

b)

$$\ddot{y} - 4y = \dot{u} - 2u$$

$$\mathcal{L} Y(s) - 4 Y(s) = s U(s) - 2 U(s)$$

$$(s^2 - 4) Y(s) = (s - 2) U(s)$$

$$H(s) = \frac{Y(s)}{U(s)} = \frac{\cancel{(s-2)}}{\cancel{(s-2)}(s+2)}$$

$$H(s) = \frac{1}{s+2}$$

 $\downarrow \mathcal{L}^{-1}$ 

$$h(t) = e^{-2t}$$