

# Smart TASEP

## Deep Q-Learning in Intelligent Matter Simulations

---

Jonas Märtens

February 8, 2024

LMU Munich

# Introduction

---

## Smart TASEP: Deep Q-Learning in Intelligent Matter Simulations

- TASEP: Totally Asymmetric Simple Exclusion Process
- Smart TASEP: TASEP with intelligent agents  
→ Intelligent Matter Simulations
- Deep Q-Learning: Reinforcement Learning with Neural Networks

cool TASEP teaser pic

## TASEP: Totally Asymmetric Simple Exclusion Process

- Stochastic Process on a grid lattice
- Exclusion: Only one particle per site
- Simple: Jumps only one cell far
- Asymmetric: Only to the right

both TASEP pics

Possible with either

- Periodic Boundary Conditions
- Insertion and Extraction rates at the boundaries

# Modifications

Two modifications (before smart)

## (T)ASEP

- Symmetric in one direction and totally asymmetric in the other
- Directed flow with multiple lanes
- compare traffic flow, kinesin transport
- motivates transport optimization

TASEP pic with speeds, maybe kinesin

## Speeds

- Each particle has a speed
- Speed is probability to jump
- Drawn from a distribution
- If different, jams

Make it Smart!

---

Smart TASEP: TASEP with intelligent agents

- have a goal (e.g. go forward)
- sense the environment
- act according to the goal and the environment
- learn from the environment themselves

→ Intelligent Matter Simulation

→ Reinforcement Learning - reward based

Observation distance pic? Leading to action?

# Deep Q-Learning

---



## Deep Q-Learning Algorithm

- Reinforcement learning with deep neural networks
- Model-free: No knowledge of the environment
- Q-Learning: Value-based method
- Off-policy: Learns from old experiences

DQL components

# Deep Q-Learning: The policy

large picture of flattened observation fed into a neural network, leading to a Q-value for each action

# Deep Q-Learning: Optimization

## How does the network learn?

- Neural Network → backpropagation on loss
- Problem: no target value for Q-Learning
- Solution: Use current best guess as target:  
$$y = r + \gamma \max_{a'} \hat{Q}(s', a')$$
- Target network with soft updates to stabilize learning
- Use gradients for AdamW optimizer
- Replay buffer
  - Sample efficiency
  - Break correlation

backpropagation pic

# Implementation

---

# The smarttasep package

## Features

- Easy installation with `pip`
- Fully Customizable
  - Environment size
  - Reward function
  - Network architecture
  - Hyperparameters
  - Training parameters
  - Algorithm choices
- Real-time visualization
- Interactive evaluation
- Management of experiments

## smarttasep components

- `smarttasep.GridEnv`: The 2D (T)ASEP environment
- `smarttasep.DQN`: The neural network
- `torchrl.ReplayBuffer`: Efficient, tensor-based replay buffer
- `smarttasep.Trainer`: Wrapper class for training, simulation and experiment management
- `smarttasep.Playground`: Real-time interactive evaluation of trained agents
- `smarttasep.EnvParams`, `smarttasep.Hyperparams`: Configuration classes

# The smarttasep package: Examples

Let's have a look at some examples! (show usage videos)

# Hyperparameter Optimization

For each experiment, the Hyperparameters should be optimized.

## Parameters

- **Learning rate** of the AdamW optimizer.
- **Discount factor**  $\gamma$ .
- **Replay buffer size**.
- **Batch size** for training.
- **Target network update rate**  $\tau$ .
- **Exploration-exploitation tradeoff** via the decay constant  $\eta$  of the exploration rate  $\epsilon(t) = \epsilon_{\text{end}} + (\epsilon_{\text{start}} - \epsilon_{\text{end}})e^{-n_{\text{steps}}/\eta}$ .
- **Neural network architecture** (number of hidden layers and neurons per layer).
- **Activation function** of the neural network.

# Hyperparameter Optimization: Example

hidden layers sizes example



Baseline

---

## Goals

- Current optimization
- General insights into intelligent matter simulations

## Experiments

1. **Baseline:** Classical 2D TASEP with speeds
2. **Naive current optimization:** Hard-coded agents
3. **Smart TASEP:** Deep Q-Learning agents with slightly different goals
  - **Simple reward:** Go forward
  - **Complex reward:** Go forward while forming lanes

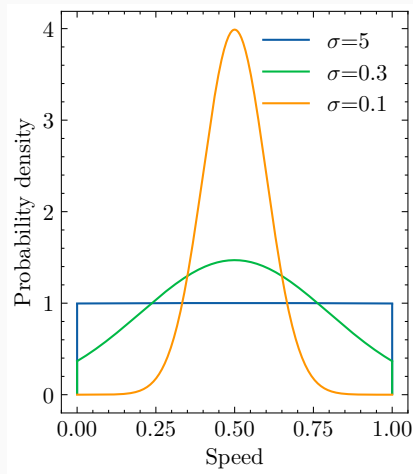
## Setup

- Classical 2D TASEP
- Periodic boundary conditions
- Checkerboard configuration

# Results: Baseline

## Setup

- Classical 2D TASEP
- Periodic boundary conditions
- Checkerboard configuration
- Normally distributed speeds

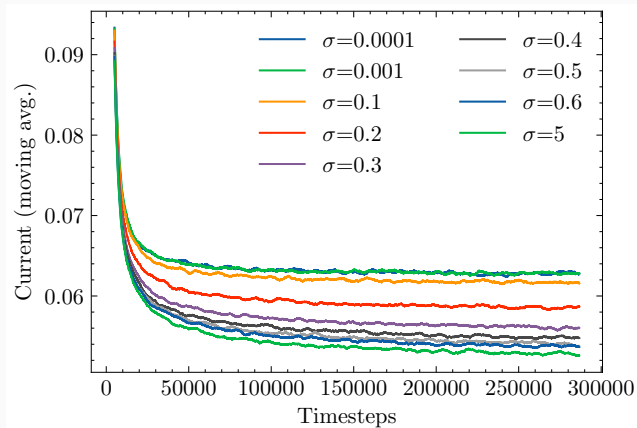


Speeds of particles in the baseline experiment.

# Results: Baseline

## Setup

- Classical 2D TASEP
- Periodic boundary conditions
- Checkerboard configuration
- Normally distributed speeds
- Waiting for steady state

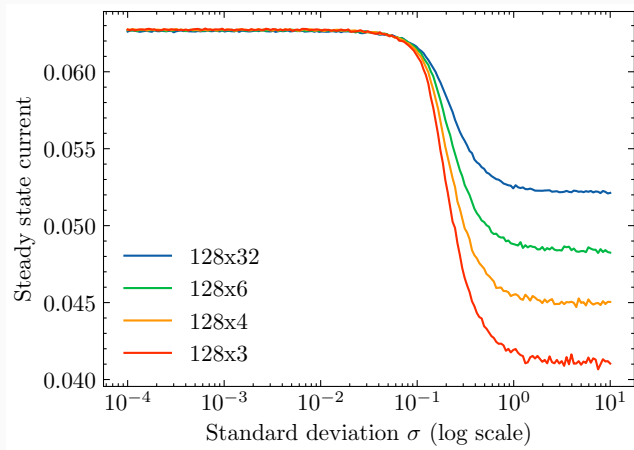


Equilibration of the current

# Results: Baseline

## Setup

- Classical 2D TASEP
- Periodic boundary conditions
- Checkerboard configuration
- Normally distributed speeds
- Waiting for steady state
- Measuring average current

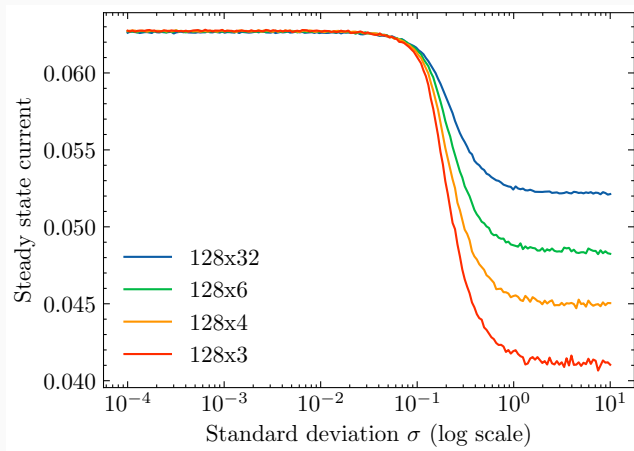


Steady state current as a function of  $\sigma$  for different system sizes.  
800 runs and 150k steps averaged.

## Conditions for a forward move

1. randomly picked cell is occupied ( $p_{\text{occ}} = \rho$ )
2. speed allows move ( $p_{\text{spd}} = \bar{v} = \mu$ )
3. forward direction is picked ( $p = 0.5$ )
4. next cell is empty ( $p_{\text{emp}} = 1 - \rho$ )<sup>\*</sup>

$$\begin{aligned}\implies \langle J \rangle &= p \cdot \mu \cdot \rho \cdot (1 - \rho) \\ &= 0.0625\end{aligned}$$



Steady state current as a function of  $\sigma$  for different system sizes.

## Naive Policy

---



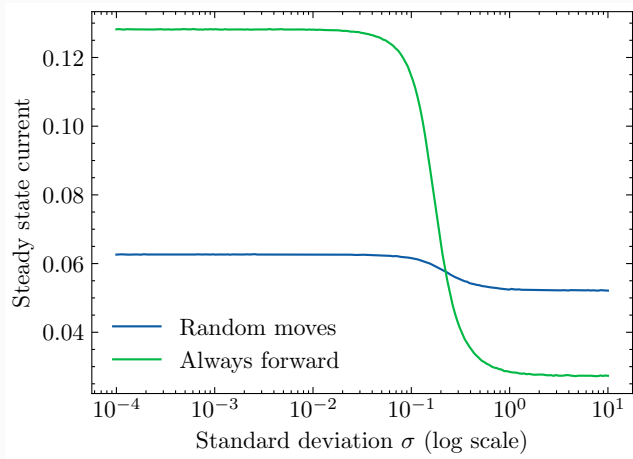
# A Naive Policy

## Just go forward?

- $p_{\text{fwd}} = 1, p_{\text{up/down}} = 0$
- starting in checkerboard configuration
- no messy mixing
- bad for high  $\sigma$
- optimum for low  $\sigma$ ?

$$\begin{aligned}\max \langle J \rangle &= \max (p_{\text{occ}} \cdot p_{\text{spd}} \cdot p_{\text{fwd}} \cdot p_{\text{emp}}) \\ &\leq \rho \cdot \mu \cdot 1 \cdot \max(p_{\text{emp}})\end{aligned}$$

$$\text{and } 0.5 \leq \max(p_{\text{emp}}) < 1$$



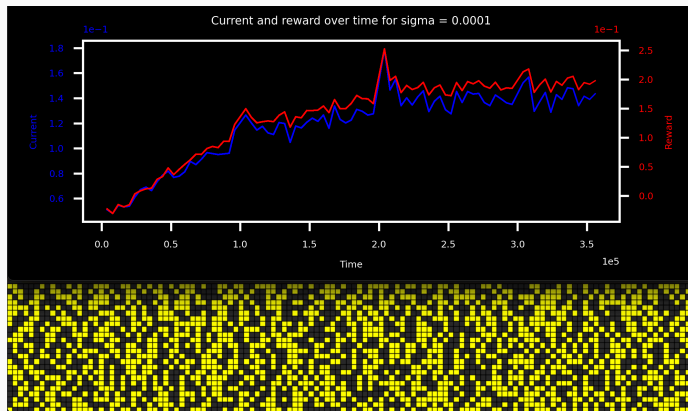
Naive policy

# Smarticles

---

## Simple reward

- Positive reward for going forward
- Negative reward for occupied destination
- Zero reward for going up or down or staying
- Small negative reward for blocking others

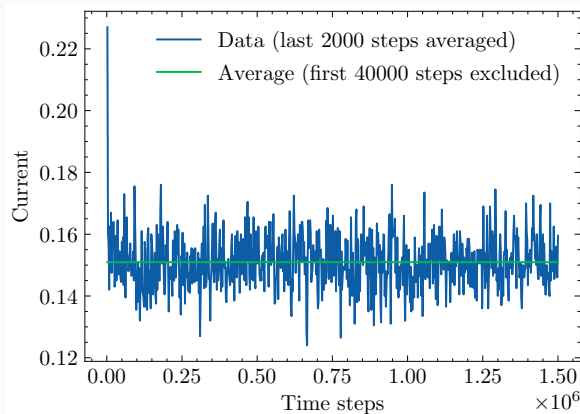


Screenshot of the first smarticle training

# Smarticles: Equal speeds

## Resulting current

- $\langle J \rangle \approx 0.152$
- +143% compared to baseline (0.0625)
- +22% compared to naive policy (0.125)

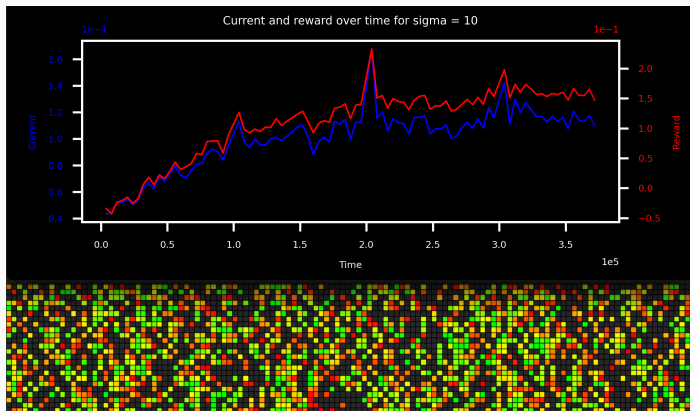


Steady state current over time for the trained smarticles.

# Smarticles: Uniform speed distribution

Similar reward,  $\sigma = 10$

- Same setup as before
- Negative reward for blocking proportional to speed

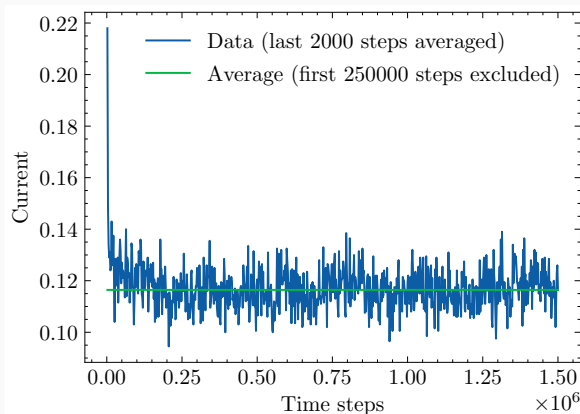


Screenshot of the second smarticle training

# Smarticles: Uniform speed distribution

## Resulting current

- $\langle J \rangle \approx 0.117$
- +125% compared to baseline (0.052)
- Lower than with equal speeds (we will see why)



Steady state current over time for the trained smarticles.

# Smarticles: Model Analysis

What did the smarticles learn? (Playground video)

# Smarticles: Why Global Structures

## Observation

- So far, the system still looks messy
- Only individual behavior
- Compare highway: Fast lane and slow lane → Could be beneficial also in TASEP

messy tasep pic fast lane slow lane picture

## Potential

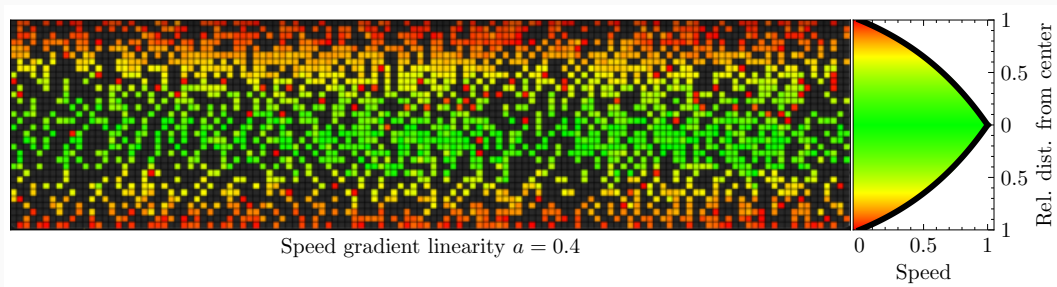
- Less jamming
- Directed flow without dispersion
- Inhomogeneous density



# Smarticles: Hard-coded Lanes

Approach 1: Hard code the lanes, supply smarticles with lane information

$$\Delta y = 1 - a \cdot \left( \frac{1+a}{a} \right)^v + a$$

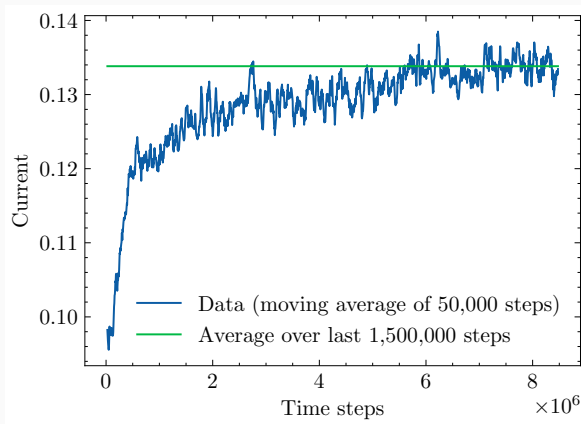


Learned smarticle behavior with the hard-coded lanes reward function (left), and the speed gradient mapping (right).

# Smarticles: Hard-coded Lanes - Results

## Resulting current

- $\langle J \rangle \approx 0.134$
- +157% compared to baseline (0.052)
- +15% compared to previous policy (0.117)
- long equilibration time



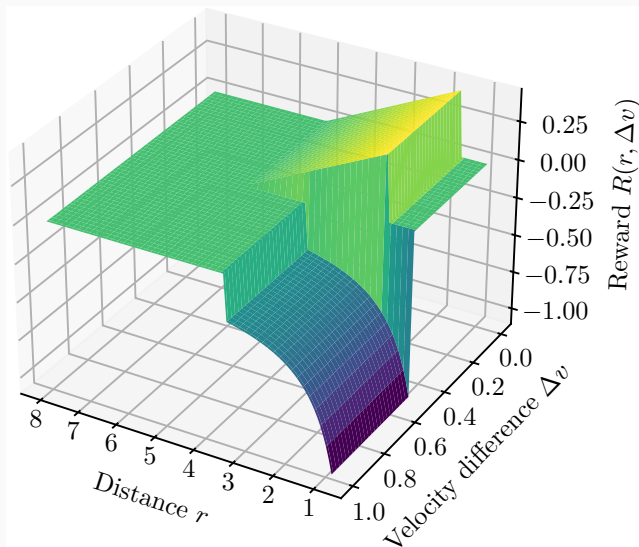
Current over time for the trained smarticles.

Approach 2: Let the smarticles learn the lanes themselves from local “interactions”

$$V(r, \Delta v) = \begin{cases} -0.125 \cdot r + 0.625 & \text{if } \Delta v < 0.5 \text{ and } 1.5 < r \leq 5 \\ -0.75 \cdot r^{-1.3} - 0.15 & \text{if } \Delta v \geq 0.5 \text{ and } r \leq 3.5 \\ 0 & \text{otherwise} \end{cases}$$

## Modifications

1. Binary speed distribution
2. Different neural networks



Visual representation of the lane reward function / “potential”

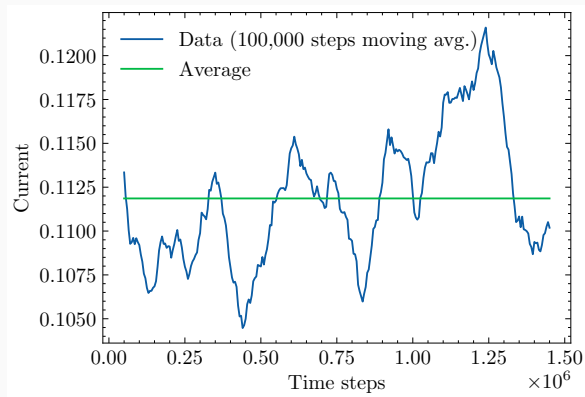
# Smarticles: Self-organized Lanes - Results

Let's see it in action! (lane formation video)

# Smarticles: Self-organized Lanes - Results

## Resulting current

- $\langle J \rangle \approx 0.112$
- baseline  
 $J = 0.4 \cdot (1 - 0.4) \cdot 0.6 \cdot 0.5 = 0.072$
- +56% compared to baseline
- lower than previous policies
- quicker equilibration
- fluctuations seem higher than they are
- proof of concept, room for improvement



Current over time for the trained smarticles.

## Conclusion and Outlook

---

# Conclusion and Outlook

Introduction  
○○○

Make it Smart!  
○○

Deep Q-Learning  
○○○

Implementation  
○○○○

Baseline  
○○○

Naive Policy  
○○

Smarticles  
○○○○○○○○○○○○○○

Conclusion and Outlook  
●