

$$13) [XY]^T$$

$$P = \begin{bmatrix} -1 & 1 \\ 1 & 1 \end{bmatrix}$$

$$C = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix} = \begin{bmatrix} \sigma_x^2 & \sigma_{xy} \\ \sigma_{xy} & \sigma_y^2 \end{bmatrix}$$

$$\lambda = 1, 3$$

$$x = \begin{pmatrix} -1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$\boxed{Z = P [XY]^T}$$

$$C' = P C P^{-1} = \begin{bmatrix} 1 & 0 \\ 0 & 3 \end{bmatrix}$$

$$\boxed{\begin{matrix} \sigma_{x'}^2 = 1 \\ \sigma_{y'}^2 = 3 \end{matrix}}$$