

International Economics I

Lecture Set 3: The HO model

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The Heckscher-Ohlin (H-O) Model

- in the classical frameworks, there is trade when there is *comparative advantage*
- in the Ricardian model, comparative advantage arises from technological differences across countries
- comparative advantage can also arise from differences in factor endowments (capital, labor, land,...)
 - e.g., the US import lumber from Canada since Canada has more land per capita than the US
- in the Heckscher-Ohlin model, a country's comparative advantage depends on:
 - its *relative factor abundance* combined with
 - the *relative intensity* in factor utilization for the production of different goods

Questions

- we'll consider 2 countries with the same technology and different factor endowments
 - ① how does production change in the open economy?
 - ② who exports/imports what?
 - ③ what are the welfare effects of trade?
 - ④ what happens if the endowment of a factor changes?
 - (e.g., due to immigration)
 - ⑤ what are the effects of trade on income distribution?
 - ⑥ what are the effects of trade on unemployment?
 - ⑦ is there empirical support to the theory?

The Heckscher-Ohlin Model: 2x2x2

- 2 countries: home and foreign ($*$)
 - same preferences
- 2 goods: textiles (T) and automobiles (A)
 - same technology to produce each good in both countries
 - T uses labor more intensively than A
- 2 factors of production: labor (L) and capital (K)
 - mobile between sectors, not between countries
 - different relative endowments of labor
 - e.g., home has relative abundance of L ($L/K > L^*/K^*$)

Relative Endowments (K/L) Across Countries

| Capital and Labor endowments, 1996 | | | |
|---|----------------------|--------------------------|----------------------------|
| Country | Labor force (mln) | Capital Stock (\$bln) | Capital per worker (\$) |
| India | 369.50 | 2,080 | 5,629 |
| China | 735.10 | 5,450 | 7,414 |
| Chile | 5.57 | 204 | 36,653 |
| Brazil | 59.13 | 2,280 | 38,560 |
| Mexico | 31.67 | 1,400 | 44,211 |
| Argentina | 14.62 | 719 | 49,192 |
| UK | 29.05 | 2,550 | 87,778 |
| Korea | 18.97 | 1,860 | 98,055 |
| Spain | 15.63 | 1,720 | 110,024 |
| Canada | 15.12 | 1,850 | 122,326 |
| US | 135.40 | 17,000 | 125,554 |
| Japan | 79.73 | 10,600 | 132,953 |
| Switzerland | 3.92 | 621 | 158,504 |

Factor Intensities Across Sectors

Capital-Labor Ratio by Selected US Industries, 2005

| INDUSTRY | Labor (th) | Capital Stock (\$ mln) | Capital per worker (\$ th) |
|-----------------------------------|------------|------------------------|----------------------------|
| APPAREL AND TEXTILES | 262 | 15821 | 60.362 |
| FURNITURE AND FIXTURES | 324 | 20241 | 62.569 |
| LUMBER AND WOOD PRODUCTS | 535 | 35961 | 67.242 |
| LEATHER AND LEATHER PRODUCTS | 27 | 1944 | 71.482 |
| PRINTING AND PUBLISHING | 436 | 43529 | 99.953 |
| FABRICATED METAL PRODUCTS | 939 | 114058 | 121.520 |
| RUBBER AND PLASTICS | 673 | 91080 | 135.255 |
| FOOD AND KINDRED PRODUCTS | 1123 | 193020 | 171.848 |
| TRANSPORTATION EQUIPMENT | 881 | 185904 | 211.110 |
| INSTRUMENTS AND RELATED PRODUCTS | 320 | 67490 | 211.169 |
| PRIMARY METAL INDUSTRIES | 380 | 112946 | 297.304 |
| PAPER AND ALLIED PRODUCTS | 371 | 110728 | 298.297 |
| ELECTRONIC AND ELECTRIC EQUIPMENT | 591 | 199212 | 337.133 |
| CHEMICALS | 406 | 225141 | 554.261 |
| PETROLEUM AND COAL PRODUCTS | 64 | 91294 | 1424.242 |

Technology and Factor Intensities

- consider a production function with constant factor requirements:

a_{KT} = capital used for 1 unit of T

a_{LT} = labor used for 1 unit of T

a_{KA} = capital used for 1 unit of A

a_{LA} = labor used for 1 unit of A

- a_{Ki} and a_{Li} are *unit factor demands* and in general depend on factor prices:

w = wage, r = rate of return on capital

but for now we consider them constant and exogenous

- A and T differ in their relative factor intensity:

$$\frac{a_{LT}}{a_{KT}} > \frac{a_{LA}}{a_{KA}}$$

- T uses L relatively more intensively than A
- T is relatively intensive in L (labor intensive)

Equilibrium in Closed Economy

- factor market clearing
 - production of A and T has to achieve full employment of L and K :

$$L = a_{LT} \times Q_T + a_{LA} \times Q_A$$

$$K = a_{KT} \times Q_T + a_{KA} \times Q_A$$

- good market clearing
 - demand of T = fraction b of income $(rK + wL)$

$$P_T D_T = b(rK + wL) \quad \& \quad P_A D_A = (1 - b)(rK + wL)$$

- RD ($= D_T/D_A$) = RS

$$\frac{D_T}{D_A} = \frac{b}{1-b} \frac{P_A}{P_T} = \frac{Q_T}{Q_A}$$

- perfect-competition pricing (price = marginal cost)

$$P_T = a_{KT} \times r + a_{LT} \times w$$

$$P_A = a_{KA} \times r + a_{LA} \times w$$

- 5 equations in 5 unknowns

Equilibrium in Closed Economy: Production (RS)

- to obtain Q_A and Q_T
 - solve the 2×2 system for factor market clearing:

$$\begin{cases} Q_A = \frac{K - a_{KT} \times Q_T}{a_{KA}} \\ L = a_{LT} \times Q_T + a_{LA} \times Q_A \end{cases} \rightarrow \begin{cases} Q_A = \frac{K}{a_{KA}} - \frac{a_{KT}}{a_{KA}} \times Q_T \\ Q_T = \frac{a_{KA}}{a_{LT}} - \frac{a_{LA}}{a_{LT}} \times Q_A \end{cases}$$

$$\begin{aligned} Q_A &= \frac{K}{a_{KA}} - \frac{a_{KT}}{a_{KA}} \frac{L}{a_{LT}} + \frac{a_{KT}}{a_{KA}} \frac{a_{LA}}{a_{LT}} Q_A \\ \frac{a_{KA}a_{LT} - a_{LA}a_{KT}}{a_{KA}a_{LT}} Q_A &= \frac{K}{a_{KA}} - \frac{a_{KT}}{a_{KA}} \frac{L}{a_{LT}} \end{aligned}$$

$$\begin{cases} Q_T = \frac{a_{KA}L - a_{LA}K}{a_{KA}a_{LT} - a_{LA}a_{KT}} \\ Q_A = \frac{a_{LT}K - a_{KT}L}{a_{KA}a_{LT} - a_{LA}a_{KT}} \end{cases}$$

- which deliver the RS (independent of relative price):

$$\frac{Q_T}{Q_A} = \frac{a_{KA}L - a_{LA}K}{a_{LT}K - a_{KT}L}$$

Equilibrium Production: Diversification

$$Q_T = \frac{a_{KA}L - a_{LA}K}{a_{KA}a_{LT} - a_{LA}a_{KT}} \quad \text{and} \quad Q_A = \frac{a_{LT}K - a_{KT}L}{a_{KA}a_{LT} - a_{LA}a_{KT}}$$

- for home to produce both goods, two conditions are required:
 - different factor intensities across sectors

$$a_{KA}a_{LT} - a_{LA}a_{KT} > 0 \Leftrightarrow a_{LA}/a_{KA} < a_{LT}/a_{KT}$$

- relative labor endowment within the "cone of diversification"

$$Q_A > 0 \Leftrightarrow a_{LT}K - a_{KT}L > 0 \Leftrightarrow L/K < a_{LT}/a_{KT}$$

$$Q_T > 0 \Leftrightarrow a_{KA}L - a_{LA}K > 0 \Leftrightarrow L/K > a_{LA}/a_{KA}$$

i.e., lying between the relative labor intensities of both goods

Equilibrium Production: Properties

$$Q_T = \frac{a_{KA}L - a_{LA}K}{a_{KA}a_{LT} - a_{LA}a_{KT}} \quad \text{and} \quad Q_A = \frac{a_{LT}K - a_{KT}L}{a_{KA}a_{LT} - a_{LA}a_{KT}}$$

- production and factor endowments:
 - production of the L -intensive good (Q_T) is increasing in the relative endowment of L (increases with L falls with K)
 - production of the K -intensive good (Q_A) is increasing in the relative endowment of K (increases with K falls with L)
- Rybczynski effect:
 - *an increase in the endowment of a factor (e.g., L) raises disproportionately the production of the good intensive in that factor (Q_T)*
$$\% \Delta Q_T > \% \Delta L > 0 > \% \Delta Q_A$$
 - intuition: to absorb ΔL in the production of T , need to employ also more $K \rightarrow$ move some K and L away from A

Equilibrium in Closed Economy: Relative Price

- to obtain the relative price (P_T/P_A)
 - replace the RS into the good market clearing condition

$$\frac{1-b}{b} \frac{P_T}{P_A} = \frac{Q_A}{Q_T} = \frac{a_{LT}K - a_{KT}L}{a_{KA}L - a_{LA}K}$$

- and simplify...

$$\frac{P_T}{P_A} = \frac{b}{1-b} \frac{a_{LT}K - a_{KT}L}{a_{KA}L - a_{LA}K} = \frac{b}{1-b} \frac{a_{LT} \frac{K}{K} - a_{KT} \frac{L}{K}}{a_{KA} \frac{L}{K} - a_{LA} \frac{K}{K}}$$

...to get

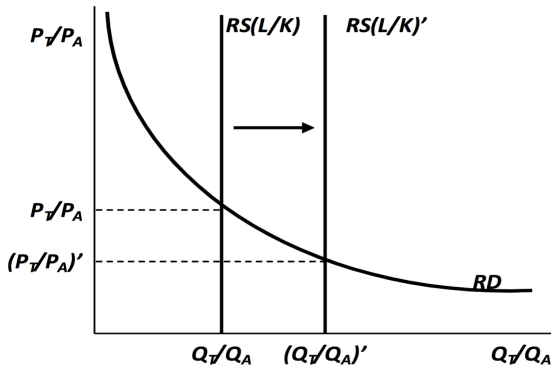
$$\frac{P_T}{P_A} = \frac{b}{1-b} \frac{a_{LT} - a_{KT} \frac{L}{K}}{a_{KA} \frac{L}{K} - a_{LA}}$$

Equilibrium Relative Price: Properties

$$\frac{P_T}{P_A} = \frac{b}{1-b} \frac{a_{LT} - a_{KT} \frac{L}{K}}{a_{KA} \frac{L}{K} - a_{LA}}$$

- P_T/P_A is a decreasing function of L/K
 - the relative price of a good is decreasing in the relative endowment of the factor it uses intensively
 - intuition: more $L/K \rightarrow$ more Q_T/Q_A (RS) \rightarrow lower P_T/P_A
- relative endowments \rightarrow relative price \rightarrow comparative advantage
 - in K -abundant countries, the K -intensive good is cheaper
 - in L -abundant countries, the L -intensive good is cheaper

Equilibrium in Closed Economy: Graph



Equilibrium in Closed Economy: Factor Prices

- intuitively, if T becomes relatively more expensive,
 - firms value more L (intensively used by T)
 - and value less K (intensively used by A)
 - the price of L increases, the price of K drops
- analytically, to obtain factor prices (w and r)
 - solve, for given P_T and P_A , the system:

$$\begin{cases} P_T = a_{KT} \times r + a_{LT} \times w \\ P_A = a_{KA} \times r + a_{LA} \times w \end{cases} \rightarrow \begin{cases} w = \frac{1}{a_{LT}} P_T - \frac{a_{KT}}{a_{LA}} r \\ r = \frac{a_{LT}}{a_{KA}} P_A - \frac{a_{LA}}{a_{KA}} w \end{cases}$$
$$r \left(\frac{a_{KA} a_{LT} - a_{LA} a_{KT}}{a_{KA} a_{LT}} \right) = \frac{1}{a_{KA}} P_A - \frac{a_{LA}}{a_{KA} a_{LT}} P_T$$
$$w = \frac{a_{KA} P_T - a_{KT} P_A}{a_{LT} a_{KA} - a_{KT} a_{LA}} \quad \text{and} \quad r = \frac{P_A a_{LT} - a_{LA} P_T}{a_{LT} a_{KA} - a_{KT} a_{LA}}$$

Relative Factor Prices: Properties

- the price of a factor:

$$w = \frac{a_{KA}P_T - a_{KT}P_A}{a_{LT}a_{KA} - a_{KT}a_{LA}} \quad \text{and} \quad r = \frac{P_A a_{LT} - a_{LA} P_T}{a_{LT}a_{KA} - a_{KT}a_{LA}}$$

- is increasing in the price of the good intensive in that factor (w of P_T , r of P_A)
 - is decreasing in the price of the other good (w of P_A , r of P_T)
- the relative price of a factor

$$\frac{w}{r} = \frac{a_{KA} \frac{P_T}{P_A} - a_{KT}}{a_{LT} - a_{LA} \frac{P_T}{P_A}}$$

- is increasing in the relative price of the good intensive in that factor

Relative Factor Prices: Properties

- *Stolper-Samuelson effect:*
 - *an increase in the price of a good (e.g., P_T) increases more than proportionally the price (w) of the factor it uses intensively (L)*

$$\% \Delta w > \% \Delta P_T > 0 > \% \Delta r$$

- if the relative endowment of a factor increases (e.g., L/K):
 - the relative price of the good that uses it intensively falls ($L/K \uparrow \rightarrow P_T/P_A \downarrow$)
 - the relative price of that factor fall ($P_T/P_A \downarrow \rightarrow w/r \downarrow$)

Equilibrium in Closed Economy: Summary

- supply

$$Q_T = \frac{a_{KA}L - a_{LA}K}{a_{KA}a_{LT} - a_{LA}a_{KT}} \quad Q_A = \frac{a_{LT}K - a_{KT}L}{a_{KA}a_{LT} - a_{LA}a_{KT}}$$

- RS is

$$\frac{Q_T}{Q_A} = \frac{a_{KA}L - a_{LA}K}{a_{LT}K - a_{KT}L}$$

- relative price of goods

$$\frac{P_T}{P_A} = \frac{b}{1-b} \frac{a_{LT} - a_{KT} \frac{L}{K}}{a_{KA} \frac{L}{K} - a_{LA}}$$

- relative price of factors

$$\frac{w}{r} = \frac{a_{KA} \frac{P_T}{P_A} - a_{KT}}{a_{LT} - a_{LA} \frac{P_T}{P_A}}$$

2 Countries

- consider home and foreign
- same tastes $\rightarrow RD=RD^*$
- same technology + different relative endowments
 - suppose $a_{LT}/a_{KT} > L/K > L^*/K^* > a_{LA}/a_{KA}$
 - A and T produced in both countries
 - home is relatively L -abundant
- in closed economy:
 - $RS > RS^*$: $L/K > L^*/K^* \rightarrow Q_T/Q_A > Q_T^*/Q_A^*$
 - $Q_T/Q_A > Q_T^*/Q_A^* \rightarrow P_T/P_A < P_T^*/P_A^*$

Equilibrium in Open Economy

- if both countries produce both goods:
 - the price of both goods has to be equal to the international (I) price in both countries:

$$P_T = P_T^* = P_T^I \quad \text{and} \quad P_A = P_A^* = P_A^I$$

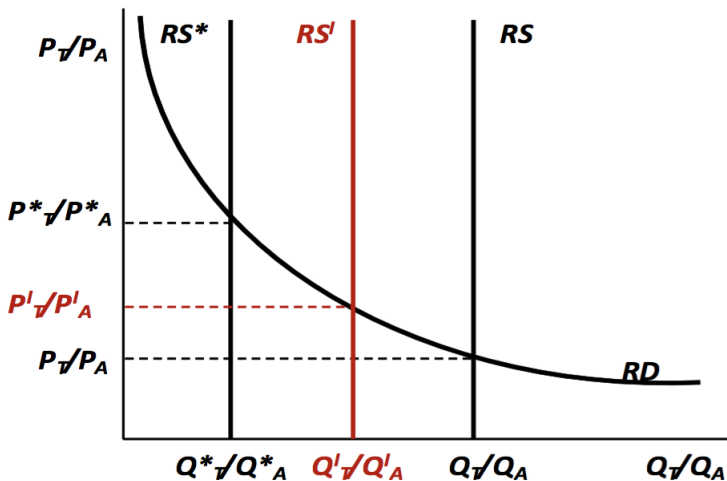
- the international goods market has to clear

$$\frac{1-b}{b} \frac{P_T^I}{P_A^I} = \frac{Q_A + Q_A^*}{Q_T + Q_T^*}$$

- given that $Q_T/Q_A > Q_T^*/Q_A^*$, the equilibrium relative price will lie between the closed-economy ones

$$P_T/P_A < P_T^I/P_A^I < P_T^*/P_A^*$$

Equilibrium in Open Economy: Graph



Equilibrium in Open Economy: Pattern of Trade

- the equilibrium relative price implies that:
 - for home, T becomes relatively more expensive \rightarrow home comparative advantage
 - for foreign, A becomes relatively more expensive \rightarrow foreign comparative advantage
- equilibrium relative demand implies that:
 - in both countries, relative demand of T is higher than RS^* and lower than RS
 - home exports T and imports A , foreign the other way around
- *Heckscher-Ohlin* Theorem:
 - in open economy, provided that no perfect specialization occurs, a country exports the good intensive in its relatively abundant factor

Equilibrium in Open Economy: Factor Prices

- if both countries produce both goods:
 - in perfect competition, prices must equal marginal costs in both countries

$$\begin{cases} P_T^I = a_{KT} \times r + a_{LT} \times w = a_{KT} \times r^* + a_{LT} \times w^* \\ P_A^I = a_{KA} \times r + a_{LA} \times w = a_{KA} \times r^* + a_{LA} \times w^* \end{cases}$$

- this requires that factor prices be equalized across countries

$$w = w^* = w^I \quad \text{and} \quad r = r^* = r^I$$

- important result: *factor price equalization*

Factor Prices and Income Distribution

- consequences for income distribution:
 - the increase in the relative price of T in home makes L gain relative to K

$$P_T^I/P_A^I > P_T/P_A \rightarrow w^I/r^I > w/r$$

- the increase in the relative price of A in foreign makes K^* gain relative to L^*

$$P_T^I/P_A^I < P_T^*/P_A^* \rightarrow w^I/r^I < w^*/r^*$$

- trade benefits the abundant factor and hurts the scarce factor

Application: Immigration to K-Abundant

- immigration from a third country into the foreign country:
 - $L^*/K^* \uparrow \rightarrow Q_T^*/Q_A^* \uparrow \rightarrow P_T^*/P_A^* \downarrow \rightarrow P_T^I/P_A^I \downarrow \rightarrow w^I/r^I \downarrow$
 - comparative advantage is weakened in both countries
 - less trade
 - lose part of the GFT
 - workers lose and capitalists gain

Application: Immigration to L-Abundant

- immigration from a third country into the home country
 - $L/K \uparrow \rightarrow Q_T/Q_A \uparrow \rightarrow P_T/P_A \downarrow \rightarrow P_T^I/P_A^I \downarrow \rightarrow w^I/r^I \downarrow$
 - comparative advantage is reinforced in both countries
 - more trade
 - larger GFT
 - workers lose relative to capitalists

Application: Migration from L to K-Abundant

- consider migration from the home to the foreign country
 - $L^*/K^* \uparrow \rightarrow Q_T^*/Q_A^* \uparrow$ and $L/K \downarrow \rightarrow Q_T/Q_A \downarrow$
 - $(L + L^*) / (K + K^*)$ unchanged $\rightarrow Q_T^I/Q_A^I$ unchanged
 - comparative advantage is weakened in both countries
 - less trade
 - smaller GFT
 - no effect on P_T^I/P_A^I and w^I/r^I since RS^I unchanged

Application: Migration from K to L-Abundant

- consider migration from the foreign to the home country
 - $L^*/K^* \downarrow \rightarrow Q_T^*/Q_A^* \downarrow$ y $L/K \uparrow \rightarrow Q_T/Q_A \uparrow$
 - $(L + L^*) / (K + K^*)$ unchanged $\rightarrow Q_T^I/Q_A^I$ unchanged
 - comparative advantage is reinforced in both countries (\rightarrow more trade)
 - more trade
 - larger GFT
 - no effect on P_T^I/P_A^I and w^I/r^I since RS^I unchanged

Application: Trade and the Skill Premium

- focus on the wage gap within a country
 - difference between the wage of different types of workers
 - skill premium: wage gap between skilled and unskilled
- rise in wage inequality and skill premium world-wide in the last 40 years
- possible determinants:
 - drop in relative supply of skilled labor world-wide
 - trade
 - technological change

Application: Trade and the Skill Premium

- Let's focus on the US-Mexico case
 - Let's assume technology is the same in both countries
 - 2 factors: High-skilled labor (H) and low-skilled labor (L)
 - 2 goods: textiles (intensive in L) and PCs (intensive in H)
 - H relatively more abundant in the US:

$$\frac{H^{USA}}{L^{USA}} > \frac{H^{MEX}}{L^{MEX}} \quad (1)$$

- Let's assume that $W_H > W_L$ in both countries

Application: Trade and the Skill Premium

Trade pattern

- Applying the theoretical results we have learned in class:
 - US exports PCs and imports textiles
 - Mexico exports textiles and imports PCs
- What happens when US and Mexico start increasing trade?
 - In the US:
 - The relative price of PCs goes up
 - The relative remuneration of H goes up $\frac{W_H}{W_L} \uparrow \Rightarrow$ skill-premium increases \Rightarrow inequality increases
 - In Mexico:
 - The relative price of PCs goes down
 - The relative remuneration of H goes down $\frac{W_H}{W_L} \downarrow \Rightarrow$ skill-premium decreases \Rightarrow inequality decreases

Application: Trade and the Skill Premium

What do we see in the data?

- skill-premium has increased in the US
- skill-premium has ALSO increased in the Mexico
- The basic HO model fails for Mexico

Application: Trade and the Skill Premium

Possible explanations

- Skill-biased technological change
 - This means that H has become more and more productive over time in both countries
 - This would imply a higher demand for H relative to L
 - This means that the skill-premium increases because of changes in technology
- Evidence in favor of this argument: production in the US has become more intensive in H in ALL sectors

Many Goods, Factors and Countries: Factor Content of Trade

- if many goods, factors and countries:
 - difficulty: which good is intensive in which factor?
 - difficulty: factor abundance relative to which other factor?
- alternative version of the H-O Theorem (HO-Vanek):
 - net factor f content of c 's trade = factor f endowment - factor f demand
 - define
 - V_c^f and V_w^f = country c and world (w) endowment of factor f
 - s_c = country c share in world income \rightarrow demand of f = $s_c V_w^f$
 - F_c^f = net factor f content of c 's trade

$$F_c^f = V_c^f - s_c V_w^f$$

- provided that no perfect specialization occurs, a country is net exporter of the services of its abundant factor and net importer of its scarce factor

Empirical Evidence: Factor Content of Trade

- Bowen et al. (1987) consider 27 countries and their endowment of 12 factors
- suppose country c has
 - endowment of factor j equal to 10% of world endowment of j
($V_c^j / V_W^j = 0.1$)
 - endowment of factor h equal to 2% of world endowment of h
($V_c^h / V_W^h = 0.02$)
 - a GDP equal to 5% of world GDP ($s_c = 0.05$)

- HO-Vanek predicts

–

$$F_c^f = V_c^f - s_c V_w^f$$

- c net exporter of j (5% of world endowment of j)
- c net importer of factor h (3% of world endowment of h)
- count for how many countries the net export of each factor follows the predicted pattern

Empirical Evidence: Factor Content of Trade (III)

- Trefler (1995) pointed out that H-O also predict the volume of net factor export
- the US had
 - 23% of world GDP
 - 5% of world workers
 - should import 4 times as many workers (18% of the world)
- in general: there is very little factor trade compared to H-O predictions (the "missing trade")
- Davis and Weinstein (2001): H-O works if you add
 - different technology (factor productivity)
 - no factor price equalization across countries
 - non-traded goods + trade costs

Empirical Evidence: Patterns of Export to the US

- Romalis (2004) shows the validity of a "quasi-H-O" prediction:
"countries abundant in skilled labor and capital capture a higher share of US imports in sectors intensive in those factors"
- intuition: given the set of exporters to a certain destination (the US),
 - skill-abundant countries are "better" at exporting skill-intensive goods
 - hence capture a higher import share the higher the skill intensity of the good
- advantages:
 - no need to assume same technology and factor price equalization
 - use high-quality and homogeneous data
- this prediction is supported by data on:
 - US import and technology for 370 sectors
 - factor endowments of 123 exporting countries

Trade and Unemployment

- countries differ markedly in labor market institutions:
 - how does trade interact with (possibly different) labor market institutions?
- Davis (1998)
 - before the 70s, unemployment in Europe was $\sim 2 - 3\%$, now it's much higher
 - European labor markets are rigid
 - claim: globalization + rigidity \rightarrow higher European unemployment
- trade model with two factors (H and L) and two countries:
 - US: flexible wages
 - Europe: binding minimum wage for unskilled workers
 - result: Europe-US trade can increase European unemployment

Wages and Unemployment

- flexible wages

- recall: $\frac{w_H}{w_L} = \left(\frac{A_H}{A_L}\right)^{\frac{\epsilon-1}{\epsilon}} \left(\frac{L}{H}\right)^{\frac{1}{\epsilon}}$
- normalize $w_H = 1$ and $(A_H/A_L)^{\frac{\epsilon-1}{\epsilon}} = a$

$$w_L^* = a^{-1} (H/L)^{1/\epsilon}$$

w_L^* wage consistent with market clearing

- rigid wages

- binding minimum wage, $\bar{w}_L > w_L$

$$\bar{w}_L = a^{-1} (H/L^e)^{1/\epsilon}$$

where $L^e = L - U$ is employed unskilled workers

- unemployment:

$$U = L - H (a\bar{w}_L)^{-\epsilon}$$

- at $\bar{w}_L > w_L^*$ firms are not willing to employ all L

Unemployment and Comparative advantage

- consider Europe and the United States

- same endowments: $L^{EU} = L^{US} = L$, $H^{EU} = H^{US} = H$
- different labor markets: flex US vs rigid EU (binding \bar{w}_L)
- autarky relative supply

$$\frac{Q_C^{US}}{Q_T^{US}} = \frac{A_H H}{A_L L} < \frac{A_H H}{A_L L^e} = \frac{Q_C^{EU}}{Q_T^{EU}}$$

- autarky relative price

$$\frac{P_C^{US}}{P_T^{US}} = \left(\frac{A_H H}{A_L L} \right)^{-1/\epsilon} > \left(\frac{A_H H}{A_L L^e} \right)^{-1/\epsilon} = \frac{P_C^{EU}}{P_T^{EU}} = \frac{A_L}{A_H \bar{w}_L}$$

- Europe has comparative advantage in C (skill-intensive good)!

Trade and European Unemployment

- if US and EU can trade
 - EU (US) consumers want to buy T (C) in the US (EU)
 - upward pressure on P_C^{EU}/P_T^{EU}
 - problem: P_C^{EU}/P_T^{EU} pinned down by \bar{w}_L
 - solution: EU keeps P_C^{EU}/P_T^{EU} by raising Q_C^{EU}/Q_T^{EU}
 - need to fire more L until

$$\bar{w}_L = \frac{1}{a} \left(\frac{2H}{L + (L^e)^I} \right)^{1/\epsilon}$$

- free-trade unemployment:

$$U_{EU}^I = 2 \left[L - \frac{H}{(a\bar{w}_L)^\epsilon} \right], \quad U_{US} = 0$$

- other global events that can raise European unemployment:
 - immigration of L to the US can increase unemployment in Europe
 - SBTC ($a \uparrow$) can increase unemployment in Europe