

MECH 6323 - Homework 2

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Problem 2

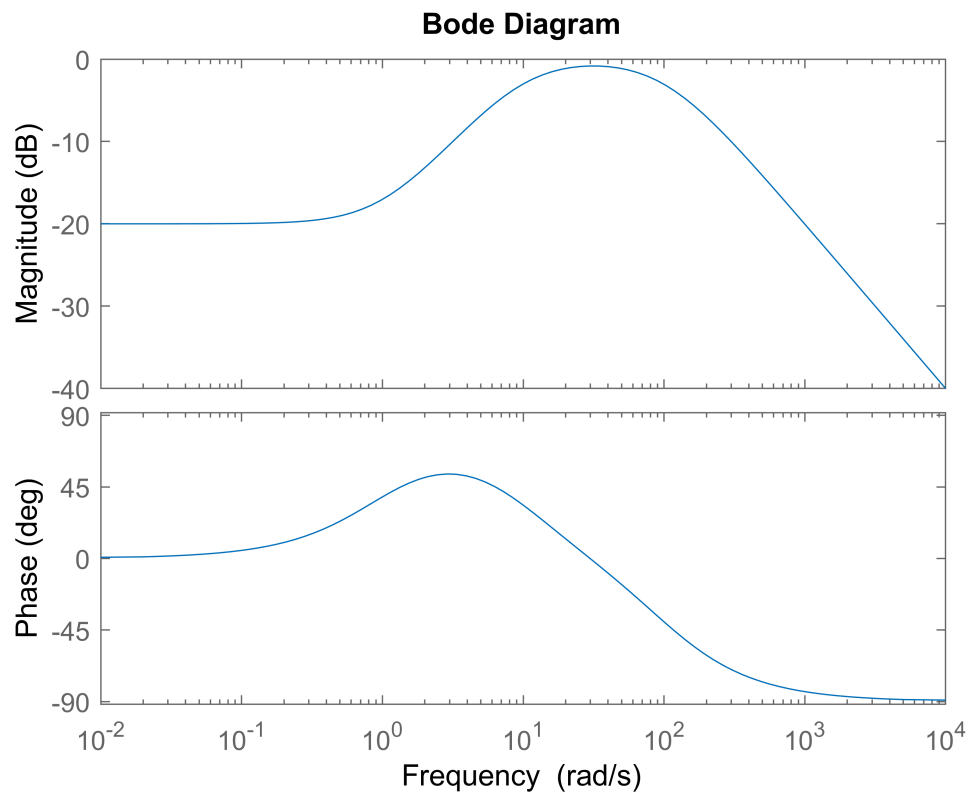
```
% a
G = zpk(tf([100 100],[1 110 1000]))
```

G =

$$\frac{100 (s+1)}{(s+100) (s+10)}$$

Continuous-time zero/pole/gain model.

```
bode(G)
```



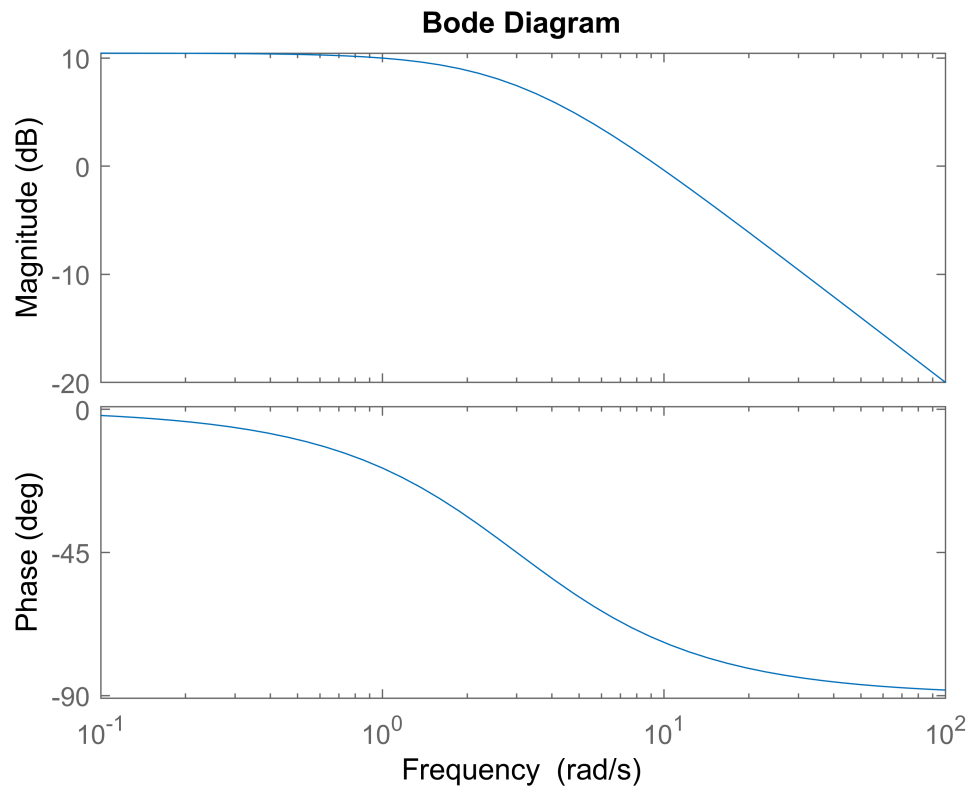
```
% b
G = zpk(tf([10 0],[1 3 0]))
```

G =

$$\frac{10 s}{s (s+3)}$$

Continuous-time zero/pole/gain model.

```
bode(G)
```



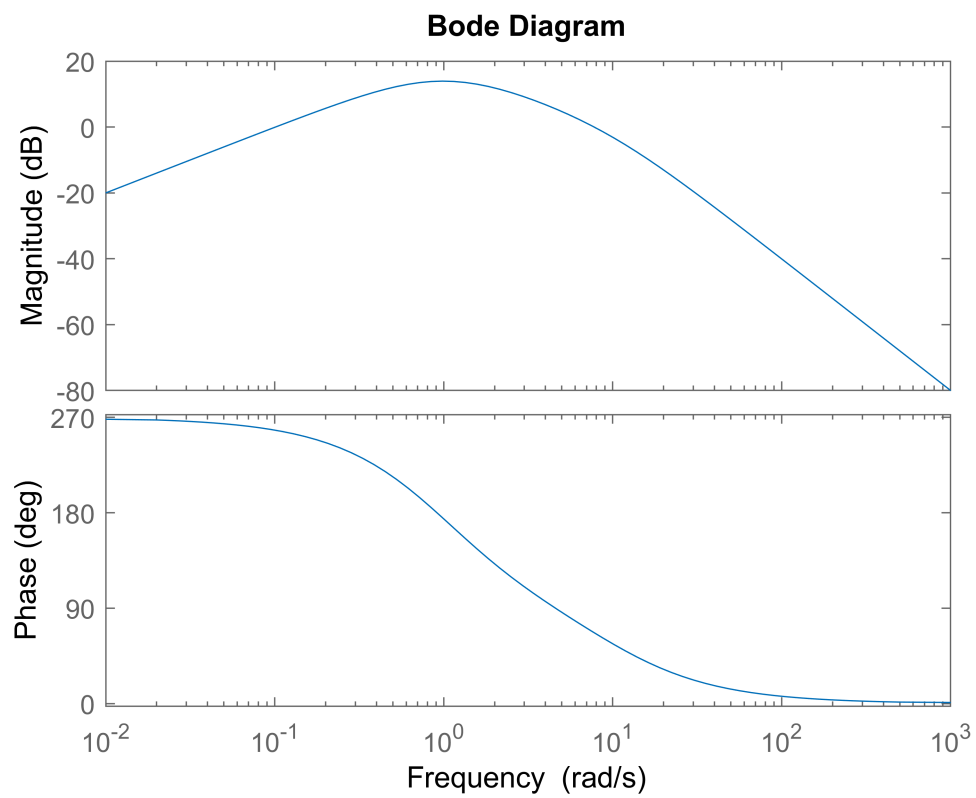
```
% c  
G = zpk([0],[-1 -1 -10],-100)
```

G =

$$\frac{-100 s}{(s+1)^2 (s+10)}$$

Continuous-time zero/pole/gain model.

```
bode(G)
```



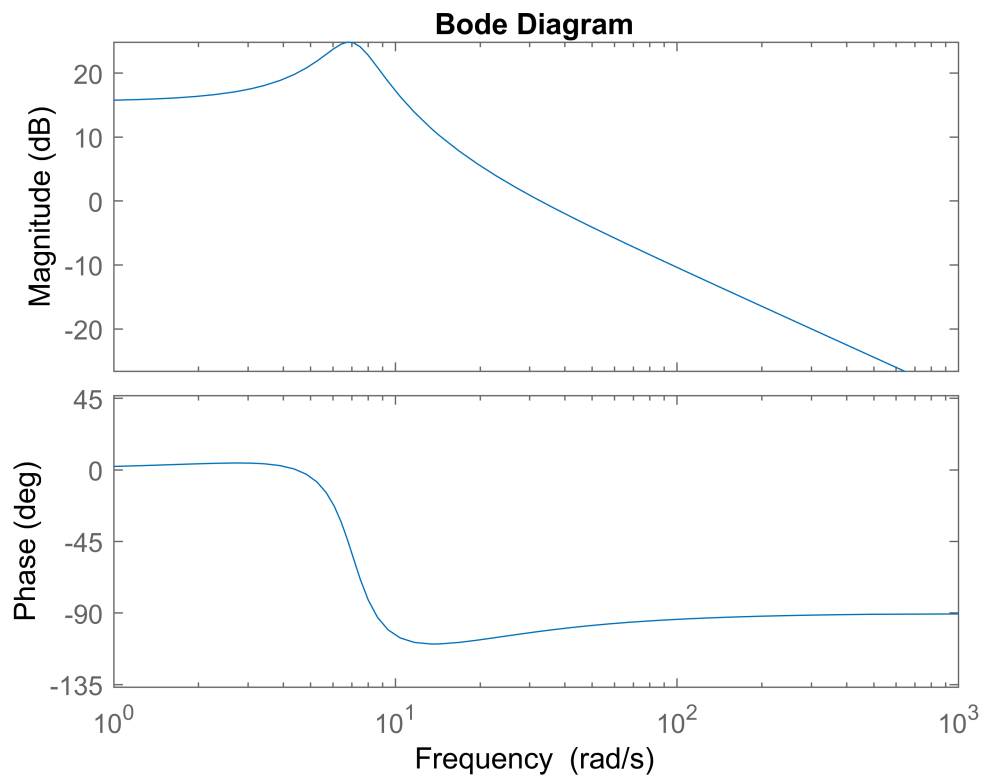
```
% d
G = zpk(tf(30*[1 10],[1 3 50]))
```

G =

$$\frac{30 (s+10)}{(s^2 + 3s + 50)}$$

Continuous-time zero/pole/gain model.

```
bode(G)
```



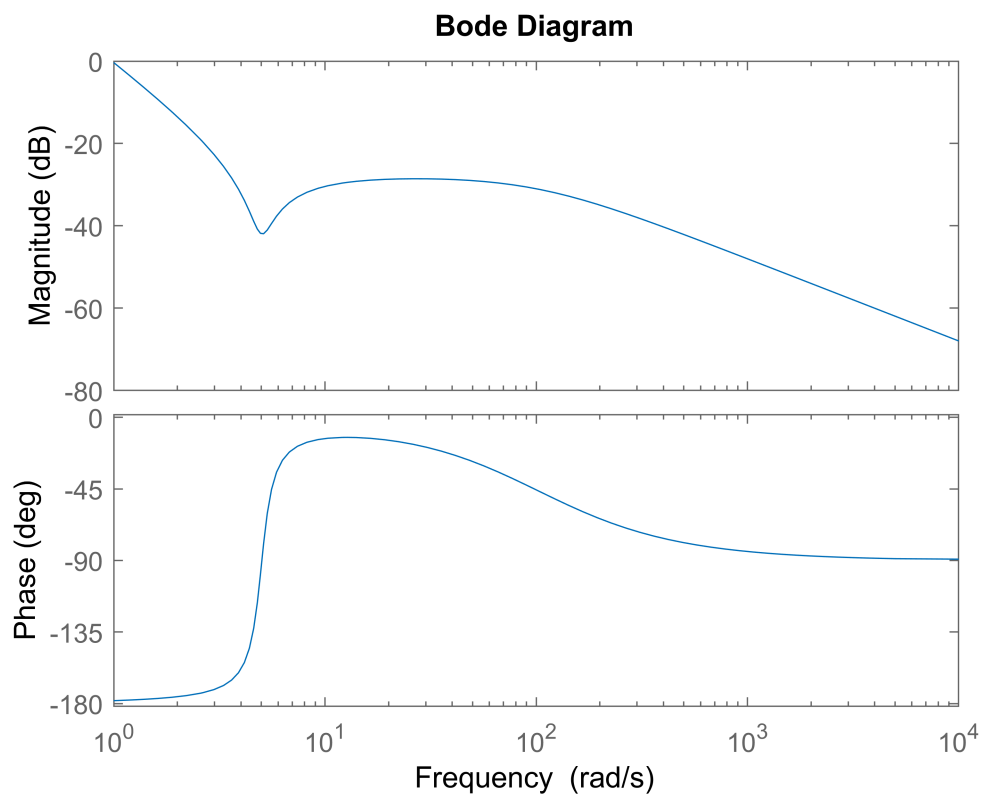
```
% e
G = zpkm(tf(4*[1 1 25],[1 100 0 0]))
```

G =

$$\frac{4 (s^2 + s + 25)}{s^2 (s+100)}$$

Continuous-time zero/pole/gain model.

```
bode(G)
```



```
% f
G = zpk([], [0 0 -5 -2], 100)
```

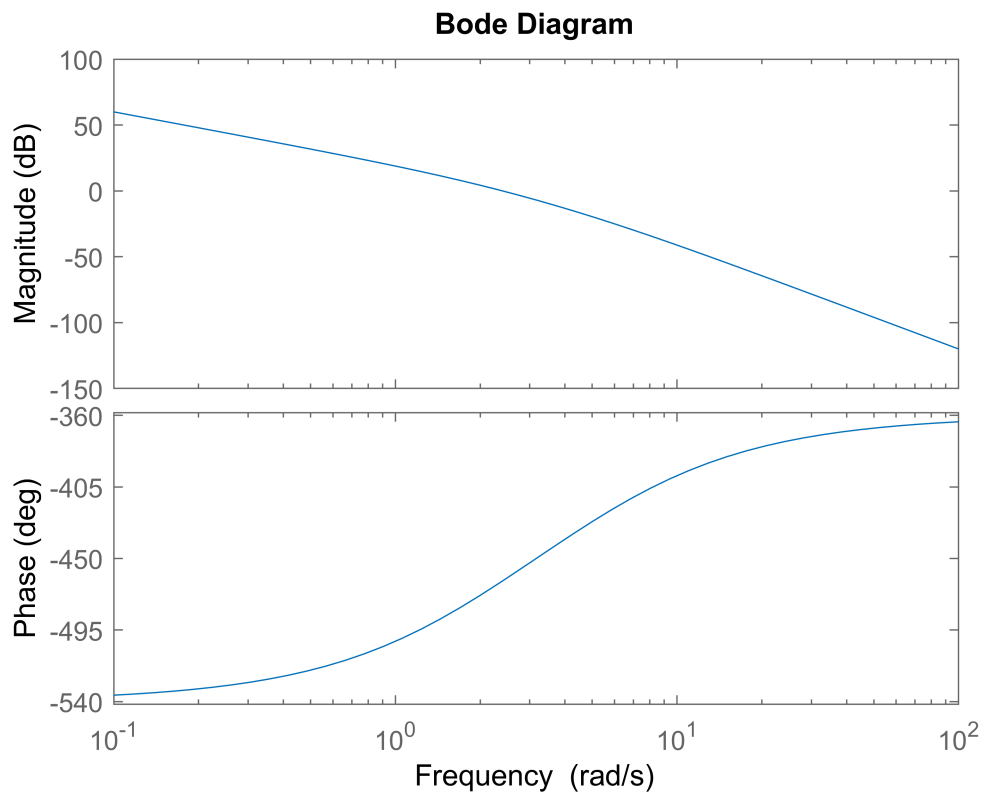
```
G =
```

```

      100
-----
s^2 (s-5) (s-2)
```

```
Continuous-time zero/pole/gain model.
```

```
bode(G)
```



Problem 3

`% 2nd TF`

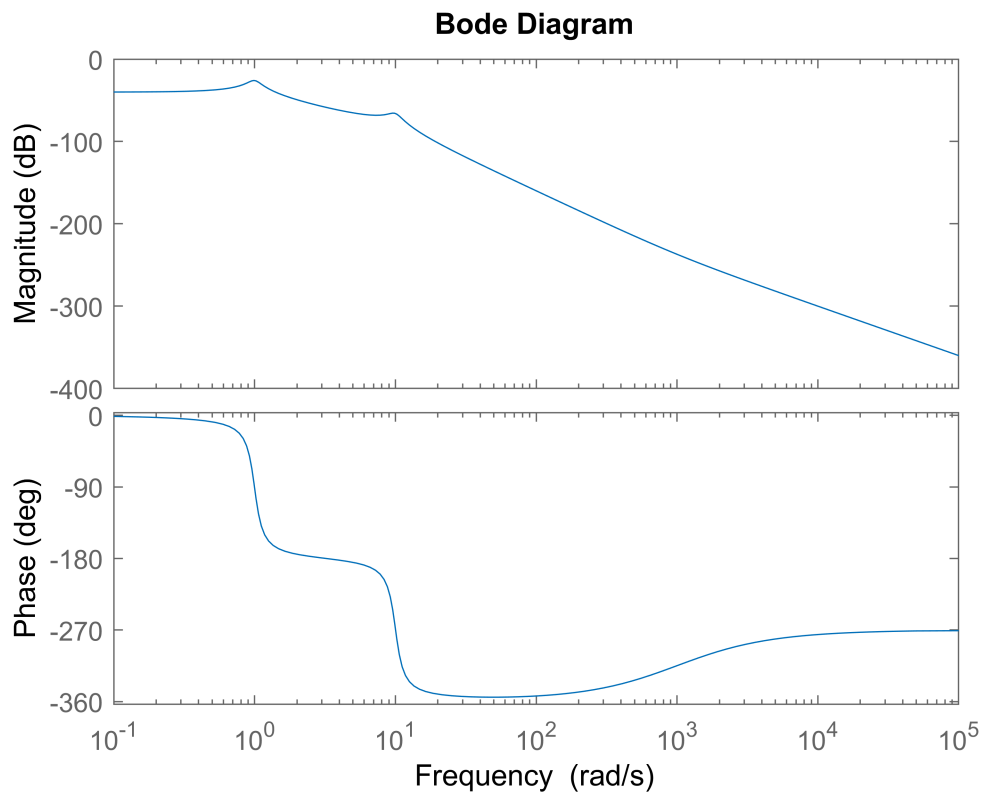
```
H1 = zpk(-1000,[],1/10);
H2 = tf([1/1], [1 2*(1/10)*1 1^2]);
H3 = tf([1/(10^2)], [1 2*(1/10)*10 (10)^2]);
H = H1 * H2 * H3
```

H =

```
      0.001 (s+1000)
-----
(s^2 + 0.2s + 1) (s^2 + 2s + 100)
```

Continuous-time zero/pole/gain model.

`bode(H)`



Problem 4

```
C = zpk(-3,0,10)
```

C =

$$\frac{10 (s+3)}{s}$$

Continuous-time zero/pole/gain model.

```
P1 = zpk([], [3], -0.5);
P2 = tf([1 0 -2000], [1 50 1000]);
P = P1 * P2
```

P =

$$\frac{-0.5 (s-44.72) (s+44.72)}{(s-3) (s^2 + 50s + 1000)}$$

Continuous-time zero/pole/gain model.

```
% Part a
H = feedback(C*P,1)
```

H =

$$\frac{-5 (s+3) (s+44.72) (s-44.72)}{(s^2 + 11.73s + 73.9) (s^2 + 30.27s + 406)}$$

Continuous-time zero/pole/gain model.

```
isstable(H)
```

```
ans = logical
      1
```

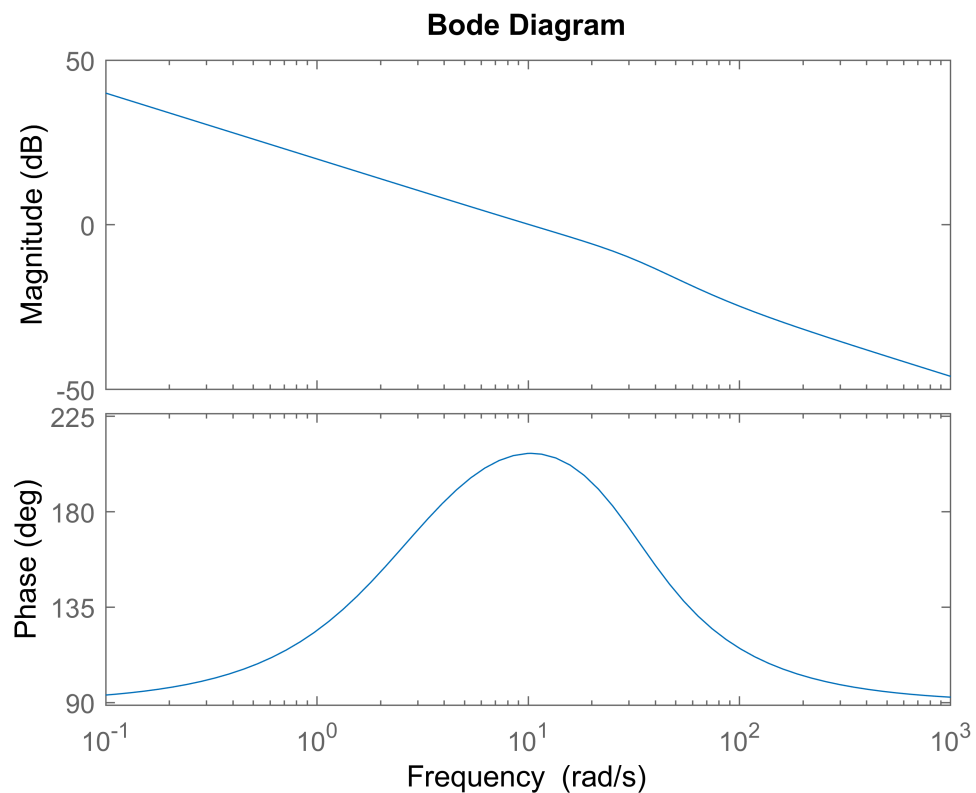
```
% Part b
L = C*P
```

```
L =
```

$$\frac{-5 (s+3) (s+44.72) (s-44.72)}{s (s-3) (s^2 + 50s + 1000)}$$

Continuous-time zero/pole/gain model.

```
bode(L)
```



```
margins = allmargin(L)
```

```
margins = struct with fields:
  GainMargin: [0.3585 2.6490]
  GMFrequency: [3.5966 26.3797]
  PhaseMargin: 27.5718
  PMFrequency: 10.2049
  DelayMargin: 0.0472
```


DMFrequency: 10.2049
Stable: 1

% Part c

```
g1 = margins.GainMargin(1)
```

```
g1 = 0.3585
```

```
L1 = g1 * L
```

```
L1 =
```

$$\frac{-1.7927 (s+3) (s+44.72) (s-44.72)}{s (s-3) (s^2 + 50s + 1000)}$$

Continuous-time zero/pole/gain model.

```
H1 = feedback(L1,1)
```

```
H1 =
```

$$\frac{-1.7927 (s-44.72) (s+44.72) (s+3)}{(s^2 + 0.0008164s + 12.93) (s^2 + 45.21s + 831.7)}$$

Continuous-time zero/pole/gain model.

```
poles1 = roots([1 0.0008164 12.93])
```

```
poles1 = 2x1 complex  
-0.0004 + 3.5958i  
-0.0004 - 3.5958i
```

```
g2 = margins.GainMargin(2)
```

```
g2 = 2.6490
```

```
L2 = g2 * L
```

```
L2 =
```

$$\frac{-13.245 (s+3) (s+44.72) (s-44.72)}{s (s-3) (s^2 + 50s + 1000)}$$

Continuous-time zero/pole/gain model.

```
H2 = feedback(L2,1)
```

```
H2 =
```

$$\frac{-13.245 (s+3) (s+44.72) (s-44.72)}{(s+29.94) (s+3.814) (s^2 + 0.003402s + 696)}$$

Continuous-time zero/pole/gain model.

```
poles2 = roots([1 0.003402 696])
```

```
poles2 = 2×1 complex
-0.0017 +26.3818i
-0.0017 -26.3818i
```

```
% Part d
```

```
S = 1/(1+P*C)
```

```
S =
```

$$\frac{s (s-3) (s^2 + 50s + 1000)}{(s^2 + 11.73s + 73.9) (s^2 + 30.27s + 406)}$$

Continuous-time zero/pole/gain model.

```
T = (P*C)/(1+P*C)
```

```
T =
```

$$\frac{-5 s (s-44.72) (s+44.72) (s+3) (s-3) (s^2 + 50s + 1000)}{s (s-3) (s^2 + 11.73s + 73.9) (s^2 + 30.27s + 406) (s^2 + 50s + 1000)}$$

Continuous-time zero/pole/gain model.

```
S_minus_T = minreal(S-T)
```

```
S_minus_T =
```

$$\frac{(s-10.45) (s+2.059) (s^2 + 60.4s + 1394)}{(s^2 + 11.73s + 73.9) (s^2 + 30.27s + 406)}$$

Continuous-time zero/pole/gain model.

```
[NINF,w_p] = hinfnorm(S_minus_T)
```

```
NINF = 4.0763
w_p = 10.0798
```

```
% Part e
```

```
m = 1/NINF
```

```
m = 0.2453
```

```
dm = diskmargin(P*C)
```

```
dm = struct with fields:
    GainMargin: [0.6060 1.6501]
    PhaseMargin: [-27.5672 27.5672]
    DiskMargin: 0.4906
    LowerBound: 0.4906
    UpperBound: 0.4906
    Frequency: 10.0623
    WorstPerturbation: [1×1 ss]
```

```
m = dm.DiskMargin/2
```

```
m = 0.2453
```

```
% Part f
```

```
z = 1/evalfr(S-T,j*w_p);  
z = (z / abs(z)) * abs(m)
```

```
z = -0.0063 - 0.2452i
```

```
alpha = (1+z)/(1-z)
```

```
alpha = 0.8760 - 0.4572i
```

```
alpha_L_plus_1 = alpha*evalfr(L,j*w_p) + 1
```

```
alpha_L_plus_1 = -2.7529e-08 - 1.2029e-06i
```