

link prediction

link inference

SYSM 6302

CLASS 19

# Edge Prediction



→ Almost all real networks are samples of a real "system"

$$G = (V, E)$$

True Network

sampling

$$\tilde{G} = (\tilde{V}, \tilde{E})$$

Sampled Network

does Facebook  
have all of  
your friendships?

→ How do we infer the edges that were missed?

↳ most methods use a generalized notion of similarity

# Classifier

Suppose  $z_{u,v} = \begin{bmatrix} 1 \\ z_1 \\ z_2 \\ \vdots \\ z_m \end{bmatrix}$

$\swarrow$  # common neighbors

$\swarrow$  # of common letters in their name

Can include network structure and non-network node attributes

$\Rightarrow$  Use a threshold to decide when to add an edge

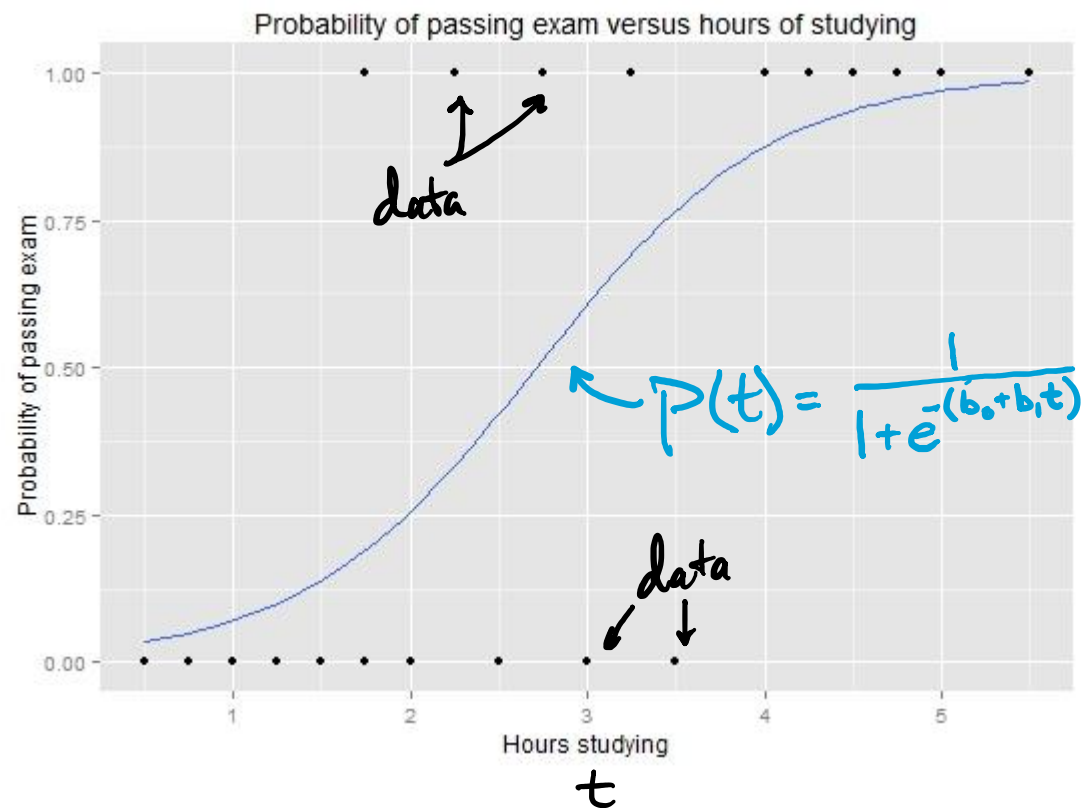
is the similarity vector between nodes  $u$  &  $v$

## Logistic Regression

$$P((u,v) \in E \mid z_{u,v} = z) = \frac{1}{1 + e^{-\beta z}}$$

$\nearrow$  probability that nodes  $u$  &  $v$  have an edge

$\beta$ : parameter vector learned from sampled data  
regression  $\rightarrow$



# Link Inference



→ If there is no "real" network that we are trying to recover

→ movie/Artist similarity

→ protein gene expression

→ Use similarity measure  $\sigma_{ij} \neq 0$  to infer an edge

recall various definitions

needs to be  
statistically  
different  
from zero

To do this  
properly

① Test statistic

② Null model

③ Deal with the multiple testing problem