

$$4) c) \quad y(t) = \sin(u(t))$$

$$\text{Let } u(t) = \alpha t$$

$$y_1 = y(u(t)) = \sin(\alpha t)$$

$$y(u(t-t_0)) = \sin(\alpha(t-t_0)) = \sin(\alpha t - \alpha t_0)$$

$$y_1(t-t_0) = \sin(\alpha t - t_0)$$

$$\underline{y(u(t-t_0)) \neq y(u(t)) - t_0}$$

Time Invariant

$$\forall t_0 \neq \pm n\pi, \\ n=0,1,\dots$$

$$d) \quad \dot{y} = \underbrace{-t}_{A(t)} y(t) + u(t), \quad t \geq 0, \quad y(0) = 0$$

state coefficient is not constant

$$A(t) = t \Rightarrow \underline{\text{Time-Invariant}}$$