

# MECH 6323 - HW 07

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## Problem 1

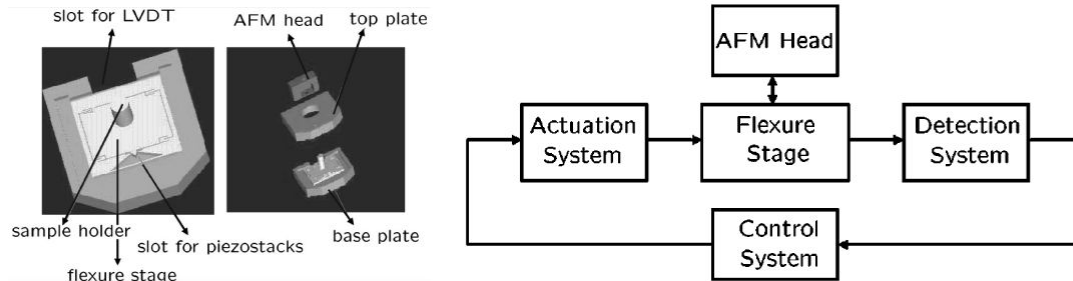


Fig. 1: Nanopositioning flexure stage (left) and feedback diagram (right); figures adapted from Salapaka et. al, *Rev. Sci. Instrum.* 2002.

```
clear
close all
```

## Part a

Load data: G, w, nano\_sp.Gfr

```
% load('C:\Users\Jonas\OneDrive - The University of Texas at Dallas\2022_Spring\MECH6323\Homework\
nano_rsp = load('npresp.mat')
```

```
nano_rsp = struct with fields:
    Gfr: [1x1 frd]
    w: [1748x1 double]
    G: [1x1x1748 double]
```

```
omega_min = min(nano_rsp.w);
omega_max = max(nano_rsp.w);
```

## Estimate system transfer function

```
tf_order = 6;
G_sys = fitfrd(nano_rsp.Gfr, tf_order)
```

```
G_sys =
```

```
A =
    x1    x2    x3    x4    x5    x6
x1 -1468   8540 -8540   8540 -8540   4270
x2 -4681   6559 -3757   3757 -3757   1878
x3 -2174   4348 -7150   9952 -9952   4976
x4 -4695   9390 -9390   6588 -3786   1893
x5 -1687   3374 -3374   3374 -6176   4489
x6 -3428   6856 -6856   6856 -6856   625.7
```

```
B =
```

```

        u1
x1  5.156
x2  11.36
x3  16.7
x4  18.15
x5  11.59
x6  11.18

```

```

C =
      x1      x2      x3      x4      x5      x6
y1  114.1 -228.1  228.1 -228.1  228.1 -114.1

```

```

D =
      u1
y1  0.08876

```

Continuous-time state-space model.

```
G_sys_tf = tf(G_sys)
```

```

G_sys_tf =
      0.08876 s^6 - 876.1 s^5 + 1.136e07 s^4 - 4.345e10 s^3 + 4.097e14 s^2 - 2.095e17 s + 3.082e21
-----
      s^6 + 1021 s^5 + 7.856e07 s^4 + 5.129e10 s^3 + 1.342e15 s^2 + 3.65e17 s + 5.421e21

```

Continuous-time transfer function.

```
G_sys_zpk = zpk(G_sys)
```

```

G_sys_zpk =
      0.088762 (s^2 + 526.7s + 9.417e06) (s^2 + 276.6s + 4.494e07) (s^2 - 1.067e04s + 8.207e07)
-----
      (s^2 + 186.2s + 6.029e06) (s^2 + 482.7s + 1.6e07) (s^2 + 352.5s + 5.621e07)

```

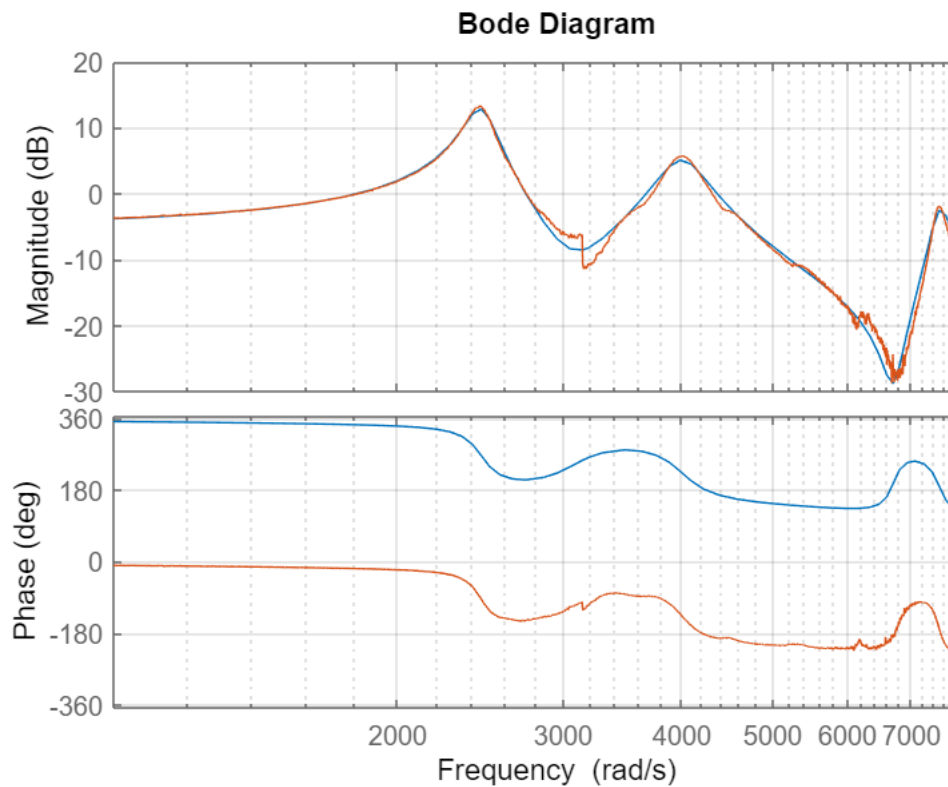
Continuous-time zero/pole/gain model.

## **Bode Diagram Data**

```

figure()
bode(G_sys)
hold on
bode(nano_rsp.Gfr)
grid on
xlim([omega_min, omega_max])

```



Clearly this plot is a good estimation for the frequency response of the system, noting that the phase of the system is offset by a 360 degree phase shift (which implies a need for another set of integrators)

## Part b

### PI - Implimentation

```
PM_min = 75;
opt = pidtuneOptions( ...
    'PhaseMargin', PM_min, ...
    'DesignFocus', 'disturbance-rejection' ...
)
```

```
opt =
    pidtune with properties:

        PhaseMargin: 75
        NumUnstablePoles: 0
        DesignFocus: 'disturbance-rejection'
```

```
[C_pi, info] = pidtune(G_sys, 'pi', opt)
```

```
C_pi =
```

```

    1
Ki * ---
    s
```

```
with Ki = 240
```

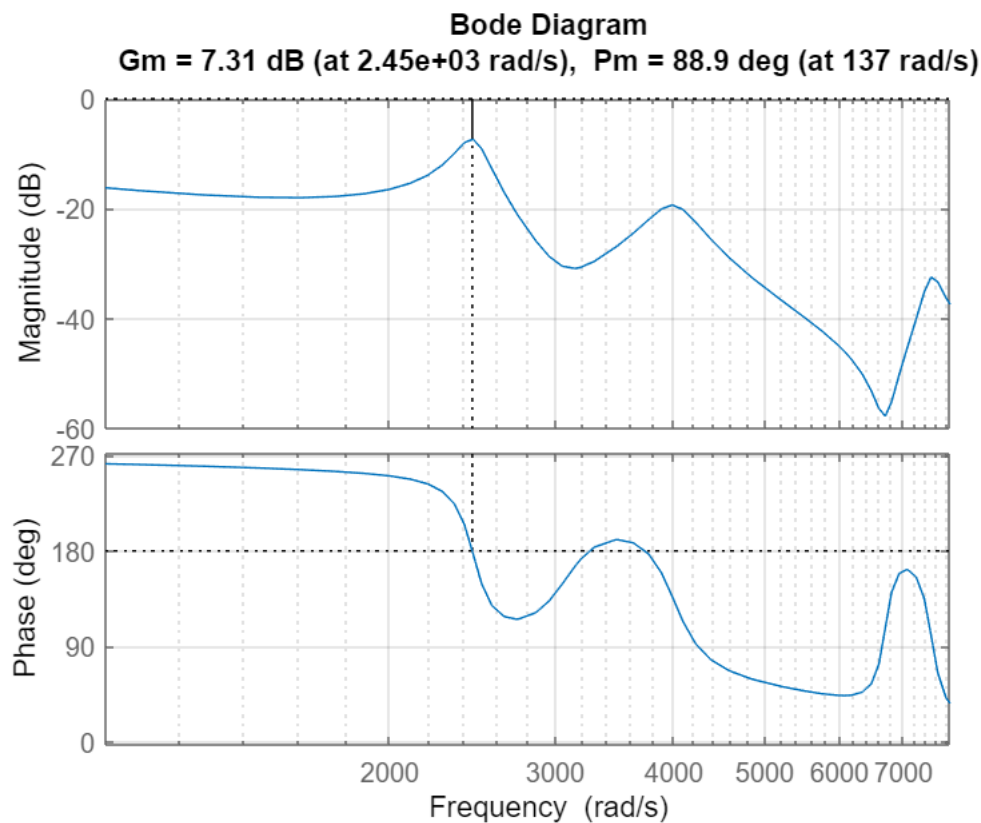
```
Continuous-time I-only controller.
info = struct with fields:
    Stable: 1
    CrossoverFrequency: 136.5946
    PhaseMargin: 88.9408
```

```
allmargin(C_pi * G_sys)
```

```
ans = struct with fields:
    GainMargin: [2.3213 31.8215 13.3190]
    GMFrequency: [2.4472e+03 3.2556e+03 3.7346e+03]
    PhaseMargin: 88.9408
    PMFrequency: 136.5946
    DelayMargin: 0.0114
    DMFrequency: 136.5946
    Stable: 1
```

## Bode Diagram of Margin

```
figure
margin(C_pi * G_sys_tf)
xlim([omega_min, omega_max])
grid on
```



As a result, the single only integral controller is a pretty weird result. However, looking at the results it does make sense.

## Sensitivity Transfer Function

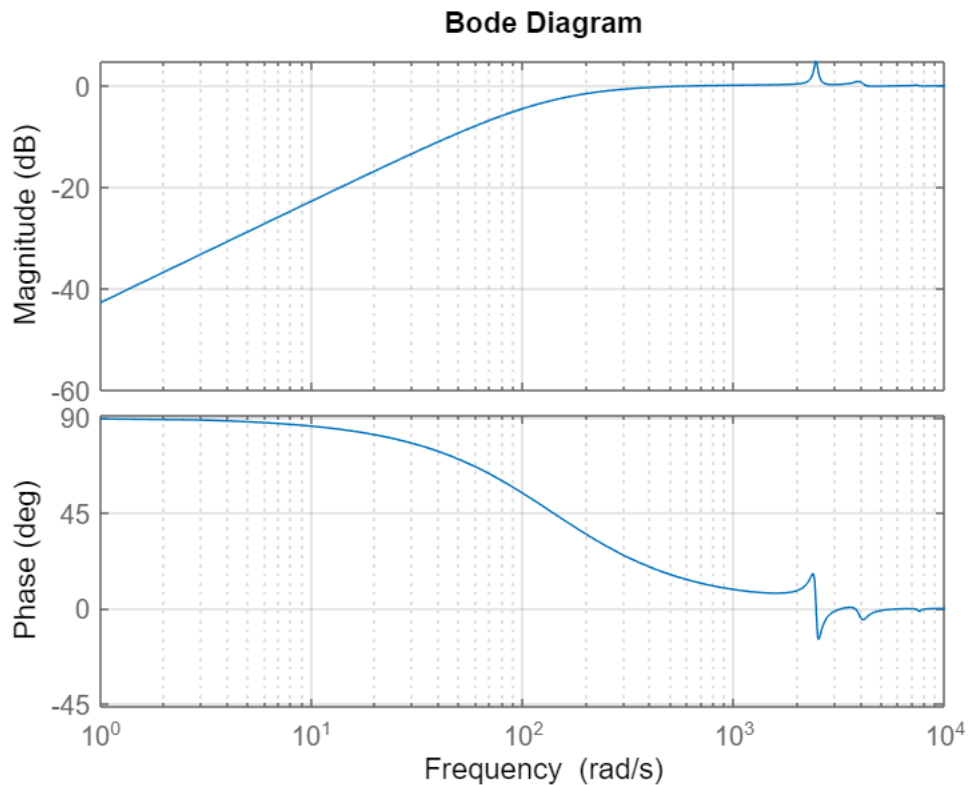
```
S_pi = zpk(1/(1+C_pi*G_sys))
```

S\_pi =

$$\frac{s (s^2 + 186.2s + 6.029e06) (s^2 + 482.7s + 1.6e07) (s^2 + 352.5s + 5.621e07)}{(s+138.6) (s^2 + 108.1s + 5.995e06) (s^2 + 446.2s + 1.584e07) (s^2 + 349.8s + 5.615e07)}$$

Continuous-time zero/pole/gain model.

```
figure
bode(S_pi)
grid on
```



### Bandwidth Calculation

```
bw_threshold = -3; %db
bw = getGainCrossover(S_pi, db2mag(bw_threshold))
```

bw = 134.4361

### Double Integrator implimentation

Instead we can also include an additional integrator into the controller, i.e.

```
G_int = tf(1,[1, 0]);
[C_pi_int, info] = pidtune(G_int * G_sys, 'pi', opt)
```

C\_pi\_int =

$$K_p + K_i * \frac{1}{s}$$

with  $K_p = 271$ ,  $K_i = 1.06 \times 10^4$

Continuous-time PI controller in parallel form.

info = struct with fields:

Stable: 1

CrossoverFrequency: 159.0729

PhaseMargin: 75.0000

```
allmargin(C_pi_int * G_int * G_sys)
```

ans = struct with fields:

GainMargin: [0 2.0518 27.8933 11.9425]

GMFrequency: [0 2.4457e+03 3.2626e+03 3.7282e+03]

PhaseMargin: 75.0002

PMFrequency: 159.0759

DelayMargin: 0.0082

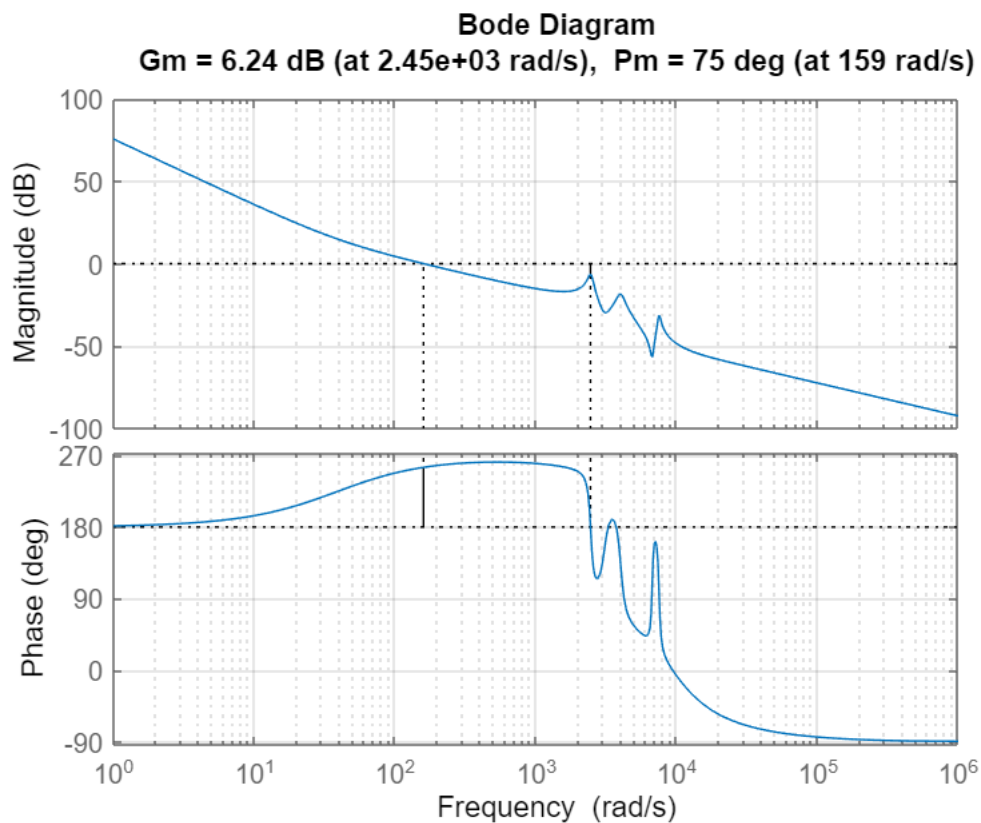
DMFrequency: 159.0759

Stable: 1

figure

```
margin(C_pi_int * G_int * G_sys)
```

```
grid on
```



### Sensitivity Transfer Function

```
S_pi_int = zpk(1/(1+C_pi_int*G_int*G_sys))
```

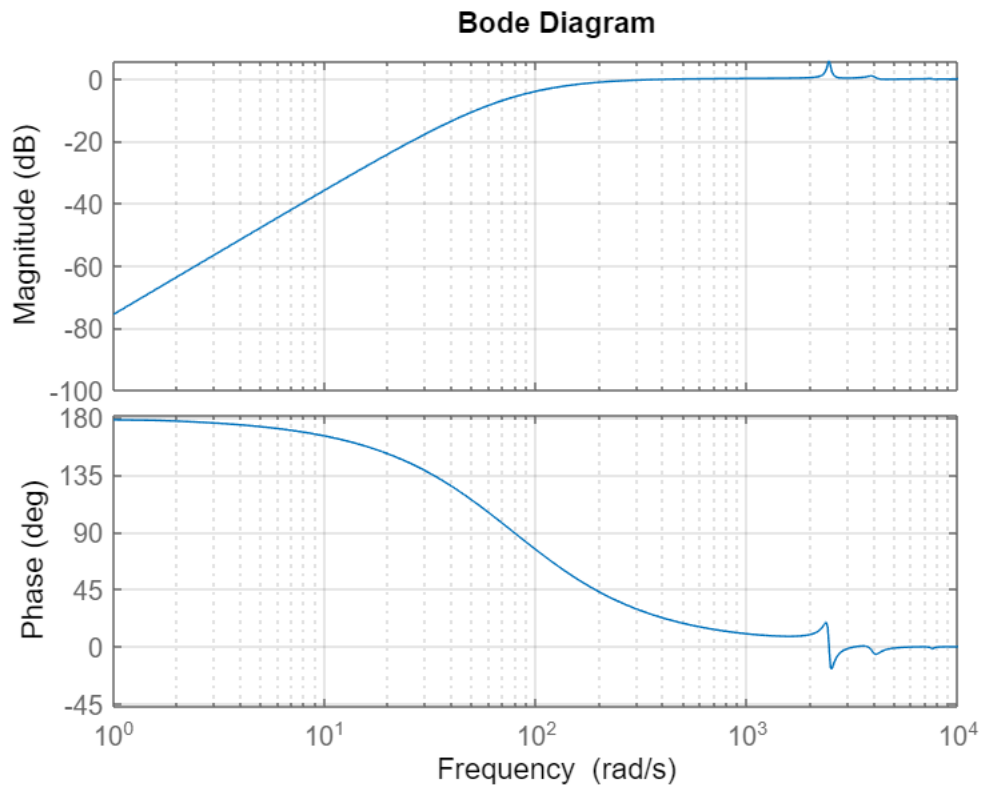
S\_pi\_int =

$$s^2 (s^2 + 186.2s + 6.029 \times 10^6) (s^2 + 482.7s + 1.6 \times 10^7) (s^2 + 352.5s + 5.621 \times 10^7)$$

-----  
 $(s^2 + 156.3s + 6120) (s^2 + 97.81s + 5.989e06) (s^2 + 441.9s + 1.582e07) (s^2 + 349.5s + 5.614e07)$

Continuous-time zero/pole/gain model.

```
figure
bode(S_pi_int)
grid on
```



### Bandwidth Calculation

```
bw_threshold = -3; %db
bw = getGainCrossover(S_pi_int, db2mag(bw_threshold))
```

bw = 117.7945

The bandwidth of this method is not as great as the original PI implimenation. I think the performance is better in certain situation though and may be worth implimenting (even if isn't really a PI controller)

### Part c

## Final Parts

```
fname = matlab.desktop.editor.getActiveFilename;  
export(fname, 'MECH6323_HW07.pdf')
```

```
ans =  
'C:\Users\Jonas\OneDrive - The University of Texas at Dallas\2022_Spring\MECH6323\Homework\HW07\MECH6323_HW07.pdf'
```