$\boldsymbol{\eta_{1,max}}$ Perturbation