

Identifying News Shocks from Forecasts

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Motivation

- Macroeconomic shocks have different effects when they are anticipated (**news** shocks) versus when they are unanticipated (**surprise** shocks)
- How can we identify news vs. surprise shocks in macroeconomic data?
 - Even cleanly identified shocks mix surprises with news about the future
- Challenging when there is news about **multiple** shocks!

Contributions

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 - Benefit of our method: *joint identification* of fiscal/monetary news and surprises
 - Coordinated monetary-fiscal policy reduces inflation (output) variance by an extra 10 (30) percent over uncoordinated.

Why Can Forecasts Help? A Simple Example

- To build intuition, consider the simple NK model:

New Keynesian Phillips curve: $\pi_t = \beta \mathbb{E}_t[\pi_{t+1}] + \kappa y_t + x_t$

Euler equation: $0 = \mathbb{E}_t[z_t + \gamma(y_t - y_{t+1}) + i_t - \pi_{t+1}]$

Taylor rule: $i_t = \phi_\pi \pi_t + h_t$

where x_t and z_t are iid shocks, and h_t is the exogenous policy residual

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- h_t is autocorrelated:

$$h_t = \rho h_{t-1} + u_t + v_{t-1}$$

u_t is monetary policy *surprise* and v_{t-1} is monetary policy *news*

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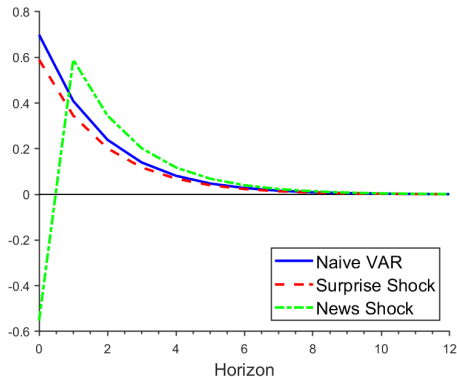
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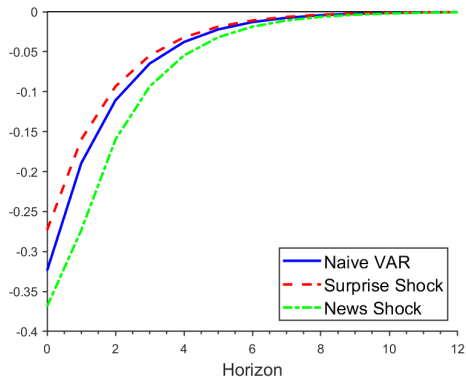
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- u_t and v_{t-1} are individually known to agents in the model, but *not the econometrician!*

Why Can Forecasts Help? A Simple Example



(a) Interest Rate IRFs



(b) Inflation IRFs

Figure 1: Impulse Response Functions in the Simple Example

“Naive VAR” identifies by causal ordering, and consistently estimates IRFs w/o news.

Information in the Simple Example

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- In this example, only one news shock, so only need one forecast: $f_t^\pi \equiv \mathbb{E}_t[\pi_{t+1}]$
- Intuition for identification: news today cause forecasts today and outcomes tomorrow to move together; surprises cause today's outcomes to depart from yesterday's forecasts.

Identification with Forecasts the Simple Example

- Model solution is:

$$\pi_t = b_h^\pi h_t + b_v^\pi v_t + b_x^\pi x_t + b_z^\pi z_t$$

$$y_t = b_h^y h_t + b_v^y v_t + b_x^y x_t + b_z^y z_t$$

$$i_t = b_h^i h_t + b_v^i v_t + b_x^i x_t + b_z^i z_t$$

$$h_t = \rho h_{t-1} + u_t + v_{t-1}$$

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- ... so inflation forecast is

$$f_t^\pi = \mathbb{E}_t[\pi_{t+1}]$$

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$$= \mathbb{E}_t[b_h^\pi h_{t+1}] = b_h^\pi \rho h_t + b_h^\pi v_t$$

- Using forecasts, we can separately identify surprise shocks ($u_t = h_t - \frac{1}{b_h^\pi} f_{t-1}^\pi$) from news shocks ($v_t = \rho h_t - \frac{1}{b_h^\pi} f_t^\pi$)!

What's in the paper

- General Case with Multiple News Shocks

- Set up
- Identification: Conditions and implementation
- Verification via Monte Carlo simulation

► Identification

- Application to the US

- Data
- Constructing forecasts
- Impulse responses and shock labeling
- Shock validation
- News versus surprise IRFs
- Accounting for sources of macro fluctuations

► Forecast cleaning

► See the data

► Shock Validation

► News vs. Surprise IRFs

- Counterfactual policies without a structural model

- Impulse responses under active policies
- Assessing the benefits of policy coordination
- Impulse responses under passive policies

► IRFs: Stabilization policies

► IRFs: Passive policies

General SVAR Representation

- $n \times 1$ vector x_t determined by lags, structural shocks ϵ_t , and news v_t :

$$x_t = \sum_{j=1}^m B_j x_{t-j} + A\epsilon_t + Cv_t$$

- $n \times 1$ structural shocks have news and surprise components:

$$\epsilon_t = u_t + v_{t-1}$$

- **Theorem 1:** Equilibrium in a large class of models has this form
- Normalize the orthogonal structural shocks $Var(\epsilon_t) = I$
- Assume news/surprise also orthogonal (i.e. ϵ_t dimensions are *independent*) so diagonal variances satisfy:

$$Var(u_t) = D_u^2 \quad Var(v_t) = D_v^2 \quad \implies D_u^2 + D_v^2 = I$$

General SVAR Identification

- **Theorem 2:** If we have unbiased forecasts f_t for all entries of x_t , we can identify A , C , D_u^2 , D_v^2 and $\{B_j\}_{j=1}^m$
- Intuition: rational forecasts imply “enough” restrictions

$$x_t = \sum_{j=1}^m B_j x_{t-j} + A\epsilon_t + Cv_t$$

$$\implies f_t = \mathbb{E}_t[x_{t+1}] = \sum_{j=1}^m B_j x_{t+1-j} + Av_t$$

- Approach: stack and estimate a VAR for $\begin{pmatrix} f_t \\ x_t \end{pmatrix}$ with linear restrictions

Application to Fiscal and Monetary Policy

- Quarterly US data from 1968:IV - 2016:IV
- Baseline model with 6 time series and associated forecasts, deseasonalized and detrended
- Clean the forecasts using additional time series and forecasts, selecting variables by machine learning
- Lag length determined by AIC
- Bootstrapped standard errors

► Forecast cleaning

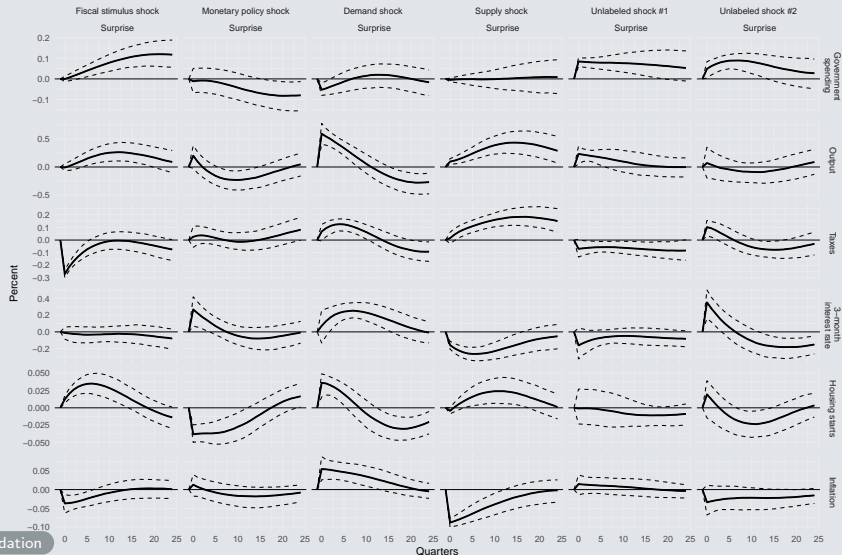
| Variable | Date range | Forecast Source |
|---------------------------------------|-------------------|--|
| <i>Baseline Specification</i> | | |
| Real GDP | 1968:IV - 2022:II | SPF |
| Federal tax receipts | 1968:IV - 2016:IV | Fed Greenbooks |
| Real government spending | 1968:IV - 2022:II | Fed Greenbooks for 1968:IV - 1981:II SPF for 1981:III - 2022:II |
| GDP deflator | 1968:IV - 2022:II | SPF |
| 3-month Treasury rate | 1968:IV - 2022:II | Yield curve |
| Housing starts | 1968:IV - 2022:II | SPF |
| <i>Additional Variables</i> | | |
| Unemployment Rate | 1968:IV - 2022:II | SPF |
| Industrial production | 1968:IV - 2022:II | SPF |
| Federal budget surpluses | 1968:IV - 2016:IV | Fed Greenbooks |
| USD/CAD exchange rate | 1968:IV - 2022:II | Futures contracts |
| Real oil price | 1983:I - 2022:II | Futures contracts |
| 1, 2, 3, 4, and 5-year Treasury rates | 1968:IV - 2022:II | Yield curve |

Table 1: List of Variables

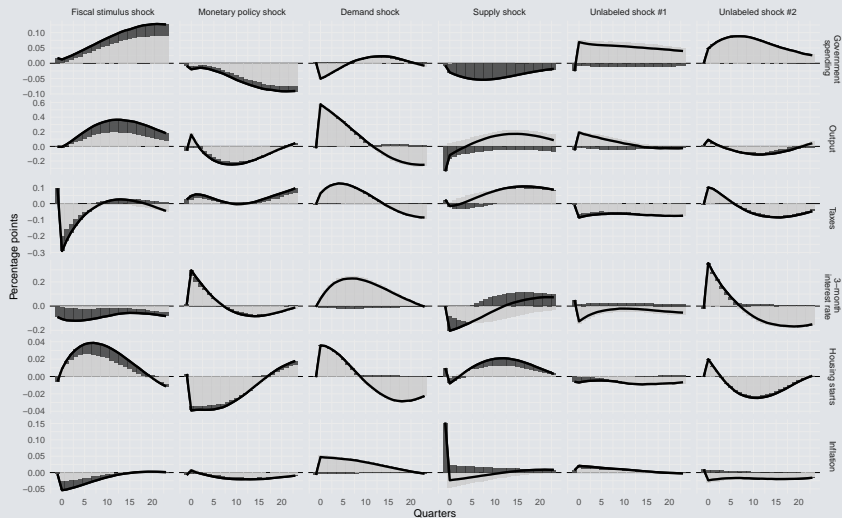
Shock Labeling

- SVARs require a scheme for labeling shocks
- We label based on responses to the surprise structural shocks u_t over the medium run. For example:
 - a “Fiscal Stimulus Shock” increases government spending, decreases taxes, and increases real activity.
 - a “Monetary Policy Shock” increases interest rates, decreases real activity and inflation
 - a “Demand Shock” increases interest rates, real activity and inflation.
 - a “Supply Shock” increases real activity, and decreases interest rates and inflation
- When bootstrapping standard errors, we label shocks to minimize the error with our baseline estimates (satisfying Lewis (2021) theorem)

Structural Shock IRFs to 1 s.d. Surprise Shocks



Structural Shock IRFs Decomposed



Long-Run Variance Decomposition

| Variable | Type | Fiscal stimulus | Mon. policy | Demand | Supply | Unlabeled #1 | Unlabeled #2 | Total |
|-----------------------|----------|-----------------|-------------|--------|--------|--------------|--------------|-------|
| Gov. spending | News | 4.5 | 3.6 | 1.6 | 5.6 | 2.2 | 1.1 | 24.3 |
| | Surprise | 20.4 | 10.0 | 3.8 | 2.3 | 14.8 | 12.3 | 75.7 |
| | Total | 25.6 | 15.8 | 6.4 | 9.7 | 18.5 | 14.5 | 100.0 |
| Output | News | 7.0 | 2.2 | 3.7 | 4.3 | 2.1 | 2.3 | 26.3 |
| | Surprise | 8.0 | 6.7 | 19.5 | 23.9 | 4.6 | 4.3 | 73.7 |
| | Total | 15.9 | 9.9 | 24.4 | 28.3 | 8.3 | 7.7 | 100.0 |
| Taxes | News | 4.9 | 3.3 | 1.9 | 1.7 | 1.8 | 2.3 | 19.4 |
| | Surprise | 12.5 | 4.7 | 11.6 | 30.3 | 7.6 | 7.4 | 80.6 |
| | Total | 18.2 | 8.6 | 14.5 | 32.1 | 10.1 | 10.9 | 100.0 |
| 3-month interest rate | News | 5.6 | 2.2 | 3.7 | 5.8 | 2.1 | 2.3 | 25.9 |
| | Surprise | 2.8 | 8.0 | 16.9 | 18.1 | 4.9 | 17.4 | 74.1 |
| | Total | 9.2 | 11.2 | 22.5 | 24.8 | 8.1 | 20.0 | 100.0 |
| Housing starts | News | 5.1 | 2.4 | 2.2 | 2.0 | 1.8 | 1.8 | 19.0 |
| | Surprise | 13.8 | 18.4 | 17.7 | 8.3 | 6.0 | 9.6 | 81.0 |
| | Total | 19.3 | 21.7 | 20.8 | 11.4 | 8.3 | 12.2 | 100.0 |
| Inflation | News | 4.1 | 1.9 | 4.3 | 17.0 | 1.5 | 2.9 | 37.8 |
| | Surprise | 5.2 | 4.0 | 12.6 | 21.9 | 2.4 | 7.0 | 62.2 |
| | Total | 10.0 | 7.4 | 19.6 | 40.4 | 4.8 | 11.8 | 100.0 |
| Unweighted average | News | 5.2 | 2.6 | 2.9 | 6.1 | 1.9 | 2.1 | 25.5 |
| | Surprise | 10.5 | 8.6 | 13.7 | 17.5 | 6.7 | 9.7 | 74.5 |
| | Total | 16.4 | 12.4 | 18.0 | 24.5 | 9.7 | 12.8 | 100.0 |

Policy Rule Counterfactuals: McKay and Wolf (2023) method

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 - ... so choose counterfactual shock covariances!

Policy Counterfactuals: Tradeoffs and policy coordination

| Target: | Inflation | | | Output | | | Dual Mandate | | |
|-----------------------|--------------|-------------|--------------|--------------|-------------|--------------|--------------|-------------|--------------|
| <i>Policy used</i> | <i>Fisc.</i> | <i>Mon.</i> | <i>Joint</i> | <i>Fisc.</i> | <i>Mon.</i> | <i>Joint</i> | <i>Fisc.</i> | <i>Mon.</i> | <i>Joint</i> |
| Inflation | 0.19 | 0.09 | 0.00 | 0.46 | 1.41 | 0.80 | 0.43 | 0.44 | 0.34 |
| Output | 1.03 | 1.45 | 1.56 | 0.30 | 0.33 | 0.01 | 0.56 | 0.58 | 0.37 |
| Government spending | 3.28 | 2.73 | 1.24 | 2.77 | 1.08 | 2.47 | 2.49 | 1.22 | 1.32 |
| Taxes | 4.56 | 2.22 | 3.06 | 5.15 | 2.09 | 3.91 | 6.02 | 1.43 | 1.72 |
| 3-month interest rate | 1.22 | 0.84 | 2.02 | 1.06 | 1.15 | 2.12 | 1.69 | 0.82 | 0.43 |
| Housing starts | 1.85 | 1.09 | 1.09 | 0.92 | 1.06 | 0.89 | 0.80 | 0.68 | 0.25 |

Table 2: Variance relative to baseline

► IRFs: Stabilization policies

► IRFs: Passive policies

Conclusion

- Including forecasts in VARs can identify news and surprise components of structural shocks
- We estimate realistic effects of fiscal and monetary shocks in US data
- News is a notable driver of business cycles
- News/surprise identification is particularly useful for estimating policy counterfactuals
- More work to do!

Identification Proof

- Constructive proof – we derive an analytical estimator for A and C given Σ and B_1
- Assumptions: structural shocks have linearly independent effects, and each shock has a news component
- Simple to implement – a few lines of matrix operations
- Only identified up to sign and column order (typical) – when calculating, ambiguity is due to non-uniqueness of the singular value decomposition

Deriving the Estimator (1/2)

- Subdivide the matrix $\Sigma = \begin{pmatrix} \Sigma_{11} & \Sigma'_{21} \\ \Sigma_{21} & \Sigma_{22} \end{pmatrix}$ into $n \times n$ blocks:

$$\begin{pmatrix} \Sigma_{11} & \Sigma'_{21} \\ \Sigma_{21} & \Sigma_{22} \end{pmatrix} = \begin{pmatrix} (B_1 C + A) D_v^2 (B_1 C + A)' + B_1 A D_u^2 A' B_1' & \\ CD_v^2 (B_1 C + A)' + A D_u^2 A' B_1' & CD_v^2 C' + A D_u^2 A' \end{pmatrix}$$

- Define the $n \times n$ matrices ϕ and ψ by

$$\begin{aligned} \phi &\equiv \Sigma_{11} - B_1 \Sigma_{21} - \Sigma'_{21} B_1' + B_1 \Sigma_{22} B_1' \\ &= A D_v^2 A' \end{aligned}$$

$$\begin{aligned} \psi &\equiv \Sigma_{22} - (\Sigma_{21} - \Sigma_{22} B_1') \phi^{-1} (\Sigma_{21} - \Sigma_{22} B_1')' \\ &= A D_u^2 A' \end{aligned}$$

Deriving the Estimator (2/2)

- The variance restriction implies:

$$\phi + \psi = AA'$$

- SVD of $\phi + \psi$ gives unitary matrix U and diagonal matrix Λ^2 such that for some unitary V

$$\phi + \psi = U\Lambda^2U' \quad A = U\Lambda V'$$

- SVD of $\Lambda^{-1}U'\phi U\Lambda^{-1}$ gives the matrices V and D_V^2 from

$$\Lambda^{-1}U'\phi U\Lambda^{-1} = V'D_V^2V$$

- This gives the matrices $A = U\Lambda V'$ and $D_u^2 = I - D_V^2$. Then the final matrix C is found from

$$C = (\Sigma_{21} - \Sigma_{22}B_1')(D_V^2A')^{-1}$$

General SVAR: Include Forecasts

- $n \times 1$ vector of forecasts $f_t = \mathbb{E} \left[x_{t+1} | \{x_{t-j}\}_{j=0}^{m-1}, \epsilon_t, v_t \right]$:

$$f_t = \sum_{j=1}^m B_j x_{t+1-j} + A v_t$$

- Stack the expectations and time series into a single VAR($m-1$):

$$\begin{pmatrix} f_t \\ x_t \end{pmatrix} = \sum_{j=1}^{m-1} \mathbf{B}_j \begin{pmatrix} f_{t-j} \\ x_{t-j} \end{pmatrix} + \mathbf{A} \begin{pmatrix} v_t \\ u_t \end{pmatrix} \quad (1)$$

- With matrices:

$$\mathbf{B}_j \equiv \begin{cases} \begin{pmatrix} B_1 & B_2 \\ I & 0 \end{pmatrix} & j = 1 \\ \begin{pmatrix} 0 & B_{j+1} \\ 0 & 0 \end{pmatrix} & j > 1 \end{cases} \quad \mathbf{A} \equiv \begin{pmatrix} B_1 C + A & B_1 A \\ C & A \end{pmatrix}$$

Identifying Restrictions

$$x_t = \sum_{j=1}^m B_j x_{t-j} + A\epsilon_t + Cv_t$$

- B_j matrices identified from \mathbf{B}_j matrices in stacked VAR
- A and C ? Classic SVAR problem:
 - Observe $2n \times 1$ innovation $w_t = \mathbf{A} \begin{pmatrix} v_t \\ u_t \end{pmatrix}$ with $\text{Var}(w_t) \equiv \Sigma$
 - $\Sigma = \mathbf{A} \text{Var} \begin{pmatrix} v_t \\ u_t \end{pmatrix} \mathbf{A}'$ is symmetric: only $2n^2 + n$ unique entries
 - $\mathbf{A} = \begin{pmatrix} B_1 C + A & B_1 A \\ C & A \end{pmatrix}$ has $2n^2$ unknowns (A and C)
 - Shock variances: $D_u^2 + D_v^2 = I$ adds $2n$ unknowns and n restrictions

Policy Rule Counterfactuals: Implementation (1/2)

- Policymaker controls shock g . Consider policy rules linear in other shocks:

$$\underbrace{\begin{bmatrix} u_t^g \\ v_t^g \end{bmatrix}}_{\text{policy shocks}} = \underbrace{\alpha}_{\text{to be found}} \underbrace{\begin{bmatrix} u_t^{-g} \\ v_t^{-g} \end{bmatrix}}_{\text{other shocks}}$$

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- The counterfactual impulse responses *to other shocks* $\psi_u(h)$ and $\psi_v(h)$ are:

$$\begin{bmatrix} \psi_u(h) & \psi_v(h) \end{bmatrix} = \begin{bmatrix} \phi_u^{-g}(h) & \phi_v^{-g}(h) \end{bmatrix} + \begin{bmatrix} \phi_u^g(h) & \phi_v^g(h) \end{bmatrix} \alpha$$

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Policy Rule Counterfactuals: Implementation (2/2)

- To estimate the counterfactual, find α to minimize some loss function for a matrix F :

$$\min ||F x_t||$$

- F may encode a policy objective (e.g. output stabilization) or a specific policy rule (e.g. a Taylor rule)
- Choose α to minimize the loss measured in IRFs over all h 's:

$$\min \left\| F \begin{bmatrix} \psi_u(h) & \psi_v(h) \end{bmatrix} \right\| = \min \left\| F \begin{bmatrix} \phi_u^{-g}(h) & \phi_v^{-g}(h) \end{bmatrix} + F \begin{bmatrix} \phi_u^g(h) & \phi_v^g(h) \end{bmatrix} \alpha \right\|$$

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 - Constructing an in-sample rational expectation
 - Removes biases and small sample correlations

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- To construct the rational expectation f_t from empirical expectations \tilde{f}_t , run the VAR(k) with $k \geq m$:

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- Cleaned forecast f_t is best linear forecast of x_{t+1} given \tilde{f}_t , x_t , and other regressors z_t . Baseline: Construct z_t as a machine-learning predictor for x_t using a large set of other variables (include lots of information without over-fitting).

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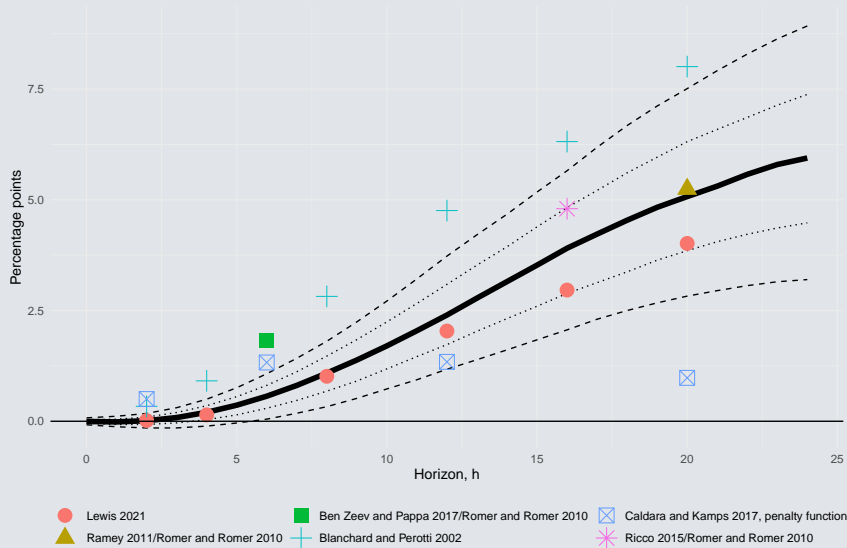
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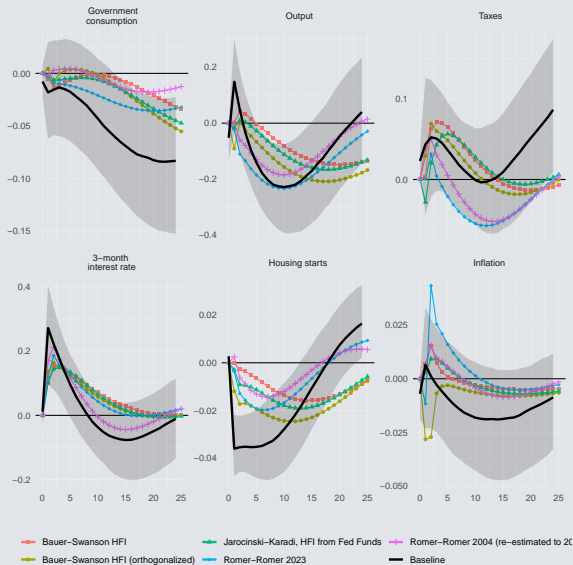
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- Monetary policy shocks
 - Compare with shocks from the literature
- Appear reasonable, and robust to alternative specifications

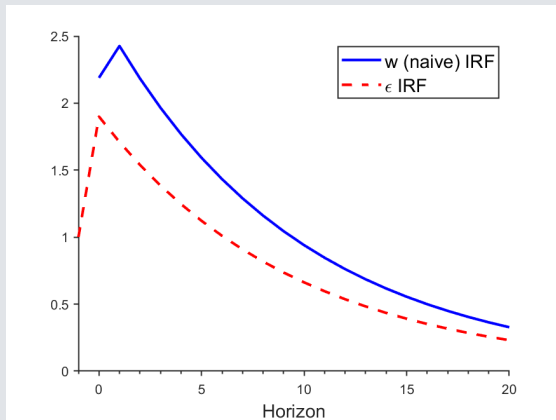
Fiscal Stimulus Cumulative Multipliers



Monetary Policy IRFs

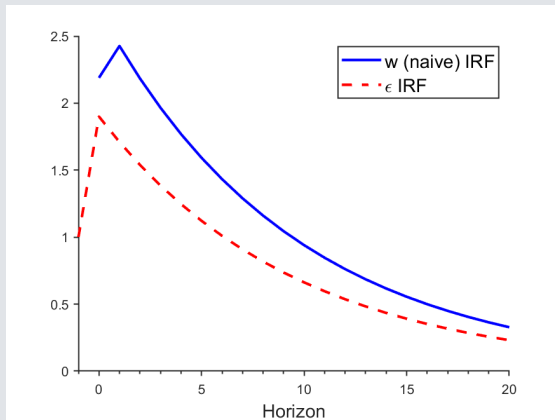


IRFs in the Simple Example



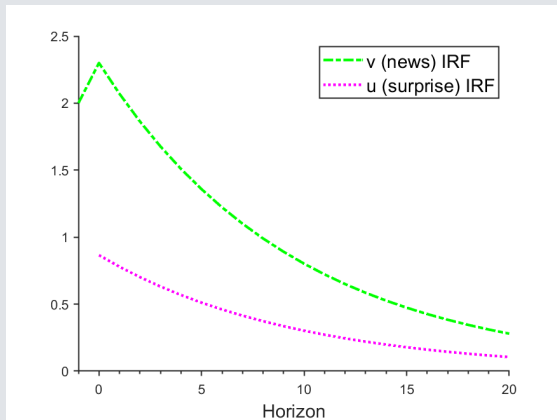
- Estimating x_t ARMA(1,1)
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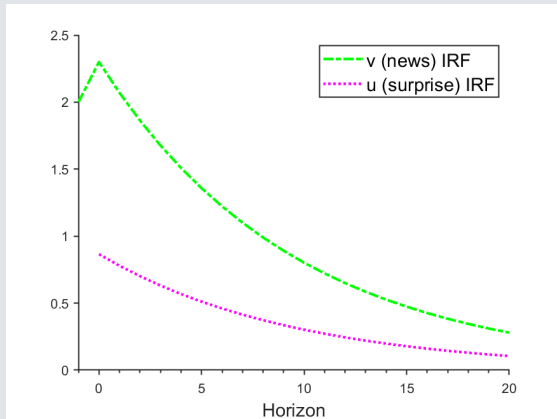
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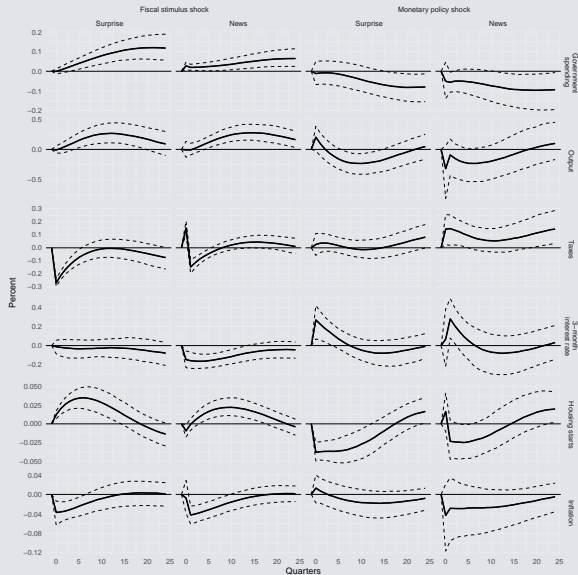


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- ... linear combination recovers the ϵ_t **IRF**

Baseline Series and Forecasts

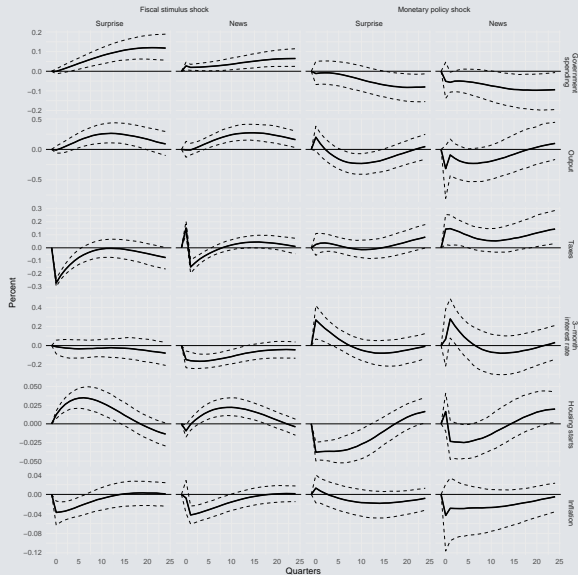


Policy Shock IRFs Decomposed



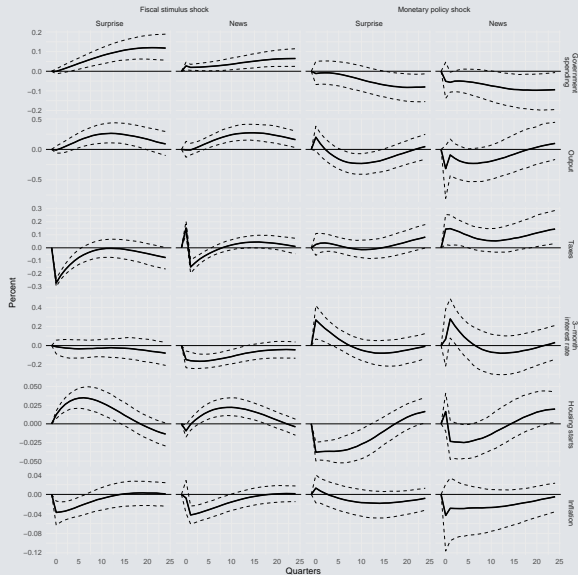
- News shock is scaled to be as if a unit SD surprise is expected in period 1.

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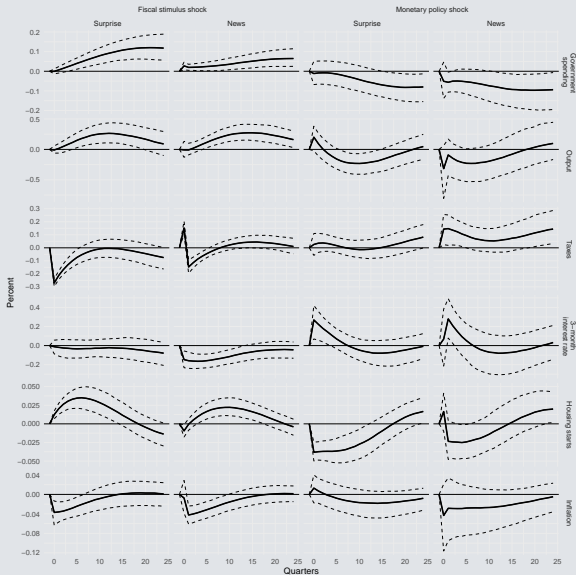
- News shock is scaled to be as large as a unit SD surprise is expected in period 1.
- In the long run, responses look similar (sense check)

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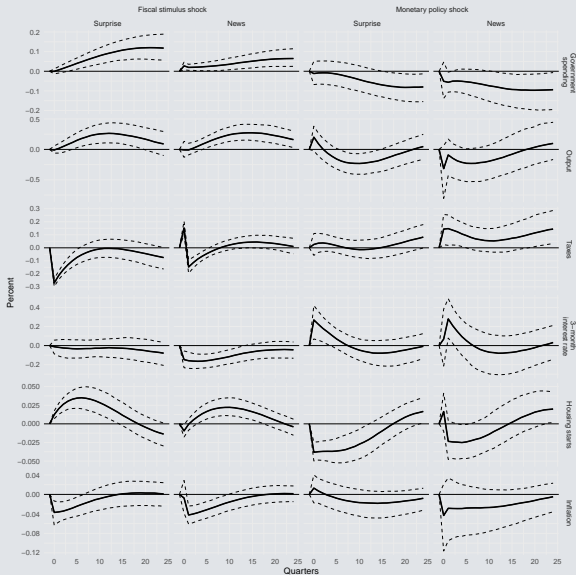
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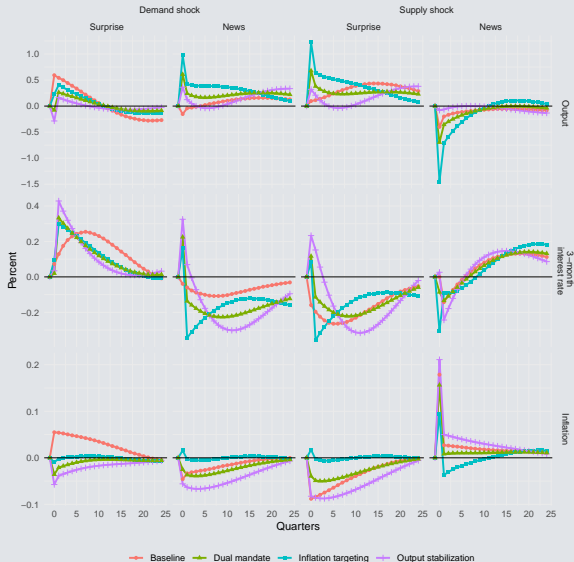
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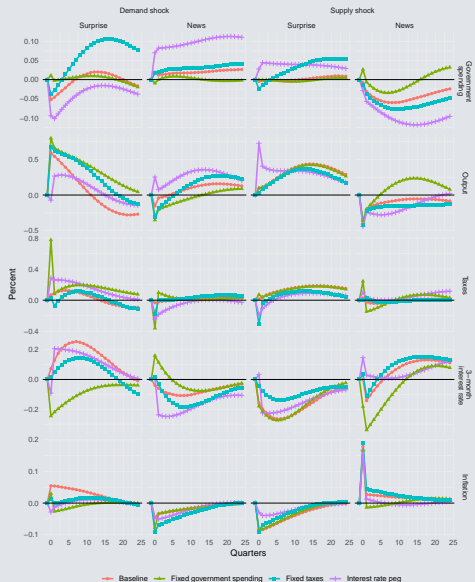
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- In the long run, responses look similar (sense check)
- Anticipation effects are non-negligible
 - Anticipated fiscal expansion (partly) pre-funded by taxes.
 - Monetary policy: no liquidity effect.

Monetary Policy Counterfactual: Business cycle stabilization



- Minimize one of three quadratic objective functions: weight on either inflation, output, or equally on both.
- Single objectives successfully implemented (not pre-baked).
- Demand surprises: raise rates to stabilize both output and inflation. (Demand news is tiny)
- Supply shocks: Cut (raise) interest rates to stabilize inflation (output).

Passive Policy Counterfactual



- What if government spending was acyclical?
- Much harder to implement.
- Substantially more output volatility Inflation depends on the nature of the shock
- Current government spending behavior moderates business cycles?

► Back