

# ST 705 Linear models and variance components

## Lab practice problem set 3

January 24, 2023

1. Let  $A$  be an  $m \times n$  matrix and  $B$  be an  $n \times p$  matrix. Prove that  $AB$  can be written as a sum of  $n$  matrices of rank at most one. Hint: think about empirical covariance matrices.
2. If  $P$  is a symmetric and idempotent matrix, show that the Pythagorean relationship holds:

$$\|y\|^2 = \|Py\|^2 + \|(I - P)y\|^2.$$