

Path Planning for Autonomous Vehicles based on Nonlinear MPC with using a Kinematic Bicycle Model

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MECH 6325 - MPC
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Outline

1 System Overview

- Hail Bopp
- Navigator

2 System Model

- Vehicle Modeling
- Bicycle Model

3 Nonlinear MPC Formulation

4 Simulation Implementation and Results

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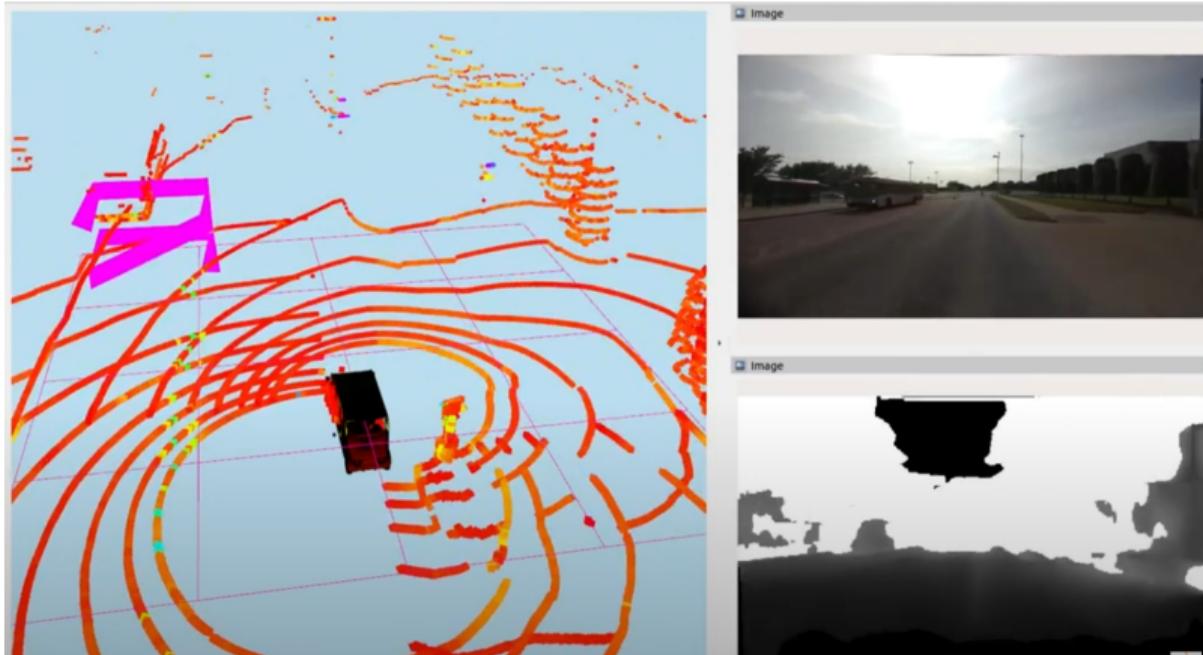
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NOVA: Hail Bopp [1]

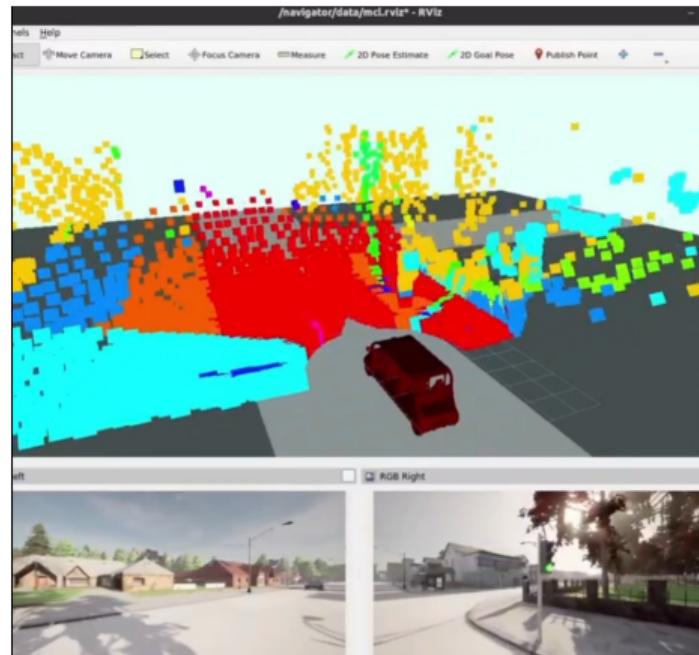


NOVA: Perception [1]



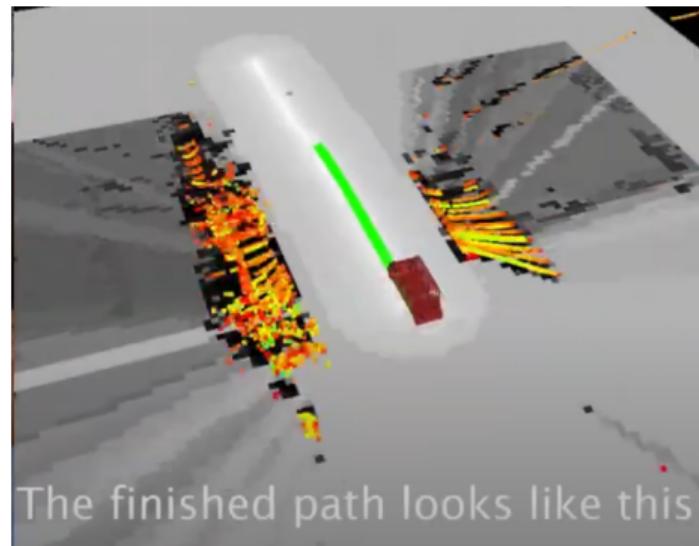
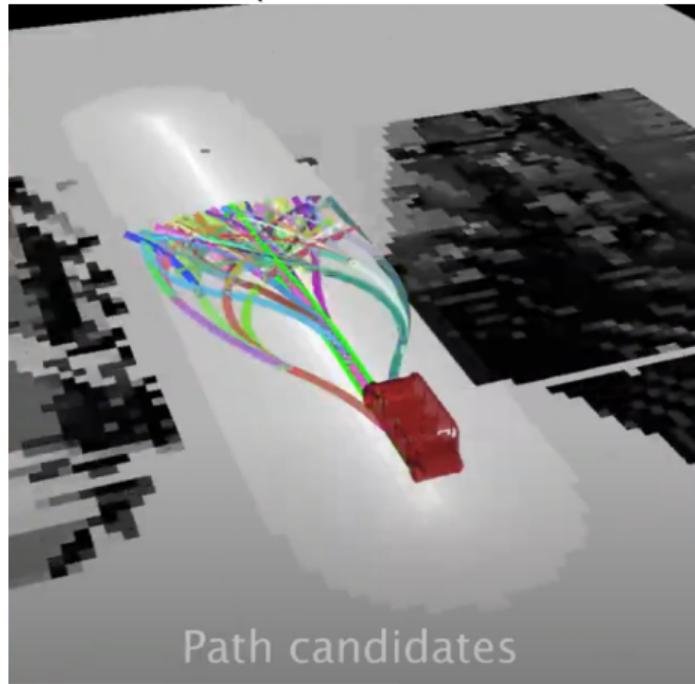
NOVA: Navigator [1]

- Navigator is the self-driving software stack being developed by NOVA.
- Simulations done in then deployed to Hail Bopp.



Path Planning Objective [1]

Current Approach (random path generation and ranking)



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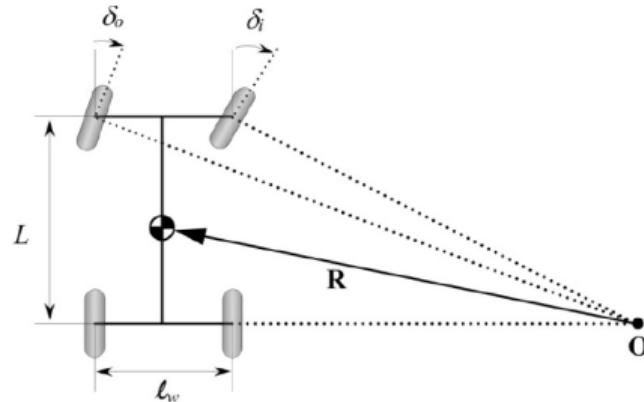
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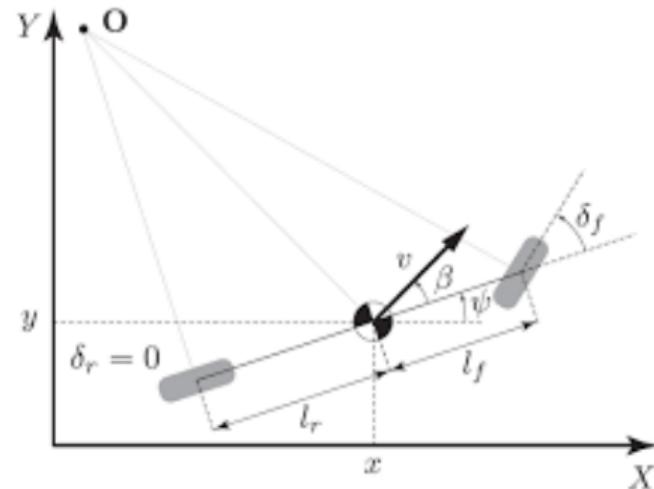
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Vehicle Kinematic Models

Akerman Steering Model



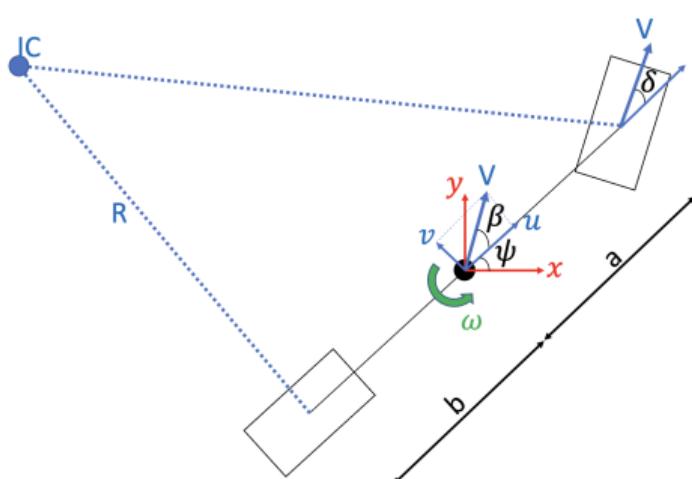
Bicycle Approximation



$$\delta \approx \frac{\delta_o + \delta_i}{2}$$

Kinematic Bicycle Model

Simple nonlinear kinematics model equations:



$$\begin{cases} \dot{x} = V \cos(\psi + \beta) \\ \dot{y} = V \sin(\psi + \beta) \\ \dot{\psi} = \frac{V \cos(\beta)}{I_f + I_r} (\tan(\delta_f) - \tan(\delta_r)) \\ \dot{\theta} = \psi \end{cases} \quad (1)$$

where

$$\beta = \tan^{-1} \left(\frac{I_f \tan(\delta_r) + I_r \tan(\delta_f)}{I_f + I_r} \right) \quad (2)$$

$$\delta_r = 0, I_f = a = 0.7[m], \text{ and } I_r = b = 0.7[m].$$

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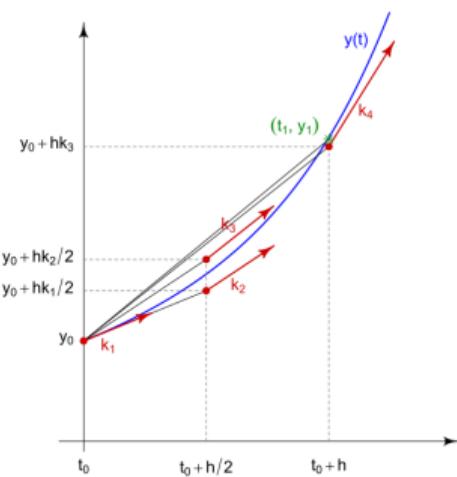
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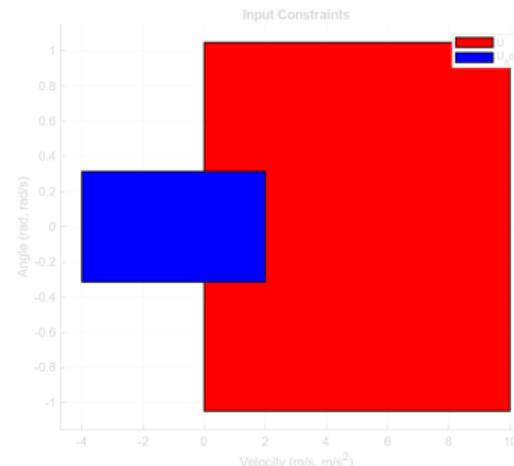
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Model Constraints



Discretized at 1 [s] intervals using **RK4 method** (other methods didn't work w/out much smaller time increments) [2]

Input Constraints



$$\begin{aligned} V &\in [0, 10] \text{ [m/s]} & \theta &\in \pm\pi/3 \text{ [rad]} & \dot{V} &\in [-4, 2] \\ \text{method} \quad \text{(other methods didn't work w/out much smaller time increments)} \quad [2] && \hat{\theta} &\in \pm\pi/10 \text{ [rad/s]} \end{aligned}$$

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Solver: Min Y unstructured: 204 [s] w/ IPOPT



NOVA.

nova-utd.github.io, 2023.



everyone.

Runge–kutta methods.