4.41 dB SPL (IR\_3)

It can be seen in Figure 2.14 that the general SPL is higher for microphone 1. Furthermore microphone 1 also shows the typical downwards refraction ground reflection interference in the frequency response which is very similar to the calculated ground reflection interference in [Piercy et al., 1977]. Microphone 2 does not have the same strong interference in the low frequency and the general SPL is lower than microphone 1. This indicate upwards refraction and some ground reflection. There was done five measurement, The resulting  $L_{eq,5}$  SPL difference is shown in Table 2.1.

**Table 2.1:** The table shows the measured  $L_{eq,5}$  SPL for all measurement ant the difference between the microphone

Measurement number	Mic 1 $L_{eq,5}$	Mic 2 $L_{eq,5}$	Difference
Measurement 1 Figure A.3	71.82 dB SPL	66.33 dB SPL	5.49 dB SPL
Measurement 2 Figure A.4	69.09 dB SPL	64.69 dB SPL	4.40 dB SPL
Measurement 3 Figure A.5	67.67 dB SPL	63.44 dB SPL	4.23 dB SPL
Measurement 4 Figure B.2	68.10 dB SPL	63.69 dB SPL	4.41 dB SPL
Measurement 5 Figure B.3	68.44 dB SPL	63.62 dB SPL	4.81 dB SPL
Average	69.02 dB SPL	64.35 dB SPL	4.67 dB SPL

As it is shown in Table 2.1, the  $L_{eq,5}$  SPL is higher for microphone 1 in all measurement. Moreover the average  $L_{eq,5}$  SPL difference is 4.67 dB SPL while for A-weighted  $L_{Aeq,5}$  SPL the average difference is 6.17 dB SPL.

**Turbulent** Turbulence is an atmospheric condition where the wind eddies. It often starts with large eddies and progressively breaks down as a cascade effect to smaller and smaller eddies which only depend on the local region. When the eddies are as small as 1 mm the energy disappears in viscosity and thermal conduction. A statistical distribution of the eddies is defined as turbulence. The turbulence wind flow is therefore a chaotic and stochastic process by the nature and is present all the time. It can occur because of change in landscape, stage and blockage, but can also be a process of flow speed increase in the wind, which makes the wind to refract on itself. Turbulence is often high at a windy afternoon day and low under the inverse of lapse. Turbulence also often occurs near the ground because the ground surface slows down the speed of wind by the resistance to the ground. The effect of turbulence on sound is known to make phase and amplitude fluctuation of pure tone. The fluctuation increases with distance until the standard deviation of the phase fluctuation is comparable to  $90^\circ$  [Piercy et al., 1977]. At this point the phase correlation for each sound path is uncorrelated.

## 2.5 sound pressure level during a concert

In Denmark there is no law limiting the SPL during a concert. The only restriction there might be of SPL is area dependent. In a city the local community has limited the total SPL average over 15 min of any event. Out on the countryside, the sound engineer can decide by himself and the often used limit is A-weighted 102 dB SPL average over 15 min.

The standard ?? for long term exposure of high SPL limits the SPL for A-weighted 94 dB SPL average over maximum of 1 h, then the ear needs to have a break to ensure no damage to the hearing. A concert is often more than 1 h with A-weighted 102 dB SPL average. This is at least 8 dB SPL A-weighted more than the regulation recommends. It shall here be clearly understood that the SPL measurement is done in the FOH and the actual exposed SPL is higher for the audience close to the stage.



## Chapter 3

# Summary of Problem Analysis

The analysis started addressing the general used method for live concert. It is found out that live concert today use line source array system to cover the audience area with sound. It is observed that a line source array is flown above the audience at the main stage and at a large concert delay tower line source array is used and placed in the middle of the audience. It is founded that a line source array is constructed of many identically speaker attached to each other in a vertical line. Based on the speaker set up the distance from every audience to the speaker depends on the position in the concert area. Therefore the distance from the speaker and the audience depends on the audience and therefore the sound system have to be optimized such that the SPL coverage is equally in all position. The following analysis in ... founded that a homogenous SPL among all audience is an impossible scenario but the SPL among all audience might be possible to optimized by knowledge of the condition of the atmosphere and make up for the spreading loss.

The experience of the author is included as knowledge for the analysis. It is observed by the author that the wind condition at a concert has a large influence of the experience of the concert. At the low frequency the influence is sparse where for high frequency the effect of the atmospheric condition have a big influence especially when the distance from the speaker is increased. The high frequency blows away for periods and comes back again.

A short introduction to the stereo sweet spot problem is also discussed. It is a hot topic today among some of the large speaker factories but the solution require heavily amount of speakers and flying tools.

The analysis of sound from a line source array started by the ideal geometric spreading loss. Here it is founded that the sound propagation of the line source array highly depend on the height of the source. The line source array propagate differently with respect to frequency. At a certain height of the line source array the propagation is a cylindrical propagation until a certain distance from the source where it starts propagating as a spherical source. In the cylindrical propagation the sound field is defined as near-field while in the spherical propagation the sound field is defined as far field.

In the non ideal senario the line source array propagate in ether a homogeneous atmospherical condition or in an inhomogeneous atmospherical condition.

In the homogeneous atmospherical condition it is founded that the temperature, humidity, pressure and wind influence the sound field. The effect of temperature and humidity is close cubled on sound propagation. When the tamperature is high and the and the humidity is low the air have an large high frequency absorbsion whereas when the temperature and humidity both is eather high or low the absorbsion is much less. The second effect the temperature and humidity have on sound propagation is the speed of sound. The higher the temperature is the higher the sound of speed is. At 0 % humidity the speed of sound incerasses with approximatli 0.6 m/s for every °C increase. The effect of humidity also effect the speed of sound by increaseing speed of sound by incerasing humidity but the speed incerse is neglible compare to the temperature effect. Thudermore effect of speed difference in sound propagation change the wavelendth and therefore the directivity of the speaker is changed, but the change is minimal.

The effect of wind seems to have a sparse effect on the sound propagation when and only when the wind is homogeneous. It is founded that the speed of wind effect the speed of sound. if the wind mowes in the direction of the sound propagation the wind speed is and addition to to speed of sound to find the resulting propagation of speed of sound. In the uppesite cace the speed of sound is lowered. In the case of oblique- or crosswind the effect seems to be unclear for high frequencies. One author has simulated a low frequency spherical source and founded that the only effect is the time of ariavle to the audience.

The impact of the atmospheric pressure is small, and the pressure close to the ground is so high that other limitation of wave propagation limite the SPL before the SPL ritches vacuum in the condensation. When the wave compress the air the wave travelse faster such that the resived wave at the audience is transformed from a sinosoid to a sawtooth wave. The effect produce harmonic distortion where some of the hamonic energy is attunatied be the viscus losses. The distortion is present in SPL lower than 120 dB SPL but is not as critical as the distortion created by the construction of the horn itself. The construction of the horn leave very littel air space within the airgab between the diaphram and the pahse plug. At high level at the phase plug at approximatly 170 dB SPL the air gets turbulent and the soundwave therefore gets distorted.

The audience area is assumed to have high absorbtion in frequency above 1.0 kHz and the while frequency in octave band 31.5 Hz is assumed to have low absorbtion of audience.

In the inhomogeneous atmospherical condition it is founded that refraction of sound wave is one of the biggest challenge for outside sound concert. The refraction orcore because of inhomogeneous speed which is pressent in both inhomogeneous wind and temperature. it is forther founted that the the refraction is frequency dependent and distance dependent. The effect, however, is low at distance lower than 50 m. Depending on the atmospehric condition two kind of refraction was founded,

upwards and downwards. Upwards refraction produce a shadow zone where turbulent atmospheric condition makes creeping wave intro the shadow zone.

For the case of oblique and crosswind the effect of high frequency, The refraction might be zero at direct crosswind but increases prograsiv as the direction of propagation diviate from crosswind. A measurement was done to resurch the effect of crosswind on a line source array. It was founded that the SPL at microphone 1 is generally higher that microphone 2.

(remember to write short about interference while playing mono from stereo setup)

The effect of

Three effect of atmospheric conditions have been observed on the analysis, pure attenuation, lowpass effect and refraction effect



## Chapter 4

# Problem statement

Based on the knowledge founded in chapter 2 and the conclusion drawn from chapter 3 a problem statement can be made. For the rest of the project the following will be the focus.

**research the effect of oblique- and crosswind on wave propagation.**

### 4.1 Deimitation

The following deimitation is made for the search for a solution of .



# Part II

## Test Design





## Chapter 5

# Design



# Part III

## Results



## Chapter 6

# Results



## Chapter 7

# Discussion and conclusion

### 7.1 Conclusion





# Part IV

## Appendix



# Appendix A

## cross wind effect on line source array

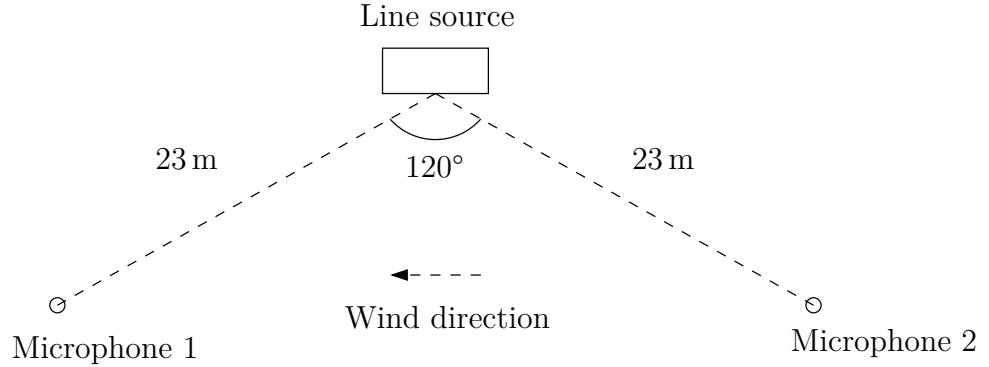
A measurement was made to measure the transfer function differences in two point in cross wind. The used speaker have a horizontal dispersion pattern of  $100^\circ$ .

### Materials and setup

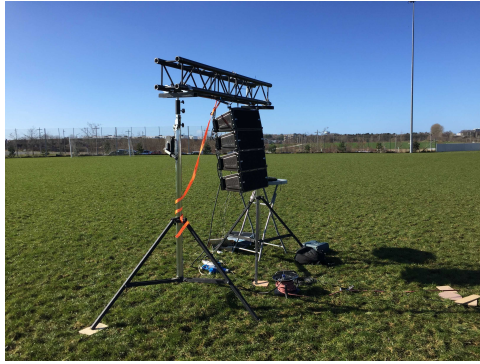
To measure the transfer function in a cross wind situation, the following materials are used:

**Table A.1:** Equipment list

Description	Model	Serial-no	AAU-no
PC	Macbook	W89242W966H	-
Audio interface	RME Fireface UCX	23811948	108230
Microphone	GRAS 26CC	78189	75583
Preamp	GRAS 40 AZ	100268	75551
Microphone	GRAS 26CC	78186	75582
Preamp	GRAS 40 AZ	100267	75550
dB technologies	DVA T4	-	-
Wind measurement tools	Drahtlose Wetterstation	-	2157-45
flying tools	-	-	-



**Figure A.1:** The figure shows the microphone position versus the position of the line source



(a) The picture shows the speaker setup



(b) The figure shows the wind direction

**Figure A.2:** The figures shows the measurement set up for Appendix A and Appendix B

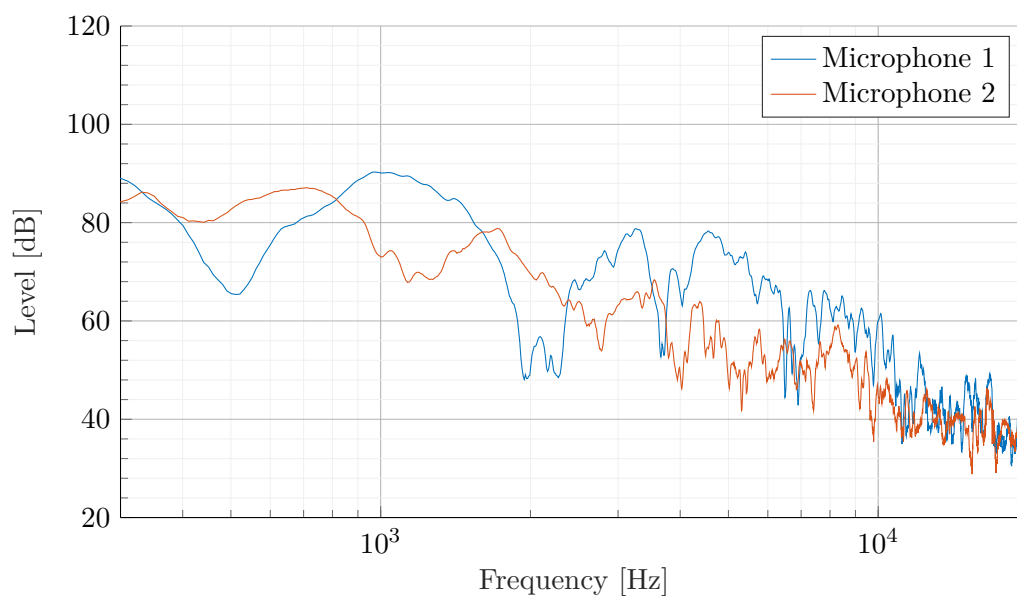
## Test procedure

1. the microphone i calibrated.
2. The wind direction is measured.
3. The materials are set up as in Figure A.1 where the speaker is placed in cross wind direction, such that the frontal wave direction is orthogonal the the wind. The microphone and speaker is connected to the audio interface.
4. The speaker and microphone is placed 1.1 m above the ground
5. the wind direction goes from microphone 2 to microphone 1.
6. 10 sine sweep is performed with a length of 5 s each.
7. The impulse response is calculated and filtered with a 4th order highpass filter at 300 Hz to exclude wind noise.
8. The correlation is calculated for each impulse response to the first impulse response for time alignment [Gunnness, 2001] of both microphone channel.

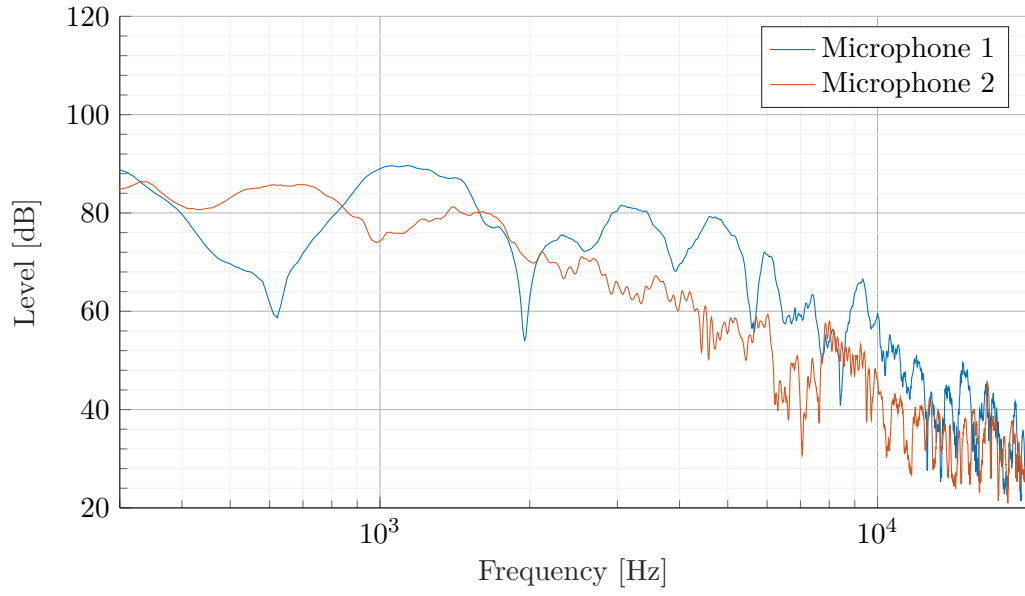
9. The mean impulse response is calculated for the 10 measurement of both microphone.
10. The transfer function is calculated with a 40 sample moving mean filter.
11. The measurement is repeated three times.

## Results

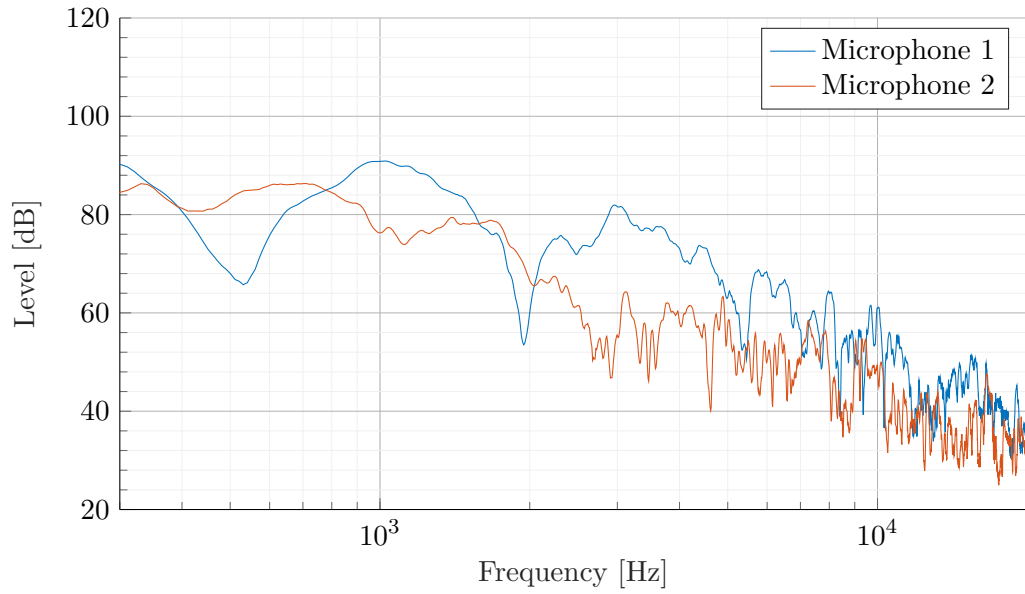
The wind speed was 14 m/s for each measurement and the temperature was 5°. The humidity was not measured.



**Figure A.3:** The graph shows the first transfer function measurement. The  $L_{eq,5}$  Sound Pressure Level (SPL) different between the microphones is 5.49 dB SPL (IR\_6)



**Figure A.4:** The graph shows the second transfer function measurement. The  $L_{eq,5}$  SPL different between the microphones is 4.40 dB SPL (IR\_7)



**Figure A.5:** The graph shows the third transfer function measurement. The  $L_{eq,5}$  SPL different between the microphones is 4.23 dB SPL (IR\_8)

On Figure A.3, Figure A.4 and Figure A.5 it is seen that the general pressure is higher for microphone 1. It is also seen that ground reflection effect is much higher on microphone 1 than microphone 2. This support the theory about upwards refraction of sound wave on microphone 2 and downwards refraction on microphone 1





## Appendix B

# cross wind effect on line source array

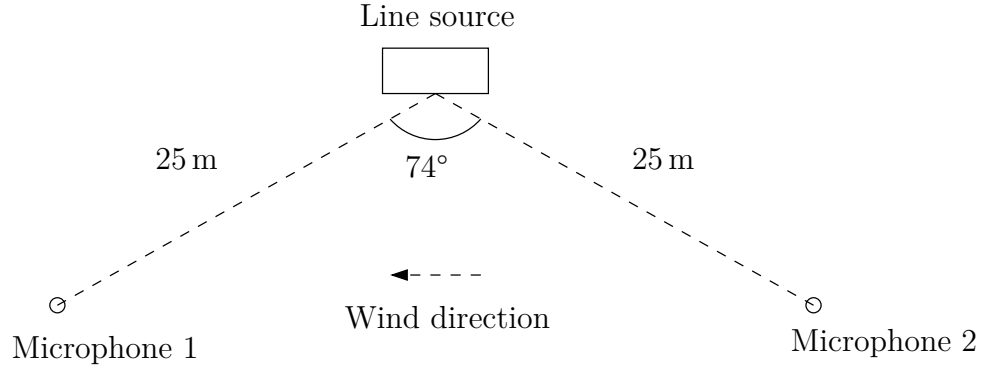
A measurement was made to measure the transfer function differences in two point in cross wind. The used speaker have a horizontal dispersion pattern of  $100^\circ$ .

### Materials and setup

To measure the transfer function in a cross wind situation, the following materials are used:

**Table B.1:** Equipment list

Description	Model	Serial-no	AAU-no
PC	Macbook	W89242W966H	-
Audio interface	RME Fireface UCX	23811948	108230
Microphone	GRAS 26CC	78189	75583
Preamp	GRAS 40 AZ	100268	75551
Microphone	GRAS 26CC	78186	75582
Preamp	GRAS 40 AZ	100267	75550
dB technologies	DVA T4	-	-
Wind measurement tools	Drahtlose Wetterstation	-	2157-45
flying tools	-	-	-



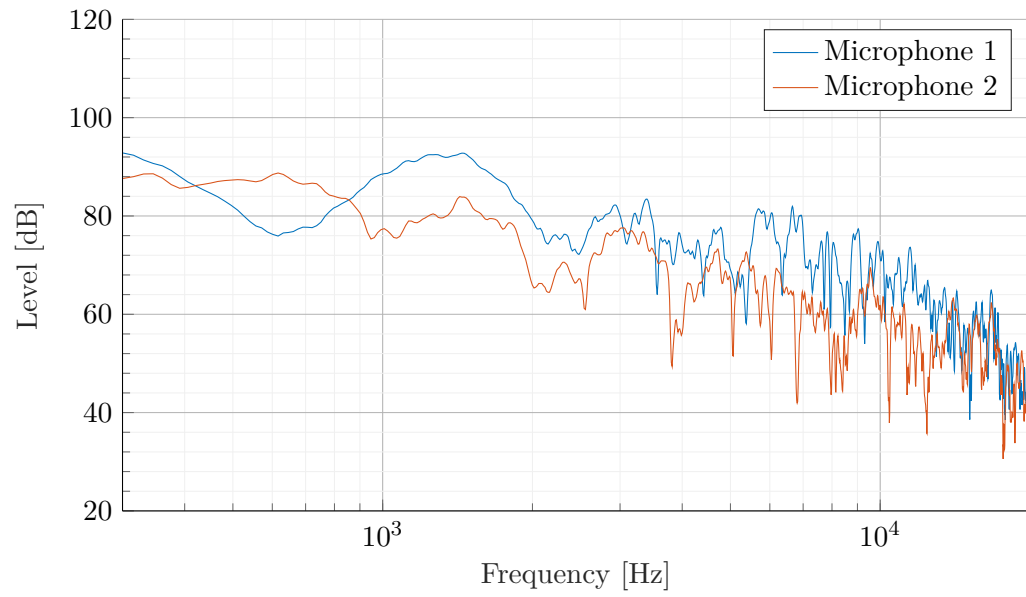
**Figure B.1:** The figure shows the microphone position versus the position of the line source

## Test procedure

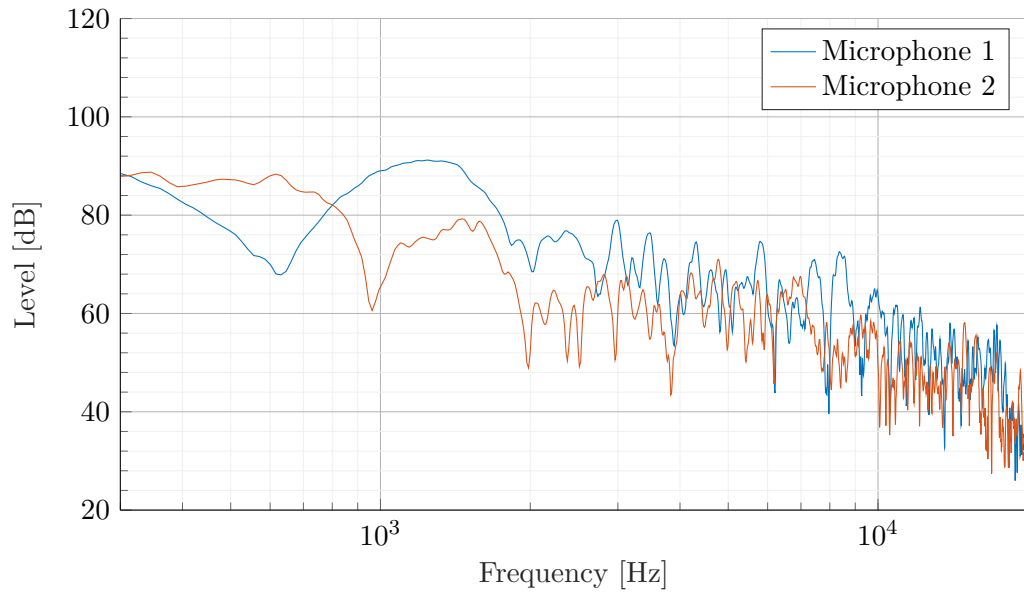
1. the microphone i calibrated.
2. The wind direction is measured.
3. The materials are set up as in Figure B.1 where the speaker is placed in cross wind direction, such that the frontal wave direction is orthogonal the the wind. The microphone and speaker is connected to the audio interface.
4. The speaker and microphone is placed 1 m above the ground
5. the wind direction goes from microphone 2 to microphone 1.
6. 10 sine sweep is performed with a length of 5 s each.
7. The impulse response is calculated and filtered with a 4th order highpass filter at 300 Hz to exclude wind noise.
8. The correlation is calculated for each impulse response to the first impulse response for time alignment [Gunness, 2001] of both microphone channel.
9. The mean impulse response is calculated for the 10 measurement of both microphone.
10. The transfer function is calculated with a 40 sample moving mean filter.
11. The measurement is repeated two times.

## Results

The wind speed was 14 m/s for each measurement and the temperature was 5°. The humidity was not measured.



**Figure B.2:** The graph shows the first transfer function measurement. The  $L_{eq,5}$  SPL different between the microphones is 4.41 dB SPL (IR\_3)



**Figure B.3:** The graph shows the second transfer function measurement. The  $L_{eq,5}$  SPL different between the microphones is 4.81 dB SPL (IR\_5)

On Figure B.2 and Figure B.3 it is seen that the general pressure is higher for microphone 1. It is also seen that ground reflection effect is much higher on microphone 1 than microphone 2. This support the theory about upwards refraction of sound wave on microphone 2 and downwards refraction on microphone 1

# Bibliography

- Association, D. W. I., 2003. *The Geostrophic Wind*, Danish Wind Industry Association. [Website]. Available at: <<http://dr\T1\omst\T1\orre.dk/wp-content/wind/miller/windpower%20web/en/tour/wres/geostro.htm>>. [Accessed 18 feb 2019].
- Ballou, G. Focal Press, Oxford, fourth edition edition, 2008. ISBN 978-0-240-80969-4. doi: <https://doi.org/10.1016/B978-0-240-80969-4.50002-X>. Available at: <<http://www.sciencedirect.com/science/article/pii/B978024080969450002X>>.
- Bauman, P., Urban, M., and Heil, C. Wavefront Sculpture Technology. In *Audio Engineering Society Convention 111*, Nov 2001. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=9813>>.
- Beranek, L. L., 2006. Analysis of Sabine and Eyring equations and their application to concert hall audience and chair absorption. *The Journal of the Acoustical Society of America*, 120(3), pp. 1399–1410. doi: 10.1121/1.2221392. Available at: <<https://doi.org/10.1121/1.2221392>>.
- Bohn, D. A. Environmental Effects on the Speed of Sound. In *Audio Engineering Society Convention 83*, Oct 1987. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=4916>>.
- Corteel, E., Sugden, S., and Montignies, F. Large Scale Open Air Sound Reinforcement in Extreme Atmospheric Conditions (Engineering Brief). In *Audio Engineering Society Conference: 2017 AES International Conference on Sound Reinforcement – Open Air Venues*, Aug 2017. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=19184>>.
- Czerwinski, E., Voishvillo, A., Alexandrov, S., and Terekhov, A., 1999. Air-Related Harmonic and Intermodulation Distortion in Large Sound Systems. *J. Audio Eng. Soc*, 47(6), pp. 427–446. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=12102>>.
- d&b audiotechnik, 2019. *d&b Soundscape*, d&b audiotechnik. [Website]. Available at: <<https://www.dbsoundscape.com/global/en/>>. [Accessed 21 feb 2019].

- de Oliveira, A. F. G. P., 2012. The effect of wind and turbulence on sound propagation in the atmosphere. *Speciale, Instituto Superior Technico Universidade Tecnica de Lisboa*. Available at: <<https://fenix.tecnico.ulisboa.pt/downloadFile/395144345754/dissertacao.pdf>>.
- Embleton, T. F. W., 1996. Tutorial on sound propagation outdoors. *The Journal of the Acoustical Society of America*, 100(1), pp. 31–48. doi: 10.1121/1.415879. Available at: <<https://doi.org/10.1121/1.415879>>.
- Gunness, D. W. Loudspeaker Transfer Function Averaging and Interpolation. In *Audio Engineering Society Convention 111*, Nov 2001. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=9850>>.
- Hornikx, M. and Renterghem, T. V., 2017. Numerical Investigation of the Effect of Crosswind on Sound Propagation Outdoors. *ACTA ACUSTICA UNITED WITH ACUSTICA*, 102, pp. 558–565.
- ISO 9613-1:1993. *Acoustics – Attenuation of sound during propagation outdoors – Part 1: Calculation of the absorption of sound by the atmosphere*.
- L-Acoustics. *KUDO Multi-Mode WST Enclosure*, L-Acoustics. Available at: <<http://www.dreamsound.com/downloadable/211>>.
- L-Acoustics, 2019. *Live Sound*, L-Acoustics. [Website]. Available at: <<https://www.lisa-immersive.com/live-sound/>>. [Accessed 21 feb 2019].
- Levine, D. R., Calza, P., Di Cola, M., Martignon, P., and Chisari, L. Influence of Horn’s Surface Temperature on its Directivity Control. In *Audio Engineering Society Convention 145*, Oct 2018. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=19746>>.
- Ostashev, V. E., Wilson, D. K., Liu, L., Aldridge, D. F., Symons, N. P., and Marlin, D., 2005. Equations for finite-difference, time-domain simulation of sound propagation in moving inhomogeneous media and numerical implementation. *The Journal of the Acoustical Society of America*, 117(2), pp. 503–517. doi: 10.1121/1.1841531. Available at: <<https://doi.org/10.1121/1.1841531>>.
- Piercy, J. E., Embleton, T. F. W., and Sutherland, L. C., 1977. Review of noise propagation in the atmosphere. *The Journal of the Acoustical Society of America*, 61(6), pp. 1403–1418. doi: 10.1121/1.381455. Available at: <<https://doi.org/10.1121/1.381455>>.

- Prospathopoulos, J. M. and Voutsinas, S. G., 2007. Determination of equivalent sound speed profiles for ray tracing in near-ground sound propagation. *The Journal of the Acoustical Society of America*, 122(3), pp. 1391–1403. doi: 10.1121/1.2764476. Available at: <<https://doi.org/10.1121/1.2764476>>.
- Roozen, N. B., Vael, J. E. M., and Nieuwendijk, J. A. Reduction of Bass-Reflex Port Nonlinearities by Optimizing the Port Geometry. In *Audio Engineering Society Convention 104*, May 1998. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=8519>>.
- Rossing, T. *Springer Handbook of Acoustics*. 01 2014. ISBN 978-1-4939-0754-0. doi: 10.1007/978-1-4939-0755-7.
- Vanderkooy, J. Nonlinearities in Loudspeaker Ports. In *Audio Engineering Society Convention 104*, May 1998. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=8432>>.
- Voishvillo, A. Comparative Analysis of Nonlinear Distortion in Compression Drivers and Horns. In *Audio Engineering Society Convention 117*, Oct 2004. Available at: <<http://www.aes.org/e-lib/browse.cfm?elib=12849>>.
- Wong, G. S. K. and Embleton, T. F. W., 1985. Variation of the speed of sound in air with humidity and temperature. *The Journal of the Acoustical Society of America*, 77 (5), pp. 1710–1712. doi: 10.1121/1.391918. Available at: <<https://doi.org/10.1121/1.391918>>.
- Yang, X. *Atmospheric Acoustics*. Walter de Gruyter GmbH Co KG, Berlin, 2016. ISBN 978-3-110-31153-2.