

CS170 — Fall 2017— Homework 5 Solutions

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0. Who Did You Work With?

Collaborators: Kevin Vo, Aleem Zaki, Jeremy Ou

1. Scheduling Homeworks

- (a)
- (b)
- (c)

2. Graph Coloring

- (a) Following the hint, allow $p(G) : G \mapsto \mathbb{N}_0$ to denote the potential of a graph G . Let this potential be explicitly defined as the number of edges in E that have the same color vertex on either end (same-color edges), which by definition always takes on a value $\in \mathbb{N}_0$. Each time that the loop runs, a vertex $v \in B$ is changed from one color to the other. $\forall v \in B$ there are ≥ 85 vertices adjacent to v and of the same color, and there are at most 85 vertices adjacent to v of the opposite color. This shows that even with the maximal number of non-similar and minimal similar adjacent vertices there is still a decrease in the number of same-color edges by at least one (namely, one of the edges with v as an end) when you switch the color of v . Thus, each iteration of the loop leads to a decrease of the value of $p(G)$ by at least one.
- (b)

3. 170-Graph

Main Idea:

ok

Run Time:

ok

4. Weighted Set Cover

5. Quaternary Huffman

Main Idea:

ok

Proof of Correctness:

ok \square

6. Simple and Naive Cluster Analysis