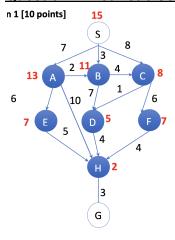
Question 1: Heuristic Search



(a) Is the heuristic admissible? Provide justification.

The Heuristic is admissible. h(n) is always lower than min cost.

Node n	Min Cost	h(n)
S	15	15
Α	13	13
В	12	11
С	8	8
E	8	7
D	7	5
F	7	7
Н	3	2

(b) Is the heuristic consistent? Provide justification.

The heuristic is not consistent. A consistent heuristic, $h(n) \le c(n,p) + h(p)$, where n is the parent node and p is a child of node n.

$$h(f) = 7;$$
 $c(f,h) = 4;$ $h(h) = 2$

 $h(f) \ge c(f,h) + h(h)$, where node f is a parent of node h. Therefore the heuristic is not consistent.

(c) Provide the search steps (as discussed in class) with DFS, BFS (with and without priority queue), Best First Search and A* search. Specify for each algorithm if the open list is queue, stack, or priority queue.

Algorithm: BFS (Queue); Path: SAHG; Cost: 20

Notation: The Open List contains the following: Node stored, Parent node. They will be represented as follows Np (N = Node in uppercase letters, p = Parent node in lowercase letters)

Step	Open list	POP	Nodes to add
1	S	S	A,B,C
2	As,Bs,Cs	As	E,H
3	Bs,Cs,Ea,Ha	Bs	D
4	Cs,Ea,Ha,Db	Cs	F
5	Ea,Ha,Db,Fc	Ea	
6	Ha,Db,Fc	На	G
7	Db,Fc,Gh	Db	
8	Fc,Gh	Fc	
9	Gh	Gh	

Algorithm: DFS (Stack); Path: SAHG; Cost: 20

Notation: The Open List contains the following: Node stored, Parent node. They will be represented as follows Np (N = Node in uppercase letters, p = Parent node in lowercase letters)

Step	Open list	POP	Nodes to add
1	S	S	A,B,C
2	As,Bs,Cs	As	E,H
3	Ea,Ha,Bs,Cs	Ea	
4	Ha,Bs,Cs	На	G
5	Gh,Bs,Cs	Gh	

Algorithm: BFS (Priority Queue); Path: SBCDHG; Cost: 15

Notation: The Open List contains the following: Node stored, Parent node, and Cost from source to node. They will be represented as follows Np20 (N = Node in uppercase letters, p = Parent node in lowercase letters, 20 = cost from source to N)

Step	Open list	POP	Nodes to add
1	S	S	A,B,C
2	Bs3,As7,Cs8	Bs3	C,D
3	As7,Cb7,Db10	As7	E,H
4	Cb7,Db10,Ea13,Ha17	Cb7	D,F
5	Dc8,Ea13,Fc13,Ha17	Dc8	Н
6	Hc12,Ea13,Fc13	Hc12	G
7	Ea13,Fc13,Gh15	Ea13	Н
8	Fc13,Gh15,He18	Fc13	Н
9	Gh15,Hf17	Gh15	

Algorithm: Best First (Priority Queue); Path: SCDHG; Cost: 16

Notation: The Open List contains the following: Node stored, Parent node, and heuristic value. They will be represented as follows Np20 (N = Node in uppercase letters, p = Parent node in lowercase letters, 20 = heuristic value of N)

Step	Open list	POP	Nodes to add
1	S	S	A,B,C
2	Cs8,Bs11,As13	Cs8	D,F
3	Dc5,Fc7,Bs11,As13	Dc5	Н
4	Hd2,Fc7,Bs11,As13	Hd2	G
5	Gh0,Fc7,Bs11,As13	Gh0	

Algorithm: A* (Priority Queue); Path: SBCDHG; Cost: 15

Notation: The Open List contains the following: Node stored, Parent node, and the sum of heuristic and incurred value - f(n) = g(n) + h(n). They will be represented as follows Np20 (N = Node in uppercase letters, p = Parent node in lowercase, 20 = f(n))

Step	Open list	POP	Nodes to add
1	S	S	A,B,C
2	Bs14,Cs16,As20	Bs14	D,C
3	Cb15,Db15,As20	Cb15	D,F
4	Dc13,As20,Fc21	Dc13	Н
5	Hd14,As20,Fc21	Hd14	G
6	Gh15,As20,Fc21	Gh15	

Question 2: Self Driving Car (A* Search)

Node: The node represents each location in the grid. For each of these locations, we record the cost to get to that location (self.g), the heuristic cost between that location and the goal location using the manhattan distance (self.h), the sum of the 2 (self.f), the current location of the node (self.loc), and lastly the parent node (self.parent)

```
class Node():
   def __init__(self, parent=None, loc=None):
       self.parent = parent
       self.loc = loc
       self.g = 0
       self.h = 0
       self.f = 0
   def __eq__(self, other):
        return self.loc[0] == other.loc[0] and self.loc[1] == other.loc[1]
   def __lt__(self, other):
       return self.f < other.f
   def __gt__(self, other):
       return self.f > other.f
   def __str__(self):
       return str(self.loc) + str(self.f)
   def __repr__(self):
       return str(self.loc) + str(self.f)
```

Drive Function: this function is called on every iteration.

- 1. It first gets the start and end locations from the environment variable.
- Then runs the Astar algorithm to get the optimal path between current location and the goal
- 3. Lastly, it converts the path given by the A star algorithm to an action sequence

```
def drive(self,goalstates,inputs):
   """Write your algorithm for self driving car"""
   # get start and end
   start = self.state['location']
   end = goalstates[0]['location']
   goalReached, path = self.a_star(inputs, start, end)
   act_sequence=[]
   prev = None
   for step in path:
       if prev is None:
          prev = step
       x = prev[0] - step[0]
       y = prev[1] - step[1]
       if x == 1 and y == 1:
           act_sequence.append('right')
       elif x == -1 and y == 1:
          act_sequence.append('left')
       elif x == 0 and y == 1:
          act_sequence.append('forward')
       elif x == 0 and y == 2:
          act_sequence.append('forward-2x')
       elif x == 0 and y == 3:
          act_sequence.append('forward-3x')
   return act_sequence
```

A* Algorithm: Find optimum path, given maze, start, and end

```
def a_star(self, maze, start, end):
    maze1dLength = len(maze)
    maze2dLength = len(maze[0])
   startNode = Node(None, start)
   endNode = Node(None, end)
   openList = []
   closedList = []
   openList.append(startNode)
   while len(openList) > 0:
        # get current Node
       currentNode = heapq.heappop(openList)
       closedList.append(currentNode)
       # create path
       if currentNode == endNode:
           return endNode, self.createPath(currentNode)
       children = []
        for action in [(1, 1), (-1, 1), (0, 1), (0, 2), (0, 3)]: # actions
           loc = (currentNode.loc[0] + action[0], currentNode.loc[1] + action[1])
            if not (loc[0] < maze1dLength and loc[1] < maze2dLength and loc[0] >= 0 and loc[1] >= 0): # not in maze
            if maze[loc[0]][loc[1]] == 1: # have car
               continue
            if action[1] > 1 and maze[loc[0]][loc[1] - 1] == 1: # if moves 2 steps or more, check car between
            if action[1] > 2 and maze[loc[0]][loc[1] - 2] == 1: # if moves 3 steps or more, check car between
           newNode = Node(currentNode, loc)
           children.append(newNode)
        # add child to set
        for child in children:
           # not in closed List
            if self.isInList(child,closedList) is not None:
           # derive cost
           child.g = currentNode.g + 1
           child.h = self.hCost(child,endNode)
           child.f = child.g + child.h
           childInOpenList = self.isInList(child,openList)
            if childInOpenList is not None and child.f > childInOpenList.f:
            # add to openList
           heapq.heappush(openList, child)
    return None, [None]
```

Helper Functions: called by the A* Algorithm

- hCost: the heuristic cost of a location to get to the goal location given by the manhattan distance.
- 2. createPath: gets the path from start to end using the pointer to its parent in each node.

3. isInList: a simple helper function to check is item x is in a list, either openList or closeList can use this function.

```
def hCost(self,child,endNode):
    return (abs(child.loc[0] - endNode.loc[0]) + abs(child.loc[1] - endNode.loc[1]))

def createPath(self,currentNode):
    path = []
    current = currentNode
    while current is not None:
        path.append(current.loc)
        current = current.parent
    return path

def isInList(self,x,xList):
    for item in xList:
        if x == item:
            return item
    return None
```

Question 3: Taxi Driver MDP

(a) You need to provide an MDP model that guides the taxi driver on "move and pickup customers". MDP is the tuple <S, A, P, R>

s (current state)	a (action)	s' (new state)	Pr(s' s,a)	R(s,a,s')
L1	L1	L1	0.7	0
		L2	0.12	7
		L3	0.105	11.5
		L4	0.075	13.75
	L2	L2	1	-1
	L3	L3	1	-1.5
	L4	L4	1	-1.25
L2	L2	L2	0.2	0
		L1	0.32	9
		L3	0.48	8.25
	L1	L1	1	-1
	L3	L3	1	-0.75
	L4	L4	1	-inf
L3	L3	L3	0.9	0
		L1	0.06	11.5
		L4	0.04	9.2
	L1	L1	1	-1.5
	L2	L2	1	-inf
	L4	L4	1	-0.8
L4	L4	L4	0.4	0
		L1	0.39	7.75
		L2	0.21	6
	L1	L1	1	-1.25
	L2	L2	1	-1
	L3	L3	1	-inf

(b) After providing the MDP, show three iterations of value iteration. Initialize

 \forall s, $V_0(s) = 0$ and calculate

- (i) \forall s, $V_1(s)$, $V_2(s)$ and $V_3(s)$
- (ii) \forall s, $\pi_1(s)$, $\pi_2(s)$ and $\pi_3(s)$

 $Q^{t+1}(s,a) = \sum Pr(s' \mid s,a) [R(s,a,s') + \gamma V^{t}(s')], given \gamma = 0.99$

Iteration 1

S	а	s'	V ⁰ (s)	$\frac{\Pr(s' s,a)}{[R(s,a,s')+\gamma V^t(s')]}$	Q¹(s,a)	V¹(s)	π¹(s)
L1	L1	L1		0	3.07875		
	L1	L2		0.84			
	L1	L3		1.2075			
	L1	L4	0	1.03125		3.07875	L1
	L2	L2		-1	-1		
	L3	L3		-1.5	-1.5		
	L4	L4		-1.25	-1.25		
	L1	L1		-1	-1		
	L2	L2		0	6.84	6.84	L2
L2	L2	L1	0	2.88			
L2	L2	L3		3.96			
	L3	L3		-0.75	-0.75		
	L4	L4		-inf	-inf		
	L1	L1		-1.5	-1.5		
	L2	L2		-inf	-inf		
L3	L3	L3	0	0	1.058	1.058	L3
LJ	L3	L1		0.69		1.000	LO
	L3	L4		0.368			
	L4	L4		-0.8	-0.8		
	L1	L1		-1.25	-1.25		
L4	L2	L2		-1	-1		
	L3	L3	0	-inf	-inf	4.2825	L4
L4	L4	L4		0	4.2825	4.2020	<u>_</u>
	L4	L1		3.0225			
	L4	L2		1.26			

Iteration 2

- Coraci	Leration 2							
S	а	s'	V¹(s)	$ \begin{array}{c} \text{Pr}(s' s,a) \\ [\text{R}(s,a,s') + \gamma V^{\text{t}}(s')] \end{array} $	Q ² (s,a)	V ² (s)	π²(s)	
L1	L1	L1		2.13357375	6.1267125			
	L1	L2		1.2057555			L1	
	L1	L3		1.527536063		6.1267125		
	L1	L4	3.07875	1.259847188				
	L2	L2		5.7716	5.7716			
	L3	L3		-0.45258	-0.45258			
	L4	L4		2.989675	2.989675			
L2	L1	L1		2.0479625	2.0479625			
	L2	L2		1.35432	13.6116	13.6116	L2	
	L2	L1	6.84	5.046912				
	L2	L3	0.04	7.210368				
	L3	L3		0.29742	0.29742			
	L4	L4		-inf	-inf			
L3	L1	L1		1.5479625	1.5479625			
	L2	L2		-inf	-inf			
	L3	L3	1.058	0.942678	2.10542	3.439675	L4	
	L3	L1	1.030	0.7528452		3.439073	LT	
	L3	L4		0.4098968				
	L4	L4		3.439675	3.439675			
L4	L1	L1		1.7979625	1.7979625			
	L2	L2		5.7716	5.7716			
	L3	L3	4.2825	-inf	-inf	8.522175	L4	
	L4	L4	4.2020	1.69587	8.522175	0.022110	LT	
	L4	L1		4.67597325				
	L4	L2		2.15033175				

Iteration 3

iteration	teration 3							
s	а	s'	V ² (s)	$\Pr(s' s,a) \\ [R(s,a,s')+\gamma V^t(s')]$	Q ³ (s,a)	V ³ (s)	π ³ (s)	
L1	L1	L1		4.245811763	9.144195375			
	L1	L2		1.567853445			L2	
	L1	L3		1.844371764				
	L1	L4	6.1267125	1.486158403		12.475484		
	L2	L2		12.475484	12.475484			
	L3	L3		1.90527825	1.90527825			
	L4	L4		7.18695325	7.18695325			
L2	L1	L1		5.065445375	5.065445375		L2	
	L2	L2		2.6950968	20.315484	- 20.315484		
	L2	L1	13.6116	7.19215488				
	L2	L3	13.0110	10.42823232				
	L3	L3		2.65527825	2.65527825			
	L4	L4		-inf	-inf			
L3	L1	L1		4.565445375	4.565445375			
	L2	L2		-inf	-inf			
	L3	L3	3.439675	3.064750425	4.46327825	7.63695325	L4	
	L3	L1	3.439073	0.894316695		7.00093323	LŦ	
	L3	L4		0.50421113				
	L4	L4		7.63695325	7.63695325			
L4	L1	L1		4.815445375	4.815445375			
	L2	L2		12.475484	12.475484			
	L3	L3	8.522175	-inf	-inf	12.71945325	L4	
	L4	L4	0.022170	3.3747813	12.71945325	12.7 1040020		
	L4	L1		6.312911768				
	L4	L2		3.031760183				

Question 4: OpenAlGym

(1) Initializing Environment

```
[21] import gym
  import numpy as np
  import random
  from pylab import *

[22] env = gym.make('FrozenLake-v0')
```

(2) Initializing FrozenLake Class

```
class FrozenLake:
    def __init__(self):
        # attributes
        self.Q = np.zeros([env.observation_space.n,env.action_space.n])
        self.reward_total = []
        self.steps_total = []
        # parameters
        self.num_episodes = 2000
        self.max_steps = 100
        self.learning_rate = 0.8
        self.gamma = 0.95
        # self.egreedy = 0.90
        # self.egreedy_decay = 0.999
        # self.egreedy_final = 0.005
```

(3) Run (Learning)

```
def run(self):
  for i in range(self.num_episodes):
    reward_episode = 0
    steps_episode = 0
    state = env.reset()
    # for each step (action made) in one episode
    while steps_episode < self.max_steps:</pre>
      # get action (with randomness)
      actions_for_state = self.Q[state,:] + np.random.randn(1, env.action_space.n) / (i + 1) #
     action = np.argmax(actions_for_state)
     # # egreedy
     # if np.random.rand(1)[0] < self.egreedy:</pre>
     # action = env.action_space.sample()
     # if self.egreedy > self.egreedy_final:
     # self.egreedy *= self.egreedy_decay
      # make step with action
      new_state, reward, done, _ = env.step(action)
      # update Q table
      old_estimate = self.Q[state,action]
      step_size = self.learning_rate
      target = reward + self.gamma * np.max(self.Q[new_state,:])
      self.Q[state,action] = old_estimate + step_size * (target - old_estimate)
      # update variables
      state = new_state
      reward_episode += reward
      steps_episode += 1
      if done:
        break
    # update graphing arrays
    self.reward_total.append(reward_episode)
    self.steps_total.append(steps_episode)
    if i%100 == 0: # printing
      print(f'Step{i}: reward - {reward_episode} :: steps - {steps_episode}')
```

(4) Printing Graph

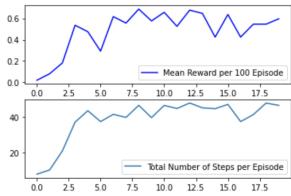
```
def plot(self):
  subplot(211)
  plot(self.avr_pass(self.reward_total), 'b', label="Mean Reward per 100 Episode")
  legend(loc="best")
  subplot(212)
  plot(self.avr_pass(self.steps_total), label="Total Number of Steps per Episode")
  legend(loc="best")
  show()
def low_pass(self, data, alpha=0.99):
  low_pass = [data[0]]
  for i in range(1,len(data)):
   low_pass.append(alpha*low_pass[-1] + (1.0-alpha)*data[i] )
  return low_pass
def avr_pass(self, data, alpha=100):
  avr_pass = []
  for i in range(alpha - 1,len(data), alpha):
   avr_pass.append(np.mean(data[i - alpha + 1:i]))
  return avr_pass
```

(5) Graph: Rewards

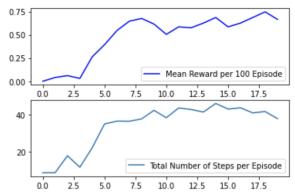
```
lake = FrozenLake()
lake.run()
lake.plot()
```

We ran the algorithm initially with the (1) epsilon greedy code, in concert with the (2) action randomization code. We got pretty similar results but the epsilon greedy code was overall a worse code, as it took longer to converge and it also resulted in lower converged rewards, due to the greater chance of using a randomized action using the epsilon greedy code. Perhaps, it might work better to use one or the other in the future.

Epsilon greedy code + Action randomization



Action randomization



Question 5: SVD Word Embeddings

(1) Load Data

- Building an NLP Pipeline

```
[1] from google.colab import drive
    drive.mount('/content/drive/')

Mounted at /content/drive/

[2] # load file into dataframe
    csv_dir = '/content/drive/My Drive/Colab Notebooks/CS420/NLPCodes'

② import nltk
    from nltk.stem import WordNetLemmatizer
    import sys
    from nltk.corpus import wordnet
    from nltk.corpus import stopwords
    from nltk.corpus import stopwords
    from nltk.parse.malt import MaltParser
    nltk.download('wordnet')
    nltk.download('wordnet')
    nltk.download('wordnet')
    import pandas as pd
    import pandas as pd
    import numpy as np

df = []
    with open(ff'{csv_dir}/200Reviews.csv', 'r') as file:
        df = pd.read_csv(file)
        df.head()
```

(2) Data Preprocessing

(3) Co-occurrence matrix Class

- Co-occurence Matrix

```
[g] class ConcurrenceMatrix:

of initial calf, window):
    self.vocabulary = [l]
    self.wartix = [l]
    self.wartix = [l]
    self.wardow = window
    self.v = None
    self.s = None
    self.newMord(oword) # add coword
    index = self.vocabulary.index(coword)] += 1

def newMord(self, word):
    # add word to natrix and vocabulary if not in vocabulary
    if word not in self.vocabulary:
    if word not in self.vocabulary:
        for each word create window, and add word
    if word not in self.vocabulary:
        for each word create window, and add word
    if word in window
    self.matrix.papend([0] for i in range(len(self.vocabulary))))

def addsentence(self, sentence):
    if or each word create window, and add word
    if word in window
    if word in window)
    if word in window)
    if word in window)
    if word in window)
    self.s, self.s, self.vocabulary);
    print(fword in window)
    self.s, self.s, self.vocabulary);
    print(fword in window)

def createEmbedding(self, size=100):
    self.matrix.self.matrix[s]);
    print(fwatrix kelf): (len(self.vocabulary));
    print(fwatrix kelf): (len(self.vocabulary));
    print(fwatrix kelf.self.self.elf.elf.elf.embedding(s)));
    print(fwatrix kelf.self.self.self.vocabulary));
    print(fwatrix kelf.self.self.self.elf.elf.embedding(s)));
    print(fwebedding windth (fen(self.wocabulary)));
    print(fwebedding windth (fen(self.embedding(s)));
    print(fwebedding windth (fen(self.embedding(s)));
    print(fwebedding windth (fen(self.embedding(self.embedding(s))));
    print(fwebedding windth (fen(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(self.embedding(s
```

(4) Create SVD Word Embedding

```
[10] #create co-occurence matrix
    matrix = CoOccurenceMatrix(5)
    for index, row in df.iterrows():
        for sentence in row.review:
            matrix.printMatrix()

[12] # get first 100 column of each matrix
    matrix.createEmbedding()

[22] matrix.createEmbedding(4)

[32] embedding width: 100
    embedding height: 7417
        [-0.00319844 -0.03302494  0.0024539  0.0214006 ]
        [-0.00056103 -0.00072078 -0.00038473  0.00099664]
        [-1.3089996e-04 -2.77688367e-03 3.47213244e-05  1.42663313e-03]
        [-4.07631138e-03 -3.56803406e-02  9.96355636e-05  2.17062358e-02]
```

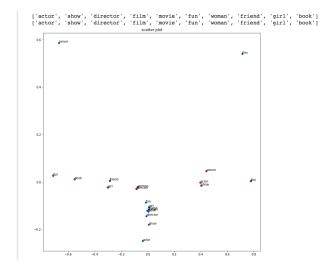
(5) Create Word2Vec Word Embedding

- Word2Vec

(6) EDA of Data Embeddings

- Plot

(7) Plotted words



The blue data points are the SVD embedding, and the red the word2vec embedding.

The SVD embeddings are a lot more inaccurate than the word2vec embeddings. The 3 data points furthest apart for the SVD are the words 'actor, film and movie'. These words are linguistically most related to each other in this set of words, whilst words like 'fun, girl, book' are much closer together despite being arbitrary in comparison with each other.

The word2vec embeddings do much better in this set of words, with 'actor, movie' being necessarily close, and the word 'film' being a little further out, but still the next closest word in the set.