

# ST 705 Linear models and variance components

## Lab practice problem set 4

January 31, 2023

1. Let  $G : \mathbb{R}^p \rightarrow \mathbb{R}$  defined by  $G(\beta) := (y - X\beta)'W(y - X\beta)$ . Derive an expression for  $\nabla_{\beta}G(\beta)$ .
2. Show that  $I_n - P_X$  is the unique symmetric projection matrix onto  $\text{null}(X')$ .