$\boldsymbol{\eta_{2,max}}$ Perturbation