

# Market Structure, Investment and Technical Efficiencies in Mobile Telecommunications\*

Jonathan Elliott,<sup>†</sup> Georges V. Hounghonon,<sup>‡</sup>  
Marc Ivaldi,<sup>§</sup> Paul Scott<sup>¶</sup>

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## Abstract

We develop a model of competition in prices and infrastructural investment among mobile network providers. Market shares and service quality (download speed) are simultaneously determined, for demand affects the network load just as delivered quality affects consumer demand. While consolidation typically has adverse impacts on consumer surplus, economies of scale, which we derive from physical principles, push in the other direction. We find that consumer surplus is maximized at a relatively high number of firms, and that the optimal number of firms is higher for lower-income consumers. Total surplus, meanwhile, is maximized at a moderate number of firms. Our modeling framework allows us to quantify the marginal social value of allocating more spectrum to mobile telecommunications, finding it is roughly five times an individual firm's willingness to pay for a marginal unit of spectrum.

**Keywords:** Market structure, scale efficiency, antitrust policy, infrastructure, endogenous quality, queuing, mobile telecommunications.

**JEL Classification:** D21, D22, L13, L40.

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<sup>†</sup>New York University, jonathan.elliott@nyu.edu

<sup>‡</sup>IFC-World Bank Group, ghounghonon@ifc.org, gvivienh@gmail.com

<sup>§</sup>Toulouse School of Economics, marc.ivaldi@tse-fr.eu

<sup>¶</sup>New York University, ptscott@stern.nyu.edu

# 1 Introduction

Numerous contentious policy questions have arisen recently in the mobile telecommunications industry related to antitrust and spectrum allocation. Common to these debates is the question of how market structure impact prices and quality of service.

In this paper, we develop a structural model of the mobile telecommunications industry to capture the impact of changes in industry structure (in particular, the number of network operators and the allocation of spectrum), on equilibrium outcomes such as prices, investment, quality of service (download speeds), and welfare. This allows us to assess the trade-off between market power and economies of scale, both in the traditional sense, where consolidation may result in higher or lower prices (Williamson, 1968), and in understanding how consolidation affects download speeds, which is endogenously determined by firms' investments, spectrum allocation, and the load on the network imposed by data consumption.<sup>1</sup>

We model the determination of quality of service using an engineering model (Blaszczyszyn, Jovanovity and Karray, 2014) with three pieces, each having important economic implications: path loss, information theory, and queuing theory. Our study thus falls within the tradition of engineering production functions of Chenery (1949).

Path loss (i.e., the reduction in power of electromagnetic waves as they travel) results in *economies of density*: a mobile network operator can serve a densely populated area more efficiently (meaning either higher download speed at a given cost or the same download speed at a lower cost) than a sparsely populated area.<sup>2</sup> As the populations density served by a firm is inversely proportional to the number of firms (at least in a symmetric equilibrium), these these economies of density mean that service can be lower cost (or higher quality) when the number of firms is small if we hold the total investment in the industry fixed. Of course, whether these economies of density actually lead to more efficient service in equilibrium depends on firms' endogenous investment decisions.

Information theory, specifically the Shannon-Hartley theorem, tells us how a firm's channel capacity (i.e., the maximum rate of data transmission) depends on the bandwidth (amount of spectrum) operated. By explicitly modeling this dependence, we can understand the impacts of spectrum allocation. For instance, we consider what happens when the spectrum allocation

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<sup>1</sup>Quality of service has featured prominently in recent merger cases. For instance, the Sprint/T-Mobile merger was allowed based on the finding "that quality benefits and dynamic competition serve as countervailing forces to the static analysis that substantially address its predicted harmful price effects" (Federal Communications Commission, 2019).

<sup>2</sup>For example, suppose that the number of base stations per person is held constant across different population densities, so that less population-dense areas have lower base station density. Because signals in the sparsely populated areas will have to travel further on average, they will experience greater path loss, and sparsely populated areas will have inferior service despite receiving the same level of investment per capita.

to the sector is fixed, but we vary the number of firms that the spectrum is divided across. We also consider how equilibrium outcomes change when the amount of spectrum allocated to the industry is varied, allowing us to compute the marginal value of spectrum allocation to mobile telecommunications.

Queuing theory allows us to understand how the allocation of shared resources leads to economies of scale, in the spirit of Mulligan (1983), De Vany (1976), and Carlton (1978). If two network operators were to combine both their customer bases and owned bandwidth, the combined firm can more efficiently allocate network capacity among customers more efficiently, leading to higher download speeds.

We embed the engineering model of data transmission within an equilibrium model of competition among firms that operate mobile networks. Firms choose prices of various mobile service plans and the level of investment in infrastructure. Consumers respond in both their mobile contract choices and their data consumption decisions to prices and the download speeds.

A challenge for accurately modeling quality of service is the fact that consumer demand for data and download speeds are simultaneously determined. Consumer demand for a network operator’s services depends on its quality of service, and its quality of service depends on consumer demand due to congestion externalities. Most demand models for mobile services do not model the simultaneous determination of demand and quality of service (including Bourreau, Sun and Verboven (2018), Cullen, Schutz and Shcherbakov (2016), Fan and Yang (2016), Sinkinson (2020), Sun (2015), Weiergräber (2018)). Only El Azouzi, Altman and Wynter (2003) and Lhost, Pinto and Sibley (2015) model the simultaneous determination of service quality and choice of service provider using queuing theory like we do. Our study builds on these by incorporating path loss (and therefore economies of density) and by estimating a product-level demand model using detailed consumption and quality data. Meanwhile, in the engineering literature, Hua, Liu and Panwar (2012) examine how integrating network resources benefits both from economies of density and pooling, but without an economic equilibrium framework that endogenizes consumers’ choices and firms’ investments.<sup>3</sup>

We estimate a model of demand for mobile plans and data consumption based on the French market in 2015. Our estimation relies on a unique data set from the French mobile market. We obtain data on choices and consumption by nearly 15 million customers in October 2015 from

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<sup>3</sup>Björkegren (2019) also models endogenous investment in infrastructure in mobile telecommunications. A key difference is that Björkegren’s setting is a less-developed country where geographic coverage is the product characteristic affected by network operators’ investments; ours is a developed country where we take full geographic coverage for granted. Instead, we model the determination of quality of service, which calls for incorporating several features in our infrastructure model that Björkegren’s model ignores – in particular, path loss, bandwidth, and congestion.

a single mobile network operator, Orange Mobile.<sup>4</sup> We also secure data on quality of mobile broadband, measured as the actual speed experienced by users. We complement these data with information on network deployment from the spectrum frequency regulator (ANFR), and income distribution from the statistical office (INSEE). While we only observe consumers subscribing to one operator, we observe the prices and characteristics for all contracts available in the market, and we prove that the estimation strategy of Berry, Levinsohn and Pakes (1995) can be employed in this setting.<sup>5</sup>

We use the estimated models of demand and infrastructure to compute counterfactual equilibria under different numbers of firms. We find that consumer surplus is maximized at a relatively high number of firms, but that aggregate consumer surplus masks considerable heterogeneity across consumers of different income levels. Consumers of different income levels value a marginal increase in download speeds differently, and we find that low income individuals prefer a market with more firms than do high income individuals.

We also explore the marginal social value of allocating more spectrum to the mobile telecommunications industry and compare this value with an individual firm’s willingness to pay for a marginal unit of spectrum.<sup>6</sup> We find that the marginal social value is about four times greater than an individual firm’s willingness to pay.

Our model is also well suited to addressing questions of within-industry spectrum allocation. Inspired by the entry of Free Mobile in 2012 in France, we consider two ways in which a regulator might allocate more spectrum to mobile telecommunications: by giving it to a new entrant (inducing entry), or distributing it among incumbents. We find that the former is better for consumer surplus (and preferred by most consumers), but the latter is better for total surplus (and high-income consumers).

The remainder of this paper is organized as follows. Section 2 presents the data along with some descriptive statistics on usage and quality of mobile data. Section 3 presents the model of infrastructural investment, and section 4 lays out the demand and cost models. Section 5 presents the estimation strategy and results. Section 6 presents some counterfactual analyses.

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<sup>4</sup>In accordance with data protection and privacy concerns, we were provided with commune-level statistics rather than accessing the detailed consumer-level data directly.

<sup>5</sup>Our model predicts shares for all products from all providers in the market, but we only require that the model rationalize product-level market shares for Orange. For other firms, we impose firm-level demand shocks and require the model to rationalize firm-level market shares.

<sup>6</sup>This willingness to pay is the value to which firms’ bids in a simple spectrum auction will be related.

## 2 Data and Descriptive Statistics

The French telecommunications market hosts four mobile network operators (MNOs): Orange (market share of 37%), SFR (29%), Bouygues (17%), and Free Mobile (17%). 92% of the population above 12 years old are mobile users according to a survey by CREDOC. Mobile services include voice and data communications as well as short message services (SMS). Statistics provided by France’s national regulator show that voice and SMS usage had stabilized by 2015, the period we focus on to estimate our model. In contrast, the volume of data per user was growing rapidly, reaching an average of 800 megabytes (MB) in 2015, up from 100 MB in 2010 (see Figure 23 in Appendix C.1). The provision of high quality data services has been a major concern in recent antitrust cases and regulatory discussions. Thus, modeling data transmission will be a major focus for us.

### 2.1 Data description

This study relies on data from several sources. A supplementary data appendix (Appendix C) provides a detailed description of these data sources.

Our main data source is a proprietary data set of 15 million residential mobile customers of one operator, Orange Mobile, in October 2015. This data set includes information on the contract subscribed to and the usage of mobile voice and data services. In the remainder of the paper, we focus on data services because network investment since 2013 has typically been made in order to improve the quality of data services, and, with the deployment of 4G technology voice and data services, can draw on the same network resources.

The customer data set is complemented by data on the quality of mobile data services, defined as download speed. Unlike fixed broadband Internet access, the quality of mobile data is hard to measure due to congestion and users’ mobility. Congestion arises because the available bandwidth is shared among users and, as a result, the greater the number of users, the lower the quality (as measured by download speed). At the same time, the number of users (and therefore the demand for data) on a network depends on quality. In our counterfactuals, we will employ a model in which demand and quality of service are simultaneously determined, but for the purpose of estimation, we rely on a direct measure of download speeds as our measure of quality. Speedtest is a service offered by the firm Ookla that allows users to check their download and upload internet speeds. The data include measured download speed, the time of the speed test, the location of the user, and the mobile network operator. We use a proprietary data set provided by Ookla on over one million speed tests in France in the fourth quarter of 2015 to construct a measure of experienced download speeds for each mobile network operator in each municipality. Section C.4 in the data appendix explains the construction of this quality measure in detail.

Markets are defined as municipalities (communes), and we limit our analysis to relatively populous markets, defined as those with a population greater than 10 000, for a total of 589 markets.<sup>7</sup> Municipality-level market size is estimated using the population above age 12 (obtained from the French National Institute of Statistics and Economic Studies, INSEE) together with surveys conducted by CREDOC that provide the share of mobile users in the population above 12. We also obtain the income distribution by municipality from INSEE.

We collect tariff data from online quarterly catalogs of offers proposed by the four MNOs and the largest mobile virtual network operator (MVNO). Tariff characteristics include monthly prices, data allowances, and voice allowances.

Most of the MNOs offer contracts that vary based on characteristics that are beyond the scope of our model, including bundling with home internet and television services. Because we want to focus on the choice of mobile data services, we aggregate contracts according to monthly data allowance categories: less than 500 MB, 500–3 000 MB, 3 000–7 000 MB, and more than 7 000 MB. These data limits are “soft,” in the sense that customers can still use data services once the limit is exceeded, but download speeds will be throttled significantly. Our demand model will take the softness of data limits into account.

For each data limit category, a representative contract is selected, and for the purposes of our demand estimation, we assume that all consumers selecting a product within a category are selecting the representative product for that category. Table 1 presents the representative contracts, which in most cases have 24-month commitment durations and are not bundled with home internet or television services. Representative products typically have unlimited voice allowances, except for the lowest data limit categories. For MVNO’s, our choice set includes one representative contract for each category; that is, we effectively assume there is one representative MVNO firm. Appendix C.5 describes in detail how we select representative contracts.

To be clear, the representative products in our model’s choice set have the characteristics of products actually available in the market. The only characteristic that is adjusted from what is actually observed in the market is the monthly price; when a representative contract is associated with a handset subsidy, the monthly price is adjusted to reflect the value of that handset subsidy (see the data appendix for details). Each actual product is then assigned to

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<sup>7</sup>We limit ourselves to populous markets because active network sharing (where network operators share the transmitting components of their infrastructure) is relatively common in rural areas but not practiced in urban areas. Thus, for our sample, we are comfortable associating a firm’s measured download speeds with that firm’s own infrastructural investments. Furthermore, antenna coverage is not limited to the boundary of municipalities, particularly so in rural areas. In order to obtain a reliable measure of quality at the lowest geographical level, we need to define a market as a municipality. There are 592 municipalities with a population greater than 10 000, and we drop three of those municipalities due to insufficient download speed tests to construct quality measures. This yields a total of 589 markets in our sample.

Table 1: The Choice Set

<b>Operator</b>	<b>Price</b>	<b>Data Limit</b>	<b>Unlimited Voice</b>	<b>Contracts Represented</b>	<b>Min Price</b>	<b>Max Price</b>	<b>Min Limit</b>	<b>Max Limit</b>
Orange	12.07	50	No	11	4.99	30.99	0	50
Orange	14.99	1000	No	4	14.99	14.99	1000	1000
Orange	22.91	1000	Yes	2	22.91	24.99	1000	1000
Orange	30.91	4000	Yes	5	19.99	48.99	3000	5000
Orange	38.74	8000	Yes	11	38.74	166.0	8000	20000
Bouygues	8.070	0	No	6	3.99	11.32	0	20
Bouygues	14.99	1000	No	3	14.99	14.99	1000	1000
Bouygues	20.91	3000	Yes	4	19.99	29.99	3000	5000
Bouygues	33.74	10000	Yes	4	32.70	72.70	10000	20000
Free Mobile	2	50	No	1	2.00	2.00	50	50
Free Mobile	19.99	3000	Yes	1	19.99	19.99	3000	3000
SFR	12.07	100	No	5	5.990	14.99	100	200
SFR	14.99	1000	No	3	14.99	19.99	1000	1000
SFR	22.91	1000	Yes	3	22.91	29.99	1000	1000
SFR	31.91	5000	Yes	5	19.99	43.99	3000	5000
SFR	37.74	10000	Yes	9	36.70	150.0	10000	20000
MVNO	7.990	No	0	13	7.990	18.99	0	200
MVNO	17.99	1000	No	5	9.990	17.99	500	1000
MVNO	19.99	500	Yes	10	19.99	35.99	500	2000
MVNO	42.99	5000	Yes	13	12.99	61.99	3000	5000
MVNO	64.99	10000	Yes	4	64.99	76.99	10000	10000

Each row corresponds to an object in the choice set, i.e., a representative product. The minimum and maximum prices and data limits are over the set of contracts represented by each representative product in the choice set.

a representative product, and our estimation takes the market shares of the representative products to be the aggregate market share of all the actual products assigned to that representative product. For instance, our econometric model features one high-data-limit contract for Orange. We treat the price of this product as 38.74 euros. This price corresponds to an observed price of 54.99 euros for this contract and an adjustment of 16.25 euros for the value of the associated handset subsidy. We measure the market share of this representative product, however, as the sum of market shares of eleven high-data-limit contracts offered by Orange that are associated with various home internet and television bundles.

Finally, we obtain detailed data on infrastructure from the national radio communications regulator (ANFR). These data describe the locations of all base stations with the number of antennas and frequencies operated by firm.

## 2.2 Descriptive statistics

Table 2 provides summary statistics of the main variables of interest from the data sets described in the previous section.

Table 2: Summary Statistics

	Mean	Std. Dev.	Min.	Max.
<b>Customer data (Orange)</b>				
Market Average Usage (MB)	1 043	194	554	1701
Fraction Users above Data Limit	0.18	0.03	0.10	0.28
Num. customers		4 425 831		
<b>Quality and market data</b>				
Quality Orange (Mbps)	33.02	11.35	3.97	89.87
Quality Bouygues (Mbps)	23.73	9.69	0.60	72.97
Quality Free (Mbps)	23.21	11.08	1.56	57.26
Quality SFR (Mbps)	17.60	8.60	0.39	52.30
Quality MVNO (Mbps)	24.79	7.12	5.13	49.06
Median income (Euros)	13 035	3 179	5 152	31 320
Number of markets		589		
<b>Tariff data</b>				
Price	23.47	14.57	2.00	64.99
Price (Orange)	23.92	11.06	12.07	38.74
Price (Others)	23.33	15.83	2.00	64.99
Data limit	3 081	3 570	0	10 000
Num. products		21		

Measured quality (download speeds) varies substantially both across and within markets. Across markets, the average standard deviation for an operator is 9.56 Mbps, and across operators, the average standard deviation for a market is 7.92 Mbps. Figure 1 displays histograms of measured quality across markets for each mobile network operator. Data usage is positively correlated with measured quality. Figure 2 plots the relationship between Orange market qualities and observed average data usage for three different data limits.<sup>8</sup> The average fraction of the data limit that is consumed is decreasing in the size of the data limit, as demonstrated in figure 3, which plots the histograms of average data consumption for three different data limits.<sup>9</sup>

<sup>8</sup>The correlations for data limits 1 000 MB, 4 000 MB, and 8 000 MB are, respectively, 0.147, 0.271, 0.246.

<sup>9</sup>For the data limits 1 000 MB, 4 000 MB, and 8 000 MB, the fraction of the data limit that is consumed is, respectively, on average, 0.656, 0.578, and 0.533.



Figure 1: Histograms of qualities by operator

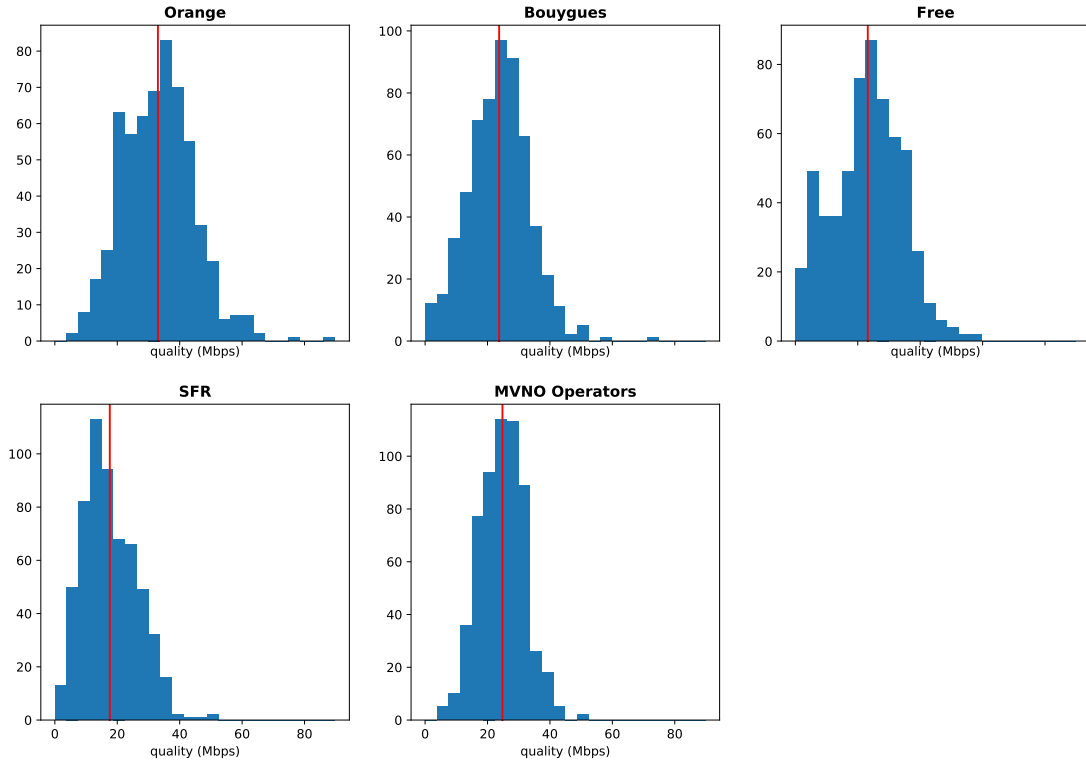


Figure 2: Average data usage vs. measured quality across markets

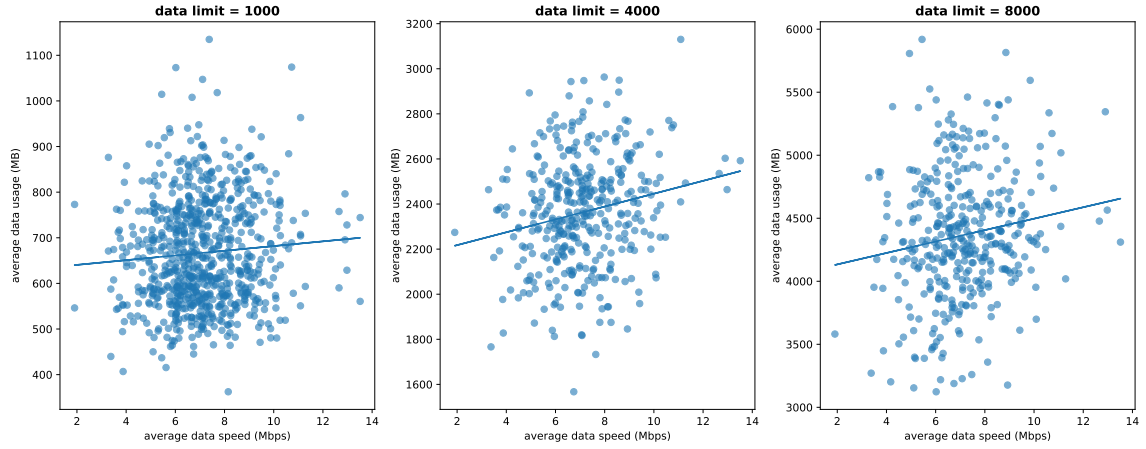
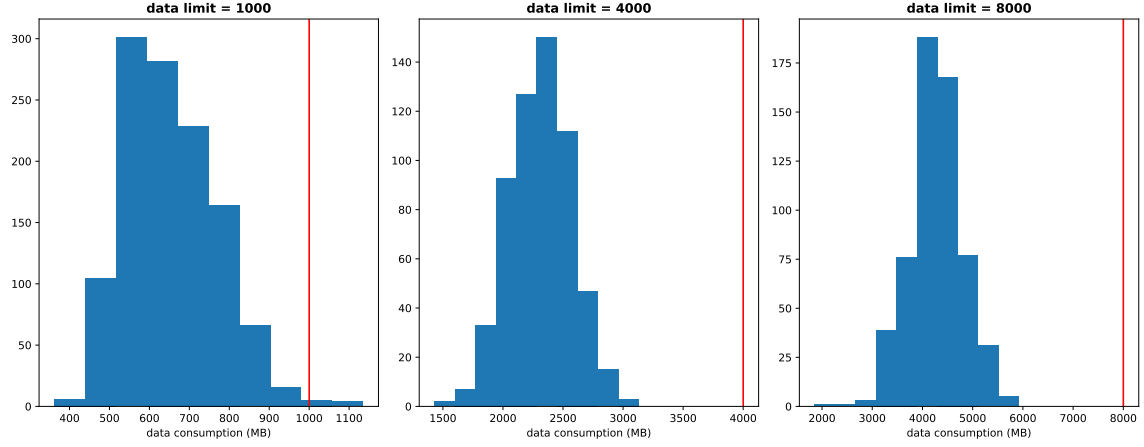
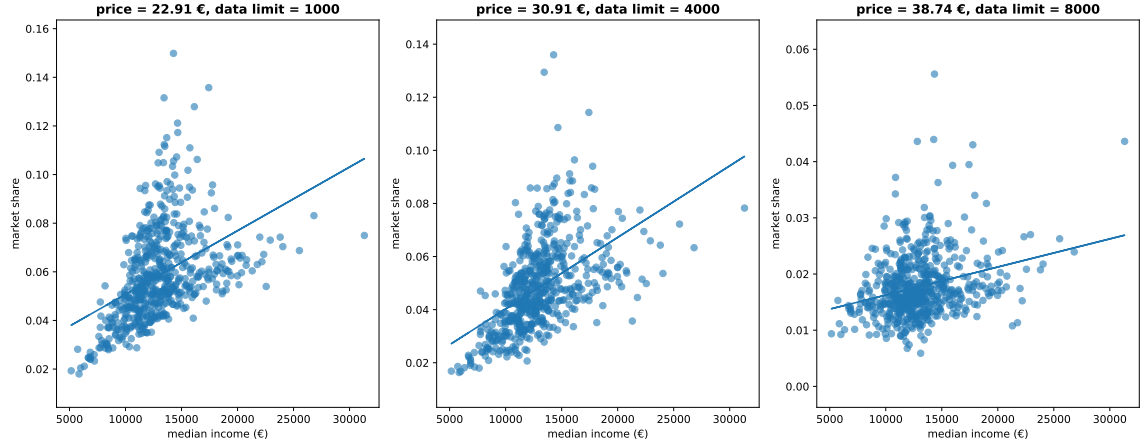


Figure 3: Average data usage across markets



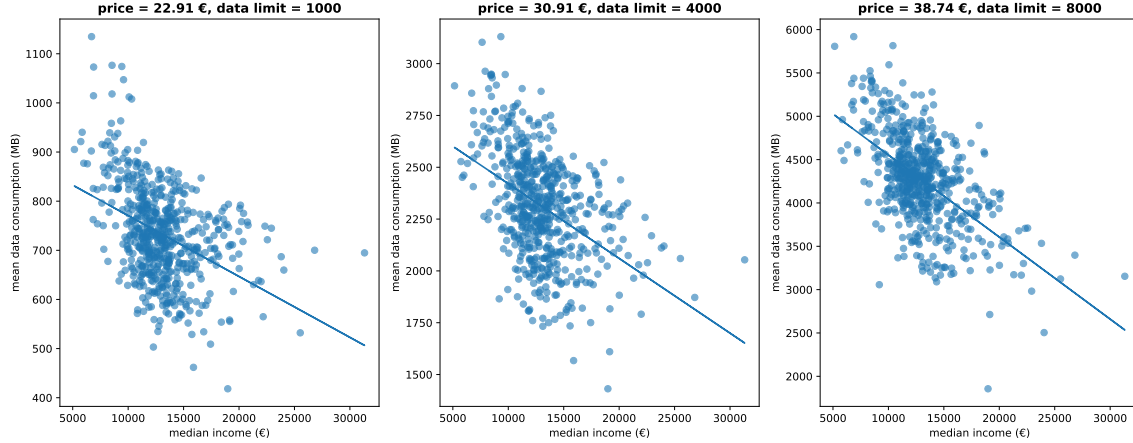
Median incomes are correlated with products market shares. Figure 4 plots the relationship between median income and market shares of the three most expensive contracts offered by Orange, which correspond to the same three contracts depicted in figures 2 and 3. Median incomes are positively correlated with the market shares of the most expensive contracts.<sup>10</sup>

Figure 4: Median income vs. expensive contract market shares



<sup>10</sup>Correlation coefficients for median incomes and market shares are, following the order of the graphs, 0.441, 0.519, 0.278.

Figure 5: Median income vs. mean data consumption



### 3 Industry Model

In this section, we describe a formal model of how download speeds are jointly determined by bandwidth allocations, infrastructure investment decisions, and the load imposed on a network by consumers. We rely on standard telecommunications engineering models and are particularly indebted to Blaszczyzyn, Jovanovicy and Karray (2014). Table 53 in the appendix provides a list of all parameters used in the industry and demand models and their definitions.

In this model, firms own and operate their own networks with no sharing of infrastructure. In practice, network sharing occurs when an MNO dedicates a part of its network resources to another MNO. *Passive network sharing* involves the physical structure of base stations and the cost of electric power, but not the resources that transmit and receive signals and affect quality determination. In contrast, *active network sharing* occurs when equipment that transmits data is shared. During 2015, active network sharing occurred primarily in areas with low population density. Because we want to associate each firm's quality of service with the firm's own investment decisions, we ultimately focus on the higher-density areas of France in our analysis.

#### 3.1 Base station infrastructure and data transmission

For each network operator and municipality, we assume the full land area is divided into equally sized hexagonal cells. Furthermore, we assume each municipality has homogeneous population density, so each cell is identical for a given operator and municipality. We assume that each cell is served by a single base station transmitting an omni-directional signal at the maximum signal strength allowed by regulation. One important network variable is band-

width,  $B_f$ , which does not have a municipality-level subscript, reflecting our assumption that each firm has the same spectrum holdings everywhere and operates using all frequencies they own everywhere.<sup>11</sup> Bandwidth  $B_f$  is not a choice variable in our model, but it is an aspect of market structure we vary in our counterfactual analysis.

A network operator  $f$ 's infrastructure choice variable is  $R_{fm}$ , the cell radius (more precisely, a hexagonal cell's side length) in municipality  $m$ . We could also think of the choice variable as being the number of base stations in a given municipality,  $NB_{fm}$ . We assume the area served by each cell is  $A_m/NB_{fm} = 3\sqrt{3}R_{fm}^2/2$ , where  $A_m$  is municipality  $m$ 's effective land area.<sup>12</sup> We assume that the municipality's area can be divided into equally sized hexagons, effectively ignoring municipality geometry and other spatially explicit details.<sup>13</sup>

For a given consumer  $i$ , the theoretical maximum download speed  $q(r_i)$  achieved by a unit of bandwidth depends on the consumer's distance  $r_i$  from the base station. Download speeds scale linearly with bandwidth, so if a consumer is allocated  $b_i$  units of bandwidth, their theoretical maximum download speed will be  $b_i q(r_i)$ . We will introduce the precise  $q(\cdot)$  function below, but for now what is important is that  $q$  is decreasing, reflecting path loss.

To aggregate download speeds over consumers, it would not be correct to compute the ordinary mean of  $q(r)$  because users who receive lower quality signal require more resources for a given download; that is, for a download of a given size, they will either tie up the base station's capacity for longer or they will require a relatively larger fraction of the bandwidth to receive the same download speed as consumers closer to the antenna. Consequently, average download speeds should be derived from harmonic means.

For the sake of exposition, begin by imagining that a unit mass of users, each of whom has one unit of demand for data, are guaranteed the same download speed,  $\bar{Q}$ , and for now we ignore queuing issues and assume constant aggregate demand. Then, a user at distance  $r$  will require bandwidth  $\bar{Q}/q(r)$ . Assuming users are uniformly distributed over the cell, the total bandwidth required to serve the cell is

$$B_f = G(R_{fm})^{-1} \int_0^{R_{fm}} \frac{\bar{Q}}{q(r)} g(r) dr,$$

where  $R_{fm}$  is the radius of the cell, and  $g(r)$  and  $G(R_{fm})$  reflect its geometry (e.g.,  $g(r) = 2\pi r$

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<sup>11</sup>This is basically true in non-rural France. Unlike the United States, France does not auction spectrum by region.

<sup>12</sup>When implementing the model empirically, we use an adjusted measure of land area because the raw land area may overstate the area that operators need to cover when large unpopulated areas are present. See appendix C.1.4 for details.

<sup>13</sup>Heterogeneity in municipality topography and other features that effect radio transmission can be captured in a municipality-level spectral efficiency parameter, explained below.

and  $G(R_{fm}) = \pi R_{fm}^2$  with circular cells, but we use hexagonal cells, which tessellate).<sup>14</sup> Rearranging the above equation to solve for the average download speed that can be sustained by a given bandwidth, we have

$$\bar{Q}_f(R_{fm}, B_f) = \frac{B_f}{G(R_{fm})^{-1} \int_0^{R_{fm}} \frac{g(r)}{q(r)} dr}. \quad (1)$$

This equation expresses *channel capacity*, describing how feasible download speeds are influenced by the firm's choice of cell radius  $R_{fm}$  and its bandwidth  $B_f$ .<sup>15</sup> We have assumed there is a unit density of users. If the density of users is  $D$ , then the channel capacity per consumer would be equal to  $\bar{Q}(R_{fm}, B_f)/D$ . Intuitively, feasible download speeds depend on the level of demand. Below, we will consider more precisely how demand affects delivered download speed using queuing theory. We will also consider how the demand level depends on delivered download speed, since consumers presumably are more likely to subscribe to a firm and download more data when a firm offers better download speeds. Thus, in equilibrium, demand and download speeds are simultaneously determined.

Next, we consider the individual download speed function  $q(\cdot)$ . The Shannon-Hartley theorem tells us that the theoretical upper bound to download speed (per hertz of bandwidth) is given by:

$$q(r) = \log_2(1 + SINR(r)) \quad (2)$$

where  $SINR(r)$  is the signal-to-noise-and-interference ratio, and  $q(r)$  is measured in bits per second. This ratio is given by the ratio of signal power to the sum of noise and interference power:

$$SINR(r) = \frac{S(r)}{N + I(r)}, \quad (3)$$

where  $S(r)$  is signal power,  $N$  is noise power, and  $I(r)$  is interference power. We now consider each of these three objects in turn.

As the signal travels, its power diminishes (path loss). We take this into account by using the

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<sup>14</sup>The area of a hexagon is given by  $G(R_{fm}) = \frac{3\sqrt{3}}{2} R_{fm}^2$ , where  $R_{fm}$  is the hexagon's side length. When we actually integrate over hexagonal cells, we do not actually use a formula for  $g(r)$ . Instead, we compute a double integral, integrating over the hexagon's apothem and perpendicular to the apothem.

<sup>15</sup>We need not assume that everybody gets the same download speed to derive this formula for channel capacity. We could also suppose everybody is allocated the same bandwidth in which case a consumer at distance  $r$ 's time spent downloading is proportional to the inverse of  $B_f q(r)$ . Then, total data downloaded dividing by total time spent downloading is

$$\frac{G(R_{fm})^{-1} \int g(r) dr}{G(R_{fm})^{-1} \int \frac{g(r)}{B_f q(r)} dr} = \frac{B_f}{G(R_{fm})^{-1} \int \frac{g(r)}{q(r)} dr},$$

or the same formula for channel capacity as (1).

Hata model of path loss. Ultimately, we assume that the signal power is equal to

$$\ln S(r) = -18.012 - 3.522 \ln(r). \quad (4)$$

Notice that this entails a path loss exponent of approximately 3.522.<sup>16</sup> In contrast, signal strength in a vacuum would have a path loss exponent of 2, but signals decay more quickly on the Earth's surface.<sup>17</sup>

Noise power  $N$  is set equal to Johnson-Nyquist noise,  $-107.01$  dBm per 5 MHz of bandwidth. Interference power is set equal to 30% of the signal power from the six adjacent cells.<sup>18</sup> The 30% number follows Blaszczyzyn, Jovanovicy and Karray (2014) and reflects that adjacent cells won't always be in use, and modern systems use directional signals to limit interference.

### 3.2 Queuing

Consumers' download requests do not arrive uniformly over time. This means that  $\bar{Q}$  derived above will not represent the actual delivered download speed in practice but a theoretical upper bound referred to as *channel capacity*.

To derive a relationship between channel capacity and average delivered download speed, we follow Blaszczyzyn, Jovanovicy and Karray (2014) and assume that download requests arrive according to a Poisson process and that download requests are served through a M/M/1 queue. Then, the average download speed will be

$$Q = \bar{Q} - Q^D, \quad (5)$$

where  $Q^D$  is the arrival rate of download requests. Each of the terms in equation 5 should be understood as rates, e.g., as values measured in Megabits per second.<sup>19</sup>

### 3.3 Transmission equilibrium

We now consider how the engineering relationships described above come together with demand to determine delivered download speeds in equilibrium. To be clear, at this point we are considering equilibrium in terms of download speeds and consumer demand, taking prices and

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<sup>16</sup>Most engineering studies use a path loss exponent between 3.5 and 4.

<sup>17</sup>The specific values in our path loss equation can be derived as follows. We begin with the Hata model for urban environments, and we assume a base station height of 30m. We assume the signal frequency of 1900 Mhz, which is approximately the median operated frequency in France in 2015. Finally, we assume a signal power of 61 dBm (or 1259 W) per 5 Mhz of bandwidth at the base station, which corresponds to the regulated limit on effective isotropic radiated power.

<sup>18</sup>When we perform the integration above, we compute each point's distance from the centroids of the six adjacent cells to calculate interference power. See Appendix A.1 for a more detailed description.

<sup>19</sup>For a derivation of this formula, see Taylor, Karlin and Taylor (1998), pp. 548-549, for example.

infrastructure as given. This can be thought of as a final-stage equilibrium. Below, we will consider how prices are set in anticipation of this transmission equilibrium and subsequently how infrastructure is determined in anticipation of price and transmission equilibria.

Formally, the equilibrium we now consider is conditional on a vector of prices  $\mathbf{P}$  and infrastructure variables  $(\mathbf{R}, \mathbf{B})$ . If each firm offers only one contract, and if price is the only contractual choice variable, then  $\mathbf{P}$  is a  $F$ -dimensional vector, where  $F$  is the number of firms. Ultimately, we will consider multi-product firms and other contractual variables besides price (i.e., data limits), in which case  $\mathbf{P}$  can represent a higher-dimensional vector including prices and non-price characteristics of all products. In either case,  $\mathbf{R}$  and  $\mathbf{B}$  are both  $F$ -dimensional vectors – each firm employs only one network to serve all its products with. The  $f$ -subscripts will denote firm-specific variables.

The demand for downloads on firm  $f$ 's network can be broken down into the product of three terms:

$$Q_f^D(Q_f, \mathbf{P}_f, \mathbf{Q}_{-f}, \mathbf{P}_{-f}) = D \times S_f(Q_f, \mathbf{P}_f, \mathbf{Q}_{-f}, \mathbf{P}_{-f}) \times \bar{x}_f(Q_f, \mathbf{P}_f, \mathbf{Q}_{-f}, \mathbf{P}_{-f}),$$

where  $D$  is the density of consumers,  $S_f(\cdot)$  represents firm  $f$ 's total market share as a function of the average download speeds for each firm and prices for each product, and  $\bar{x}_f(\cdot)$  represents the average data consumption among firm  $f$ 's subscribers. The market share and average download speed functions will be derived from a discrete-continuous model of demand, specified in the following section, in which consumers choose which product to subscribe to and how much data to consume.

Combining equations (1) and (5), we have

$$\forall f = 1, \dots, F: \quad Q_f = B_f \left[ G(R_f)^{-1} \int_0^{R_f} \frac{g(r)}{q(r)} dr \right]^{-1} - Q_f^D(Q_f, \mathbf{P}_f, \mathbf{Q}_{-f}, \mathbf{P}_{-f}). \quad (6)$$

If prices and the infrastructure variables are given, then we have  $F$  equations and  $F$  download speeds  $Q_f$  to solve for, so, under appropriate conditions on the demand system, the above equation uniquely defines a vector of equilibrium download speeds  $\mathbf{Q}^*$ .

We have now defined the transmission equilibrium as a function of prices and infrastructure,  $\mathbf{Q}^*(\mathbf{P}, \mathbf{R}, \mathbf{B})$ . Subsequently, we will consider the price equilibrium as a function of infrastructure,  $\mathbf{P}^*(\mathbf{R}, \mathbf{B})$ , and then finally the equilibrium in infrastructural investment.

### 3.4 Spectral efficiency calibration

In practice, the efficiency of data transmission is affected by topography and the presence of buildings. This means that the efficiency of data transmission may vary by market, so we introduce a market-level subscript and spectral efficiency parameter into our download speed function:

$$q_m(r) = \gamma_m q(r). \quad (7)$$

In the empirical implementation of the industry model, we replace  $q(r)$  with  $q_m(r)$  in all of the above equations.

We calibrate the spectral efficiency parameter  $\gamma_m$  using delivered download speed data for each municipality. This is done by solving for the value of  $\gamma_m$  that makes equation (6) hold for Orange (we do not have usage data for other operators). In this calibration,  $Q_f$  is the average download speed in Mbps between noon and 1pm in the delivered download speed obtained from Ookla.  $Q^D$  is given by the total data consumption in the Orange data in October, 2015, in Mb divided by  $31 \cdot 8 \cdot 3600$ . That is, we try to capture the transmission equilibrium during peak hours, and we assume that days effectively consist of eight peak hours.

### 3.5 Price competition

We can understand the network equilibrium model above as holding at the market level  $m$  with potentially different infrastructural variables in each market,  $(\mathbf{R}_m, \mathbf{B}_m)$ . However, prices are set nationally, so we will not introduce subscripts on the price vectors. From now on, when the infrastructure variables appear without market subscripts, they refer to the stacked vector of infrastructure variables for all markets.

Each firm  $f$  sets prices to maximize its variable profits. We define

$$\mathbf{P}_f^*(\mathbf{R}, \mathbf{B}) = \arg \max_{\mathbf{P}_f} \left\{ (\mathbf{P}_f - \mathbf{c}_{u,f}) \cdot \sum_m N_m \mathbf{S}_{mf}^*(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m) \right\}, \quad (8)$$

where  $\mathbf{c}_u$  is the variable cost per customer,  $N_m$  is the size of market  $m$ , and  $\mathbf{S}_{mf}^*$  denotes a vector of product-level shares for products owned by firm  $f$ . The market share function is derived from the demand system and the transmission equilibrium function as follows:

$$\mathbf{S}_{mf}^*(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m) = \mathbf{S}_{mf}(Q_{mf}^*(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m), \mathbf{P}_f, \mathbf{Q}_{m,-f}^*(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m), \mathbf{P}_{-f}),$$

where the  $\mathbf{S}_{mf}(Q_{mf}, \mathbf{P}_f, \mathbf{Q}_{m,-f}, \mathbf{P}_{-f})$  function stacks firm  $f$ 's product-level market shares as a function of prices and download speeds. The market share function has an  $m$ -subscript to allow for variation in local demographics.



Note that equilibrium download speeds depend on price, so the first-order condition for optimal price-setting must not only take into account the direct effect of lowering price on consumer demand, but also the indirect effect of endogenous download speeds. The indirect effect lowers price elasticities because as demand for firm  $f$  falls,  $f$ 's download speeds increase due to reduced network load, which has a positive effect on demand, thereby dampening the demand reduction. We discuss demand elasticities further in section 6.

### 3.6 Infrastructure competition

The first stage of competition involves firms deciding on their infrastructural investments in each market. Infrastructure costs in market  $m$  are given by the following function:

$$C_{mf}(R_{mf}, B_{mf}) = c_{fc,m} \frac{A_m}{G(R_{mf})} B_{mf}, \quad (9)$$

where  $A_m$  is the land area of market  $m$ , and  $c_{0,m}$  captures costs per base station and unit of bandwidth (which may vary by market), and  $G(R) = 3\sqrt{3}R^2/2$  is the area of a hexagonal cell with side length  $R$ .

This cost function reflects the idea that the main costs associated with a base station would be the electricity costs, cost of installing antennas, and other costs that are proportional to the bandwidth being operated. Another advantage of this cost function is that, if we suppose that all firms operate at the same base station locations, then redistributing bandwidth among firms and/or changing the number of firms does not change the total costs incurred within the industry. Thus, this cost function shuts down a potential source of economies of scale associated with the duplication of fixed costs.

That said, it's natural to think that there are some fixed costs associated with operating a base station, such as rents or setup costs, that don't scale with the bandwidth being operated. We conduct robustness exercises with an alternative cost function that treats all infrastructure costs as fixed costs per base station (that is, dropping the  $B_{mf}$  term from equation (9)). Appendix B includes results for this alternative cost function.

Next, we can define market-level profits as follows:

$$\Pi_{mf}(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m) = (\mathbf{P}_f - \mathbf{c}_{u,f}) \cdot \sum_m N_m \mathbf{S}_{mf}(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m) - C_{mf}(R_{mf}, B_{mf}). \quad (10)$$

Finally, we can define the national profit function for each firm  $f$ :

$$\Pi_f(\mathbf{R}, \mathbf{B}) = \sum_m \Pi_{mf}(\mathbf{P}^*(\mathbf{R}, \mathbf{B}), \mathbf{R}_m, \mathbf{B}_m), \quad (11)$$

where  $\mathbf{P}^*(\mathbf{R}, \mathbf{B})$  is the solution to the national pricing game defined above.

Equation (11), taken for each firm  $f$ , defines the payoffs for the first-stage game in infrastructural investment. Each firm  $f$  chooses  $(\mathbf{R}_f, \mathbf{B}_f)$  to maximize national profits, taking others firms'  $(\mathbf{R}_{-f}, \mathbf{B}_{-f})$  as given:

$$\max_{\mathbf{R}_f, \mathbf{B}_f} \{\Pi_f(\mathbf{R}, \mathbf{B})\}.$$

In this section, we have considered market shares and data demand as abstract functions of delivered download speeds and prices. In the following section, we will be explicit about the model of consumer behavior. Following that, we will consider the estimation of the demand model and the cost parameters  $(\mathbf{c}_u, \mathbf{c}_{fc})$ .

### 3.7 Economies of Scale

A merger between two firms in this model will exhibit cost efficiencies if, post merger, the merged firm is able to provide the same quality at a lower cost or higher quality at the same cost. Our model allows for efficiencies that result from *economies of density* and *economies of pooling*.

#### 3.7.1 Economies of Pooling

It has long been recognized in the economics literature that “there are economies of scale in servicing a stochastic market” (Carlton, 1978).<sup>20</sup> In operations management, the same phenomenon has been referred to as the “Pooling Principle” (Cattani and Schmidt, 2005). Thus, we use “economies of pooling” to describe economies of scale coming from consolidating bandwidth.

It is easy to see how economies of scale result from our queuing theory model. Equation (5) holds that delivered download speed corresponds to the difference between channel capacity and the download demand rate. Crucially, channel capacity is linear in bandwidth. Thus, if two identical firms combine their bandwidth and their customer bases (holding the download demand rate per customer fixed), then both terms on the right-hand side of equation (5) would double. Consequently, download speeds (the left-hand side) would also double.

#### 3.7.2 Economies of Density

Due to path loss, captured by the function  $q(\cdot)$ , the closer users are to a base station, the more efficiently that station can serve them. Thus, if we increase the density of users served

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<sup>20</sup>Robinson (1948) was perhaps the first to describe the phenomenon, under the heading of “the economy of the large machine.” De Vany (1976) was an early application using queuing theory to derive economies of scale. Mulligan (1983) shows formally how economies of scale result from queuing theory.

by a firm while keeping constant the numbers of users per base station, users will be closer to base stations serving them on average, improving download speeds. If two network operators were to merge and combine their user bases, the merged entity would effectively serve a higher population density of users. This creates the opportunity for the merged firm to deliver higher download speeds to its customers with the same total investment level of the pre-merger firms, which we refer to as “economies of density.”<sup>21</sup>

## 4 Demand Model

**Notation** Individuals are indexed by  $i$ , the various contracts are denoted by  $j \in \mathcal{J} = \{1, \dots, J\}$ , and geographic markets are indexed by  $m \in \mathcal{M} = \{1, \dots, M\}$ . Quality of service, measured as average download speed, is captured by  $Q_{m,f}$ , where  $f$  denotes a firm. Quality is constant across  $j \in \mathcal{J}_f$  in commune  $m$ , where  $\mathcal{J}_f$  represents the set of products produced by firm  $f$ . We write  $f(j)$  to denote the firm associated with product  $j$ .

We consider the consumer’s static consumption decision. A consumer’s indirect utility from a contract  $j$ , consuming  $x$  megabytes of data, in market  $m$ , is denoted by

$$v_m(j, x; \theta_i, \vartheta_i, \varepsilon_i) \equiv u_j(x, Q_{m,f(j)}; \vartheta_i, \theta_i) + \theta_v v_j - \theta_{pi} p_j + \xi_{jm} + \varepsilon_{ij}, \quad (12)$$

where  $p_j$  is the contract price;  $u_j(\cdot)$  maps the contract  $j$ , data consumption  $x$ , and data quality  $Q_{m,f(j)}$  into the utility from consumption of mobile services;  $v_j$  is a dummy variable equal to one if plan  $j$  has an unlimited voice allowance;  $\xi_{jm}$  is the product-market-specific demand shock; and  $\theta$  and  $\vartheta$  are parameters describing preferences. Idiosyncratic tastes  $\varepsilon_{ij}$  are realized before the choice of contract  $j$  is made. The preference parameter  $\vartheta_i$  is a random variable capturing how much agent  $i$  values data; it is realized *after* the choice of contract is made, but an agent chooses the contract with knowledge of its distribution. The object is to estimate the distribution of preference parameters  $\theta_i$  and  $\vartheta_i$ .

**Consumer Behavior** To maximize utility, the consumer chooses a plan  $j$  and data usage  $x$ . We first consider what the agent’s usage behavior would be, conditional on contract. Usage behavior depends on the consumer’s  $\vartheta_i$ , which is a random variable, reflecting that consumers may be unable to perfectly forecast their utility for data when choosing a phone contract. We then consider the optimal choice of contract, which consumers choose after forming expectations over  $u_j(\cdot; \vartheta_i, \theta_i)$ .

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<sup>21</sup>Here we ignore the dynamics of merging two firms and integrating their existing infrastructure; we are making statements about what would happen with a given level of investment spread across two firms in comparison to what one integrated firm would achieve with the same level of total investment.

**Mobile Data Consumption** To rationalize finite data consumption even when additional data consumption entails no monetary cost, our functional form includes a term which corresponds to the disutility of download times. This disutility is proportional to the amount of data downloaded and inversely proportional to the download speed; it can be thought of as the opportunity cost of time spent downloading. Consumers will consume data until the marginal utility of extra data corresponds to the disutility of additional download time.

A consumer's utility of data consumption is given by the following functional form:

$$u_j(x, Q; \vartheta_i, \theta_i) = \vartheta_i \log(1 + x) - \theta_c c_j(x, Q), \quad (13)$$

where  $c_j(\cdot)$  is the opportunity cost of time spent downloading and is given by the following formula:

$$c_j(x, Q) = \begin{cases} \frac{x}{\bar{Q}} & \text{if } x \leq \bar{x}_j \\ \frac{\bar{x}_j}{\bar{Q}} + \frac{\bar{x}_j - x}{Q^L} & \text{if } x > \bar{x}_j, \end{cases} \quad (14)$$

There is a discontinuity in download speeds when a consumer reaches their monthly data limit,  $\bar{x}_j$ . Data consumed after reaching the data limit downloads at the throttled speed  $Q^L \ll \mathbf{Q}$ , where  $\mathbf{Q}$  is stacked firm-market-specific download speeds. This creates a discontinuity in the marginal cost of data consumption. Let

$$x_j^*(Q; \vartheta_i, \theta_c) \equiv \arg \max_{x \in \mathbb{R}_+} \{u_j(x, Q; \vartheta_i, \theta_i)\}$$

be the data choice that maximizes data utility for contract  $j$ . The first order condition and the structure of the marginal cost of data consumption yield four possible cases that determine the optimal data consumption:<sup>22</sup>

$$x_j^*(Q_{f(j)}; \vartheta_i, \theta_i) = \begin{cases} 0 & \text{if } \vartheta_i \leq \frac{\theta_c}{Q_{f(j)}} \\ \frac{\vartheta_i Q_{f(j)}}{\theta_c} - 1 & \text{if } \frac{\theta_c}{Q_{f(j)}} \leq \vartheta_i < \frac{\theta_c}{Q_{f(j)}} (\bar{x}_j + 1) \\ \bar{x}_j & \text{if } \frac{\theta_c}{Q_{f(j)}} (\bar{x}_j + 1) \leq \vartheta_i < \frac{\theta_c}{Q^L} (\bar{x}_j + 1) \\ \frac{\vartheta_i Q^L}{\theta_c} - 1 & \text{if } \vartheta_i \geq \frac{\theta_c}{Q^L} (\bar{x}_j + 1). \end{cases} \quad (15)$$

The first case captures consumer types  $\vartheta_i$  that would not consume any data.<sup>23</sup> The second case captures consumer types that consume less than  $\bar{x}_j$  even without throttling. The third case captures consumer types that would consume greater than  $\bar{x}_j$  if data speeds were not throttled, but under throttling, the marginal cost of an additional unit of data is greater than

<sup>22</sup>We are using here the assumption that  $Q^L \ll \mathbf{Q}$ , which holds in our data.

<sup>23</sup>We interpret such consumers as those that unexpectedly do not need their mobile plan (e.g., they went out of the country for the month). Indeed, in our data, we observe a point mass of consumers that consume zero data—even among those that adopt high data limit plans.

the marginal benefit, so they choose to consume exactly the data limit. Finally, the fourth case captures consumer types that would consume greater than  $\bar{x}_j$  even under throttled data speeds.<sup>24</sup>

**Contract Decision** The consumer chooses the contract that maximizes her expected utility. The expectation is with respect to the data consumption utility parameter  $\vartheta_i$ , which we will assume is distributed

$$\vartheta_i \sim \text{Exponential}(\theta_{di}).$$

While the consumer does not know her  $\vartheta_i$  *ex ante*, she does know her  $\theta_{di}$ , which we allow to vary by  $i$ . Each market has an outside option,  $j = 0$ , which has indirect utility normalized to  $\varepsilon_{i0}$ . We estimate a random coefficient nested logit model, nesting out the outside option. Specifically,

$$\varepsilon_{ij} = \zeta_{ig} + (1 - \sigma) \eta_{ij},$$

where  $\eta_{ij}$  is i.i.d. extreme value and  $\zeta_{ig}$  has the distribution such that  $\varepsilon_{ij}$  is extreme value. The value  $\sigma \in [0, 1)$  is the nesting parameter, and all contracts (but not the outside option) belong to a single nest.<sup>25</sup> The addition of a nest for all contracts allows for more flexible substitution patterns to the outside option.

The consumer observes  $\theta_i$ , as well as  $\varepsilon_{ij}$ , but must choose a contract before observing the  $\vartheta_i$ . Thus,

$$j_{i,m}^* = \arg \max_{j \in \mathcal{J} \cup \{0\}} \left\{ \mathbb{E} \left[ v_m \left( j, x_j^* \left( Q_{m,f(j)}; \vartheta_i, \theta_i \right); \theta_i, \vartheta_i, \varepsilon_{ij} \right) \right] \right\},$$

where the expectation is taken over  $\vartheta_i$  conditional on  $\theta_{di}$ .

See Appendix A.3 for an analytic expression of expected utility from data conditional on contract and  $\theta_i$ .

## 5 Estimation

We estimate the demand model using a modified version of Berry, Levinsohn and Pakes (1995), described below. After estimating demand, we infer firm's costs based on the assumption that firms set prices and invest in quality optimally.

<sup>24</sup>Small data limit plans have hard data limits (i.e., there is no throttling). We therefore impose that all contracts with data limits less than 500 MB cannot consume greater than the associated data limit.

<sup>25</sup>Note that if  $\sigma = 0$ , the model is equivalent to a random coefficients model without nesting.

## 5.1 Demand estimation

We seek to estimate the distribution of consumer parameters  $\theta_i$ . Specifically, we have the following parameters

$$\theta_i = [\theta_{pi}, \theta_c, \theta_{di}, \theta_v]'$$

Note that we have two heterogeneous parameters that we will allow to vary by income. Specifically,

$$\begin{pmatrix} \log(\theta_{pi}) \\ \log(\theta_{di}) \end{pmatrix} = \begin{pmatrix} \theta_{p0} \\ \theta_{d0} \end{pmatrix} + \begin{pmatrix} \theta_{pz} \\ \theta_{dz} \end{pmatrix} z_i, \quad (16)$$

where  $z_i$  is the consumer's income. The specifications for  $\theta_{pi}$  and  $\theta_{di}$  are with respect to the log parameters in order to ensure the correct sign: for all income levels, the price coefficient must be negative and the rate parameter must be positive.

### 5.1.1 Unobserved demand component

As is standard in the demand estimation literature, we use market shares to back out the unobserved demand components  $\xi$ . The standard BLP contraction mapping used to solve for  $\xi$  does not apply in our setting, however. We observe the set of products offered by all firms, but we only observe detailed market share data for Orange. Specifically, we observe market shares for each of Orange's products for each market  $m$ , but we only observe firm-level national market shares for the other firms.

Our modified estimation technique rationalizes product-level market shares for Orange products and only the firm-level aggregate market shares for the other firms. Formally, we assume

$$\forall j \in \mathcal{J}_{-O}, \forall m : \quad \xi_{jm} = \xi_{f(j)},$$

where  $\mathcal{J}_{-O}$  is the set of non-Orange products, and  $f(j)$  is the firm that corresponds to product  $j$ . Appendix A.2 shows that a modified version of the BLP contraction mapping still applies in our context that is capable of solving for the unique vector  $\xi$  under the above assumption.

### 5.1.2 Elasticity and nesting parameter imputations

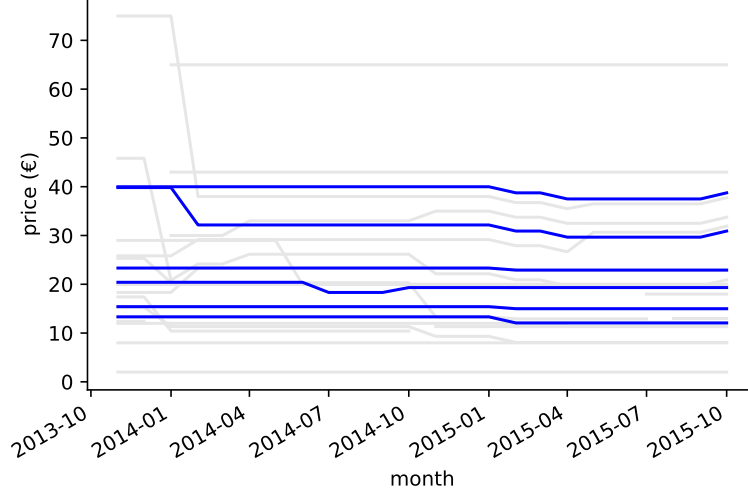
Prices are set nation-wide and do not vary by market. Moreover, prices varied very little over time around our sample period.<sup>26</sup> See Figure 6 for prices over the two years prior to our sample period. Prices of Orange contracts are in blue, and the prices of other operator

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<sup>26</sup>Note that Bourreau, Sun and Verboven (2018) consider a time period that includes the entry of Free Mobile in 2012. Following this entry, there were substantial price changes as the incumbent MNOs reacted to the new low-cost competitor. In contrast, during the two years leading up to our sample period, price variation was quite limited.

contracts are in light gray. Given the lack of price variation, it is difficult to identify price elasticities from the data.

Figure 6: Prices of Orange contracts over two years



We therefore take an approach where we impute price elasticities over a wide range of possible elasticities. For each elasticity considered, we impose that the price elasticity of Orange products corresponds to the imposed elasticity. Formally, we calculate the implied Orange products price elasticity in market  $m$ , defined as follows:

$$e_m^O(\theta) = \frac{s_{m,O}(1.01\mathbf{p}_O, \mathbf{p}_{-O}, \mathbf{Q}_m; \theta) - s_{m,O}(\mathbf{p}_O, \mathbf{p}_{-O}, \mathbf{Q}_m; \theta)}{0.01s_{m,O}(\mathbf{p}_O, \mathbf{p}_{-O}, \mathbf{Q}_m; \theta)},$$

where  $s_{m,O}(\cdot)$  is the share of contracts in  $m$  produced by Orange,

$$s_{m,O}(\mathbf{p}_O, \mathbf{p}_{-O}, \mathbf{Q}_m; \theta) = \sum_{j \in \mathcal{J}_O} \int s_{ijm}(\mathbf{p}_O, \mathbf{p}_{-O}, \mathbf{Q}_m; \theta_i) dF_m(\theta_i),$$

and  $s_{ijm}(\cdot)$  gives the share of consumers of type  $\theta_i$  in market  $m$  who purchase contract  $j$ , and  $F_m(\theta_i)$  denotes the CDF of consumer types  $\theta_i$  in market  $m$ . The vector  $\mathbf{p}_O$  represents the vector of Orange product prices, and  $\mathbf{p}_{-O}$  represents the prices of those produced by non-Orange firms.

For a range of price elasticities  $E \in \mathcal{E}$ , we impose

$$\mathbb{E} [e_m^O(\theta) - E] = 0$$

as a moment in our estimation procedure, described below.

We also impute values for the nesting parameter,  $\sigma$ . For a given own-price elasticity imputation, the nesting parameter effectively controls how much substitution goes to the outside option. As the imputed  $\sigma$  approaches one, there is effectively no outside option. At the opposite extreme,  $\sigma = 0$  yields a mixed logit model with no nesting.

While these imputations assume a lot, note that there are still important aspects of consumer demand to be estimated, particularly how consumers trade off prices and download speeds (and how consumers differ in such preferences).

Appendix B displays results for a range of elasticity and nesting parameter imputations.

### 5.1.3 Identification

For each Orange contract, we observe monthly data consumption. We identify the data utility parameters  $\theta_{d0}$ ,  $\theta_{dz}$ , and  $\theta_c$ , in part, by matching predicted data consumption with observed data consumption. Formally, from the data we construct  $\bar{x}_{jm}$ , which is the average data consumption across consumers using product  $j$  in market  $m$ . Given  $\theta$ , we can construct the mean data consumption across consumers in market  $m$  that chose product  $j$ :

$$\bar{x}_{jm}(\theta) \equiv (s_{jm}(\mathbf{p}, \mathbf{Q}_m; \theta))^{-1} \int \int s_{ijm}(\mathbf{p}, \mathbf{Q}_m; \theta_i) x_{jm}^*(\vartheta_i) dF(\vartheta_i | \theta_i) dF_m(\theta_i).$$

Appendix A.3 shows how to integrate over  $\vartheta_i$  analytically.

Matching observed and predicted data consumption effectively identifies the average  $\theta_{di}$ . To identify both  $\theta_{d0}$  and  $\theta_{dz}$ , which controls how  $\theta_{di}$  varies with income, we use a moment interacting the difference between predicted and observed data consumption and median market income.

Simply matching mean data consumption and shares consuming above limits does not identify the level of the data utility (and therefore  $\theta_c$ ). The level of data utility comes from the trade-off between the data utility and the contract's other components (price and voice allowance), which is identified by imposing that demand shocks  $\boldsymbol{\xi}$  are uncorrelated with data limits (which are correlated with data utility).

The imputed elasticity moment effectively identifies the average  $\theta_{pi}$ , and we separately identify  $\theta_{p0}$  and  $\theta_{pz}$  by imposing that the demand shocks  $\boldsymbol{\xi}$  are uncorrelated with median incomes. Voice allowances are assumed to be uncorrelated with the demand shocks.

In summary, we have the following moments that we use to identify the distribution of preference parameters  $\theta$ . Note that the moments are only imposed for Orange products since we only observe data consumption and product-market shares for Orange.



### Moments

$$\begin{aligned}
\mathbb{E} \left[ e_m^O(\theta) - E \right] &= 0 \\
\mathbb{E} \left[ \xi_{jm}(\theta) inc_m^{med} \right] &= 0 \\
\mathbb{E} \left[ \bar{x}_{jm}(\theta) - \bar{x}_{jm} \right] &= 0 \\
\mathbb{E} \left[ (\bar{x}_{jm}(\theta) - \bar{x}_{jm}) inc_m^{med} \right] &= 0 \\
\mathbb{E} \left[ \xi_{jm}(\theta) v_j \right] &= 0 \\
\mathbb{E} \left[ \xi_{jm}(\theta) \bar{x}_j \right] &= 0
\end{aligned}$$

We use two-stage efficient GMM to estimate  $\theta$ , searching for  $\theta$  in an outer loop and solving for  $\xi(\theta)$ ,  $e^O(\theta)$ , and  $\bar{x}(\theta)$  in an inner loop. Further details can be found in Appendix A.4.

## 5.2 Results

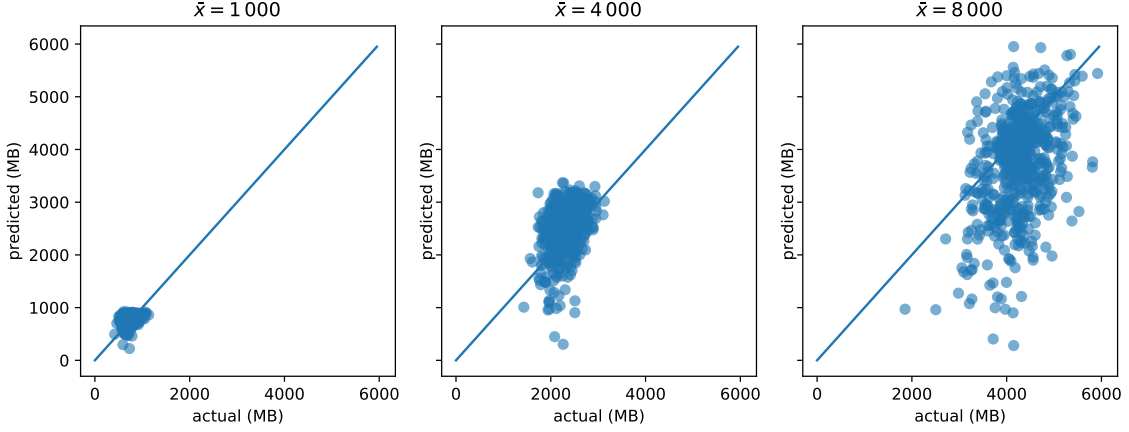
Demand parameter estimates are listed in table 6 in Appendix B.1 for a range of imputed price elasticities and imputed nesting parameters. The price elasticity implied by Bourreau, Sun and Verboven (2018) is -2.5, the middle imputed price elasticity, which we regard as our preferred specification. For all imputations, price sensitivity is decreasing in income. The data utility parameter is increasing in income, which implies an inverse relationship between income and the value of data consumption, suggesting a higher opportunity cost of time spent downloading for higher income individuals. The variance parameter is increasing in income. While signs are consistent across elasticities, the parameter estimates appear to be sensitive to the price elasticity chosen, especially price, voice allowance, and Orange dummy coefficients.

To interpret the results above, tables 7–9 in Appendix B.1 convert the parameter estimates into willingness to pay for certain contract characteristics across income percentiles. Figure 7 considers how well our model predicts actual data consumption by plotting predicted and actual average data consumption across markets for three Orange contracts with different data limits.<sup>27</sup> The diagonal line is a 45-degree line. Markets in which predicted average consumption equals observed average consumption will lie upon the line. Our estimated model correctly predicts the average level, even though this level is not a constant fraction of the data limit. While it predicts across-market heterogeneity less well, it does weakly predict high data consumption for markets with high observed data consumption and low data consumption for markets with low observed data consumption. The correlation coefficients between actual and predicted consumption for the three contracts across markets are, respectively, 0.305, 0.386, and 0.405.

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<sup>27</sup>The predicted average data consumption is based on parameter estimates for the imputed elasticity -2.5 and a nesting parameter of 0.8.

Figure 7: Predicted vs. actual average data consumption



### 5.3 Cost Estimation

There are two costs parameters to be estimated:  $c_u$ , the cost per user and  $c_{f,c,m}$ , the fixed cost per base station in market  $m$ .

#### 5.3.1 Costs per user

From equation (8), the first-order condition from the price setting game is

$$\sum_m N_m \mathbf{S}_{mf}(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m) + \left( \sum_m N_m J_f \mathbf{S}_{mf}(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m) \right) (\mathbf{P}_f - \mathbf{c}_{u,f}) = 0, \quad (17)$$

where  $J_f$  represents the Jacobian operator with respect to  $\mathbf{P}_f$ .

Therefore, an estimate of marginal cost is given by

$$\hat{\mathbf{c}}_{u,f} = \mathbf{P}_f + \left( \sum_m N_m J_f \mathbf{S}_{mf}(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m) \right)^{-1} \sum_m N_m \mathbf{S}_{mf}(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m).$$

Estimated costs for our elasticity and nesting parameter imputations are given in Table 10 in Appendix B.2.

#### 5.3.2 Infrastructure costs

Given the demand estimates, and the model of how the infrastructure variables  $(\mathbf{R}, \mathbf{B})$  map into delivered quality, we can simulate how equilibrium revenues change as the infrastructure is changed. Intuitively, we can measure the marginal revenue of infrastructure, and this allows us to infer the marginal cost of infrastructure.

Formally, we compute the marginal operating income from each market based on a 1% change in cell radius:

$$MR_{mf,R}(\mathbf{R}_m, \mathbf{B}_m) = \frac{\Pi_{mf}(\mathbf{P}, (.01 + R_{mf}, \mathbf{R}_{m,-f}), \mathbf{B}_m) - \Pi_{mf}(\mathbf{P}, \mathbf{R}_m, \mathbf{B}_m)}{.01}.$$

For these calculations, we use the prices observed in equilibrium, implicitly assuming that the equilibrium prices (which are set nationally) will not respond to a change in infrastructure in a single market  $m$ . As each commune is quite small, this is a plausible approximation. Note that these profit functions are defined in terms of the equilibrium download speeds that result from the infrastructure and prices. Thus, the above expressions for marginal revenue should be understood as implicitly taking into account how quality changes as infrastructural investment is changed.

Next, assuming that infrastructure investments are chosen to maximize profits, we can use the marginal revenues above to recover the remaining cost function parameters using equation (9). The marginal cost of increasing  $R_{mf}$  is obtained by differentiating the cost function in equation (9). Therefore, setting marginal cost equal to marginal revenue, we can set the derivative of (9) equal to the marginal revenue with respect to  $R$ . This allows us to identify cost function parameters.

Estimated infrastructure costs for our elasticity and nesting parameter imputations are given in Table 11 in Appendix B.2.

## 6 Counterfactual Simulations

Our framework can address questions of market structure, both in terms of traditional antitrust questions and questions related to the management of the electromagnetic spectrum. In section 6.1, we consider the optimal number of firms and the trade-off between market power and scale economies. Then, in section 6.2, we consider the marginal value of spectrum allocated to mobile telecommunications and find that the marginal contribution to consumer surplus far exceeds firms' willingness to pay. In section 6.3 we consider two different ways of allocating new spectrum in the industry: sponsoring the entry of a new firm, or allocating it among existing firms. Finally, in section 6.4 we take a short-run focus, considering a change in the number of firms while holding infrastructure fixed.

For the following counterfactuals, we compute equilibria for a representative commune that has an income distribution matching the overall income distribution our sample, population density equal to our sample's median, spectral efficiency parameter equal to the median in the calibration described in section 3.4, and cost parameter equal to the mean estimated with equation (9).

## 6.1 Market Power and Scale Efficiencies

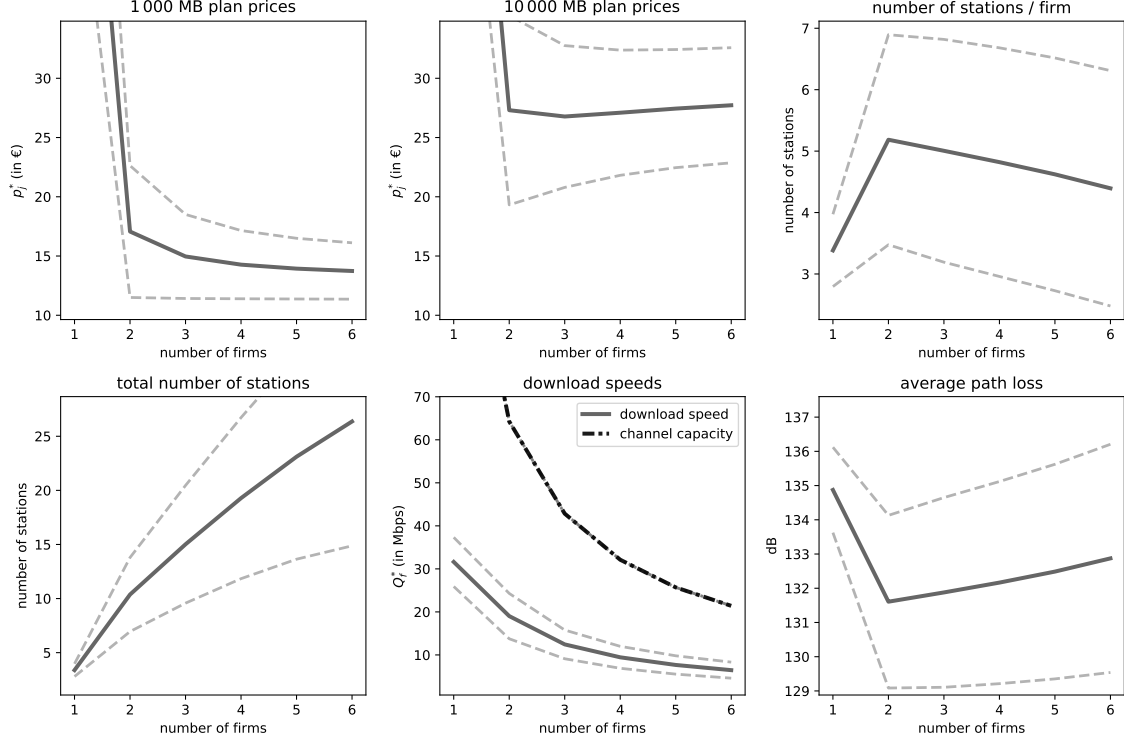
In this section, we explore the trade-off between market power and economies of scale by considering the optimal number of firms in a static equilibrium. Given the gradual nature of network deployment in the industry, this exercise cannot hope to capture the short-run impacts of potential merger; instead, we aim to capture the long-run trade-offs associated with consolidation.

We simulate counterfactual equilibria using the estimated cost and demand parameters, assuming symmetric firms. Each firm offers two data plans: one with a 1 GB limit and another with a 10 GB limit. The former represents a small to moderate data allowance; the latter, an extremely generous data allowance (in 2015). All plans are assumed to have unlimited voice.

As we vary the number of firms, total bandwidth available to the industry is divided equally among firms. We compute equilibria based on a representative municipality with median characteristics across municipalities in our sample. We present results below for a nesting parameters of 0.8, and a price elasticity of -2.5, which is approximately the price elasticity implied by the demand model of Bourreau, Sun and Verboven (2018). Results for other possible nesting parameters are located in Appendix B.3, and it does not appear that the choice of nesting parameter affects our results in a substantial way.

Figure 8 displays endogenous variables for symmetric equilibria as we vary the number of firms.

Figure 8: Counterfactual prices and qualities



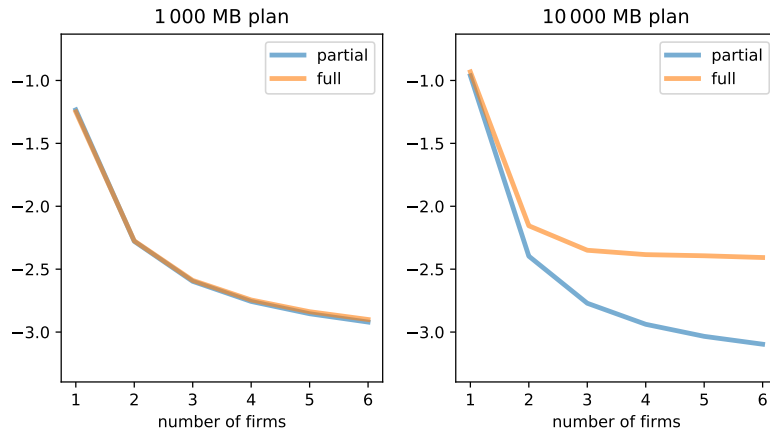
Equilibrium prices have a subtly non-standard relationship with the number of firms. At low numbers of firms, prices do decline with the number of firms, but as we get beyond a few firms, prices can actually increase (seen in Figure 8 for the 10GB data limit product). The reason for this non-standard relationship has to do with the non-standard nature of price elasticities in our setting. Figure 9 displays *partial price elasticities*, the price elasticity holding quality of service fixed, evaluated at equilibrium prices. These elasticities display the typical relationship with the number of firms. However, this partial price elasticity is not the relevant price elasticity for firms' price setting.

As a firm lowers its price, it attracts more customers, causing the load on its network to increase, lowering download speeds, and dampening the appeal of the lowered price for consumers. In other words, the relevant elasticity for the purposes of setting optimal prices involves a full derivative that takes into account the indirect effect of changing prices on download speeds. Figure 9 also displays these *full price elasticities*, which decline less with the number of firms than the partial elasticities. The reason for the divergence between the full and partial price elasticities is the worsening of the indirect quality effect as the number of firms grows. When there are many firms, a firm's own capacity is small relative to the number of consumers that they can potentially attract from other firms, making quality of

service degrade more for a given price increase.

Investment patterns display a non-monotonic relationship in the number of firms. For a small number of firms, the number of base stations each firm builds is increasing in the number of the firms (alternatively, the cell radius characterizing each base station is decreasing). Increasing the number of firms beyond 2, however, decreases investment at the firm level: for each increase in the number of firms, each firm builds fewer base stations (increases the cell radius). Despite this non-monotonicity in investment, download speeds are always decreasing in the number of firms. Comparing the monopoly case to the duopoly one, despite fewer base stations for the monopolist, the economies of pooling and density result in higher download speeds.

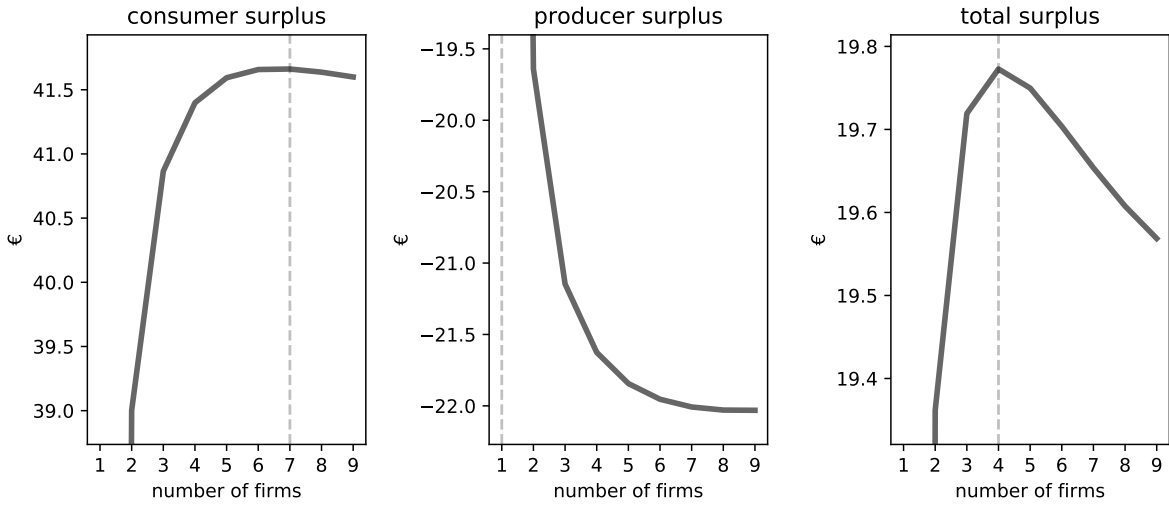
Figure 9: Full and partial price elasticities



Notes: Partial elasticities are derivatives in which download speeds are held fixed. Full elasticities take into account how download speeds change endogenously as prices are changed. Price elasticities are evaluated at the equilibrium prices and quantities.

Figure 10 considers welfare compared to the monopoly case as the number of firms is varied. For our preferred demand specification (elasticity of -2.5 and nesting parameter of 0.8), the optimal number of firms is four in terms of total surplus, and six in terms of consumer surplus.

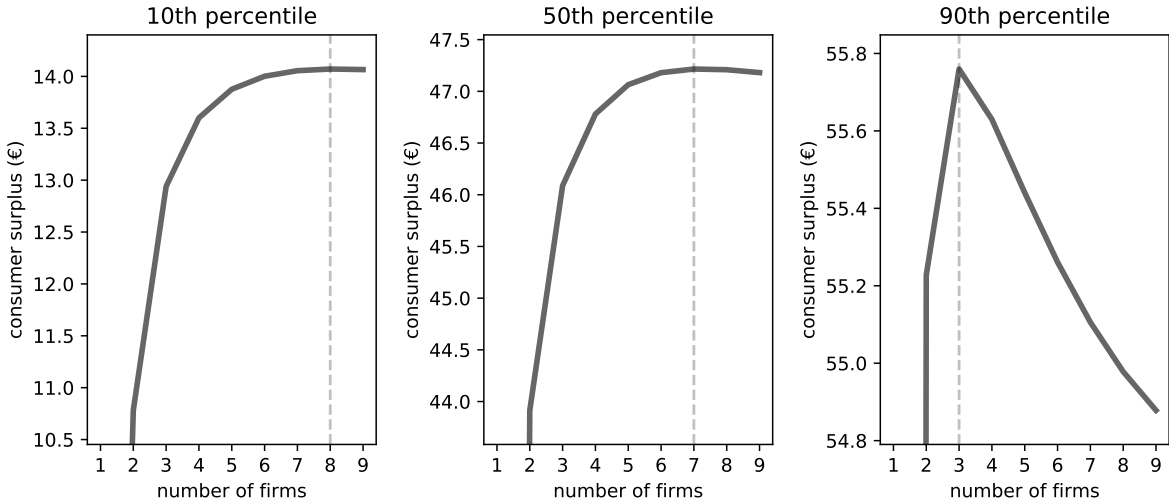
Figure 10: Counterfactual welfare



Notes: Welfare is measured in euros per capita relative to monopoly.

However, as Figure 11 illustrates, consumers do not agree on the optimal number of firms. We plot welfare for various income deciles against the number of firms for our preferred specification. While consumer surplus is increasing in the number of firms for most consumers (up to eight firms), the optimal number of firms for high-income consumers is three. In all our simulations, we have observed that the optimal number of firms is (weakly) decreasing with income.

Figure 11: Counterfactual welfare by income level



Notes: Welfare is measured in euros per capita relative to monopoly.

## 6.2 Allocating Spectrum to the Industry

Regulators such as the FCC in the US and ARCEP and ANFR in France are tasked with bandwidth allocation, determining which industries (and firms) are allowed to operate which frequencies of electromagnetic spectrum and for what purposes. It is therefore crucial for such agencies to understand how allocating bandwidth to mobile telecommunications will affect social welfare.<sup>28</sup>

In this section, we quantify how allocating more bandwidth to the telecommunications industry affects firm profits, consumer welfare, and total surplus.

First, let's consider how a firm's profits change when just that firm receives a larger bandwidth allocation. The derivative

$$\frac{\partial \Pi_f(\mathbf{R}^*(b_f, \mathbf{b}_{-f}), (b_f, \mathbf{b}_{-f}))}{\partial b_f} \quad (18)$$

captures an individual firm's willingness to pay for more bandwidth at the margin.

Next,

$$\frac{\partial \Pi_f(\mathbf{R}^*(b\mathbf{1}), b\mathbf{1})}{\partial b} \quad (19)$$

captures how the equilibrium profits of an individual firm changes when all firms are allocated more bandwidth.

Finally, we can consider how consumer surplus changes as all firms are allocated more bandwidth

$$\frac{\partial CS_f(\mathbf{R}^*(b\mathbf{1}), b\mathbf{1})}{\partial b}. \quad (20)$$

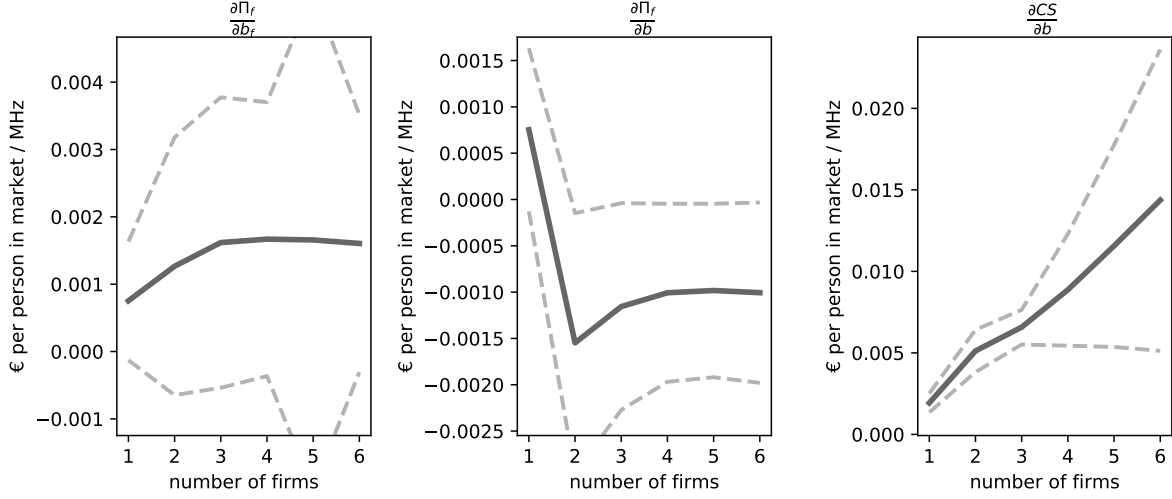
In a simple spectrum auction, the firms' bids will be related to (18). However, the regulator's spectrum decision should be based on comparing (19) and (20) to the marginal social value to allocation spectrum to other industries and purposes.

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<sup>28</sup>The FCC's mandate is explicitly in "the public interest." To allocate spectrum optimally among different industries – or to allocate the optimal among of spectrum to mobile telecommunications – one would need to quantify the social opportunity cost of spectrum, which is beyond our scope.



Figure 12: Bandwidth derivatives



Notes: Derivatives are evaluated at the symmetric equilibrium values.

As Figure 12 shows, with four firms, the firm's willingness to pay for additional bandwidth (the left panel) is about five times less than a unit of bandwidth allocated to the industry would add to consumer surplus (the right panel). This reflects the importance of using a structural model such as ours to quantify the social value of bandwidth. While auctions may allow us to observe signals of operators' willingness to pay for spectrum, such measures may be far lower than the social value of spectrum.

### 6.3 Allocating Spectrum within the Industry

Spectrum allocation questions go well beyond the question of how much spectrum to allocate to each industry. In particular, how should spectrum be allocated among firms? In this section, we consider two ways of allocating new spectrum to the mobile telecommunications industry. First, the regulator could distribute the new spectrum among existing operators. Alternatively, it could sponsor the entry of a new operator, as happened in France with Free Mobile, which received regulatory approval to become France's fourth MNO in 2009, and launched in 2012.

Our baseline equilibrium is the symmetric equilibrium with three firms from section 6.1. Then, we compute an equilibrium in which each firm's bandwidth holdings are 33.3% higher. Finally, we compute an equilibrium in which each firm's bandwidth holdings are the same as in the baseline, but there are four firms. Thus, we consider two different ways of increasing the total amount of spectrum in the industry by 33.3%.

Figure 13 illustrates how various endogenous variables change with the additional bandwidth.

Unsurprisingly, introducing a new firm leads to lower prices than increasing bandwidth per firm. However, download speeds benefit considerably more when bandwidth per firm is increased.

Figure 13: Counterfactual prices and qualities

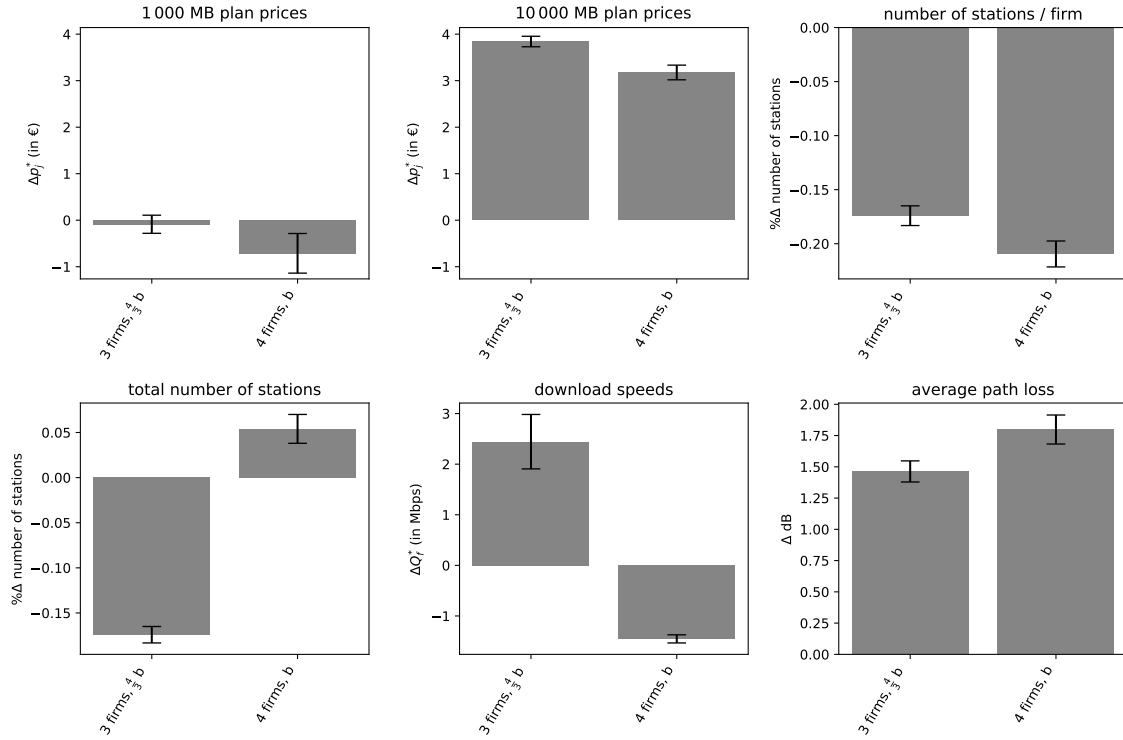


Figure 14 considers the overall effects on welfare and present an interesting tension. Increasing the number of firms is better for consumer surplus, but increasing bandwidth-per-firm is better for total surplus.

Figure 14: Counterfactual welfare

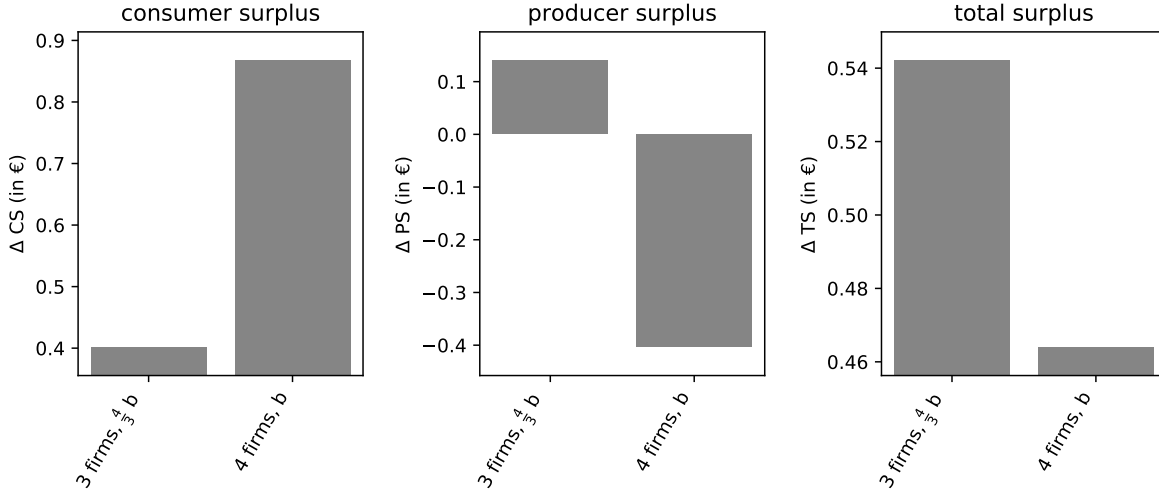
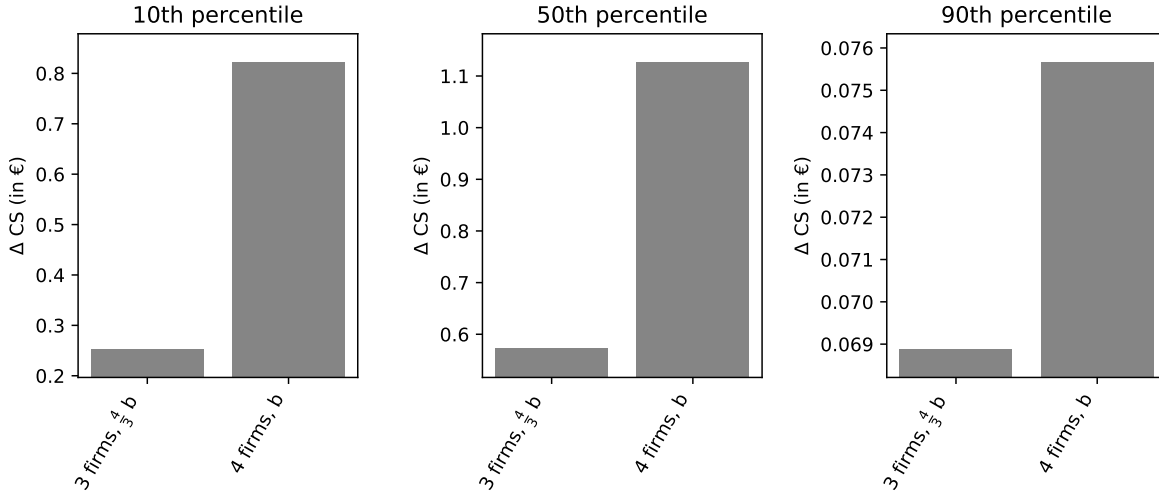


Figure 15 shows that consumers disagree on which way of allocating new bandwidth is better. Most consumers prefer the situation with four firms, but high-income consumers prefer higher bandwidth per firm.

Figure 15: Counterfactual welfare by income level



## 6.4 Short-Run Analysis

We performed comparative statics with respect to the number of firms in section 6.1. Such an exercise should be interpreted with caution when extrapolating to merger analysis; because those counterfactuals involve static equilibria, they certainly cannot capture the short-run

impacts of mergers, for infrastructure cannot be rearranged instantaneously and costlessly in response to a change in the number of firms.

In this section, we consider the impact of consolidation in the short-run. That is, we change the number of firms and recompute an equilibrium without allowing infrastructure to adjust.

Tables 3-5 describe how outcomes change when we move from the four-firm equilibrium of section 15 to an equilibrium with three firms with the base station radius is fixed at the equilibrium radius from the original four-firm equilibrium. That is, we are crudely approximating a symmetric four-to-three merger in the short run.

To be clear, bandwidth is redistributed, so that each firm in the three-firm equilibrium has 33.3% more bandwidth than each firm in the four-firm equilibrium. Furthermore, we impose that each firm's base station radius (or cell size) is the same in the three-firm and four-firm equilibrium. What we imagine is that all firms are sharing passive infrastructure, meaning they all have base stations located at the same places, and they each operate their own antennas on shared physical structures. When we consolidate to three firms, the antennas (and bandwidth) are simply consolidated, and each of the three operators now owns one third of the network infrastructure at each base station site rather than one quarter.

Table 3 shows that low-end contract prices change very little, but high-end prices and download speeds increase by a non-trivial amount. Table 4 shows that both consumer and producer surplus improve. Table 5 breaks down the consumer surplus impacts by income decile.

Table 3: Three firms with four-firm base station density: endogenous variables

$\Delta$ 1 000 MB plan prices (in €)	$\Delta$ 10 000 MB plan prices (in €)	$\Delta$ download speeds (in Mbps)
-0.003 (0.067)	2.091 (0.230)	0.168 (0.037)

In section 6.1, there was a higher number of base stations per firm with three firms than with four firms. Here, we have fixed the number of base stations per firm, so the four-to-three comparison involves a more modest gain in download speeds here, where the gains in quality of service are driven entirely by consolidation of bandwidth.

Another difference is that the four-to-three comparison previously involved higher prices (see Figure 8), but now we see slightly lower prices for low-end contracts with three firms.

Table 4: Three firms with four-firm base station density: welfare

$\Delta$ CS	$\Delta$ PS	$\Delta$ TS
0.081 (0.152)	0.124 (0.030)	0.205 (0.182)

Welfare measured in euros per capita per month.

Table 5: Three firms with four-firm base station density: consumer surplus by income

$\Delta$ CS 10 %ile	$\Delta$ CS 30 %ile	$\Delta$ CS 50 %ile	$\Delta$ CS 70 %ile	$\Delta$ CS 90 %ile
0.039 (0.156)	0.125 (0.195)	0.190 (0.116)	0.149 (0.077)	-0.238 (0.256)
Consumer surplus measured in euros per capita per month.				

Ultimately, the sign of the change in consumer surplus for the four-to-three firm comparison depends on whether we take the a long-run or short-run view. Consumer surplus is higher with three firms in the short-run setting here, but it was higher with four firms in section 6.1. However the stakes are small for the four-to-three comparison in both cases. As Table 5 shows, the change in consumer surplus is less than 25 euro cents per month for all consumers.

## 7 Conclusion

The regulation of the mobile telecommunications industry, including antitrust policy and spectrum allocation, call for an understanding of scale efficiencies as well as market power. Our approach has effectively been an interdisciplinary one, drawing from tools in empirical industrial organization to understand market power, and from wireless engineering to understand scale efficiencies. Our simulations show how our framework can shed light on many issues related to industry structure, including the optimal number of firms, across-industry spectrum allocation, and within-industry spectrum allocation.

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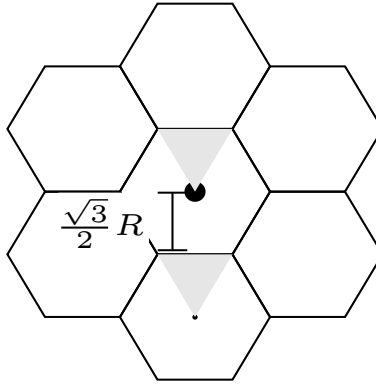
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## A Technical Appendix

### A.1 Interference

To calculate the interference from neighboring cells, we consider the six cells adjacent to a particular cell, pictured in Figure 16. For a given point in the center cell, we compute the distances between that point and the centroids of the adjacent cells, which is the location of the antennas corresponding to each cell.

Figure 16: A hexagonal cell and its six adjacent cells



The signal power from each of the adjacent cells is the path loss (equation 4) implied by the distance between the given point and the cell's centroid. To determine the overall interference power, we follow Blaszczyszyn, Jovanovicy and Karray (2014) and set interference power to 30% of the signal power from the six adjacent cells and sum over the cells.

### A.2 Contraction Mapping

Here we consider an alternative version of the Berry, Levinsohn and Pakes (1995) (BLP) contraction mapping. We observe market shares at the product-market level for Orange products but only aggregate firm-level market shares for the other products. We first show that if we observe market shares at the firm-market level, the problem can be rewritten in such a way that the BLP contraction mapping proof holds. We then show that if we observe some firm market shares only at the aggregate level (as is our case), the problem no longer fits into the BLP proof setup, but that the standard function used to recover mean utilities is still a contraction mapping.

#### A.2.1 Standard BLP contraction mapping setup

We will start with the standard BLP setting in order to introduce notation.



For the standard BLP setting, with products  $j \in \mathcal{J} = \{1, \dots, J\}$ , we observe market shares  $\varsigma_{jm}$  for each product.

We can express an individual's utility for a product as follows:

$$u_{ijm} = \delta_{jm} + \mu_{ijm} + \varepsilon_{ijm},$$

and the type-specific market shares are as follows:

$$s_{ijm} = \frac{\exp(\delta_{jm} + \mu_{ijm})}{\sum_{j'} \exp(\delta_{j'm} + \mu_{ij'm})}.$$

The contraction mapping takes for granted the distribution over the heterogeneous component of preferences  $F(\mu_m)$ . That is, given a conjectured parameter value  $\theta$ , we have  $F(\mu)$ , and we want to use the contraction mapping to recover mean utilities  $\delta_{jm}$ .

Specifically, aggregate market shares are

$$s_{jm}(\delta) = \int \frac{\exp(\delta_{jm} + \mu_{ijm})}{\sum_{j'} \exp(\delta_{j'm} + \mu_{ij'm})} dF(\mu_m).$$

The existence of the contraction mapping implies that there is a unique vector  $\delta$  such that  $s_m(\delta) = \varsigma_m$  for any observed vector of shares  $s_m$ .

### A.2.2 Grouped products extension

Our setting is one in which market shares are observed only for certain groupings of products. That is, let  $\mathcal{J}$  be partitioned into subsets  $\mathcal{J}_f$  with  $f \in \mathcal{F} = \{1, 2, \dots, F\}$ . For each  $f$ , we observe only the market share  $\varsigma_{ft}$  for all the products within  $\mathcal{J}_f$ .

The subsets  $\mathcal{J}_f$  may include individual products (i.e., in our application each Orange product would have its own  $\mathcal{J}_f$  set), or several products (i.e., each non-Orange firm has one  $\mathcal{J}_f$  group that includes all that firm's products).

Providing a parametric form:

$$\delta_{jm} = \theta_1 x_{jm} + \xi_{jm},$$

where  $\theta_1$  would capture what is often referred to as “linear parameters”; i.e., parameters that can typically be estimated outside of the contraction mapping because they only shift the mean utility component  $\delta_{jm}$  that the contraction mapping aims to recover. In this extension, the  $\theta_1$  parameters must be included in the contraction mapping.

We definitely cannot recover  $\delta_{jm}$  (or  $\xi_{jm}$ ) separately for different  $j \in \mathcal{J}_f$ . So, let's assume

$\xi_{jm} = \xi_{fm}$  for all  $j \in \mathcal{J}_f$ , and for each  $f$ .

Let  $\bar{x}_{fm}$  be the mean value of  $x_{fm}$  for those products within  $\mathcal{J}_f$ . Then, we have

$$\delta_{jm} = \theta_1 \bar{x}_{fm} + \theta_1 x_{jm}^d + \xi_{fm},$$

where  $x_{jm}^d := x_{jm} - \bar{x}_{fm}$ .

Now, define

$$\tilde{\delta}_{fm} = \theta_1 \bar{x}_{fm} + \xi_{fm},$$

$$\tilde{\mu}_{ijm} = \theta_1 x_{jm}^d + \mu_{ijm}.$$

This very nearly allows us to re-define the model in terms where we could apply the original BLP proof strategy to establish the contraction mapping. The only problem is that  $\tilde{\mu}_{ijm}$  is defined over  $j$ , where we would need it to be defined over  $f$  in order to apply the same proof strategy. Let's consider the aggregation over  $j$  to  $f$ :

$$s_{ifm}(\tilde{\delta}) = \sum_{j \in \mathcal{J}_f} \frac{\exp(\tilde{\delta}_{fm} + \tilde{\mu}_{ijm})}{\sum_{j' \in \mathcal{J}} \exp(\tilde{\delta}_{f(j')m} + \tilde{\mu}_{ij'm})},$$

where  $f(j')$  refers to the  $f$  associated with product  $j'$ .

Notice that

$$\sum_{j \in \mathcal{J}_f} \exp(\tilde{\delta}_{fm} + \tilde{\mu}_{ijm}) = \exp(\tilde{\delta}_{fm}) \sum_{j \in \mathcal{J}_f} \exp(\tilde{\mu}_{ijm}).$$

Now, let's define

$$\tilde{\mu}_{ifm} \equiv \log \left( \sum_{j \in \mathcal{J}_f} \exp(\tilde{\mu}_{ijm}) \right).$$

It follows that

$$\sum_{j \in \mathcal{J}_f} \exp(\tilde{\delta}_{fm} + \tilde{\mu}_{ijm}) = \exp(\tilde{\delta}_{fm} + \tilde{\mu}_{ifm}),$$

and therefore

$$s_{ifm}(\tilde{\delta}) = \sum_{j \in \mathcal{J}_f} \frac{\exp(\tilde{\delta}_{fm} + \tilde{\mu}_{ijm})}{\sum_{f'} \exp(\tilde{\delta}_{f'm} + \tilde{\mu}_{if'm})}.$$

We can then aggregate up to market-level shares  $s_{fm}$  by integrating over the  $\tilde{\mu}_{ifm}$ , and we have rewritten our extended setting in a way that allows us to apply the BLP proof strategy.

### A.2.3 Grouped products extension with nested logit

In the more general random coefficients nested logit (RCNL) model we use to model demand, the market share equations as well as the formulas for  $\tilde{\delta}$  and  $\tilde{\mu}$  no longer hold. We can, however, construct analogous formulas that will allow us to recover firm-specific mean demands  $\tilde{\delta}$ .

In the RCNL model, an individual's utility for a product is as follows:

$$u_{ijm} = \delta_{jm} + \mu_{ijm} + \bar{\varepsilon}_{ijm},$$

where

$$\bar{\varepsilon}_{ijm} = \zeta_{ig(j)m} + (1 - \sigma) \varepsilon_{ijm},$$

where  $\sigma \in [0, 1)$  is the nesting parameter, the function  $g(j)$  returns the group identifier to which  $j$  belongs,  $\varepsilon_{ijm}$  is i.i.d. type-1 extreme value, and  $\zeta_{ig(j)}$  has the distribution such that  $\bar{\varepsilon}_{ijm}$  is extreme value.

Type-specific market shares are as follows:

$$s_{ijm} = \frac{\exp\left(\frac{\delta_{jm} + \mu_{ijm}}{1 - \sigma}\right) \exp(I_{ig(j)})}{\exp\left(\frac{I_{ig(j)}}{1 - \sigma}\right) \exp(I_i)},$$

where

$$I_{ig} = (1 - \sigma) \log\left(\sum_{j \in \mathcal{J}_g} \exp\left(\frac{\delta_{jm} + \mu_{ijm}}{1 - \sigma}\right)\right),$$

$$I_i = \log\left(1 + \sum_{g \in \mathcal{G}} \exp(I_{ig})\right).$$

In this model, we must redefine  $\tilde{\delta}_{fm}$  and  $\tilde{\mu}_{ijm}$  to incorporate  $\rho$ . Define

$$\tilde{\delta}_{fm} = \frac{\theta_1 \bar{x}_{fm} + \xi_{fm}}{1 - \sigma},$$

$$\tilde{\mu}_{ijm} = \frac{\theta_1 x_{jm}^d + \mu_{ijm}}{1 - \sigma}.$$

Then note that

$$s_{ifm} = \sum_{j \in \mathcal{J}_f} s_{ijm} = \exp(\tilde{\delta}_{fm}) \sum_{j \in \mathcal{J}_f} \frac{\exp(\tilde{\mu}_{ijm})}{\exp\left(\frac{I_{ig(j)}}{1 - \sigma}\right)} \frac{\exp(I_{ig(j)})}{\exp(I_i)}.$$

We will assume that products produced by the same firm belong to the same product group. Formally,  $g(j) = g(j')$  for all  $(j, j') \in \mathcal{J}_f^2$  for all  $f$ . This assumption implies that the product-relevant inclusive values  $\{I_{ig}\}_{g \in \mathcal{G}}$  are common within firms, and we can write the product group identifier function  $g(\cdot)$  as a function of the firm identifier rather than the product

identifier. In our context where all contracts belong to the same group, this assumption holds. It follows that

$$s_{ifm} = \frac{\exp(\tilde{\delta}_{fm})}{\exp\left(\frac{I_{ig(f)}}{1-\sigma}\right)} \frac{\exp(I_{ig(f)})}{\exp(I_i)} \sum_{j \in \mathcal{J}_f} \exp(\tilde{\mu}_{ijm}). \quad (21)$$

Let's define

$$\tilde{\mu}_{ifm} = \log \left( \sum_{j \in \mathcal{J}_f} \exp(\tilde{\mu}_{ijm}) \right).$$

Then

$$s_{ifm} = \frac{\exp(\tilde{\delta}_{fm} + \tilde{\mu}_{ifm})}{\exp\left(\frac{I_{ig(f)}}{1-\sigma}\right)} \frac{\exp(I_{ig(f)})}{\exp(I_i)}$$

and

$$I_{ig} = (1 - \sigma) \log \left( \sum_{f \in \mathcal{F}_g} \exp(\tilde{\delta}_{fm} + \tilde{\mu}_{ifm}) \right),$$

where  $\mathcal{F}_g = \{f \in \mathcal{F} : g(f) = g\}$ . This is now in terms of firm-specific variables.

Equation 21 is similar to that of GV, except in the numerator of the first fraction. GV note that, substituting in our notation,

$$f(\tilde{\delta}) = \tilde{\delta} + \log(\varsigma) - \log(s(\tilde{\delta})),$$

where  $\varsigma$  is observed shares, is a contraction mapping if<sup>29</sup>

$$1 - \frac{1}{s_f} \frac{\partial s_f}{\partial \tilde{\delta}_f} \geq 0.$$

Unlike in GV, this holds in our case. Explicitly,

$$\frac{\partial s_f}{\partial \tilde{\delta}_f} = \left( 1 - \frac{\sigma}{1 - \sigma} s_{f|g} - s_f \right) s_f,$$

and so

$$\frac{\partial s_f}{\partial \tilde{\delta}_f} = \frac{\sigma}{1 - \sigma} s_{f|g} + s_f \geq 0 \quad \Leftrightarrow \quad \sigma s_{f|g} + (1 - \sigma) s_f \geq 0.$$

This holds for all  $\sigma \in [0, 1)$ , and so therefore iterating on the standard BLP contraction mapping using Equation 21 will yield the unique vector  $\tilde{\delta}$ .

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<sup>29</sup>GV also note a few other conditions that must hold, but these conditions do not differ between our modified setup and theirs, and so we therefore do not include them here.

#### A.2.4 Market aggregation extension

The firm-aggregation provided in the previous sections still does not apply to our setting because we observe market shares only at the aggregate level for certain firms. We can still proceed by imposing the more restrictive assumption  $\xi_{jm} = \xi_{f(j)}$  for all  $j, m$ . This will allow us to recover  $\xi_f$  for each  $f$ .

Analogous to the previous setup, let  $\bar{x}_f$  be the mean value of  $x_{jm}$  across products  $j \in \mathcal{J}_f$  and markets  $m$ . That is

$$\bar{x}_f := \frac{1}{MJ_f} \sum_m \sum_{j \in \mathcal{J}_f} x_{jm},$$

Then

$$\delta_{jm} = \theta_1 \bar{x}_{f(j)} + \theta_1 x_{jm}^d + \xi_{f(j)},$$

where we now define  $x_{jm}^d := x_{jm} - \bar{x}_{f(j)}$ .

Define

$$\begin{aligned} \tilde{\delta}_f &:= \theta_1 \bar{x}_f + \xi_f, \\ \tilde{\mu}_{ijm} &:= \theta_1 x_{jm}^d + \mu_{ijm}. \end{aligned}$$

If we sum market shares across products within a firm, we get

$$s_{ifm} = \sum_{j \in \mathcal{J}_f} \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ijm})}{\sum_{j' \in \mathcal{J}} \exp(\tilde{\delta}_{f(j')} + \tilde{\mu}_{ij'm})}.$$

This is very similar to what we had in the previous section, except that here we have  $\tilde{\delta}_f$  instead of  $\tilde{\delta}_{fm}$  because we are additionally averaging over markets.

Now let's average shares across markets, weighting by population,

$$\bar{s}_{if} = \sum_m w(m) \sum_{j \in \mathcal{J}_f} \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ijm})}{\sum_{j' \in \mathcal{J}} \exp(\tilde{\delta}_{j'm} + \tilde{\mu}_{ij'm})}.$$

Note that

$$\sum_{j \in \mathcal{J}_f} \exp(\tilde{\delta}_f + \tilde{\mu}_{ijm}) = \exp(\tilde{\delta}_f) \sum_{j \in \mathcal{J}_f} \exp(\tilde{\mu}_{ijm}).$$

Now define

$$\tilde{\mu}_{ifm} := \log \left( \sum_{j \in \mathcal{J}_f} \exp(\tilde{\mu}_{ijm}) \right).$$

Then

$$\sum_{j \in \mathcal{J}_f} \exp(\tilde{\delta}_f + \tilde{\mu}_{ijm}) = \exp(\tilde{\delta}_f + \tilde{\mu}_{ifm}),$$

so

$$\bar{s}_{if}(\tilde{\delta}) = \sum_m w(m) \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ifm})}{\sum_{f'} \exp(\tilde{\delta}'_f + \tilde{\mu}_{if'm})}.$$

We can aggregate up to aggregate firm shares  $\bar{s}_f$  by integrating over  $\tilde{\mu}_{ifm}$ , i.e.,

$$\bar{s}_f = \int \sum_m w(m) \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ifm})}{1 + \sum_{f'} \exp(\tilde{\delta}'_f + \tilde{\mu}_{if'm})} dF(\tilde{\mu}_{ifm}), \quad (22)$$

where we have normalized the utility of the outside option to 0.

We next need to show that the BLP contraction mapping holds in this case. Consider the following BLP-style fixed point that gives the mean utilities  $\tilde{\delta}$  that set theoretical shares to observed market shares  $\bar{\varsigma}$ :

$$\delta = \underbrace{\delta + \log(\bar{\varsigma}) - \log(\bar{s}(\tilde{\delta}; \theta))}_{=: f(\tilde{\delta})}. \quad (23)$$

The proof that  $f(\cdot)$  is a contraction mapping closely follows that of BLP. In short, if we recognize that averaging across markets is simply integrating over  $\tilde{\mu}_{ijm}$  in another dimension, we can rewrite Equation 22 as follows:

$$\bar{s}_f = \int \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ifm})}{1 + \sum_{f'} \exp(\tilde{\delta}'_f + \tilde{\mu}_{if'm})} dG(\tilde{\mu}_{ifm}).$$

The BLP proof depends on the integrand, not the integral itself, so the proof holds for any arbitrary distribution in an arbitrary number of dimensions. The full proof is provided below.

Berry, Levinsohn and Pakes (1995) show that  $f : \mathbb{R}^K \rightarrow \mathbb{R}^K$  in the metric space  $(\mathbb{R}, d)$ , where  $d$  is the sup-norm, is a contraction mapping if

1. for all  $x \in \mathbb{R}^K$ ,  $f(x)$  is continuously differentiable with, for all  $j$  and  $k$ ,

$$\frac{\partial f_j(x)}{\partial x_k} \geq 0$$

and

$$\sum_{k=1}^K \frac{\partial f_j(x)}{\partial x_k} < 1;$$

2.  $\min_j \inf_x f(x) > -\infty$ ; and
3. there exists a value  $\bar{x}$  with the property that if for any  $j$ ,  $x_j \geq \bar{x}$ , then for some  $k$ ,  $f_k(x) < x_k$ .

We will now show that  $f(\cdot)$  is a contraction mapping.

*Proof.* Beginning with (1), it is clear from the definition of  $\bar{s}_f(\tilde{\delta})$  that  $f(\tilde{\delta})$  is continuously differentiable. The derivatives of  $f(\tilde{\delta})$  are as follows:

$$\begin{aligned}\frac{\partial f_j}{\partial \tilde{\delta}_j}(\tilde{\delta}) &= 1 - \frac{1}{\bar{s}_j(\tilde{\delta})} \frac{\partial \bar{s}_j}{\partial \tilde{\delta}_j}(\tilde{\delta}), \\ \frac{\partial f_j}{\partial \tilde{\delta}_k}(\tilde{\delta}) &= -\frac{1}{\bar{s}_j(\tilde{\delta})} \frac{\partial \bar{s}_j}{\partial \tilde{\delta}_k}(\tilde{\delta}) \quad \text{for all } k \neq j,\end{aligned}$$

where

$$\begin{aligned}\frac{\partial \bar{s}_f}{\partial \tilde{\delta}_f}(\tilde{\delta}) &= \int \sum_m w(m) \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ifm}) \left[1 + \sum_{f' \neq f} \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if'm})\right]}{\left[1 + \sum_{f'} \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if'm})\right]^2} dF(\tilde{\mu}_{ifm}), \\ \frac{\partial \bar{s}_f}{\partial \tilde{\delta}_{f'}}(\tilde{\delta}) &= - \int \sum_m w(m) \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ifm}) \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if'm})}{\left[1 + \sum_{f''} \exp(\tilde{\delta}_{f''} + \tilde{\mu}_{if''m})\right]^2} dF(\tilde{\mu}_{ifm}) \quad \text{for all } g \neq f.\end{aligned}$$

Note that  $\frac{\partial \bar{s}_f}{\partial \tilde{\delta}_g}(\tilde{\delta})$  is negative for all  $\tilde{\delta} \in \mathbb{R}^K$ , so  $\frac{\partial f_j}{\partial \tilde{\delta}_k}(\tilde{\delta})$  is positive since  $\bar{s}(\tilde{\delta}) \gg 0$ . Next note that  $\frac{\partial f_j}{\partial \tilde{\delta}_j}(\tilde{\delta})$  is positive if and only if  $\frac{1}{\bar{s}_j(\tilde{\delta})} \frac{\partial \bar{s}_j}{\partial \tilde{\delta}_j}(\tilde{\delta}) < 1$ . Comparing the integrands of  $\frac{\partial \bar{s}_j}{\partial \tilde{\delta}_j}$  and  $\bar{s}_j$ , since

$$1 + \sum_{f' \neq f} \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if't}) < 1 + \sum_{f'} \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if't}),$$

we have that  $\frac{\partial \bar{s}_j}{\partial \tilde{\delta}_j}(\tilde{\delta}) > \bar{s}_j(\tilde{\delta})$  for all  $\tilde{\delta} \in \mathbb{R}^K$ , and therefore  $\frac{\partial f_j}{\partial \tilde{\delta}_k}(\tilde{\delta})$  is positive. Lastly, we need to show that  $\sum_{k=1}^K \frac{\partial f_j(x)}{\partial x_k} < 1$ :

$$\begin{aligned}\sum_{k=1}^K \frac{\partial f_j(x)}{\partial x_k} &= 1 - \frac{1}{\bar{s}_j(\tilde{\delta})} \sum_k \frac{\partial \bar{s}_j}{\partial \tilde{\delta}_k}(\tilde{\delta}) \\ &= 1 - \frac{1}{\bar{s}_j(\tilde{\delta})} \int \sum_m w(m) \frac{\exp(\tilde{\delta}_j + \tilde{\mu}_{ijm})}{\left[1 + \sum_{f'} \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if'm})\right]^2} dF(\tilde{\mu}_{ifm}) \\ &< 1.\end{aligned}$$

Next we must show that  $f(\cdot)$  satisfies Assumption (2). Note we can rewrite  $f(\tilde{\delta})$  as

$$f(\tilde{\delta}) = \log(\bar{\varsigma}) - \log \left( \int \sum_m w(m) \frac{\exp(\tilde{\mu})}{1 + \sum_{f'} \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if'm})} dF(\tilde{\mu}) \right).$$

We showed earlier that  $f$  is increasing in  $\tilde{\delta}_k$  for all  $k$ . Therefore, let  $\tilde{\delta}_k \rightarrow -\infty$  for all  $k$ . Then

$$\underline{f} = \log(\tilde{s}) - \log \left( \int \sum_t w(t) \exp(\tilde{\mu}) dF(\tilde{\mu}) \right).$$

Note  $\underline{f} \gg -\infty$ , so we have satisfied (2).

Finally, we turn to (3). Following Berry (1994), consider a firm  $f$ . Set  $\tilde{\delta}_{f'} = -\infty$  for all  $f' \neq f$ . Define  $\tilde{\delta}_f$  as the value that sets the market share of the outside good  $\bar{s}_0(\tilde{\delta}) = \bar{\varsigma}_0$ , the observed market share. How do we know that such a  $\tilde{\delta}_f$  exists? Note that  $g(x) = \frac{1}{1+\exp(x+\mu)}$  maps from  $\mathbb{R}$  into  $(0, 1)$  for any  $\mu \in \mathbb{R}$ , and  $\bar{\varsigma}_0 \in (0, 1)$ . Define  $\tilde{\delta} > \max_f \tilde{\delta}_f$ . Consider  $\tilde{\delta} \in \mathbb{R}^K$  such that for some  $f$ ,  $\tilde{\delta}_f > \tilde{\delta}$ . From our definition of  $\tilde{\delta}$ , this will yield  $\bar{s}_0(\tilde{\delta}) < \bar{\varsigma}_0$ , and therefore  $\sum_f \bar{s}_f(\tilde{\delta}) > \sum_f \tilde{s}_f$ . In order for that inequality to hold, there must be some  $f$  such that  $\bar{s}_f(\tilde{\delta}) > \bar{\varsigma}_f$ . Then  $f_f(\tilde{\delta}) < \tilde{\delta}_f$ , satisfying (3).  $\square$

We therefore can iterate on the following

$$\tilde{\delta}_f^{(k)}(\theta_1, \theta_2) = \tilde{\delta}_f^{(k-1)}(\theta_1, \theta_2) + \log(\bar{\varsigma}_f) - \log \left( \bar{s}_f \left( \tilde{\delta}_f^{(k-1)}; \theta_1, \theta_2 \right) \right) \quad (24)$$

to obtain (approximately) the unique fixed point  $\tilde{\delta}$  that rationalizes the observed shares  $\tilde{\varsigma}$ .

### A.2.5 Implementation

The setup outlined in the above section is more restrictive than is necessary given our data. We observe product-level market shares for every market for Orange products. We can therefore allow  $\xi_{jm}$  to differ by product and market for all  $j \in \mathcal{J}_O$ , where  $O$  denotes Orange. This setup is isomorphic to one in which we treat each  $(j, m)_{j \in \mathcal{J}_O, m \in \mathcal{M}}$  as a separate firm, so long as we ensure that the set of “firms” differs across markets (because  $(j, m)$  will not be available in  $(j, m')$ ).

To be more explicit, let  $f(j, m)$  give a unique identity for each  $(j, m)_{j \in \mathcal{J}_O, m \in \mathcal{M}}$ , but for a non-Orange firm  $f \in \mathcal{F}_{-O}$ ,  $f(j, m) = f(j', m')$  for all  $j, j' \in \mathcal{J}_f$  for all  $m, m'$ . Now let's denote the set of “firms”  $\mathcal{F} \equiv \{f(j, m) : j \in \mathcal{J}, m \in \mathcal{M}\}$ .

In our predicted market share equation, we must be sure to include in the terms corresponding to market  $m$  only the firms  $f \in \mathcal{F}$  such that there exists  $j \in \mathcal{J}$  such that  $f(j, m) = f$ . An



Orange product-market  $f$  corresponding to market  $m$  will only show up in the denominator of equation (22) in the  $m$ th term. This also holds for the numerator so that  $\bar{s}_f$  for an Orange  $f$  is an average across markets only in a vacuous sense since there will only be one term.

To be explicit, in this case we will have “firm”-specific market weights:

$$w_f(m) = \begin{cases} w_f(m) & \text{if } \exists j \in \mathcal{J}_{-O} : f(j, m) = f \\ 1 & \text{if } \exists j \in \mathcal{J}_O : f(j, m) = f \\ 0 & \text{otherwise.} \end{cases}$$

We can rewrite equation (22) as

$$\bar{s}_f(\tilde{\delta}; \theta) = \int \sum_m w_f(m) \frac{\exp(\tilde{\delta}_f + \tilde{\mu}_{ifm}(\theta_1))}{\sum_{f' \in \mathcal{F}(f)} \exp(\tilde{\delta}_{f'} + \tilde{\mu}_{if'm}(\theta_1))} dF(\tilde{\mu}(\theta_1); \theta_2), \quad (25)$$

where  $\mathcal{F}(f) \equiv \{f' \in \mathcal{F} : M(f) \cap M(f') \neq \emptyset\}$ , where  $M(f) = \{m \in \mathcal{M} : \exists j \in \mathcal{J} \text{ such that } f(j, m) = f\}$ .<sup>30</sup>

### A.3 Expectation Expressions

As demonstrated in Section 4,

$$x_j^*(Q_{f(j)}; \vartheta_i, \theta_i) = \begin{cases} 0 & \text{if } \vartheta_i \leq \frac{\theta_c}{Q_{f(j)}} \\ \frac{\vartheta_i Q_{f(j)}}{\theta_c} - 1 & \text{if } \frac{\theta_c}{Q_{f(j)}} \leq \vartheta_i < \frac{\theta_c}{Q_{f(j)}} (\bar{x}_j + 1) \\ \bar{x}_j & \text{if } \frac{\theta_c}{Q_{f(j)}} (\bar{x}_j + 1) \leq \vartheta_i < \frac{\theta_c}{Q_L} (\bar{x}_j + 1) \\ \frac{\vartheta_i Q_L}{\theta_c} - 1 & \text{if } \vartheta_i \geq \frac{\theta_c}{Q_L} (\bar{x}_j + 1). \end{cases}$$

We will use this to derive analytic expressions for expected utility from data consumption and predicted average data consumption, integrating over  $\vartheta_i$ , which is distributed

$$\vartheta_i \sim \text{Exponential}(\theta_{di}),$$

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<sup>30</sup>Note that in this setup, we have to make a few adjustments to the contraction mapping proof. First note that  $\frac{\partial f_k(x)}{\partial \delta_j}(\tilde{\delta})$  might be zero not positive, but that is still permissible under the sufficient conditions for the contraction mapping. The partial derivatives will still sum to less than one. Thus, we still satisfy (1). This setup doesn't change the argument for (2). Finally, we must note the following for condition (3). Consider  $\bar{\bar{\delta}}_f$ . In this setup, if  $f$  corresponds to an Orange  $(j, m)$ , then  $\bar{\delta}_f$  shows up in only one of the market-specific terms. The function still maps from  $\mathbb{R}$  to  $(0, 1)$ , so we can still find a  $\bar{\bar{\delta}}_f$ . The rest of the argument holds, so therefore (3) does as well, and we have a contraction mapping even in this setup with product-market-specific demand shocks for Orange and firm-specific demand shocks for all other firms.

meaning that the pdf of  $\vartheta_i$  for an agent of type  $i$  is

$$f_i(\vartheta_i) = \begin{cases} \theta_{di} e^{-\theta_{di}\vartheta_i} & \text{if } \vartheta_i \geq 0 \\ 0 & \text{if } \vartheta_i < 0. \end{cases}$$

### A.3.1 Expected utility from data consumption

We assume that consumers select plans knowing only their  $\theta_{di}$  type; their  $\vartheta_i$  value is realized after choosing a plan.

Their expected value of data consumption  $\mathbb{E}[u_j(x^*(Q; \theta_i), Q)]$  is

$$\begin{aligned} \mathbb{E}[u_j(x^*(Q; \vartheta_i, \theta_i), Q; \vartheta_i, \theta_i)] &= \int_{\theta_c/Q}^{\theta_c(\bar{x}_j+1)/Q} \left( \vartheta_i \log\left(\frac{\vartheta_i Q}{\theta_c}\right) - \vartheta_i + \frac{\theta_c}{Q} \right) dF_i(\vartheta_i) \\ &\quad + \int_{\theta_c(\bar{x}_j+1)/Q}^{\theta_c(\bar{x}_j+1)/Q^L} \left( \vartheta_i \log(1 + \bar{x}_j) - \theta_c \frac{\bar{x}_j}{Q} \right) dF_i(\vartheta_i) \\ &\quad + \int_{\theta_c(\bar{x}_j+1)/Q^L}^{\infty} \left( \vartheta_i \log\left(\frac{\vartheta_i Q^L}{\theta_c}\right) - \theta_c \left[ \frac{\bar{x}_j}{Q} + \frac{\vartheta_i Q^L / \theta_c - 1 - \bar{x}_j}{Q^L} \right] \right) dF_i(\vartheta_i), \end{aligned}$$

where

$$\begin{aligned} &\int_{\theta_c/Q}^{\theta_c(\bar{x}_j+1)/Q} \left( \vartheta_i \log\left(\frac{\vartheta_i Q}{\theta_c}\right) - \vartheta_i + \frac{\theta_c}{Q} \right) dF_i(\vartheta_i) \\ &= \frac{\exp(-\theta_{di}\vartheta_i)}{\theta_{di}Q} \left( -(\theta_{di}Q\vartheta_i + Q) \log\left(\frac{Q\vartheta_i}{\theta_c}\right) - \theta_c\theta_{di} + Q \exp(\theta_{di}\vartheta_i) \text{Ei}(-\theta_{di}\vartheta_i) + \theta_{di}Q\vartheta_i \right) \Big|_{\vartheta_i=\theta_c/Q}^{\theta_c(\bar{x}_j+1)/Q} \\ &= \frac{\exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q)}{\theta_{di}Q} \left( -(\theta_{di}\theta_c(\bar{x}_j+1) + Q) \log(\bar{x}_j+1) + Q \exp\left(\frac{\theta_{di}\theta_c(\bar{x}_j+1)}{Q}\right) \text{Ei}\left(\frac{-\theta_{di}\theta_c(\bar{x}_j+1)}{Q}\right) + \theta_{di}\theta_c\bar{x}_j \right) \\ &\quad - \frac{\exp(-\theta_{di}\theta_c/Q)}{\theta_{di}Q} Q \exp(\theta_{di}\theta_c/Q) \text{Ei}(-\theta_{di}\theta_c/Q) \\ &\int_{\theta_c(\bar{x}_j+1)/Q}^{\theta_c(\bar{x}_j+1)/Q^L} \left( \vartheta_i \log(1 + \bar{x}_j) - \theta_c \frac{\bar{x}_j}{Q} \right) dF_i(\vartheta_i) \\ &= \frac{\exp(-\theta_{di}\vartheta_i)}{\theta_{di}Q} (\theta_c\theta_{di}\bar{x}_j - \log(\bar{x}_j+1)(\theta_{di}Q\vartheta_i + Q)) \Big|_{\vartheta_i=\theta_c(\bar{x}_j+1)/Q}^{\theta_c(\bar{x}_j+1)/Q^L} \\ &= \frac{\exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q^L)}{\theta_{di}Q} \left( \theta_c\theta_{di}\bar{x}_j - \log(\bar{x}_j+1) \left( \frac{\theta_{di}Q\theta_c(\bar{x}_j+1)}{Q^L} + Q \right) \right) \\ &\quad - \frac{\exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q)}{\theta_{di}Q} (\theta_c\theta_{di}\bar{x}_j - \log(\bar{x}_j+1)(\theta_{di}\theta_c(\bar{x}_j+1) + Q)) \\ &\int_{\theta_c(\bar{x}_j+1)/Q^L}^{\infty} \left( \vartheta_i \log\left(\frac{\vartheta_i Q^L}{\theta_c}\right) - \theta_c \left[ \frac{\bar{x}_j}{Q} + \frac{\vartheta_i Q^L / \theta_c - 1 - \bar{x}_j}{Q^L} \right] \right) dF_i(\vartheta_i) \\ &= \frac{\exp(-\theta_{di}\vartheta_i)}{\theta_{di}Q^L} \left( -\theta_c\theta_{di}(-Q^L\bar{x}_j + Q^2 + Q\bar{x}_j) - QQ^L(\theta_{di}\vartheta_i + 1) \log\left(\frac{Q^L\vartheta_i}{\theta_c}\right) \right. \\ &\quad \left. + QQ^L \exp(\theta_{di}\vartheta_i) \text{Ei}(-\theta_{di}\vartheta_i) + \theta_{di}QQ^L\vartheta_i \right) \Big|_{\vartheta_i=\theta_c(\bar{x}_j+1)/Q^L}^{\infty} \\ &= -\frac{\exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q^L)}{\theta_{di}QQ^L} \left( -\theta_c\theta_{di}(-Q^L\bar{x}_j + Q^2 + Q\bar{x}_j) - QQ^L(\theta_{di}\theta_c(\bar{x}_j+1)/Q^L + 1) \log(\bar{x}_j+1) \right. \\ &\quad \left. + QQ^L \exp(\theta_{di}\theta_c(\bar{x}_j+1)/Q^L) \text{Ei}(-\theta_{di}\theta_c(\bar{x}_j+1)/Q^L) + \theta_{di}Q\theta_c(\bar{x}_j+1) \right) \end{aligned}$$

where  $\text{Ei}(\cdot)$  is the exponential integral defined as  $\text{Ei}(x) = -\int_{-x}^{\infty} \frac{\exp(-t)}{t} dt$ .

### A.3.2 Mean data consumption

Mean data consumption is

$$\begin{aligned}\mathbb{E} [x_j^* (Q; \vartheta_i, \theta_i)] &= \int_{\theta_c/Q}^{\theta_c(\bar{x}_j+1)/Q} \left[ \frac{\vartheta_i Q}{\theta_c} - 1 \right] dF_i(\vartheta_i) \\ &\quad + \int_{\theta_c(\bar{x}_j+1)/Q}^{\theta_c(\bar{x}_j+1)/Q^L} \bar{x}_j dF_i(\vartheta_i) \\ &\quad + \int_{\theta_c(\bar{x}_j+1)/Q^L}^{\infty} \left[ \frac{\vartheta_i Q^L}{\theta_c} - 1 \right] dF_i(\vartheta_i),\end{aligned}$$

where

$$\begin{aligned}\int_{\theta_c/Q}^{\theta_c(\bar{x}_j+1)/Q} \left[ \frac{\vartheta_i Q}{\theta_c} - 1 \right] dF_i(\vartheta_i) &= \frac{\exp(-\theta_{di}\vartheta_i)}{\theta_c\theta_{di}} (\theta_c\theta_{di} - Q(\theta_{di}\vartheta_i + 1)) \Big|_{\vartheta_i=\theta_c/Q}^{\theta_c(\bar{x}_j+1)/Q} \\ &= \frac{\exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q)}{\theta_c\theta_{di}} (\theta_c\theta_{di} - Q(\theta_{di}\theta_c(\bar{x}_j+1)/Q + 1)) \\ &\quad - \frac{\exp(-\theta_{di}\theta_c/Q)}{\theta_c\theta_{di}} (\theta_c\theta_{di} - Q(\theta_{di}\theta_c/Q + 1)) \\ \int_{\theta_c(\bar{x}_j+1)/Q}^{\theta_c(\bar{x}_j+1)/Q^L} \bar{x}_j dF_i(\vartheta_i) &= -\bar{x}_j \exp(-\theta_{di}\vartheta_i) \Big|_{\vartheta_i=\theta_c(\bar{x}_j+1)/Q}^{\theta_c(\bar{x}_j+1)/Q^L} \\ &= -\bar{x}_j \exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q^L) \\ &\quad + \bar{x}_j \exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q) \\ \int_{\theta_c(\bar{x}_j+1)/Q^L}^{\infty} \left[ \frac{\vartheta_i Q^L}{\theta_c} - 1 \right] dF_i(\vartheta_i) &= \frac{\exp(-\theta_{di}\vartheta_i)}{\theta_c\theta_{di}} (\theta_c\theta_{di} - Q^L(\theta_{di}\vartheta_i + 1)) \Big|_{\vartheta_i=\theta_c(\bar{x}_j+1)/Q^L}^{\infty} \\ &= -\frac{\exp(-\theta_{di}\theta_c(\bar{x}_j+1)/Q^L)}{\theta_c\theta_{di}} (\theta_c\theta_{di} - Q^L(\theta_{di}\theta_c(\bar{x}_j+1)/Q^L + 1)).\end{aligned}$$

### A.4 Demand Estimation Details

The moments listed in Section 5.1.3 are imposed only for Orange products. The MVNO demand shock  $\xi_{MVNO}$  is normalized to 0, so the moments presented in Section 5.1.3 are not correctly specified if Orange demand shocks differ from the MVNO demand shock. Therefore, we add an Orange dummy variable  $O_j$  defined as follows

$$O_j = \begin{cases} 1 & \text{if } f(j) = \text{Orange} \\ 0 & \text{otherwise,} \end{cases}$$

and  $O_j$  enters utility additively so that Equation 12 becomes

$$v(j, x, m; \theta_i, \vartheta_i, \varepsilon_i) \equiv u_j(x, Q_{m,f(j)}; \vartheta_i, \theta_i) + \theta_v v_j - \theta_{pi} p_j + \theta_O O_j + \xi_{jm} + \varepsilon_{ij}.$$

The inclusion of the term  $\theta_O O_j$  allows Orange products to differ in a systematic way from the products offered by other firms, restoring the validity of moments of the form presented in Section 5.1.3. To identify the parameter  $\theta_O$ , we impose the following additional moment

$$\mathbb{E}[\xi_{jm}(\theta) O_j] = 0,$$

which is equivalent to imposing

$$\mathbb{E}[\xi_{jm}(\theta)] = 0,$$

since the moments are only imposed for Orange products.

In addition to the parameterization in Equation 16, we make an additional transformation to ensure the correct sign of  $\theta_c$ . Let  $\theta^m$  denote the model  $\theta$ , presented in Section 4, and let  $\theta^p$  denote the parameter that we estimate. Equation 26 below provides the mapping between  $\theta^p$  and  $\theta^m$ .

$$\theta_c^m = \exp(\theta_c^p). \quad (26)$$

Incomes are in units of 10,000 €. Data limits are in GB and quality measures are in GBps.<sup>31</sup>

## B Supplementary Results

### B.1 Demand Estimation Results

Demand parameter estimates are listed in table 6 for a range of imputed price elasticities and nesting parameters.

To interpret the results above, the following tables convert the parameter estimates into willingness to pay for certain contract characteristics across income percentiles. Each percentile corresponds to the estimated willingness to pay for an individual with an income that is the average across all markets of that percentile.<sup>32</sup> Table 7 presents willingness to pay for an increase from a 1 000 MB plan to a 4 000 MB plan, with quality equal to the median data speed observed in our data (24.3 Mbps). Table 8 presents willingness to pay for a unlimited voice allowance. Finally, Table 9 presents willingness to pay for an increase in data speeds from 10 Mbps to 20 Mbps on a 10 000 MB plan.

### B.2 Cost Estimation Results

Tables 10 and 11 present per-user and per-tower cost estimates, respectively, for our imputed parameters. Table 10 presents the estimated costs per-user, averaged across products with similar data limits. Table 11 presents estimated costs per-tower for each MNO, averaged across markets.

### B.3 Counterfactual Results

## C Data Appendix

This appendix describes the French telecom industry, the main datasets and variables, and the construction of the statistical inputs. It is organized into five sections. Section C.1 presents the scope of the study as well as some background information about market structure and network sharing in the French mobile industry. Section C.2 presents the characteristics of mobile tariffs and the tariff dataset. Section C.3 describes the Orange customers dataset and socio-economic characteristics.

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<sup>31</sup>Note that quality measures are in *Gigabytes* per second (GBps), not *Gigabits* per second (Gbps). This conversion is needed so that the second term in Equation 14 has the interpretation of seconds spent downloading data.

<sup>32</sup>Specifically, the 10th percentile is 3 759 €, the 30th percentile is 8 705 €, the 50th percentile is 13 015 €, the 70th percentile is 18 101 €, and the 90th percentile is 28 096 €.

Table 6: Demand Parameter Estimates

Elasticity	Nesting Parameter	$\hat{\theta}_{p0}$	$\hat{\theta}_{pz}$	$\hat{\theta}_v$	$\hat{\theta}_O$	$\hat{\theta}_{d0}$	$\hat{\theta}_{dz}$	$\hat{\theta}_c$
-3.2	0.0	-0.301	-0.725	1.807	4.214	-1.348	0.32	-6.724
		(0.487)	(0.215)	(0.065)	(0.688)	(0.097)	(0.068)	(0.128)
	0.2	-0.52	-0.728	1.452	3.714	-1.12	0.319	-6.95
		(0.489)	(0.219)	(0.058)	(0.599)	(0.092)	(0.067)	(0.14)
	0.4	-0.804	-0.731	1.096	3.248	-0.826	0.317	-7.241
		(0.493)	(0.225)	(0.058)	(0.499)	(0.089)	(0.065)	(0.155)
	0.6	-1.204	-0.735	0.737	2.837	-0.412	0.314	-7.649
		(0.516)	(0.242)	(0.066)	(0.385)	(0.09)	(0.062)	(0.173)
	0.8	-1.89	-0.743	0.373	2.505	0.289	0.312	-8.345
		(0.684)	(0.34)	(0.085)	(0.27)	(0.096)	(0.066)	(0.225)
	0.9	-2.406	-0.837	0.197	2.422	1.012	0.32	-9.099
		(1.077)	(0.535)	(0.089)	(0.231)	(0.085)	(0.084)	(0.244)
-2.5	0.0	-0.474	-0.804	1.562	3.447	-0.787	0.324	-7.283
		(0.532)	(0.248)	(0.046)	(0.587)	(0.096)	(0.067)	(0.197)
	0.2	-0.69	-0.809	1.256	3.117	-0.557	0.322	-7.511
		(0.538)	(0.254)	(0.045)	(0.518)	(0.106)	(0.066)	(0.216)
	0.4	-0.969	-0.815	0.949	2.819	-0.26	0.32	-7.804
		(0.548)	(0.264)	(0.05)	(0.437)	(0.122)	(0.063)	(0.236)
	0.6	-1.364	-0.822	0.639	2.566	0.156	0.318	-8.215
		(0.59)	(0.291)	(0.062)	(0.346)	(0.143)	(0.061)	(0.26)
	0.8	-2.045	-0.833	0.323	2.381	0.856	0.317	-8.912
		(0.822)	(0.426)	(0.083)	(0.255)	(0.169)	(0.069)	(0.332)
	0.9	-2.173	-1.142	0.182	2.437	1.738	0.335	-9.868
		(1.203)	(0.566)	(0.068)	(0.269)	(0.09)	(0.068)	(0.165)
-1.8	0.0	-0.649	-0.949	1.324	2.743	0.514	0.326	-8.578
		(0.641)	(0.323)	(0.031)	(0.506)	(0.497)	(0.062)	(0.633)
	0.2	-0.859	-0.958	1.066	2.57	0.76	0.325	-8.821
		(0.653)	(0.333)	(0.034)	(0.454)	(0.56)	(0.061)	(0.692)
	0.4	-1.131	-0.969	0.806	2.425	1.074	0.323	-9.132
		(0.673)	(0.349)	(0.042)	(0.39)	(0.624)	(0.059)	(0.751)
	0.6	-1.519	-0.983	0.542	2.318	1.505	0.322	-9.56
		(0.739)	(0.391)	(0.056)	(0.318)	(0.689)	(0.059)	(0.821)
	0.8	-2.193	-1.0	0.274	2.267	2.217	0.322	-10.271
		(1.057)	(0.58)	(0.078)	(0.243)	(0.816)	(0.07)	(0.996)
	0.9	-1.694	-0.86	0.247	1.583	1.202	0.352	-9.722
		(0.407)	(0.166)	(0.04)	(0.2)	(0.082)	(0.046)	(0.044)

Table 7: Willingness to pay to go from 1 000 MB data plan to 4 000 MB plan

<b>Elasticity</b>	<b>Nesting Parameter</b>	10th %ile	30th %ile	50th %ile	70th %ile	90th %ile
−3.2	0.0	3.79 €	4.37 €	4.85 €	5.42 €	6.48 €
	0.2	3.76 €	4.34 €	4.83 €	5.40 €	6.50 €
	0.4	3.72 €	4.31 €	4.81 €	5.39 €	6.52 €
	0.6	3.67 €	4.27 €	4.78 €	5.38 €	6.56 €
	0.8	3.62 €	4.23 €	4.76 €	5.38 €	6.63 €
	0.9	3.07 €	3.75 €	4.37 €	5.14 €	6.83 €
−2.5	0.0	2.63 €	3.15 €	3.61 €	4.16 €	5.31 €
	0.2	2.60 €	3.12 €	3.58 €	4.15 €	5.33 €
	0.4	2.56 €	3.09 €	3.55 €	4.13 €	5.36 €
	0.6	2.51 €	3.05 €	3.53 €	4.12 €	5.40 €
	0.8	2.47 €	3.02 €	3.51 €	4.12 €	5.47 €
	0.9	1.32 €	1.87 €	2.44 €	3.28 €	5.64 €
−1.8	0.0	0.90 €	1.15 €	1.40 €	1.72 €	2.49 €
	0.2	0.87 €	1.12 €	1.36 €	1.69 €	2.47 €
	0.4	0.83 €	1.09 €	1.33 €	1.66 €	2.46 €
	0.6	0.80 €	1.05 €	1.30 €	1.63 €	2.45 €
	0.8	0.78 €	1.03 €	1.28 €	1.61 €	2.47 €
	0.9	1.40 €	1.74 €	2.05 €	2.44 €	3.36 €

Table 8: Willingness to pay for unlimited voice allowance

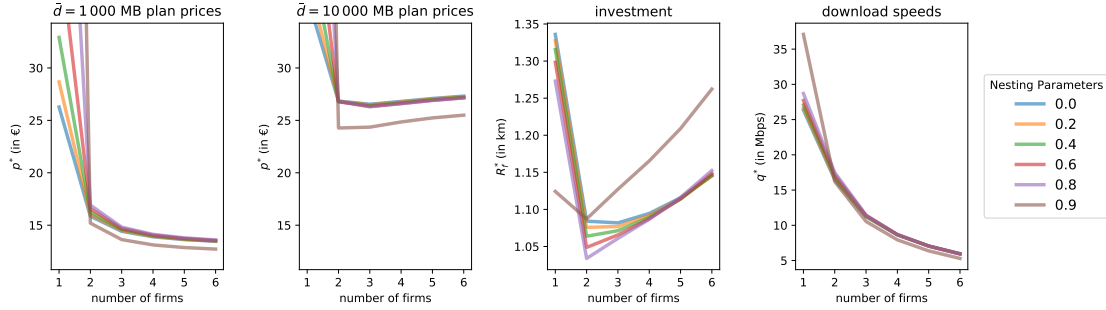
<b>Elasticity</b>	<b>Nesting Parameter</b>	10th %ile	30th %ile	50th %ile	70th %ile	90th %ile
−3.2	0.0	3.14 €	4.56 €	6.13 €	8.58 €	16.61 €
	0.2	3.15 €	4.57 €	6.15 €	8.62 €	16.72 €
	0.4	3.16 €	4.59 €	6.18 €	8.68 €	16.89 €
	0.6	3.17 €	4.62 €	6.24 €	8.78 €	17.16 €
	0.8	3.19 €	4.67 €	6.33 €	8.93 €	17.56 €
	0.9	2.92 €	4.48 €	6.31 €	9.30 €	19.93 €
−2.5	0.0	3.32 €	5.01 €	6.96 €	10.10 €	21.01 €
	0.2	3.32 €	5.02 €	6.98 €	10.16 €	21.23 €
	0.4	3.32 €	5.04 €	7.03 €	10.25 €	21.54 €
	0.6	3.33 €	5.07 €	7.09 €	10.39 €	21.98 €
	0.8	3.34 €	5.12 €	7.19 €	10.58 €	22.59 €
	0.9	2.38 €	4.27 €	6.80 €	11.54 €	32.68 €
−1.8	0.0	3.52 €	5.73 €	8.44 €	13.10 €	31.10 €
	0.2	3.51 €	5.74 €	8.48 €	13.22 €	31.64 €
	0.4	3.50 €	5.75 €	8.54 €	13.38 €	32.36 €
	0.6	3.49 €	5.77 €	8.62 €	13.60 €	33.33 €
	0.8	3.48 €	5.81 €	8.74 €	13.90 €	34.58 €
	0.9	1.82 €	2.82 €	4.01 €	5.97 €	13.08 €

Section C.4 describes the measurement of the quality of mobile data. Finally, section C.5 presents the main statistical inputs of the estimation model: market characteristics, choice set and empirical moments.

Table 9: Willingness to pay for increase from 10 Mbps to 20 Mbps

Elasticity	Nesting		10th %ile	30th %ile	50th %ile	70th %ile	90th %ile
	Parameter						
−3.2	0.0		2.90 €	3.61 €	4.24 €	5.04 €	6.79 €
	0.2		2.88 €	3.59 €	4.23 €	5.03 €	6.80 €
	0.4		2.85 €	3.57 €	4.21 €	5.02 €	6.82 €
	0.6		2.82 €	3.54 €	4.19 €	5.01 €	6.86 €
	0.8		2.79 €	3.51 €	4.17 €	5.01 €	6.93 €
	0.9		2.33 €	3.08 €	3.80 €	4.75 €	7.11 €
−2.5	0.0		2.02 €	2.61 €	3.16 €	3.89 €	5.59 €
	0.2		2.00 €	2.59 €	3.14 €	3.87 €	5.60 €
	0.4		1.97 €	2.56 €	3.12 €	3.86 €	5.63 €
	0.6		1.94 €	2.53 €	3.10 €	3.85 €	5.67 €
	0.8		1.91 €	2.51 €	3.08 €	3.85 €	5.74 €
	0.9		0.98 €	1.51 €	2.10 €	3.02 €	5.86 €
−1.8	0.0		0.69 €	0.96 €	1.23 €	1.61 €	2.63 €
	0.2		0.67 €	0.93 €	1.20 €	1.58 €	2.61 €
	0.4		0.64 €	0.90 €	1.17 €	1.55 €	2.60 €
	0.6		0.62 €	0.88 €	1.14 €	1.53 €	2.59 €
	0.8		0.60 €	0.86 €	1.13 €	1.52 €	2.61 €
	0.9		0.85 €	1.17 €	1.48 €	1.92 €	3.03 €

Figure 17: Counterfactual prices and qualities



## C.1 Industry Background

### C.1.1 Market Description

The French telecommunications market includes both fixed and mobile services. Fixed services cover fixed telephony, internet, and television over the internet, and generate slightly more than half of operators' total revenue. Mobile services include voice, data, and short messages services (SMS) and generated 44 percent of total telecommunications revenues in 2015.<sup>33</sup> We focus on mobile services.

Mobile services are supplied using network technology that improves regularly. Each improvement corresponds to a generation of mobile network technology. In our year of study, 2015, French MNOs had largely already deployed 4G technology, especially in the urban areas we consider.

<sup>33</sup>Source: ARCEP, Series Chronologiques Trimestrielles, April 2016.

Table 10: Per-user cost estimates

<b>Elasticity</b>	<b>Nesting Parameter</b>	$\bar{d} < 1\,000$ (in €)	$1\,000 \leq \bar{d} < 5\,000$ (in €)	$\bar{d} \geq 5\,000$ (in €)
-1.8	0.0	3.74	9.15	18.86
		(1.38)	(0.88)	(3.18)
	0.2	3.76	9.16	18.74
		(1.36)	(0.90)	(3.30)
	0.4	3.79	9.19	18.58
		(1.36)	(0.93)	(3.52)
	0.6	3.84	9.23	18.41
		(1.49)	(1.04)	(4.07)
	0.8	3.91	9.28	18.24
		(2.19)	(1.53)	(6.39)
	0.9	8.04	14.30	23.69
		(0.21)	(0.31)	(2.63)
-2.5	0.0	5.68	10.87	20.25
		(0.73)	(0.64)	(2.16)
	0.2	5.68	10.89	20.18
		(0.71)	(0.64)	(2.17)
	0.4	5.68	10.91	20.10
		(0.69)	(0.66)	(2.25)
	0.6	5.70	10.95	20.00
		(0.72)	(0.73)	(2.55)
	0.8	5.74	11.00	19.92
		(1.03)	(1.05)	(3.99)
	0.9	6.25	11.11	16.81
		(1.26)	(1.23)	(6.10)
-3.2	0.0	6.83	11.48	19.82
		(0.45)	(0.57)	(1.81)
	0.2	6.82	11.50	19.78
		(0.43)	(0.59)	(1.84)
	0.4	6.81	11.52	19.73
		(0.40)	(0.61)	(1.91)
	0.6	6.82	11.55	19.67
		(0.40)	(0.66)	(2.08)
	0.8	6.84	11.61	19.63
		(0.53)	(0.88)	(2.90)
	0.9	6.97	11.78	18.94
		(0.90)	(1.19)	(4.61)



Table 11: Per-base station cost estimates

<b>Elasticity</b>	<b>Nesting Parameter</b>	<b>Orange (in €)</b>	<b>SFR (in €)</b>	<b>Free (in €)</b>	<b>Bouygues (in €)</b>
-1.8	0.0	77 543	61 301	23 993	83 656
		(28 047)	(26 437)	(10 117)	(47 697)
	0.2	76 149	59 485	22 446	82 025
		(27 564)	(25 686)	(9 477)	(46 872)
	0.4	74 606	57 437	20 755	80 205
		(27 030)	(24 828)	(8 779)	(45 918)
	0.6	73 071	55 309	19 028	78 360
		(26 500)	(23 917)	(8 066)	(44 882)
	0.8	71 845	53 403	17 446	76 810
		(26 079)	(23 074)	(7 419)	(43 885)
	0.9	129 602	22 150	4 089	85 316
		(45 611)	(14 784)	(2 770)	(69 618)
-2.5	0.0	195 260	177 211	59 532	216 030
		(64 988)	(81 937)	(24 805)	(132 594)
	0.2	194 649	174 900	56 696	215 021
		(64 823)	(80 909)	(23 598)	(132 211)
	0.4	193 973	172 110	53 471	213 835
		(64 643)	(79 632)	(22 241)	(131 678)
	0.6	193 288	168 902	49 956	212 499
		(64 463)	(78 100)	(20 787)	(130 861)
	0.8	192 672	165 611	46 465	211 072
		(64 293)	(76 406)	(19 384)	(129 456)
	0.9	164 752	105 855	9 808	180 318
		(57 470)	(51 467)	(4 417)	(119 275)
-3.2	0.0	255 321	266 587	76 212	290 865
		(81 656)	(139 613)	(35 475)	(193 442)
	0.2	255 016	264 121	72 794	290 088
		(81 573)	(138 305)	(33 713)	(193 190)
	0.4	254 688	261 026	68 884	289 130
		(81 476)	(136 600)	(31 738)	(192 744)
	0.6	254 376	257 242	64 470	287 959
		(81 368)	(134 412)	(29 575)	(191 858)
	0.8	254 091	253 178	59 964	286 506
		(81 231)	(131 866)	(27 475)	(189 858)
	0.9	248 956	224 140	34 274	278 917
		(80 810)	(116 643)	(14 885)	(188 661)

We estimate base station costs using using monthly profits. To recover the cost of long-lived base stations, we assume the static game is infinitely repeated with a monthly discount rate of 0.5%. The above results are therefore  $\frac{1}{1-0.995} = 200$  times the per-base station costs we recover. Values in parentheses are standard deviations of the distribution of estimated costs across markets (not standard errors in the estimates).

Table 12: Counterfactual Endogenous Variables  $E = -1.8$ 

<b>Nesting Parameter</b>	<b>No. Firms</b>	1 000 MB plan prices (in €)	10 000 MB plan prices (in €)	radius (in km)	download speeds (in Mbps)
0.0	1	33.929 (10.065)	51.563 (9.464)	1.377 (0.029)	33.011 (1.069)
	2	17.618 (0.079)	33.569 (1.361)	1.123 (0.028)	19.451 (0.928)
	3	15.220 (0.816)	31.788 (1.721)	1.109 (0.055)	13.029 (0.991)
	4	14.336 (0.999)	31.353 (1.800)	1.118 (0.069)	9.880 (0.868)
	5	13.876 (1.046)	31.204 (1.854)	1.137 (0.078)	7.984 (0.754)
	6	13.593 (1.058)	31.140 (1.899)	1.164 (0.086)	6.694 (0.667)
0.2	1	38.211 (11.484)	55.597 (11.220)	1.375 (0.029)	33.082 (1.053)
	2	17.564 (0.827)	33.501 (1.410)	1.120 (0.040)	19.514 (1.166)
	3	15.188 (1.231)	31.718 (1.648)	1.107 (0.061)	13.043 (1.056)
	4	14.314 (1.231)	31.291 (1.737)	1.118 (0.071)	9.877 (0.879)
	5	13.858 (1.204)	31.145 (1.811)	1.138 (0.079)	7.973 (0.757)
	6	13.579 (1.181)	31.081 (1.871)	1.166 (0.087)	6.680 (0.670)
0.4	1	45.643 (13.941)	62.757 (13.892)	1.372 (0.028)	33.188 (1.022)
	2	17.591 (1.742)	33.428 (1.594)	1.114 (0.053)	19.634 (1.443)
	3	15.173 (1.590)	31.633 (1.669)	1.106 (0.066)	13.063 (1.113)
	4	14.293 (1.450)	31.217 (1.757)	1.118 (0.074)	9.870 (0.902)
	5	13.839 (1.368)	31.077 (1.842)	1.140 (0.082)	7.957 (0.775)
	6	13.562 (1.317)	31.016 (1.913)	1.169 (0.091)	6.660 (0.689)
0.6	1	61.029 (19.808)	77.867 (19.614)	1.367 (0.028)	33.357 (1.002)
	2	17.710 (2.624)	33.363 (2.110)	1.106 (0.066)	19.813 (1.774)
	3	15.168 (1.984)	31.546 (1.964)	1.104 (0.075)	13.083 (1.251)
	4	14.275 (1.732)	31.144 (2.025)	1.119 (0.084)	9.858 (1.004)
	5	13.821 (1.601)	31.012 (2.108)	1.143 (0.093)	7.935 (0.863)
	6	13.547 (1.523)	30.955 (2.184)	1.174 (0.104)	6.634 (0.771)
0.8	1	108.423 (47.917)	125.033 (46.063)	1.361 (0.030)	33.634 (1.036)
	2	17.848 (4.268)	33.325 (4.179)	1.097 (0.102)	20.011 (2.765)
	3	15.168 (2.993)	31.487 (3.535)	1.103 (0.117)	13.100 (1.915)
	4	14.263 (2.549)	31.099 (3.476)	1.121 (0.131)	9.840 (1.540)
	5	13.809 (2.325)	30.976 (3.516)	1.146 (0.148)	7.906 (1.329)
	6	13.537 (2.191)	30.925 (3.574)	1.179 (0.168)	6.600 (1.191)
0.9	1	50.383 (2.284)	63.368 (0.625)	1.779 (0.037)	15.395 (0.684)
	2	14.794 (0.506)	27.737 (2.719)	1.317 (0.055)	12.413 (0.865)
	3	14.079 (0.373)	27.633 (2.558)	1.269 (0.068)	8.888 (0.685)
	4	13.840 (0.328)	27.799 (2.504)	1.246 (0.078)	7.063 (0.585)
	5	13.723 (0.305)	27.963 (2.481)	1.237 (0.088)	5.900 (0.522)
	6	13.655 (0.291)	28.097 (2.472)	1.239 (0.100)	5.076 (0.479)

Table 13: Counterfactual Endogenous Variables  $E = -2.5$ 

<b>Nesting Parameter</b>	<b>No. Firms</b>	1 000 MB plan prices (in €)	10 000 MB plan prices (in €)	radius (in km)	download speeds (in Mbps)
0.0	1	26.421 (12 492.885)	37.291 (2 434.253)	1.428 (10.396)	29.049 (515.460)
	2	16.007 (0.640)	27.332 (1.871)	1.151 (0.046)	17.960 (1.392)
	3	14.559 (0.843)	27.035 (1.649)	1.142 (0.069)	12.183 (1.166)
	4	14.034 (0.813)	27.333 (1.522)	1.150 (0.077)	9.373 (0.919)
	5	13.769 (0.771)	27.651 (1.473)	1.166 (0.081)	7.669 (0.753)
	6	13.609 (0.737)	27.910 (1.461)	1.189 (0.084)	6.497 (0.639)
0.2	1	28.817 (6 280.023)	39.326 (28.223)	1.419 (2.005)	29.376 (121.011)
	2	16.159 (1.061)	27.301 (1.900)	1.143 (0.053)	18.127 (1.537)
	3	14.635 (0.984)	26.971 (1.602)	1.137 (0.069)	12.242 (1.152)
	4	14.080 (0.874)	27.272 (1.469)	1.147 (0.073)	9.396 (0.882)
	5	13.800 (0.806)	27.594 (1.421)	1.164 (0.076)	7.677 (0.719)
	6	13.631 (0.760)	27.857 (1.410)	1.189 (0.080)	6.497 (0.610)
0.4	1	33.067	43.088	1.406	29.844
	2	16.402 (1.461)	27.275 (2.024)	1.131 (0.058)	18.373 (1.654)
	3	14.733 (1.104)	26.891 (1.622)	1.131 (0.067)	12.313 (1.125)
	4	14.136 (0.936)	27.196 (1.472)	1.144 (0.070)	9.419 (0.849)
	5	13.837 (0.849)	27.526 (1.418)	1.164 (0.073)	7.681 (0.693)
	6	13.659 (0.796)	27.794 (1.405)	1.189 (0.077)	6.493 (0.593)
0.6	1				
	2	16.729 (1.877)	27.268 (2.419)	1.115 (0.064)	18.696 (1.827)
	3	14.847 (1.264)	26.810 (1.851)	1.125 (0.070)	12.386 (1.169)
	4	14.200 (1.044)	27.121 (1.657)	1.142 (0.074)	9.436 (0.883)
	5	13.882 (0.938)	27.459 (1.585)	1.164 (0.078)	7.678 (0.728)
	6	13.693 (0.877)	27.734 (1.562)	1.191 (0.084)	6.481 (0.629)
0.8	1	70.039 (9.825)	78.507 (7.669)	1.362 (0.055)	31.618 (2.912)
	2	17.065 (2.839)	27.307 (4.078)	1.100 (0.093)	19.027 (2.689)
	3	14.962 (1.809)	26.774 (3.053)	1.120 (0.103)	12.447 (1.703)
	4	14.271 (1.469)	27.094 (2.695)	1.141 (0.112)	9.444 (1.302)
	5	13.935 (1.307)	27.442 (2.543)	1.165 (0.122)	7.668 (1.088)
	6	13.737 (1.214)	27.723 (2.479)	1.195 (0.133)	6.462 (0.951)
0.9	1	166.716 (79.217)	156.439 (55.882)	1.194 (0.096)	41.410 (4.869)
	2	15.298 (3.512)	24.505 (7.654)	1.151 (0.116)	17.753 (3.345)
	3	13.726 (2.395)	24.588 (6.248)	1.185 (0.155)	11.520 (2.361)
	4	13.215 (2.020)	25.132 (5.672)	1.218 (0.189)	8.667 (1.924)
	5	12.966 (1.834)	25.571 (5.389)	1.256 (0.225)	6.975 (1.678)
	6	12.818 (1.725)	25.885 (5.256)	1.300 (0.266)	5.825 (1.516)

Table 14: Counterfactual Endogenous Variables  $E = -3.2$ 

<b>Nesting Parameter</b>	<b>No. Firms</b>	1 000 MB plan prices (in €)	10 000 MB plan prices (in €)	radius (in km)	download speeds (in Mbps)
0.0	1	32.293 (297.436)	29.481 (25.469)	1.334 (2.880)	31.678 (156.901)
	2	15.229 (0.691)	23.957 (1.820)	1.161 (0.057)	16.992 (1.553)
	3	14.041 (0.832)	23.886 (1.374)	1.159 (0.084)	11.579 (1.337)
	4	13.640 (0.705)	24.295 (1.203)	1.168 (0.088)	8.989 (0.992)
	5	13.451 (0.629)	24.708 (1.134)	1.184 (0.089)	7.416 (0.787)
	6	13.343 (0.577)	25.049 (1.114)	1.205 (0.090)	6.326 (0.654)
0.2	1				
	2	15.437 (6 106.845)	23.964 (5.722)	1.149 (8.395)	17.214 (274.929)
	3	14.136 (0.867)	23.847 (1.283)	1.152 (0.081)	11.657 (1.287)
	4	13.700 (0.695)	24.253 (1.110)	1.164 (0.081)	9.025 (0.929)
	5	13.494 (0.606)	24.668 (1.042)	1.181 (0.081)	7.434 (0.730)
	6	13.376 (0.551)	25.013 (1.021)	1.204 (0.081)	6.334 (0.604)
0.4	1				
	2	26.634 (49.932)	23.674 (1.139)	0.913 (0.919)	24.120 (29.617)
	3	14.264 (0.890)	23.796 (1.227)	1.144 (0.075)	11.753 (1.213)
	4	13.777 (0.681)	24.198 (1.046)	1.159 (0.074)	9.065 (0.857)
	5	13.549 (0.585)	24.617 (0.974)	1.178 (0.073)	7.451 (0.671)
	6	13.419 (0.530)	24.966 (0.949)	1.202 (0.074)	6.340 (0.558)
0.6	1				
	2	22.564 (149.045)	23.800 (5.144)	0.946 (1.407)	22.548 (63.453)
	3	14.422 (0.936)	23.742 (1.307)	1.134 (0.073)	11.860 (1.183)
	4	13.873 (0.691)	24.139 (1.102)	1.154 (0.071)	9.102 (0.829)
	5	13.619 (0.587)	24.563 (1.016)	1.176 (0.072)	7.462 (0.655)
	6	13.475 (0.531)	24.916 (0.983)	1.202 (0.073)	6.339 (0.550)
0.8	1	88.841 (5.311)	56.698 (0.890)	1.055 (0.077)	51.626 (7.427)
	2	39.537 (406.829)	25.396 (32.271)	0.776 (4.029)	30.603 (192.186)
	3	14.597 (1.221)	23.737 (2.046)	1.126 (0.099)	11.955 (1.580)
	4	13.985 (0.878)	24.132 (1.719)	1.151 (0.100)	9.127 (1.125)
	5	13.706 (0.736)	24.562 (1.571)	1.176 (0.104)	7.464 (0.908)
	6	13.548 (0.660)	24.920 (1.505)	1.204 (0.110)	6.329 (0.778)
0.9	1	131.393 (6.858)	97.348 (5.149)	1.053 (0.134)	51.914 (12.173)
	2	39.931 (457.251)	24.765 (40.391)	0.769 (4.484)	30.702 (215.979)
	3	14.364 (1.802)	23.217 (4.120)	1.147 (0.161)	11.658 (2.463)
	4	13.808 (1.369)	23.700 (3.583)	1.175 (0.177)	8.889 (1.852)
	5	13.552 (1.178)	24.175 (3.318)	1.203 (0.193)	7.256 (1.543)
	6	13.406 (1.073)	24.555 (3.191)	1.235 (0.212)	6.140 (1.352)

Table 15: Price Elasticities  $E = -1.8$ 

<b>Nesting Parameter</b>	<b>No. Firms</b>	1 000 MB plan partial elasticity	1 000 MB plan full elasticity	10 000 MB plan partial elasticity	10 000 MB plan full elasticity
0.0	1	-1.316 (0.030)	-1.317 (0.029)	-0.902 (0.097)	-0.890 (0.086)
	2	-1.681 (0.171)	-1.681 (0.171)	-1.665 (0.256)	-1.611 (0.226)
	3	-1.865 (0.285)	-1.864 (0.285)	-1.982 (0.334)	-1.892 (0.289)
	4	-1.966 (0.350)	-1.964 (0.350)	-2.145 (0.370)	-2.033 (0.315)
	5	-2.030 (0.392)	-2.027 (0.392)	-2.242 (0.389)	-2.117 (0.328)
	6	-2.075 (0.421)	-2.070 (0.421)	-2.307 (0.401)	-2.176 (0.336)
0.2	1	-1.294 (0.031)	-1.295 (0.030)	-0.865 (0.106)	-0.854 (0.095)
	2	-1.697 (0.210)	-1.697 (0.210)	-1.646 (0.309)	-1.592 (0.278)
	3	-1.881 (0.320)	-1.880 (0.320)	-1.967 (0.374)	-1.879 (0.326)
	4	-1.980 (0.377)	-1.978 (0.377)	-2.129 (0.400)	-2.020 (0.341)
	5	-2.043 (0.414)	-2.039 (0.414)	-2.226 (0.415)	-2.104 (0.349)
	6	-2.086 (0.439)	-2.082 (0.439)	-2.290 (0.424)	-2.163 (0.354)
0.4	1	-1.267 (0.032)	-1.268 (0.031)	-0.815 (0.106)	-0.805 (0.096)
	2	-1.712 (0.255)	-1.712 (0.255)	-1.627 (0.369)	-1.573 (0.337)
	3	-1.899 (0.355)	-1.897 (0.355)	-1.950 (0.415)	-1.863 (0.364)
	4	-1.998 (0.408)	-1.995 (0.408)	-2.110 (0.436)	-2.003 (0.373)
	5	-2.059 (0.441)	-2.056 (0.441)	-2.205 (0.449)	-2.087 (0.377)
	6	-2.101 (0.465)	-2.097 (0.465)	-2.268 (0.457)	-2.146 (0.381)
0.6	1	-1.233 (0.038)	-1.234 (0.036)	-0.746 (0.095)	-0.737 (0.084)
	2	-1.725 (0.309)	-1.725 (0.309)	-1.608 (0.440)	-1.554 (0.406)
	3	-1.920 (0.413)	-1.918 (0.414)	-1.929 (0.482)	-1.843 (0.427)
	4	-2.020 (0.469)	-2.017 (0.469)	-2.087 (0.504)	-1.982 (0.433)
	5	-2.081 (0.503)	-2.077 (0.503)	-2.181 (0.516)	-2.066 (0.437)
	6	-2.122 (0.527)	-2.118 (0.527)	-2.243 (0.525)	-2.123 (0.440)
0.8	1	-1.191 (0.063)	-1.193 (0.061)	-0.656 (0.052)	-0.648 (0.041)
	2	-1.739 (0.472)	-1.739 (0.472)	-1.585 (0.652)	-1.532 (0.611)
	3	-1.943 (0.625)	-1.942 (0.625)	-1.905 (0.723)	-1.819 (0.655)
	4	-2.045 (0.703)	-2.043 (0.702)	-2.061 (0.759)	-1.957 (0.672)
	5	-2.107 (0.750)	-2.103 (0.749)	-2.153 (0.781)	-2.039 (0.682)
	6	-2.148 (0.782)	-2.144 (0.781)	-2.215 (0.795)	-2.097 (0.689)
0.9	1	-1.291 (0.025)	-1.296 (0.025)	-0.515 (0.057)	-0.392 (0.040)
	2	-4.894 (0.826)	-4.884 (0.822)	-3.387 (0.383)	-1.860 (0.442)
	3	-6.135 (1.089)	-6.111 (1.078)	-4.307 (0.486)	-1.494 (1.131)
	4	-6.758 (1.221)	-6.718 (1.203)	-4.763 (0.537)	-1.035 (1.721)
	5	-7.134 (1.300)	-7.076 (1.275)	-5.038 (0.567)	-0.712 (2.165)
	6	-7.386 (1.354)	-7.310 (1.322)	-5.221 (0.586)	-0.540 (2.479)

Table 16: Price Elasticities  $E = -2.5$ 

Nesting Parameter	No. Firms	1 000 MB plan partial elasticity	1 000 MB plan full elasticity	10 000 MB plan partial elasticity	10 000 MB plan full elasticity
0.0	1	-1.410 (905.497)	-1.415 (2 186 865.136)	-1.153 (9.200)	-1.107 (187 632.489)
	2	-2.180 (0.305)	-2.178 (0.304)	-2.358 (0.235)	-2.116 (0.238)
	3	-2.486 (0.421)	-2.480 (0.419)	-2.782 (0.327)	-2.346 (0.361)
	4	-2.652 (0.477)	-2.641 (0.473)	-2.978 (0.370)	-2.398 (0.414)
	5	-2.757 (0.515)	-2.742 (0.508)	-3.091 (0.394)	-2.413 (0.435)
	6	-2.830 (0.543)	-2.811 (0.534)	-3.163 (0.409)	-2.429 (0.441)
0.2	1	-1.384 (1 124.262)	-1.391 (2 339 711.740)	-1.132 (1.515)	-1.087 (1.718)
	2	-2.196 (0.340)	-2.194 (0.339)	-2.364 (0.286)	-2.121 (0.297)
	3	-2.504 (0.443)	-2.497 (0.440)	-2.782 (0.357)	-2.351 (0.392)
	4	-2.668 (0.499)	-2.657 (0.494)	-2.973 (0.393)	-2.402 (0.430)
	5	-2.771 (0.536)	-2.756 (0.529)	-3.082 (0.415)	-2.417 (0.444)
	6	-2.842 (0.563)	-2.823 (0.554)	-3.153 (0.429)	-2.432 (0.446)
0.4	1	-1.349	-1.358	-1.096	-1.055
	2	-2.217 (0.367)	-2.214 (0.366)	-2.374 (0.333)	-2.132 (0.348)
	3	-2.528 (0.469)	-2.521 (0.467)	-2.781 (0.391)	-2.357 (0.420)
	4	-2.690 (0.527)	-2.679 (0.522)	-2.965 (0.424)	-2.404 (0.448)
	5	-2.791 (0.564)	-2.776 (0.556)	-3.070 (0.445)	-2.418 (0.456)
	6	-2.860 (0.590)	-2.841 (0.580)	-3.138 (0.459)	-2.433 (0.454)
0.6	1				
	2	-2.245 (0.409)	-2.242 (0.408)	-2.387 (0.388)	-2.146 (0.405)
	3	-2.559 (0.526)	-2.552 (0.523)	-2.778 (0.452)	-2.358 (0.470)
	4	-2.720 (0.588)	-2.708 (0.582)	-2.954 (0.490)	-2.400 (0.492)
	5	-2.818 (0.626)	-2.803 (0.618)	-3.054 (0.513)	-2.413 (0.494)
	6	-2.886 (0.652)	-2.866 (0.641)	-3.119 (0.528)	-2.428 (0.489)
0.8	1	-1.234 (0.168)	-1.249 (0.167)	-0.963 (0.111)	-0.932 (0.099)
	2	-2.279 (0.591)	-2.275 (0.589)	-2.397 (0.558)	-2.155 (0.588)
	3	-2.597 (0.759)	-2.589 (0.754)	-2.771 (0.684)	-2.350 (0.696)
	4	-2.757 (0.843)	-2.745 (0.834)	-2.938 (0.753)	-2.384 (0.726)
	5	-2.854 (0.893)	-2.838 (0.880)	-3.034 (0.794)	-2.394 (0.725)
	6	-2.921 (0.926)	-2.900 (0.909)	-3.097 (0.820)	-2.407 (0.713)
0.9	1	-0.449 (0.342)	-0.438 (0.346)	-1.140 (0.098)	-1.140 (0.100)
	2	-2.734 (1.351)	-2.729 (1.345)	-1.964 (0.417)	-1.753 (0.433)
	3	-3.182 (1.699)	-3.171 (1.686)	-2.261 (0.567)	-1.914 (0.563)
	4	-3.405 (1.871)	-3.387 (1.849)	-2.390 (0.648)	-1.954 (0.616)
	5	-3.540 (1.976)	-3.515 (1.944)	-2.464 (0.695)	-1.980 (0.632)
	6	-3.631 (2.047)	-3.599 (2.006)	-2.513 (0.722)	-2.009 (0.631)

Table 17: Price Elasticities  $E = -3.2$ 

<b>Nesting Parameter</b>	<b>No. Firms</b>	1 000 MB plan partial elasticity	1 000 MB plan full elasticity	10 000 MB plan partial elasticity	10 000 MB plan full elasticity
0.0	1	-0.556 (12.754)	-0.464 (16.212)	-1.599 (2.818)	-1.555 (2.541)
	2	-2.681 (0.493)	-2.675 (0.490)	-3.153 (0.180)	-2.681 (0.260)
	3	-3.102 (0.585)	-3.088 (0.579)	-3.615 (0.297)	-2.728 (0.555)
	4	-3.328 (0.636)	-3.306 (0.625)	-3.802 (0.353)	-2.554 (0.698)
	5	-3.471 (0.672)	-3.440 (0.656)	-3.902 (0.386)	-2.379 (0.755)
	6	-3.569 (0.700)	-3.531 (0.678)	-3.964 (0.406)	-2.260 (0.762)
0.2	1				
	2	-2.696 (279.773)	-2.690 (594 635.234)	-3.178 (17.840)	-2.711 (25.525)
	3	-3.119 (0.588)	-3.104 (0.583)	-3.627 (0.318)	-2.758 (0.576)
	4	-3.343 (0.648)	-3.320 (0.636)	-3.806 (0.367)	-2.583 (0.698)
	5	-3.483 (0.688)	-3.452 (0.671)	-3.900 (0.397)	-2.408 (0.745)
	6	-3.580 (0.717)	-3.541 (0.695)	-3.959 (0.416)	-2.288 (0.749)
0.4	1				
	2	-2.693 (0.288)	-2.536 (0.964)	-3.883 (2.179)	-3.632 (3.149)
	3	-3.145 (0.602)	-3.130 (0.596)	-3.642 (0.341)	-2.793 (0.588)
	4	-3.365 (0.669)	-3.342 (0.657)	-3.808 (0.388)	-2.615 (0.692)
	5	-3.502 (0.711)	-3.471 (0.694)	-3.896 (0.419)	-2.440 (0.731)
	6	-3.596 (0.740)	-3.557 (0.717)	-3.952 (0.438)	-2.321 (0.731)
0.6	1				
	2	-2.929 (3.095)	-2.855 (5.808)	-3.930 (0.484)	-3.628 (1.365)
	3	-3.184 (0.648)	-3.168 (0.641)	-3.659 (0.384)	-2.830 (0.614)
	4	-3.397 (0.720)	-3.374 (0.707)	-3.809 (0.439)	-2.644 (0.703)
	5	-3.530 (0.763)	-3.499 (0.745)	-3.889 (0.474)	-2.467 (0.729)
	6	-3.622 (0.792)	-3.582 (0.769)	-3.940 (0.496)	-2.349 (0.721)
0.8	1	-0.226 (0.149)	-0.040 (0.086)	-1.121 (0.054)	-1.115 (0.053)
	2	-2.723 (7.753)	-2.370 (14.467)	-4.036 (1.858)	-3.829 (4.994)
	3	-3.234 (0.881)	-3.217 (0.870)	-3.674 (0.572)	-2.852 (0.826)
	4	-3.442 (0.973)	-3.417 (0.955)	-3.806 (0.673)	-2.650 (0.911)
	5	-3.572 (1.027)	-3.539 (1.001)	-3.878 (0.731)	-2.468 (0.910)
	6	-3.661 (1.062)	-3.621 (1.029)	-3.924 (0.768)	-2.347 (0.870)
0.9	1	-0.193 (0.148)	-0.087 (0.017)	-1.065 (0.005)	-1.063 (0.004)
	2	-2.525 (17.582)	-2.218 (23.489)	-4.253 (2.745)	-4.017 (6.838)
	3	-3.488 (1.603)	-3.468 (1.580)	-3.499 (0.861)	-2.648 (1.098)
	4	-3.717 (1.750)	-3.687 (1.712)	-3.601 (1.023)	-2.438 (1.173)
	5	-3.860 (1.838)	-3.820 (1.786)	-3.656 (1.113)	-2.268 (1.137)
	6	-3.958 (1.898)	-3.908 (1.831)	-3.692 (1.166)	-2.167 (1.059)

Table 18: Bandwidth Derivatives  $E = -1.8$  (bandwidth cost specification)

<b>Nesting</b>	<b>No.</b>	$\frac{\partial \Pi_f}{\partial b_f}$	$\frac{\partial \Pi_f}{\partial b}$	$\frac{\partial CS}{\partial b}$
<b>Parameter</b>	<b>Firms</b>	(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)
0.0	1	0.029 (0.023)	0.029 (0.023)	0.041 (0.006)
	2	0.048 (0.044)	-0.044 (0.018)	0.190 (0.067)
	3	0.064 (0.059)	-0.048 (0.025)	0.291 (0.116)
	4	0.069 (0.055)	-0.047 (0.028)	0.400 (0.188)
	5	0.068 (0.063)	-0.048 (0.031)	0.516 (0.270)
	6	0.066 (0.062)	-0.049 (0.033)	0.633 (0.357)
0.2	1	0.028 (0.023)	0.028 (0.023)	0.044 (0.010)
	2	0.046 (0.047)	-0.044 (0.022)	0.192 (0.075)
	3	0.063 (0.061)	-0.046 (0.030)	0.289 (0.139)
	4	0.067 (0.058)	-0.046 (0.032)	0.398 (0.218)
	5	0.067 (0.065)	-0.046 (0.034)	0.513 (0.305)
	6	0.065 (0.063)	-0.047 (0.036)	0.627 (0.398)
0.4	1	0.027 (0.024)	0.027 (0.024)	0.048 (0.013)
	2	0.045 (0.049)	-0.043 (0.029)	0.194 (0.091)
	3	0.061 (0.063)	-0.045 (0.035)	0.291 (0.161)
	4	0.065 (0.012)	-0.044 (0.035)	0.398 (0.244)
	5	0.065 (0.066)	-0.044 (0.036)	0.512 (0.337)
	6	0.063 (0.064)	-0.046 (0.038)	0.624 (0.436)
0.6	1	0.027 (0.024)	0.027 (0.024)	0.051 (0.014)
	2	0.044 (0.053)	-0.044 (0.037)	0.199 (0.104)
	3	0.060 (0.067)	-0.044 (0.038)	0.297 (0.176)
	4	0.063 (0.071)	-0.042 (0.038)	0.404 (0.266)
	5	0.063 (0.069)	-0.043 (0.038)	0.516 (0.367)
	6	0.060 (0.067)	-0.044 (0.040)	0.627 (0.474)
0.8	1	0.026 (0.027)	0.026 (0.027)	0.055 (0.005)
	2	0.044 (0.063)	-0.046 (0.045)	0.207 (0.095)
	3	0.059 (0.082)	-0.043 (0.044)	0.308 (0.182)
	4	0.062 (0.088)	-0.041 (0.043)	0.416 (0.293)
	5	0.061 (0.084)	-0.041 (0.044)	0.529 (0.419)
	6	0.058 (0.082)	-0.042 (0.046)	0.639 (0.555)
0.9	1	0.007 (0.001)	0.007 (0.001)	0.018 (0.004)
	2	0.022 (0.004)	-0.014 (0.001)	0.097 (0.009)
	3	0.035 (0.007)	-0.014 (0.001)	0.174 (0.021)
	4	0.042 (0.009)	-0.017 (0.001)	0.268 (0.035)
	5	0.046 (0.010)	-0.020 (0.002)	0.375 (0.054)
	6	0.048 (0.012)	-0.023 (0.002)	0.489 (0.076)



Table 19: Bandwidth Derivatives  $E = -2.5$  (bandwidth cost specification)

<b>Nesting</b>	<b>No.</b>	$\frac{\partial \Pi_f}{\partial b_f}$	$\frac{\partial \Pi_f}{\partial b}$	$\frac{\partial CS}{\partial b}$
<b>Parameter</b>	<b>Firms</b>	(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)
0.0	1	0.073 (0.621)	0.073 (0.621)	0.140 (2.267)
	2	0.127 (0.067)	-0.145 (0.028)	0.430 (0.029)
	3	0.167 (0.082)	-0.121 (0.031)	0.582 (0.031)
	4	0.175 (0.082)	-0.108 (0.030)	0.811 (0.103)
	5	0.176 (0.062)	-0.107 (0.031)	1.079 (0.188)
	6	0.171 (0.087)	-0.110 (0.033)	1.361 (0.280)
0.2	1	0.073 (3.906)	0.073 (3.906)	0.153 (13.774)
	2	0.127 (0.072)	-0.145 (0.039)	0.440 (0.023)
	3	0.166 (0.083)	-0.119 (0.040)	0.590 (0.055)
	4	0.174 (0.083)	-0.107 (0.036)	0.819 (0.133)
	5	0.174 (0.048)	-0.105 (0.035)	1.086 (0.223)
	6	0.169 (0.082)	-0.108 (0.036)	1.367 (0.320)
0.4	1	0.074	0.074	0.167
	2	0.127 (0.075)	-0.147 (0.052)	0.458 (0.031)
	3	0.165 (0.084)	-0.118 (0.046)	0.606 (0.076)
	4	0.172 (0.082)	-0.105 (0.039)	0.833 (0.157)
	5	0.173 (0.077)	-0.103 (0.038)	1.100 (0.253)
	6	0.165 (0.091)	-0.106 (0.039)	1.380 (0.356)
0.6	1	0.258 (8.583)	0.258 (8.583)	0.693 (23.645)
	2	0.127 (0.076)	-0.150 (0.062)	0.483 (0.034)
	3	0.164 (0.088)	-0.117 (0.050)	0.629 (0.083)
	4	0.170 (0.092)	-0.103 (0.042)	0.856 (0.173)
	5	0.169 (0.126)	-0.101 (0.040)	1.124 (0.277)
	6	0.163 (0.081)	-0.103 (0.042)	1.403 (0.392)
0.8	1	0.075 (0.045)	0.075 (0.045)	0.193 (0.030)
	2	0.127 (0.098)	-0.155 (0.071)	0.512 (0.066)
	3	0.162 (0.110)	-0.116 (0.057)	0.658 (0.054)
	4	0.167 (0.104)	-0.101 (0.049)	0.887 (0.175)
	5	0.166 (0.188)	-0.098 (0.048)	1.156 (0.316)
	6	0.161 (0.098)	-0.101 (0.050)	1.437 (0.472)
0.9	1			
	2	0.078 (0.049)	-0.113 (0.020)	0.540 (0.167)
	3	0.102 (0.066)	-0.083 (0.024)	0.637 (0.053)
	4	0.105 (0.067)	-0.073 (0.025)	0.795 (0.081)
	5	0.104 (0.168)	-0.070 (0.027)	0.979 (0.196)
	6	0.099 (0.065)	-0.071 (0.031)	1.162 (0.334)

Table 20: Bandwidth Derivatives  $E = -3.2$  (bandwidth cost specification)

<b>Nesting</b>	<b>No.</b>	$\frac{\partial \Pi_f}{\partial b_f}$	$\frac{\partial \Pi_f}{\partial b}$	$\frac{\partial CS}{\partial b}$
<b>Parameter</b>	<b>Firms</b>	(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)
0.0	1			
	2	0.191 (0.084)	-0.323 (0.081)	0.737 (0.361)
	3	0.244 (0.115)	-0.191 (0.064)	0.691 (0.040)
	4	0.244 (0.110)	-0.147 (0.045)	0.949 (0.085)
	5	0.242 (0.097)	-0.137 (0.039)	1.285 (0.180)
	6	0.239 (0.094)	-0.139 (0.038)	1.649 (0.279)
0.2	1	< 0.001 (0.649)	< 0.001 (0.649)	< 0.001 (9.830)
	2	0.194 (0.111)	-0.323 (0.113)	0.757 (0.131)
	3	0.243 (0.116)	-0.190 (0.074)	0.706 (0.038)
	4	0.242 (0.104)	-0.145 (0.050)	0.963 (0.116)
	5	0.241 (0.095)	-0.136 (0.043)	1.298 (0.214)
	6	0.237 (0.091)	-0.137 (0.041)	1.662 (0.316)
0.4	1	< 0.001 (< 0.001)	< 0.001 (< 0.001)	< 0.001 (< 0.001)
	2			
	3	0.242 (0.117)	-0.189 (0.080)	0.732 (0.061)
	4	0.240 (0.105)	-0.144 (0.053)	0.986 (0.144)
	5	0.238 (0.094)	-0.134 (0.045)	1.321 (0.245)
	6	0.235 (0.087)	-0.135 (0.044)	1.684 (0.352)
0.6	1	< 0.001 (< 0.001)	< 0.001 (< 0.001)	< 0.001 (< 0.001)
	2			
	3	0.240 (0.121)	-0.187 (0.085)	0.769 (0.079)
	4	0.237 (0.104)	-0.142 (0.056)	1.019 (0.165)
	5	0.235 (0.094)	-0.132 (0.047)	1.353 (0.272)
	6	0.231 (0.093)	-0.133 (0.046)	1.717 (0.387)
0.8	1	0.389	0.389	0.912
	2			
	3	0.236 (0.164)	-0.184 (0.094)	0.813 (0.062)
	4	0.233 (0.122)	-0.138 (0.063)	1.060 (0.176)
	5	0.230 (0.114)	-0.128 (0.054)	1.395 (0.319)
	6	0.225 (0.115)	-0.129 (0.053)	1.760 (0.474)
0.9	1			
	2			
	3	0.204 (0.140)	-0.161 (0.083)	0.835 (0.089)
	4	0.203 (0.136)	-0.122 (0.062)	1.049 (0.157)
	5	0.201 (0.133)	-0.114 (0.057)	1.350 (0.345)
	6	0.197 (0.133)	-0.116 (0.058)	1.678 (0.553)

Table 21: Bandwidth Derivatives  $E = -1.8$  (fixed cost specification)

<b>Nesting Parameter</b>	<b>No. Firms</b>	$\frac{\partial \Pi_f}{\partial b_f}$ (in 0.01 € / person / MHz)	$\frac{\partial \Pi_f}{\partial b}$ (in 0.01 € / person / MHz)	$\frac{\partial CS}{\partial b}$ (in 0.01 € / person / MHz)
0.0	1	0.111 (0.081)	0.111 (0.081)	0.091 (0.009)
	2	0.163 (0.134)	-0.030 (0.014)	0.402 (0.123)
	3	0.201 (0.159)	-0.046 (0.005)	0.638 (0.213)
	4	0.208 (0.174)	-0.050 (0.011)	0.891 (0.355)
	5	0.206 (0.174)	-0.056 (0.018)	1.161 (0.518)
	6	0.199 (0.166)	-0.063 (0.026)	1.435 (0.692)
0.2	1	0.109 (0.085)	0.109 (0.085)	0.098 (0.016)
	2	0.158 (0.143)	-0.030 (0.011)	0.405 (0.137)
	3	0.196 (0.173)	-0.043 (0.011)	0.635 (0.264)
	4	0.203 (0.177)	-0.048 (0.018)	0.887 (0.422)
	5	0.201 (0.175)	-0.053 (0.024)	1.154 (0.599)
	6	0.194 (0.171)	-0.061 (0.032)	1.425 (0.787)
0.4	1	0.106 (0.087)	0.106 (0.087)	0.105 (0.024)
	2	0.155 (0.148)	-0.031 (0.005)	0.408 (0.167)
	3	0.191 (0.179)	-0.042 (0.019)	0.640 (0.310)
	4	0.198 (0.184)	-0.046 (0.023)	0.890 (0.479)
	5	0.196 (0.181)	-0.051 (0.029)	1.156 (0.669)
	6	0.188 (0.176)	-0.059 (0.036)	1.423 (0.871)
0.6	1	0.104 (0.090)	0.104 (0.090)	0.113 (0.026)
	2	0.151 (0.156)	-0.034 (0.015)	0.418 (0.189)
	3	0.186 (0.189)	-0.041 (0.023)	0.653 (0.339)
	4	0.193 (0.193)	-0.044 (0.026)	0.905 (0.522)
	5	0.190 (0.186)	-0.049 (0.031)	1.169 (0.727)
	6	0.182 (0.183)	-0.056 (0.038)	1.435 (0.946)
0.8	1	0.102 (0.100)	0.102 (0.100)	0.121 (0.011)
	2	0.149 (0.184)	-0.038 (0.018)	0.433 (0.155)
	3	0.182 (0.222)	-0.041 (0.023)	0.677 (0.325)
	4	0.188 (0.229)	-0.043 (0.026)	0.934 (0.541)
	5	0.185 (0.230)	-0.048 (0.031)	1.202 (0.789)
	6	0.177 (0.218)	-0.055 (0.039)	1.470 (1.056)
0.9	1	0.060 (0.004)	0.060 (0.004)	0.075 (0.015)
	2	0.116 (0.014)	0.009 (0.007)	0.291 (0.012)
	3	0.153 (0.020)	0.008 (0.007)	0.515 (0.030)
	4	0.170 (0.024)	0.003 (0.009)	0.774 (0.049)
	5	0.179 (0.027)	-0.006 (0.010)	1.061 (0.072)
	6	0.183 (0.031)	-0.016 (0.011)	1.366 (0.101)

Table 22: Bandwidth Derivatives  $E = -2.5$  (fixed cost specification)

Nesting Parameter	No. Firms	$\frac{\partial \Pi_f}{\partial b_f}$	$\frac{\partial \Pi_f}{\partial b}$	$\frac{\partial CS}{\partial b}$
		(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)	(in 0.01 € / person / MHz)
0.0	1	0.289 (1.246)	0.289 (1.246)	0.294 (3.272)
	2	0.434 (0.180)	-0.135 (0.032)	0.907 (0.108)
	3	0.524 (0.210)	-0.117 (0.013)	1.306 (0.056)
	4	0.537 (0.209)	-0.105 (0.006)	1.848 (0.104)
	5	0.531 (0.208)	-0.112 (0.006)	2.468 (0.253)
	6	0.516 (0.202)	-0.129 (0.013)	3.122 (0.415)
0.2	1	0.289 (5.685)	0.289 (5.685)	0.322 (20.867)
	2	0.432 (0.190)	-0.135 (0.021)	0.928 (0.082)
	3	0.521 (0.213)	-0.115 (0.016)	1.325 (0.041)
	4	0.533 (0.211)	-0.103 (0.013)	1.868 (0.173)
	5	0.527 (0.211)	-0.110 (0.015)	2.489 (0.335)
	6	0.512 (0.201)	-0.126 (0.021)	3.143 (0.509)
0.4	1	0.289	0.289	0.352
	2	0.431 (0.192)	-0.138 (0.026)	0.962 (0.051)
	3	0.517 (0.217)	-0.114 (0.027)	1.361 (0.080)
	4	0.528 (0.213)	-0.101 (0.021)	1.905 (0.229)
	5	0.521 (0.208)	-0.107 (0.021)	2.528 (0.403)
	6	0.506 (0.201)	-0.124 (0.027)	3.183 (0.591)
0.6	1	0.616 (15.282)	0.616 (15.282)	1.089 (32.438)
	2	0.429 (0.200)	-0.145 (0.040)	1.012 (0.054)
	3	0.512 (0.224)	-0.113 (0.032)	1.414 (0.089)
	4	0.522 (0.221)	-0.099 (0.024)	1.962 (0.253)
	5	0.514 (0.206)	-0.105 (0.024)	2.589 (0.445)
	6	0.498 (0.208)	-0.122 (0.029)	3.249 (0.651)
0.8	1	0.290 (6.959)	0.290 (6.959)	0.408 (14.764)
	2	0.426 (0.234)	-0.154 (0.034)	1.069 (0.232)
	3	0.507 (0.271)	-0.113 (0.029)	1.482 (0.073)
	4	0.515 (0.267)	-0.097 (0.021)	2.039 (0.187)
	5	0.506 (0.253)	-0.103 (0.022)	2.677 (0.429)
	6	0.489 (0.258)	-0.119 (0.028)	3.345 (0.694)
0.9	1			
	2	0.290 (0.127)	-0.131 (0.037)	1.190 (0.509)
	3	0.345 (0.159)	-0.098 (0.020)	1.523 (0.335)
	4	0.352 (0.166)	-0.087 (0.017)	1.957 (0.186)
	5	0.344 (0.166)	-0.093 (0.015)	2.451 (0.094)
	6	0.330 (0.122)	-0.105 (0.012)	2.955 (0.219)

Table 23: Bandwidth Derivatives  $E = -3.2$  (fixed cost specification)

<b>Nesting Parameter</b>	<b>No. Firms</b>	$\frac{\partial \Pi_f}{\partial b_f}$ (in 0.01 € / person / MHz)	$\frac{\partial \Pi_f}{\partial b}$ (in 0.01 € / person / MHz)	$\frac{\partial CS}{\partial b}$ (in 0.01 € / person / MHz)
0.0	1			
	2	0.642 (0.211)	-0.377 (0.082)	1.476 (0.733)
	3	0.757 (0.269)	-0.216 (0.050)	1.563 (0.181)
	4	0.750 (0.249)	-0.146 (0.024)	2.199 (0.051)
	5	0.737 (0.231)	-0.139 (0.018)	2.983 (0.208)
	6	0.719 (0.229)	-0.155 (0.020)	3.828 (0.381)
0.2	1	< 0.001 (16.832)	< 0.001 (16.832)	< 0.001 (15.577)
	2	0.645 (0.269)	-0.376 (0.088)	1.513 (0.181)
	3	0.754 (0.275)	-0.215 (0.067)	1.598 (0.103)
	4	0.746 (0.250)	-0.145 (0.035)	2.234 (0.111)
	5	0.732 (0.230)	-0.138 (0.027)	3.019 (0.290)
	6	0.714 (0.208)	-0.154 (0.028)	3.866 (0.473)
0.4	1	< 0.001 (< 0.001)	< 0.001 (< 0.001)	< 0.001 (< 0.001)
	2			
	3	0.750 (0.280)	-0.215 (0.081)	1.657 (0.061)
	4	0.740 (0.249)	-0.144 (0.044)	2.290 (0.177)
	5	0.726 (0.229)	-0.136 (0.034)	3.077 (0.366)
	6	0.707 (0.207)	-0.153 (0.035)	3.926 (0.561)
0.6	1	< 0.001 (< 0.001)	< 0.001 (< 0.001)	< 0.001 (< 0.001)
	2			
	3	0.744 (0.284)	-0.214 (0.090)	1.743 (0.072)
	4	0.732 (0.251)	-0.142 (0.048)	2.372 (0.219)
	5	0.718 (0.230)	-0.135 (0.038)	3.163 (0.421)
	6	0.698 (0.220)	-0.151 (0.038)	4.019 (0.631)
0.8	1			
	2			
	3	0.734 (0.330)	-0.211 (0.090)	1.849 (0.158)
	4	0.722 (0.291)	-0.139 (0.048)	2.479 (0.181)
	5	0.706 (0.270)	-0.132 (0.037)	3.279 (0.435)
	6	0.686 (0.268)	-0.148 (0.038)	4.144 (0.701)
0.9	1			
	2			
	3	0.653 (0.335)	-0.190 (0.046)	1.944 (0.450)
	4	0.647 (0.315)	-0.128 (0.022)	2.511 (0.122)
	5	0.635 (0.302)	-0.124 (0.018)	3.254 (0.291)
	6	0.617 (0.275)	-0.140 (0.021)	4.061 (0.603)

Table 24: Welfare  $E = -1.8$ 

Nesting Parameter	No. Firms	Consumer Surplus	Producer Surplus	Total Surplus
0.0	1	-	-	-
	2	8.669 (2.234)	-2.348 (0.745)	6.322 (1.512)
	3	10.523 (2.442)	-3.418 (0.894)	7.104 (1.581)
	4	11.208 (2.457)	-3.879 (0.882)	7.330 (1.619)
	5	11.538 (2.446)	-4.128 (0.847)	7.410 (1.656)
	6	11.717 (2.445)	-4.281 (0.820)	7.436 (1.691)
	7	11.819 (2.452)	-4.380 (0.802)	7.440 (1.724)
	8	11.880 (2.466)	-4.446 (0.791)	7.434 (1.754)
	9	11.916 (2.483)	-4.492 (0.785)	7.424 (1.781)
0.2	1	-	-	-
	2	11.465 (2.877)	-3.549 (0.909)	7.917 (1.994)
	3	13.515 (2.861)	-4.775 (0.911)	8.739 (1.998)
	4	14.282 (2.771)	-5.285 (0.841)	8.997 (2.001)
	5	14.661 (2.728)	-5.556 (0.796)	9.105 (2.020)
	6	14.872 (2.714)	-5.718 (0.771)	9.154 (2.045)
	7	14.999 (2.718)	-5.822 (0.757)	9.177 (2.071)
	8	15.078 (2.730)	-5.892 (0.751)	9.187 (2.095)
	9	15.130 (2.747)	-5.939 (0.749)	9.191 (2.117)
0.4	1	-	-	-
	2	16.380 (3.744)	-5.746 (1.042)	10.633 (2.741)
	3	18.729 (3.384)	-7.218 (0.840)	11.511 (2.644)
	4	19.609 (3.222)	-7.795 (0.752)	11.814 (2.619)
	5	20.051 (3.155)	-8.091 (0.715)	11.959 (2.623)
	6	20.305 (3.132)	-8.265 (0.698)	12.040 (2.637)
	7	20.465 (3.129)	-8.375 (0.690)	12.090 (2.655)
	8	20.570 (3.138)	-8.447 (0.688)	12.123 (2.673)
	9	20.644 (3.152)	-8.496 (0.689)	12.148 (2.689)
0.6	1	-	-	-
	2	26.875 (4.937)	-10.661 (0.944)	16.214 (4.147)
	3	29.631 (4.259)	-12.478 (0.739)	17.153 (3.964)
	4	30.645 (4.033)	-13.133 (0.745)	17.512 (3.915)
	5	31.164 (3.940)	-13.458 (0.764)	17.706 (3.905)
	6	31.475 (3.901)	-13.645 (0.778)	17.830 (3.911)
	7	31.679 (3.888)	-13.762 (0.786)	17.917 (3.922)
	8	31.822 (3.889)	-13.838 (0.790)	17.984 (3.935)
	9	31.928 (3.897)	-13.889 (0.792)	18.039 (3.947)
0.8	1	-	-	-
	2	60.461 (8.119)	-27.045 (2.369)	33.416 (9.773)
	3	63.620 (6.900)	-29.230 (3.249)	34.391 (9.462)
	4	64.774 (6.516)	-29.962 (3.551)	34.812 (9.378)
	5	65.386 (6.350)	-30.318 (3.695)	35.068 (9.356)
	6	65.769 (6.270)	-30.521 (3.774)	35.248 (9.357)
	7	66.035 (6.233)	-30.648 (3.820)	35.386 (9.368)
	8	66.231 (6.218)	-30.731 (3.845)	35.500 (9.381)
	9	66.385 (6.216)	-30.788 (3.858)	35.597 (9.396)
0.9	1	-	-	-
	2	17.053 (1.437)	-9.018 (0.874)	8.034 (0.730)
	3	17.668 (1.531)	-9.516 (0.968)	8.153 (0.734)
	4	17.848 (1.565)	-9.687 (1.003)	8.160 (0.734)
	5	17.912 (1.581)	-9.770 (1.024)	8.142 (0.732)
	6	17.931 (1.591)	-9.815 (1.037)	8.117 (0.729)
	7	17.929 (1.595)	-9.838 (1.047)	8.090 (0.727)
	8	17.915 (1.598)	-9.850 (1.054)	8.066 (0.724)
	9	17.896 (1.598)	-9.853 (1.060)	8.043 (0.721)

Welfare is defined in comparison to the monopoly case and therefore is not provided for the case of one firm.

Table 25: Welfare  $E = -2.5$ 

Nesting Parameter	No. Firms	Consumer Surplus	Producer Surplus	Total Surplus
0.0	1	-	-	-
	2	6.114 (70.644)	-2.982 (90.701)	3.132 (20.078)
	3	6.942 (70.706)	-3.725 (90.799)	3.218 (20.113)
	4	7.120 (70.787)	-4.006 (90.892)	3.114 (20.125)
	5	7.113 (70.829)	-4.139 (90.953)	2.974 (20.145)
	6	7.036 (70.845)	-4.203 (90.993)	2.833 (20.168)
	7	6.932 (70.847)	-4.229 (91.018)	2.703 (20.192)
	8	6.820 (70.839)	-4.232 (91.033)	2.588 (20.215)
	9	6.707 (70.826)	-4.220 (91.041)	2.487 (20.236)
0.2	1	-	-	-
	2	7.757 (48.876)	-3.742 (58.496)	4.015 (9.655)
	3	8.733 (49.114)	-4.584 (58.698)	4.148 (9.619)
	4	8.973 (49.243)	-4.900 (58.812)	4.073 (9.604)
	5	9.003 (49.298)	-5.049 (58.875)	3.953 (9.611)
	6	8.950 (49.317)	-5.123 (58.911)	3.828 (9.628)
	7	8.864 (49.317)	-5.155 (58.931)	3.709 (9.648)
	8	8.765 (49.307)	-5.161 (58.941)	3.604 (9.668)
	9	8.663 (49.291)	-5.152 (58.944)	3.511 (9.687)
0.4	1	-	-	-
	2	10.738 (26.175)	-5.171 (30.740)	5.568 (4.639)
	3	11.946 (25.869)	-6.175 (30.530)	5.771 (4.750)
	4	12.272 (25.747)	-6.538 (30.442)	5.734 (4.791)
	5	12.348 (25.697)	-6.707 (30.400)	5.641 (4.801)
	6	12.327 (25.679)	-6.791 (30.380)	5.535 (4.796)
	7	12.263 (25.677)	-6.829 (30.370)	5.434 (4.787)
	8	12.182 (25.684)	-6.840 (30.368)	5.342 (4.775)
	9	12.095 (25.696)	-6.833 (30.370)	5.262 (4.763)
0.6	1	-	-	-
	2	14.884 (113.744)	-5.838 (120.472)	9.047 (6.792)
	3	16.411 (113.160)	-7.076 (120.089)	9.335 (6.984)
	4	16.838 (112.964)	-7.495 (119.958)	9.343 (7.048)
	5	16.970 (112.887)	-7.688 (119.900)	9.282 (7.065)
	6	16.988 (112.859)	-7.784 (119.871)	9.203 (7.063)
	7	16.954 (112.856)	-7.829 (119.858)	9.124 (7.054)
	8	16.897 (112.865)	-7.845 (119.855)	9.052 (7.042)
	9	16.831 (112.881)	-7.841 (119.858)	8.990 (7.029)
0.8	1	-	-	-
	2	39.003 (13.701)	-19.641 (16.863)	19.362 (3.452)
	3	40.866 (14.697)	-21.146 (17.476)	19.719 (3.119)
	4	41.398 (15.024)	-21.626 (17.676)	19.773 (3.009)
	5	41.594 (15.161)	-21.844 (17.768)	19.750 (2.970)
	6	41.658 (15.220)	-21.954 (17.816)	19.704 (2.959)
	7	41.662 (15.242)	-22.008 (17.841)	19.654 (2.960)
	8	41.637 (15.242)	-22.029 (17.852)	19.608 (2.967)
	9	41.600 (15.231)	-22.031 (17.854)	19.569 (2.977)
0.9	1	-	-	-
	2	84.774 (13.443)	-39.220 (18.809)	45.554 (6.043)
	3	86.168 (14.827)	-40.445 (19.731)	45.723 (5.552)
	4	86.563 (15.319)	-40.824 (20.042)	45.739 (5.363)
	5	86.716 (15.564)	-40.994 (20.198)	45.722 (5.269)
	6	86.777 (15.707)	-41.078 (20.290)	45.699 (5.216)
	7	86.797 (15.787)	-41.120 (20.348)	45.678 (5.187)
	8	86.799 (15.837)	-41.136 (20.386)	45.662 (5.171)
	9	86.793 (15.864)	-41.138 (20.410)	45.655 (5.165)

Welfare is defined in comparison to the monopoly case and therefore is not provided for the case of one firm.

Table 26: Welfare  $E = -3.2$ 

Nesting Parameter	No. Firms	Consumer Surplus	Producer Surplus	Total Surplus
0.0	1	-	-	-
	2	3.395 (36.058)	-2.176 (10.944)	1.219 (26.586)
	3	3.765 (41.549)	-2.759 (18.888)	1.006 (23.218)
	4	3.730 (41.477)	-2.961 (18.808)	0.769 (23.212)
	5	3.579 (41.447)	-3.044 (18.765)	0.534 (23.216)
	6	3.390 (41.439)	-3.072 (18.740)	0.318 (23.227)
	7	3.192 (41.442)	-3.067 (18.725)	0.124 (23.241)
	8	2.998 (41.451)	-3.043 (18.718)	-0.045 (23.255)
	9	2.815 (41.464)	-3.005 (18.715)	-0.191 (23.268)
0.2	1	-	-	-
	2	14.183 (476.912)	3.587 (99.444)	17.770 (574.964)
	3	14.665 (311.247)	2.939 (122.332)	17.603 (433.512)
	4	14.675 (311.369)	2.715 (122.228)	17.390 (433.530)
	5	14.549 (311.414)	2.622 (122.178)	17.171 (433.525)
	6	14.377 (311.425)	2.588 (122.151)	16.964 (433.508)
	7	14.191 (311.417)	2.588 (122.138)	16.779 (433.488)
	8	14.006 (311.402)	2.610 (122.134)	16.617 (433.468)
	9	13.830 (311.381)	2.646 (122.135)	16.476 (433.448)
0.4	1	-	-	-
	2	16.346 (2.248)	2.352 (5.790)	18.698 (7.746)
	3	17.465 (1.244)	2.993 (0.776)	20.458 (1.072)
	4	17.540 (1.178)	2.739 (0.677)	20.279 (1.072)
	5	17.448 (1.158)	2.633 (0.633)	20.080 (1.068)
	6	17.297 (1.153)	2.592 (0.613)	19.889 (1.062)
	7	17.128 (1.156)	2.588 (0.605)	19.715 (1.056)
	8	16.956 (1.162)	2.606 (0.605)	19.562 (1.051)
	9	16.790 (1.171)	2.640 (0.610)	19.429 (1.046)
0.6	1	-	-	-
	2	21.690 (15.585)	3.269 (13.304)	24.958 (2.670)
	3	23.621 (1.649)	3.052 (0.708)	26.674 (1.354)
	4	23.777 (1.555)	2.761 (0.613)	26.537 (1.334)
	5	23.728 (1.524)	2.638 (0.574)	26.366 (1.326)
	6	23.606 (1.516)	2.588 (0.558)	26.194 (1.322)
	7	23.458 (1.518)	2.579 (0.554)	26.037 (1.320)
	8	23.303 (1.525)	2.594 (0.556)	25.897 (1.318)
	9	23.152 (1.535)	2.624 (0.564)	25.776 (1.318)
0.8	1	-	-	-
	2	24.193 (28.798)	-16.192 (30.318)	8.001 (1.579)
	3	25.339 (1.921)	-15.833 (3.101)	9.506 (1.409)
	4	25.584 (2.150)	-16.168 (3.230)	9.416 (1.273)
	5	25.585 (2.232)	-16.310 (3.286)	9.275 (1.233)
	6	25.498 (2.257)	-16.370 (3.311)	9.128 (1.227)
	7	25.377 (2.255)	-16.386 (3.322)	8.991 (1.237)
	8	25.246 (2.239)	-16.376 (3.323)	8.869 (1.252)
	9	25.114 (2.216)	-16.350 (3.319)	8.765 (1.270)
0.9	1	-	-	-
	2	56.385 (31.463)	-32.713 (33.034)	23.672 (1.777)
	3	57.868 (9.771)	-32.710 (9.804)	25.157 (0.668)
	4	58.086 (10.213)	-33.034 (10.041)	25.053 (0.652)
	5	58.088 (10.395)	-33.170 (10.152)	24.918 (0.659)
	6	58.012 (10.474)	-33.229 (10.213)	24.783 (0.659)
	7	57.907 (10.504)	-33.245 (10.248)	24.661 (0.653)
	8	57.793 (10.506)	-33.237 (10.267)	24.555 (0.644)
	9	57.680 (10.491)	-33.214 (10.275)	24.466 (0.635)

Welfare is defined in comparison to the monopoly case and therefore is not provided for the case of one firm.



Table 27: Consumer Surplus by Income Level  $E = -1.8$ 

Nesting Parameter	No. Firms	10 %ile	30 %ile	50 %ile	70 %ile	90 %ile
0.0	1	-	-	-	-	-
	2	-0.993 (1.862)	0.730 (5.074)	9.505 (3.612)	16.697 (8.767)	17.352 (10.764)
	3	-1.587 (0.533)	2.826 (5.168)	12.116 (2.757)	19.180 (9.705)	19.160 (11.548)
	4	-1.703 (0.613)	3.707 (5.068)	13.064 (2.507)	20.029 (9.989)	19.586 (11.793)
	5	-1.715 (1.298)	4.158 (5.019)	13.528 (2.404)	20.423 (10.115)	19.695 (11.915)
	6	-1.707 (1.729)	4.420 (4.982)	13.787 (2.339)	20.631 (10.197)	19.700 (12.000)
	7	-1.700 (2.014)	4.583 (4.948)	13.944 (2.289)	20.747 (10.260)	19.670 (12.068)
	8	-1.695 (2.212)	4.690 (4.914)	14.042 (2.244)	20.813 (10.314)	19.628 (12.126)
	9	-1.695 (2.353)	4.762 (4.881)	14.105 (2.204)	20.850 (10.362)	19.587 (12.177)
0.2	1	-	-	-	-	-
	2	-1.364 (0.982)	2.446 (5.744)	12.585 (2.790)	20.912 (10.560)	22.406 (13.168)
	3	-1.393 (1.048)	4.728 (5.780)	15.237 (2.340)	23.464 (11.106)	24.359 (13.675)
	4	-1.199 (2.021)	5.646 (5.824)	16.215 (2.284)	24.356 (11.199)	24.866 (13.802)
	5	-1.049 (2.529)	6.120 (5.842)	16.703 (2.258)	24.783 (11.248)	25.031 (13.882)
	6	-0.945 (2.824)	6.398 (5.840)	16.982 (2.232)	25.016 (11.292)	25.079 (13.949)
	7	-0.875 (3.010)	6.575 (5.826)	17.154 (2.203)	25.152 (11.334)	25.081 (14.008)
	8	-0.826 (3.133)	6.692 (5.804)	17.264 (2.172)	25.234 (11.375)	25.066 (14.062)
	9	-0.793 (3.217)	6.773 (5.779)	17.338 (2.142)	25.284 (11.413)	25.047 (14.110)
0.4	1	-	-	-	-	-
	2	-1.297 (1.080)	5.564 (6.820)	17.883 (2.107)	28.026 (13.289)	30.930 (16.927)
	3	-0.432 (3.089)	8.084 (7.160)	20.660 (2.180)	30.735 (13.271)	33.157 (17.036)
	4	0.087 (3.808)	9.063 (7.327)	21.693 (2.256)	31.706 (13.220)	33.812 (17.085)
	5	0.392 (4.147)	9.567 (7.400)	22.217 (2.284)	32.184 (13.210)	34.080 (17.142)
	6	0.584 (4.332)	9.867 (7.428)	22.523 (2.287)	32.456 (13.223)	34.205 (17.202)
	7	0.713 (4.442)	10.059 (7.432)	22.716 (2.277)	32.622 (13.246)	34.268 (17.258)
	8	0.802 (4.510)	10.190 (7.424)	22.845 (2.260)	32.730 (13.273)	34.304 (17.311)
	9	0.867 (4.554)	10.283 (7.409)	22.935 (2.239)	32.803 (13.301)	34.328 (17.359)
0.6	1	-	-	-	-	-
	2	0.706 (4.943)	12.436 (10.294)	29.037 (2.227)	42.665 (18.633)	48.100 (24.626)
	3	2.654 (6.569)	15.268 (11.056)	32.042 (2.659)	45.637 (18.123)	50.761 (24.414)
	4	3.467 (7.082)	16.318 (11.344)	33.150 (2.835)	46.716 (17.957)	51.650 (24.430)
	5	3.901 (7.316)	16.859 (11.475)	33.720 (2.913)	47.267 (17.896)	52.088 (24.490)
	6	4.166 (7.439)	17.184 (11.538)	34.061 (2.945)	47.594 (17.878)	52.347 (24.560)
	7	4.343 (7.509)	17.397 (11.566)	34.284 (2.955)	47.808 (17.881)	52.523 (24.629)
	8	4.468 (7.549)	17.545 (11.576)	34.438 (2.953)	47.955 (17.894)	52.654 (24.694)
	9	4.560 (7.572)	17.653 (11.575)	34.549 (2.944)	48.063 (17.911)	52.761 (24.753)
0.8	1	-	-	-	-	-
	2	11.623 (19.424)	35.130 (30.170)	64.550 (5.753)	88.277 (41.401)	99.940 (58.058)
	3	14.452 (21.122)	38.264 (31.670)	67.810 (6.923)	91.546 (40.235)	103.151 (57.479)
	4	15.463 (21.686)	39.384 (32.202)	69.000 (7.338)	92.754 (39.876)	104.375 (57.498)
	5	15.983 (21.954)	39.963 (32.460)	69.625 (7.535)	93.399 (39.724)	105.074 (57.620)
	6	16.298 (22.101)	40.316 (32.601)	70.011 (7.639)	93.805 (39.653)	105.552 (57.764)
	7	16.509 (22.188)	40.552 (32.682)	70.271 (7.696)	94.085 (39.623)	105.915 (57.909)
	8	16.659 (22.241)	40.721 (32.730)	70.459 (7.728)	94.293 (39.613)	106.212 (58.047)
	9	16.772 (22.272)	40.847 (32.758)	70.602 (7.743)	94.454 (39.614)	106.467 (58.177)
0.9	1	-	-	-	-	-
	2	0.019 (2.117)	7.033 (4.214)	16.614 (2.742)	26.614 (2.500)	35.694 (4.485)
	3	0.341 (2.348)	7.586 (4.355)	17.255 (2.852)	27.324 (2.416)	36.501 (4.285)
	4	0.434 (2.422)	7.747 (4.400)	17.438 (2.890)	27.525 (2.382)	36.757 (4.196)
	5	0.466 (2.454)	7.805 (4.419)	17.502 (2.907)	27.593 (2.362)	36.861 (4.140)
	6	0.473 (2.470)	7.823 (4.428)	17.519 (2.916)	27.608 (2.349)	36.904 (4.099)
	7	0.469 (2.477)	7.821 (4.431)	17.513 (2.920)	27.600 (2.339)	36.918 (4.068)
	8	0.459 (2.479)	7.809 (4.431)	17.496 (2.921)	27.579 (2.332)	36.919 (4.044)
	9	0.445 (2.478)	7.791 (4.429)	17.472 (2.921)	27.553 (2.326)	36.915 (4.025)

Welfare is defined in comparison to the monopoly case and therefore is not provided for the case of one firm.

Table 28: Consumer Surplus by Income Level  $E = -2.5$ 

Nesting Parameter	No. Firms	10 %ile	30 %ile	50 %ile	70 %ile	90 %ile
0.0	1	-	-	-	-	-
	2	-1.014 (0.450)	2.629 (6.420)	8.853 (36.053)	10.290 (115.457)	8.621 (226.792)
	3	-1.094 (1.052)	4.009 (6.328)	10.201 (35.656)	11.237 (115.109)	8.357 (226.893)
	4	-1.078 (1.733)	4.438 (6.345)	10.591 (35.594)	11.436 (115.030)	7.847 (227.014)
	5	-1.098 (2.064)	4.577 (6.354)	10.700 (35.573)	11.433 (114.994)	7.386 (227.093)
	6	-1.145 (2.242)	4.599 (6.346)	10.695 (35.555)	11.352 (114.967)	6.989 (227.144)
	7	-1.206 (2.341)	4.567 (6.328)	10.637 (35.534)	11.238 (114.943)	6.651 (227.176)
	8	-1.274 (2.398)	4.509 (6.304)	10.555 (35.511)	11.112 (114.920)	6.364 (227.195)
	9	-1.344 (2.430)	4.438 (6.277)	10.463 (35.487)	10.986 (114.898)	6.122 (227.205)
0.2	1	-	-	-	-	-
	2	-1.031 (0.520)	3.916 (9.489)	10.619 (37.401)	12.651 (78.812)	11.119 (130.776)
	3	-0.723 (2.037)	5.413 (9.616)	12.076 (37.273)	13.702 (78.698)	10.940 (131.056)
	4	-0.555 (2.607)	5.894 (9.714)	12.522 (37.293)	13.952 (78.691)	10.469 (131.236)
	5	-0.499 (2.860)	6.064 (9.751)	12.664 (37.300)	13.982 (78.681)	10.033 (131.341)
	6	-0.500 (2.983)	6.107 (9.755)	12.681 (37.293)	13.923 (78.664)	9.655 (131.406)
	7	-0.530 (3.043)	6.090 (9.740)	12.640 (37.275)	13.825 (78.643)	9.331 (131.446)
	8	-0.576 (3.069)	6.043 (9.717)	12.571 (37.253)	13.712 (78.621)	9.056 (131.471)
	9	-0.629 (3.077)	5.983 (9.689)	12.490 (37.228)	13.596 (78.599)	8.824 (131.484)
0.4	1	-	-	-	-	-
	2	-0.591 (1.859)	6.225 (3.690)	13.802 (18.246)	16.733 (45.485)	15.609 (79.766)
	3	0.250 (3.243)	7.926 (4.020)	15.444 (18.142)	17.959 (45.369)	15.588 (79.353)
	4	0.590 (3.688)	8.478 (4.160)	15.964 (18.080)	18.284 (45.322)	15.188 (79.150)
	5	0.726 (3.866)	8.685 (4.210)	16.148 (18.057)	18.357 (45.311)	14.797 (79.037)
	6	0.772 (3.939)	8.752 (4.219)	16.194 (18.054)	18.329 (45.314)	14.453 (78.970)
	7	0.773 (3.965)	8.753 (4.208)	16.173 (18.062)	18.255 (45.325)	14.157 (78.928)
	8	0.751 (3.966)	8.721 (4.187)	16.121 (18.076)	18.160 (45.339)	13.904 (78.901)
	9	0.716 (3.955)	8.672 (4.162)	16.053 (18.093)	18.060 (45.354)	13.691 (78.886)
0.6	1	-	-	-	-	-
	2	1.414 (4.503)	11.151 (4.316)	19.131 (80.523)	21.375 (190.239)	17.956 (339.784)
	3	2.928 (5.706)	13.148 (3.778)	21.030 (80.159)	22.845 (189.885)	18.180 (339.040)
	4	3.445 (6.053)	13.783 (3.584)	21.637 (80.032)	23.261 (189.786)	17.890 (338.722)
	5	3.659 (6.176)	14.032 (3.510)	21.870 (79.986)	23.391 (189.757)	17.577 (338.551)
	6	3.749 (6.216)	14.127 (3.488)	21.949 (79.976)	23.403 (189.755)	17.294 (338.448)
	7	3.780 (6.219)	14.148 (3.491)	21.954 (79.984)	23.360 (189.764)	17.049 (338.383)
	8	3.779 (6.204)	14.133 (3.508)	21.923 (80.001)	23.293 (189.780)	16.840 (338.342)
	9	3.760 (6.179)	14.097 (3.530)	21.873 (80.023)	23.215 (189.797)	16.667 (338.317)
0.8	1	-	-	-	-	-
	2	10.782 (16.232)	28.678 (18.741)	43.915 (11.573)	52.611 (9.732)	55.228 (12.200)
	3	12.939 (17.580)	30.996 (19.723)	46.088 (12.313)	54.339 (10.511)	55.760 (13.571)
	4	13.601 (17.968)	31.713 (20.060)	46.781 (12.546)	54.853 (10.735)	55.630 (14.128)
	5	13.876 (18.104)	32.004 (20.197)	47.064 (12.639)	55.048 (10.819)	55.440 (14.422)
	6	14.001 (18.145)	32.126 (20.250)	47.180 (12.675)	55.111 (10.851)	55.261 (14.596)
	7	14.055 (18.144)	32.169 (20.261)	47.216 (12.681)	55.111 (10.859)	55.106 (14.703)
	8	14.071 (18.121)	32.171 (20.251)	47.209 (12.673)	55.081 (10.856)	54.978 (14.767)
	9	14.066 (18.088)	32.151 (20.228)	47.181 (12.655)	55.036 (10.845)	54.878 (14.803)
0.9	1	-	-	-	-	-
	2	16.125 (24.876)	43.574 (41.041)	86.137 (47.826)	129.532 (11.033)	145.705 (55.752)
	3	17.771 (26.194)	45.371 (42.335)	87.935 (48.998)	130.889 (9.810)	145.609 (53.495)
	4	18.281 (26.601)	45.916 (42.782)	88.519 (49.398)	131.322 (9.417)	145.276 (52.519)
	5	18.509 (26.780)	46.144 (42.991)	88.769 (49.601)	131.507 (9.227)	145.021 (51.980)
	6	18.626 (26.868)	46.250 (43.102)	88.883 (49.720)	131.586 (9.114)	144.838 (51.655)
	7	18.689 (26.914)	46.299 (43.163)	88.931 (49.794)	131.613 (9.039)	144.713 (51.459)
	8	18.724 (26.935)	46.317 (43.196)	88.946 (49.841)	131.613 (8.987)	144.638 (51.349)
	9	18.742 (26.941)	46.320 (43.211)	88.943 (49.870)	131.601 (8.951)	144.604 (51.299)

Welfare is defined in comparison to the monopoly case and therefore is not provided for the case of one firm.

Table 29: Consumer Surplus by Income Level  $E = -3.2$ 

Nesting Parameter	No. Firms	10 %ile	30 %ile	50 %ile	70 %ile	90 %ile
0.0	1	-	-	-	-	-
	2	-0.855 (0.609)	3.498 (6.793)	5.426 (36.781)	4.463 (53.891)	3.263 (94.255)
	3	-0.555 (2.432)	4.502 (6.983)	6.140 (51.815)	4.667 (67.703)	2.273 (86.560)
	4	-0.474 (2.886)	4.726 (6.941)	6.270 (51.816)	4.573 (67.716)	1.485 (86.424)
	5	-0.511 (3.044)	4.714 (6.921)	6.210 (51.812)	4.394 (67.724)	0.865 (86.343)
	6	-0.596 (3.091)	4.614 (6.921)	6.075 (51.815)	4.183 (67.733)	0.359 (86.290)
	7	-0.700 (3.087)	4.479 (6.931)	5.910 (51.823)	3.964 (67.742)	-0.065 (86.252)
	8	-0.810 (3.058)	4.332 (6.946)	5.736 (51.836)	3.749 (67.752)	-0.423 (86.225)
	9	-0.921 (3.017)	4.184 (6.965)	5.564 (51.852)	3.546 (67.762)	-0.726 (86.204)
0.2	1	-	-	-	-	-
	2	-0.785 (9.203)	3.478 (24.109)	9.476 (239.994)	18.697 (675.002)	48.701 (1 888.024)
	3	-0.219 (2.523)	4.597 (4.048)	10.292 (152.764)	18.976 (429.962)	47.753 (1 231.189)
	4	-0.056 (2.122)	4.872 (3.943)	10.471 (152.800)	18.921 (429.975)	46.983 (1 231.381)
	5	-0.056 (1.991)	4.888 (3.902)	10.438 (152.816)	18.764 (429.971)	46.376 (1 231.486)
	6	-0.119 (1.960)	4.806 (3.897)	10.321 (152.814)	18.569 (429.960)	45.879 (1 231.549)
	7	-0.208 (1.972)	4.685 (3.910)	10.169 (152.801)	18.362 (429.945)	45.462 (1 231.590)
	8	-0.308 (2.004)	4.548 (3.932)	10.005 (152.783)	18.157 (429.929)	45.110 (1 231.617)
	9	-0.411 (2.046)	4.408 (3.959)	9.841 (152.761)	17.960 (429.912)	44.812 (1 231.634)
0.4	1	-	-	-	-	-
	2	-0.937 (1.872)	3.902 (3.400)	11.128 (1.795)	21.832 (1.562)	55.541 (17.417)
	3	0.610 (2.937)	6.149 (3.073)	12.531 (2.030)	22.312 (1.513)	54.787 (15.457)
	4	0.876 (3.298)	6.493 (3.220)	12.776 (2.085)	22.311 (1.487)	54.052 (15.226)
	5	0.921 (3.406)	6.544 (3.272)	12.780 (2.103)	22.188 (1.484)	53.468 (15.103)
	6	0.883 (3.424)	6.485 (3.277)	12.687 (2.099)	22.015 (1.489)	52.988 (15.029)
	7	0.810 (3.403)	6.379 (3.260)	12.551 (2.084)	21.825 (1.497)	52.586 (14.982)
	8	0.721 (3.364)	6.255 (3.232)	12.401 (2.063)	21.632 (1.506)	52.246 (14.951)
	9	0.627 (3.318)	6.125 (3.199)	12.247 (2.039)	21.447 (1.516)	51.958 (14.930)
0.6	1	-	-	-	-	-
	2	-0.129 (0.653)	6.723 (5.270)	15.288 (12.628)	28.252 (22.249)	70.068 (43.088)
	3	2.727 (4.344)	9.688 (3.970)	17.513 (2.565)	29.571 (2.035)	69.782 (20.953)
	4	3.117 (4.666)	10.117 (4.142)	17.838 (2.636)	29.641 (1.985)	69.105 (20.650)
	5	3.213 (4.753)	10.209 (4.200)	17.886 (2.655)	29.560 (1.976)	68.563 (20.491)
	6	3.202 (4.757)	10.176 (4.206)	17.822 (2.649)	29.417 (1.979)	68.116 (20.394)
	7	3.145 (4.728)	10.088 (4.187)	17.708 (2.631)	29.250 (1.987)	67.743 (20.330)
	8	3.068 (4.684)	9.978 (4.157)	17.574 (2.608)	29.077 (1.998)	67.428 (20.287)
	9	2.982 (4.635)	9.860 (4.121)	17.435 (2.581)	28.909 (2.009)	67.163 (20.258)
0.8	1	-	-	-	-	-
	2	8.128 (17.947)	21.610 (22.066)	28.296 (24.545)	30.419 (34.899)	28.321 (44.439)
	3	12.114 (14.355)	24.333 (6.073)	29.632 (3.243)	30.183 (5.086)	25.986 (1.878)
	4	12.629 (14.735)	24.849 (6.321)	30.041 (3.108)	30.332 (4.916)	25.403 (1.475)
	5	12.772 (14.833)	24.983 (6.405)	30.135 (3.068)	30.301 (4.870)	24.934 (1.318)
	6	12.785 (14.834)	24.976 (6.420)	30.103 (3.064)	30.197 (4.863)	24.550 (1.255)
	7	12.744 (14.797)	24.907 (6.403)	30.014 (3.078)	30.062 (4.871)	24.230 (1.234)
	8	12.676 (14.744)	24.812 (6.369)	29.900 (3.101)	29.916 (4.885)	23.965 (1.233)
	9	12.597 (14.683)	24.707 (6.327)	29.779 (3.129)	29.770 (4.902)	23.746 (1.241)
0.9	1	-	-	-	-	-
	2	19.538 (30.355)	45.652 (37.384)	63.876 (23.705)	72.802 (25.975)	73.506 (40.483)
	3	24.482 (35.772)	49.026 (29.463)	65.631 (3.494)	72.658 (10.796)	70.646 (7.733)
	4	24.958 (36.229)	49.517 (29.853)	66.041 (3.694)	72.800 (10.445)	69.975 (6.787)
	5	25.098 (36.353)	49.648 (30.002)	66.147 (3.771)	72.784 (10.316)	69.477 (6.280)
	6	25.122 (36.367)	49.648 (30.050)	66.130 (3.798)	72.700 (10.261)	69.090 (5.974)
	7	25.095 (36.334)	49.593 (30.049)	66.058 (3.799)	72.585 (10.239)	68.780 (5.782)
	8	25.044 (36.280)	49.514 (30.023)	65.962 (3.787)	72.458 (10.233)	68.532 (5.662)
	9	24.983 (36.217)	49.425 (29.983)	65.858 (3.766)	72.333 (10.237)	68.336 (5.591)

Welfare is defined in comparison to the monopoly case and therefore is not provided for the case of one firm.

Figure 18: Full and partial price elasticities

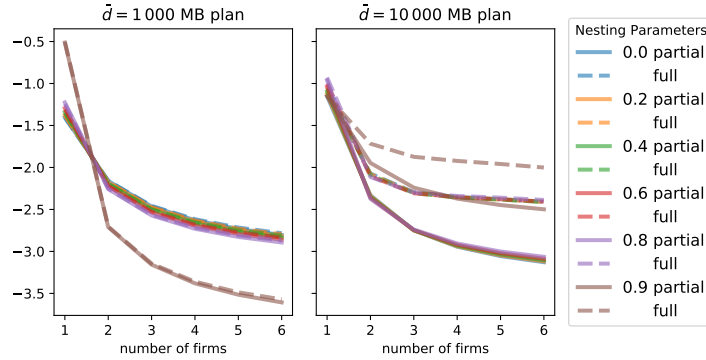


Figure 19: Counterfactual welfare

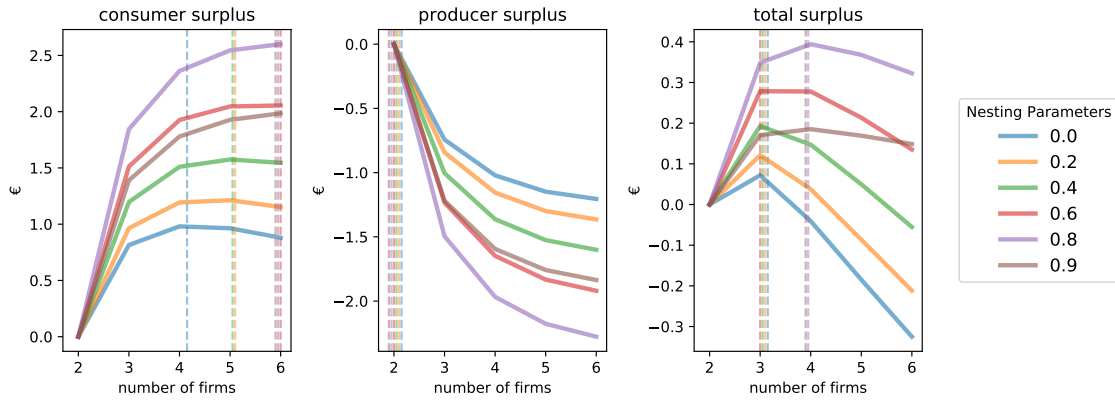


Table 30: Impact of Adding Additional Bandwidth on Endogenous Variables  $E = -1.8$  (bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ 1000 MB plan prices (in €)	$\Delta$ 10000 MB plan prices (in €)	$\Delta$ radius (in km)	$\Delta$ download speeds (in Mbps)
0.0	3 firms, $\frac{4}{3}b$	0.167 (0.021)	2.011 (0.815)	0.114 (0.008)	2.201 (0.365)
	4 firms, $b$	-0.779 (0.164)	0.982 (0.731)	0.123 (0.021)	-1.636 (0.134)
0.2	3 firms, $\frac{4}{3}b$	0.117 (0.017)	2.000 (0.881)	0.116 (0.009)	2.171 (0.400)
	4 firms, $b$	-0.799 (0.018)	0.985 (0.787)	0.126 (0.018)	-1.672 (0.098)
0.4	3 firms, $\frac{4}{3}b$	0.067 (0.018)	1.989 (0.926)	0.118 (0.010)	2.140 (0.423)
	4 firms, $b$	-0.835 (0.150)	0.990 (0.821)	0.130 (0.017)	-1.718 (0.077)
0.6	3 firms, $\frac{4}{3}b$	0.021 (0.039)	1.980 (0.942)	0.120 (0.010)	2.110 (0.449)
	4 firms, $b$	-0.876 (0.273)	0.999 (0.812)	0.134 (0.018)	-1.771 (0.060)
0.8	3 firms, $\frac{4}{3}b$	-0.017 (0.092)	1.978 (0.917)	0.122 (0.012)	2.084 (0.571)
	4 firms, $b$	-0.913 (0.497)	1.010 (0.706)	0.139 (0.027)	-1.828 (0.031)
0.9	3 firms, $\frac{4}{3}b$	0.053 (0.015)	1.964 (0.071)	0.159 (0.004)	0.951 (0.094)
	4 firms, $b$	-0.195 (0.034)	1.629 (0.057)	0.131 (0.016)	-1.109 (0.033)

The penetration rate of mobile services reached 110% in 2015 (see figure 22). According to surveys conducted by the French research institute CREDOC, mobile users represent 92% of the population

Figure 20: Counterfactual welfare by income level

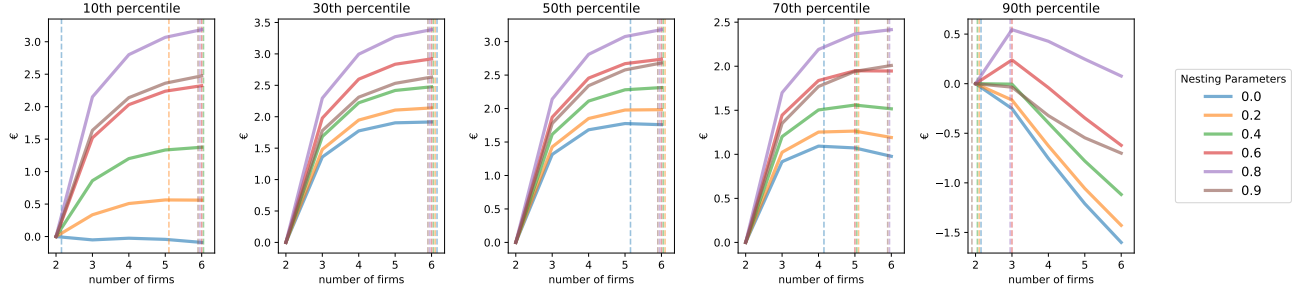


Figure 21: Bandwidth derivatives

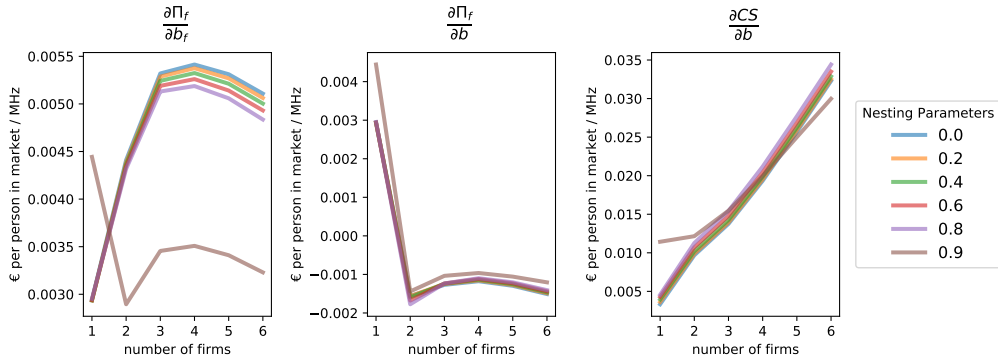


Table 31: Impact of Adding Additional Bandwidth on Endogenous Variables  $E = -2.5$  (bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ 1000 MB plan prices (in €)	$\Delta$ 10000 MB plan prices (in €)	$\Delta$ radius (in km)	$\Delta$ download speeds (in Mbps)
0.0	3 firms, $\frac{4}{3}b$	0.325 (0.148)	3.767 (0.315)	0.085 (0.005)	2.794 (0.345)
	4 firms, $b$	-0.283 (0.171)	3.081 (0.231)	0.105 (0.008)	-1.051 (0.104)
0.2	3 firms, $\frac{4}{3}b$	0.237 (0.138)	3.785 (0.319)	0.091 (0.008)	2.729 (0.380)
	4 firms, $b$	-0.371 (0.216)	3.103 (0.226)	0.112 (0.008)	-1.127 (0.098)
0.4	3 firms, $\frac{4}{3}b$	0.132 (0.126)	3.805 (0.303)	0.097 (0.011)	2.648 (0.414)
	4 firms, $b$	-0.480 (0.241)	3.128 (0.200)	0.120 (0.010)	-1.223 (0.077)
0.6	3 firms, $\frac{4}{3}b$	0.019 (0.129)	3.825 (0.254)	0.104 (0.013)	2.551 (0.447)
	4 firms, $b$	-0.599 (0.278)	3.155 (0.142)	0.129 (0.014)	-1.335 (0.061)
0.8	3 firms, $\frac{4}{3}b$	-0.087 (0.195)	3.842 (0.113)	0.112 (0.016)	2.444 (0.538)
	4 firms, $b$	-0.712 (0.426)	3.176 (0.158)	0.140 (0.022)	-1.453 (0.080)
0.9	3 firms, $\frac{4}{3}b$	-0.034 (0.096)	3.814 (0.544)	0.122 (0.007)	2.127 (0.323)
	4 firms, $b$	-0.519 (0.423)	3.259 (0.775)	0.161 (0.042)	-1.512 (0.148)

above 12 years old in 2015. We rely on the statistics from these surveys in order to determine the market size. A decomposition according to the technology shows that mobile data is less popular than voice, particularly 4G mobile data whose penetration rate was 34% in 2015.

In terms of usage, figure 23 shows that voice and SMS consumption has reached a plateau since 2011. There is roughly no more growth in the number of minutes consumed, which stabilizes around 3 hours

Table 32: Impact of Adding Additional Bandwidth on Endogenous Variables  $E = -3.2$  (bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ 1 000 MB plan prices (in €)	$\Delta$ 10 000 MB plan prices (in €)	$\Delta$ radius (in km)	$\Delta$ download speeds (in Mbps)
0.0	3 firms, $\frac{4}{3}b$	0.303 (0.250)	4.103 (0.305)	0.042 (0.005)	3.576 (0.425)
	4 firms, $b$	-0.129 (0.332)	3.555 (0.197)	0.084 (0.008)	-0.559 (0.260)
0.2	3 firms, $\frac{4}{3}b$	0.214 (0.252)	4.129 (0.292)	0.050 (0.007)	3.488 (0.481)
	4 firms, $b$	-0.224 (0.341)	3.575 (0.179)	0.092 (0.005)	-0.654 (0.227)
0.4	3 firms, $\frac{4}{3}b$	0.099 (0.243)	4.159 (0.266)	0.060 (0.013)	3.370 (0.552)
	4 firms, $b$	-0.346 (0.335)	3.598 (0.150)	0.103 (0.005)	-0.777 (0.173)
0.6	3 firms, $\frac{4}{3}b$	-0.041 (0.242)	4.189 (0.225)	0.072 (0.019)	3.217 (0.616)
	4 firms, $b$	-0.493 (0.339)	3.620 (0.114)	0.117 (0.010)	-0.931 (0.124)
0.8	3 firms, $\frac{4}{3}b$	-0.185 (0.316)	4.217 (0.148)	0.087 (0.024)	3.021 (0.711)
	4 firms, $b$	-0.645 (0.454)	3.636 (0.163)	0.133 (0.018)	-1.105 (0.136)
0.9	3 firms, $\frac{4}{3}b$	-0.178 (0.321)	4.221 (0.188)	0.098 (0.018)	2.772 (0.669)
	4 firms, $b$	-0.607 (0.555)	3.692 (0.466)	0.146 (0.033)	-1.177 (0.209)

Table 33: Impact of Adding Additional Bandwidth on Endogenous Variables  $E = -1.8$  (fixed cost specification)

Nesting Parameter	Market	$\Delta$ 1 000 MB plan prices (in €)	$\Delta$ 10 000 MB plan prices (in €)	$\Delta$ radius (in km)	$\Delta$ download speeds (in Mbps)
0.0	3 firms, $\frac{4}{3}b$	0.143 (0.037)	0.777 (0.415)	-0.021 (0.005)	4.956 (0.381)
	4 firms, $b$	-0.801 (0.193)	-0.015 (0.392)	-0.019 (0.006)	0.346 (0.147)
0.2	3 firms, $\frac{4}{3}b$	0.101 (0.031)	0.777 (0.441)	-0.019 (0.005)	4.929 (0.430)
	4 firms, $b$	-0.815 (0.017)	-0.005 (0.413)	-0.017 (0.003)	0.314 (0.112)
0.4	3 firms, $\frac{4}{3}b$	0.057 (0.018)	0.776 (0.457)	-0.017 (0.005)	4.901 (0.460)
	4 firms, $b$	-0.845 (0.130)	0.008 (0.420)	-0.014 (0.001)	0.271 (0.089)
0.6	3 firms, $\frac{4}{3}b$	0.017 (0.009)	0.775 (0.473)	-0.015 (0.007)	4.875 (0.488)
	4 firms, $b$	-0.882 (0.252)	0.020 (0.406)	-0.010 (0.001)	0.220 (0.069)
0.8	3 firms, $\frac{4}{3}b$	-0.016 (0.046)	0.771 (0.536)	-0.014 (0.015)	4.851 (0.603)
	4 firms, $b$	-0.915 (0.465)	0.030 (0.351)	-0.006 (0.004)	0.165 (0.030)
0.9	3 firms, $\frac{4}{3}b$	0.040 (0.014)	0.754 (0.101)	0.014 (0.013)	2.715 (0.124)
	4 firms, $b$	-0.208 (0.035)	0.664 (0.050)	-0.015 (0.002)	0.208 (0.010)

per consumer per month. The monthly number of SMS per consumer stays around 250 since 2011. The picture looks quite different for mobile data consumption. As shown in figure 23, the average monthly consumption of data has been growing so far. The volume of monthly data rises from 100 MB in 2010 to 800 MB in 2015.

Mobile services are typically purchased under two types of contracts, postpaid and prepaid, and by two types of customers, residential and business. Postpaid contracts require the subscriber to pay a monthly fee for a certain allowance of mobile services, and they may or may not involve a multi-month commitment in the contract. In contrast, prepaid contracts require consumers to pay as they consume and do not involve long-term commitments. Postpaid contracts represent a large majority of the mobile market, 83% as of December 2015.<sup>34</sup>

<sup>34</sup>Source: ARCEP, Series Chronologiques Trimestrielles, April 2016.

Table 34: Impact of Adding Additional Bandwidth on Endogenous Variables  $E = -2.5$  (fixed cost specification)

Nesting Parameter	Market	$\Delta$ 1 000 MB plan prices (in €)	$\Delta$ 10 000 MB plan prices (in €)	$\Delta$ radius (in km)	$\Delta$ download speeds (in Mbps)
0.0	3 firms, $\frac{4}{3}b$	0.318 (0.048)	1.021 (0.276)	-0.061 (0.009)	5.457 (0.503)
	4 firms, $b$	-0.313 (0.086)	0.960 (0.151)	-0.043 (0.005)	0.781 (0.057)
0.2	3 firms, $\frac{4}{3}b$	0.242 (0.041)	1.048 (0.257)	-0.056 (0.006)	5.406 (0.547)
	4 firms, $b$	-0.392 (0.144)	0.988 (0.127)	-0.038 (0.005)	0.713 (0.054)
0.4	3 firms, $\frac{4}{3}b$	0.150 (0.031)	1.079 (0.225)	-0.051 (0.003)	5.341 (0.585)
	4 firms, $b$	-0.491 (0.181)	1.019 (0.090)	-0.031 (0.003)	0.626 (0.062)
0.6	3 firms, $\frac{4}{3}b$	0.050 (0.026)	1.109 (0.198)	-0.044 (0.002)	5.261 (0.622)
	4 firms, $b$	-0.601 (0.222)	1.050 (0.055)	-0.022 (0.002)	0.523 (0.071)
0.8	3 firms, $\frac{4}{3}b$	-0.046 (0.057)	1.131 (0.241)	-0.037 (0.007)	5.165 (0.753)
	4 firms, $b$	-0.704 (0.355)	1.077 (0.098)	-0.013 (0.002)	0.410 (0.049)
0.9	3 firms, $\frac{4}{3}b$	-0.045 (0.040)	0.962 (0.486)	-0.044 (0.044)	4.786 (0.417)
	4 firms, $b$	-0.535 (0.391)	1.087 (0.126)	-0.011 (0.011)	0.334 (0.083)

Table 35: Impact of Adding Additional Bandwidth on Endogenous Variables  $E = -3.2$  (fixed cost specification)

Nesting Parameter	Market	$\Delta$ 1 000 MB plan prices (in €)	$\Delta$ 10 000 MB plan prices (in €)	$\Delta$ radius (in km)	$\Delta$ download speeds (in Mbps)
0.0	3 firms, $\frac{4}{3}b$	0.441 (0.086)	0.635 (0.280)	-0.116 (0.015)	6.293 (0.851)
	4 firms, $b$	-0.127 (0.195)	0.949 (0.099)	-0.072 (0.015)	1.186 (0.080)
0.2	3 firms, $\frac{4}{3}b$	0.363 (0.079)	0.668 (0.241)	-0.110 (0.012)	6.235 (0.914)
	4 firms, $b$	-0.216 (0.221)	0.979 (0.058)	-0.064 (0.012)	1.103 (0.075)
0.4	3 firms, $\frac{4}{3}b$	0.257 (0.077)	0.707 (0.186)	-0.102 (0.010)	6.153 (0.990)
	4 firms, $b$	-0.331 (0.228)	1.014 (0.026)	-0.054 (0.006)	0.994 (0.083)
0.6	3 firms, $\frac{4}{3}b$	0.127 (0.075)	0.749 (0.131)	-0.092 (0.013)	6.038 (1.069)
	4 firms, $b$	-0.469 (0.239)	1.052 (0.085)	-0.042 (0.002)	0.856 (0.107)
0.8	3 firms, $\frac{4}{3}b$	-0.011 (0.048)	0.789 (0.132)	-0.080 (0.011)	5.873 (1.272)
	4 firms, $b$	-0.611 (0.338)	1.088 (0.180)	-0.029 (0.003)	0.693 (0.101)
0.9	3 firms, $\frac{4}{3}b$	-0.074 (0.031)	0.786 (0.337)	-0.073 (0.019)	5.518 (1.182)
	4 firms, $b$	-0.592 (0.449)	1.152 (0.199)	-0.021 (0.006)	0.588 (0.030)

Unlike residential customers, business customers can bargain over their contracts and, therefore, exert some buyer power. Residential customers represent 89% of the mobile market in 2015.<sup>35</sup> We focus only on the market for residential contracts.

<sup>35</sup>Source: ARCEP, Series Chronologiques Trimestrielles, April 2016.

Table 36: Impact of Adding Additional Bandwidth on Welfare  $E = -1.8$  (bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ CS	$\Delta$ PS	$\Delta$ TS
0.0	3 firms, $\frac{4}{3}b$	-0.029 (0.079)	0.206 (0.098)	0.177 (0.173)
	4 firms, $b$	0.705 (0.090)	-0.327 (0.034)	0.379 (0.108)
0.2	3 firms, $\frac{4}{3}b$	0.004 (0.095)	0.178 (0.095)	0.183 (0.188)
	4 firms, $b$	0.809 (0.200)	-0.396 (0.059)	0.413 (0.149)
0.4	3 firms, $\frac{4}{3}b$	0.041 (0.116)	0.147 (0.086)	0.188 (0.201)
	4 firms, $b$	0.944 (0.280)	-0.485 (0.101)	0.459 (0.183)
0.6	3 firms, $\frac{4}{3}b$	0.077 (0.150)	0.113 (0.069)	0.191 (0.218)
	4 firms, $b$	1.099 (0.365)	-0.585 (0.150)	0.514 (0.217)
0.8	3 firms, $\frac{4}{3}b$	0.108 (0.240)	0.082 (0.038)	0.190 (0.277)
	4 firms, $b$	1.258 (0.599)	-0.684 (0.306)	0.574 (0.294)
0.9	3 firms, $\frac{4}{3}b$	0.040 (0.012)	0.032 (0.008)	0.072 (0.005)
	4 firms, $b$	0.225 (0.050)	-0.151 (0.033)	0.074 (0.017)

Table 37: Impact of Adding Additional Bandwidth on Welfare  $E = -2.5$  (bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ CS	$\Delta$ PS	$\Delta$ TS
0.0	3 firms, $\frac{4}{3}b$	0.069 (0.219)	0.392 (0.044)	0.461 (0.244)
	4 firms, $b$	0.294 (0.305)	-0.028 (0.125)	0.266 (0.186)
0.2	3 firms, $\frac{4}{3}b$	0.134 (0.238)	0.346 (0.037)	0.480 (0.257)
	4 firms, $b$	0.404 (0.343)	-0.098 (0.135)	0.306 (0.212)
0.4	3 firms, $\frac{4}{3}b$	0.217 (0.251)	0.287 (0.030)	0.503 (0.265)
	4 firms, $b$	0.543 (0.360)	-0.188 (0.128)	0.355 (0.236)
0.6	3 firms, $\frac{4}{3}b$	0.311 (0.275)	0.215 (0.021)	0.526 (0.283)
	4 firms, $b$	0.704 (0.397)	-0.293 (0.127)	0.411 (0.272)
0.8	3 firms, $\frac{4}{3}b$	0.402 (0.396)	0.140 (0.029)	0.542 (0.371)
	4 firms, $b$	0.867 (0.602)	-0.403 (0.212)	0.464 (0.391)
0.9	3 firms, $\frac{4}{3}b$	0.213 (0.255)	0.121 (0.032)	0.334 (0.224)
	4 firms, $b$	0.598 (0.684)	-0.319 (0.326)	0.278 (0.358)

Table 38: Impact of Adding Additional Bandwidth on Welfare  $E = -3.2$  (bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ CS	$\Delta$ PS	$\Delta$ TS
0.0	3 firms, $\frac{4}{3}b$	0.288 (0.344)	0.360 (0.057)	0.649 (0.304)
	4 firms, $b$	0.219 (0.400)	0.039 (0.174)	0.258 (0.232)
0.2	3 firms, $\frac{4}{3}b$	0.357 (0.370)	0.318 (0.066)	0.675 (0.316)
	4 firms, $b$	0.312 (0.410)	-0.015 (0.164)	0.296 (0.253)
0.4	3 firms, $\frac{4}{3}b$	0.450 (0.382)	0.260 (0.066)	0.709 (0.326)
	4 firms, $b$	0.434 (0.405)	-0.086 (0.140)	0.348 (0.272)
0.6	3 firms, $\frac{4}{3}b$	0.563 (0.397)	0.186 (0.061)	0.749 (0.344)
	4 firms, $b$	0.585 (0.415)	-0.174 (0.118)	0.411 (0.303)
0.8	3 firms, $\frac{4}{3}b$	0.681 (0.518)	0.104 (0.083)	0.784 (0.439)
	4 firms, $b$	0.746 (0.578)	-0.273 (0.159)	0.473 (0.422)
0.9	3 firms, $\frac{4}{3}b$	0.606 (0.582)	0.083 (0.095)	0.689 (0.489)
	4 firms, $b$	0.679 (0.809)	-0.283 (0.273)	0.396 (0.537)



Table 39: Impact of Adding Additional Bandwidth on Welfare  $E = -1.8$  (fixed cost specification)

Nesting Parameter	Market	$\Delta$ CS	$\Delta$ PS	$\Delta$ TS
0.0	3 firms, $\frac{4}{3}b$	0.054 (0.067)	0.165 (0.099)	0.219 (0.162)
	4 firms, $b$	0.795 (0.087)	-0.362 (0.035)	0.433 (0.107)
0.2	3 firms, $\frac{4}{3}b$	0.087 (0.089)	0.142 (0.091)	0.228 (0.179)
	4 firms, $b$	0.898 (0.205)	-0.428 (0.060)	0.470 (0.152)
0.4	3 firms, $\frac{4}{3}b$	0.124 (0.115)	0.113 (0.080)	0.238 (0.194)
	4 firms, $b$	1.034 (0.292)	-0.514 (0.105)	0.520 (0.191)
0.6	3 firms, $\frac{4}{3}b$	0.164 (0.148)	0.083 (0.064)	0.246 (0.211)
	4 firms, $b$	1.192 (0.379)	-0.612 (0.154)	0.580 (0.227)
0.8	3 firms, $\frac{4}{3}b$	0.200 (0.209)	0.054 (0.043)	0.254 (0.252)
	4 firms, $b$	1.357 (0.593)	-0.709 (0.300)	0.649 (0.293)
0.9	3 firms, $\frac{4}{3}b$	0.124 (0.012)	0.047 (0.015)	0.171 (0.010)
	4 firms, $b$	0.322 (0.053)	-0.138 (0.026)	0.185 (0.027)

Table 40: Impact of Adding Additional Bandwidth on Welfare  $E = -2.5$  (fixed cost specification)

Nesting Parameter	Market	$\Delta$ CS	$\Delta$ PS	$\Delta$ TS
0.0	3 firms, $\frac{4}{3}b$	0.191 (0.102)	0.283 (0.054)	0.474 (0.143)
	4 firms, $b$	0.443 (0.223)	-0.098 (0.101)	0.345 (0.126)
0.2	3 firms, $\frac{4}{3}b$	0.259 (0.127)	0.244 (0.037)	0.503 (0.154)
	4 firms, $b$	0.555 (0.272)	-0.163 (0.120)	0.392 (0.155)
0.4	3 firms, $\frac{4}{3}b$	0.348 (0.145)	0.193 (0.026)	0.541 (0.161)
	4 firms, $b$	0.700 (0.299)	-0.248 (0.120)	0.453 (0.181)
0.6	3 firms, $\frac{4}{3}b$	0.454 (0.160)	0.129 (0.017)	0.583 (0.171)
	4 firms, $b$	0.871 (0.334)	-0.347 (0.122)	0.524 (0.214)
0.8	3 firms, $\frac{4}{3}b$	0.562 (0.202)	0.061 (0.007)	0.623 (0.199)
	4 firms, $b$	1.049 (0.493)	-0.452 (0.194)	0.597 (0.300)
0.9	3 firms, $\frac{4}{3}b$	0.484 (0.042)	0.034 (0.028)	0.518 (0.066)
	4 firms, $b$	0.844 (0.547)	-0.378 (0.283)	0.467 (0.265)

Table 41: Impact of Adding Additional Bandwidth on Welfare  $E = -3.2$  (fixed cost specification)

Nesting Parameter	Market	$\Delta$ CS	$\Delta$ PS	$\Delta$ TS
0.0	3 firms, $\frac{4}{3}b$	0.363 (0.121)	0.157 (0.039)	0.520 (0.094)
	4 firms, $b$	0.348 (0.266)	-0.064 (0.154)	0.284 (0.113)
0.2	3 firms, $\frac{4}{3}b$	0.438 (0.160)	0.123 (0.062)	0.561 (0.105)
	4 firms, $b$	0.447 (0.292)	-0.114 (0.158)	0.333 (0.136)
0.4	3 firms, $\frac{4}{3}b$	0.545 (0.185)	0.074 (0.078)	0.618 (0.113)
	4 firms, $b$	0.580 (0.301)	-0.180 (0.145)	0.401 (0.157)
0.6	3 firms, $\frac{4}{3}b$	0.682 (0.198)	0.010 (0.084)	0.692 (0.118)
	4 firms, $b$	0.748 (0.316)	-0.262 (0.131)	0.486 (0.186)
0.8	3 firms, $\frac{4}{3}b$	0.833 (0.220)	-0.062 (0.096)	0.771 (0.127)
	4 firms, $b$	0.934 (0.434)	-0.354 (0.166)	0.580 (0.269)
0.9	3 firms, $\frac{4}{3}b$	0.850 (0.158)	-0.072 (0.054)	0.778 (0.105)
	4 firms, $b$	0.914 (0.597)	-0.358 (0.246)	0.557 (0.351)

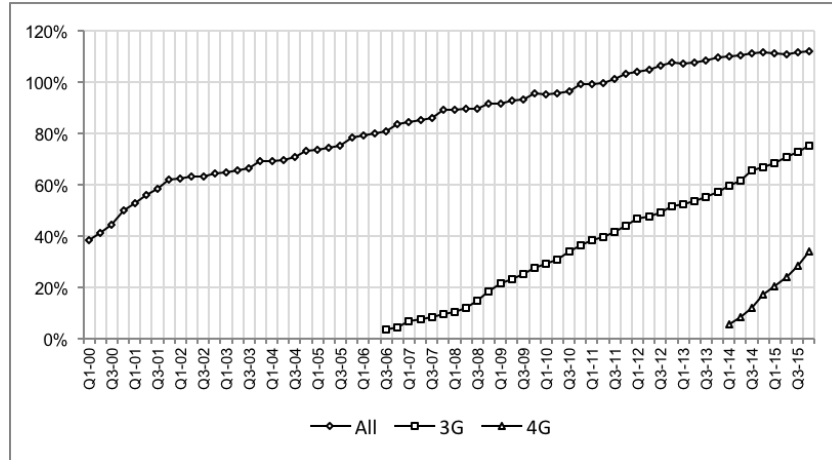
Table 42: Impact of Adding Additional Bandwidth on Consumer Surplus by Income Level  $E = -1.8$   
(bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ 10 %ile	$\Delta$ 30 %ile	$\Delta$ 50 %ile	$\Delta$ 70 %ile	$\Delta$ 90 %ile
0.0	3 firms, $\frac{4}{3}b$	0.002 (0.099)	-0.027 (0.136)	0.046 (0.130)	0.017 (0.088)	-0.237 (0.075)
	4 firms, $b$	-0.128 (1.098)	0.888 (0.053)	1.021 (0.122)	0.919 (0.173)	0.344 (0.170)
0.2	3 firms, $\frac{4}{3}b$	-0.016 (0.031)	0.016 (0.159)	0.094 (0.138)	0.060 (0.085)	-0.209 (0.068)
	4 firms, $b$	0.180 (0.991)	0.953 (0.188)	1.079 (0.082)	0.989 (0.024)	0.441 (0.086)
0.4	3 firms, $\frac{4}{3}b$	-0.012 (0.046)	0.063 (0.181)	0.143 (0.150)	0.102 (0.088)	-0.186 (0.070)
	4 firms, $b$	0.518 (0.775)	1.041 (0.315)	1.163 (0.244)	1.091 (0.155)	0.602 (0.085)
0.6	3 firms, $\frac{4}{3}b$	0.017 (0.113)	0.109 (0.220)	0.188 (0.176)	0.137 (0.108)	-0.171 (0.098)
	4 firms, $b$	0.833 (0.602)	1.140 (0.456)	1.263 (0.393)	1.219 (0.282)	0.844 (0.119)
0.8	3 firms, $\frac{4}{3}b$	0.057 (0.209)	0.151 (0.318)	0.226 (0.241)	0.161 (0.180)	-0.166 (0.226)
	4 firms, $b$	1.057 (0.715)	1.235 (0.768)	1.368 (0.673)	1.363 (0.529)	1.181 (0.188)
0.9	3 firms, $\frac{4}{3}b$	-0.013 (0.008)	-0.010 (0.005)	0.006 (0.006)	0.051 (0.014)	0.207 (0.025)
	4 firms, $b$	0.087 (0.071)	0.163 (0.046)	0.201 (0.043)	0.257 (0.044)	0.449 (0.070)

Table 43: Impact of Adding Additional Bandwidth on Consumer Surplus by Income Level  $E = -2.5$   
(bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ 10 %ile	$\Delta$ 30 %ile	$\Delta$ 50 %ile	$\Delta$ 70 %ile	$\Delta$ 90 %ile
0.0	3 firms, $\frac{4}{3}b$	-0.020 (0.071)	0.033 (0.340)	0.168 (0.261)	0.167 (0.198)	-0.068 (0.240)
	4 firms, $b$	-0.015 (0.703)	0.477 (0.325)	0.566 (0.209)	0.433 (0.138)	-0.402 (0.325)
0.2	3 firms, $\frac{4}{3}b$	-0.016 (0.100)	0.119 (0.347)	0.254 (0.251)	0.242 (0.180)	-0.029 (0.244)
	4 firms, $b$	0.153 (0.688)	0.584 (0.382)	0.679 (0.260)	0.538 (0.176)	-0.334 (0.374)
0.4	3 firms, $\frac{4}{3}b$	0.033 (0.235)	0.223 (0.348)	0.356 (0.235)	0.326 (0.162)	0.012 (0.258)
	4 firms, $b$	0.364 (0.618)	0.719 (0.417)	0.818 (0.286)	0.669 (0.197)	-0.235 (0.428)
0.6	3 firms, $\frac{4}{3}b$	0.131 (0.327)	0.341 (0.365)	0.467 (0.230)	0.414 (0.164)	0.047 (0.307)
	4 firms, $b$	0.603 (0.551)	0.873 (0.466)	0.973 (0.320)	0.818 (0.235)	-0.100 (0.533)
0.8	3 firms, $\frac{4}{3}b$	0.253 (0.481)	0.459 (0.485)	0.572 (0.296)	0.490 (0.257)	0.069 (0.510)
	4 firms, $b$	0.822 (0.676)	1.026 (0.673)	1.126 (0.474)	0.968 (0.416)	0.076 (0.910)
0.9	3 firms, $\frac{4}{3}b$	0.096 (0.182)	0.232 (0.310)	0.439 (0.170)	0.368 (0.139)	-0.262 (0.498)
	4 firms, $b$	0.578 (0.527)	0.703 (0.658)	0.905 (0.557)	0.795 (0.542)	-0.347 (1.299)

Figure 22: Penetration rate (ARCEP)



Note: Ratio of the number of active SIM cards (postpaid and prepaid excluding MtoM) to the population size.

Source: Own computations using data released by the regulator (ARCEP) - Series Chronologiques Trimestrielles (April 2016). Population data provided by INSEE.

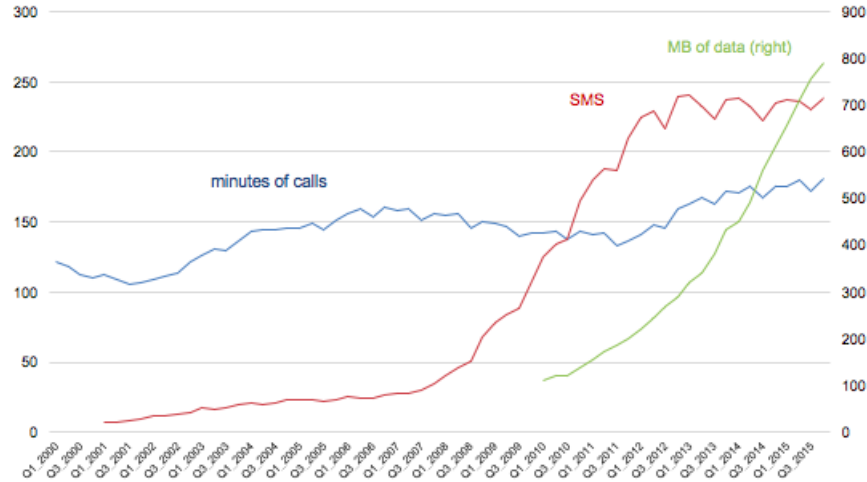
Table 44: Impact of Adding Additional Bandwidth on Consumer Surplus by Income Level  $E = -3.2$   
(bandwidth cost specification)

Nesting Parameter	Market	$\Delta$ 10 %ile	$\Delta$ 30 %ile	$\Delta$ 50 %ile	$\Delta$ 70 %ile	$\Delta$ 90 %ile
0.0	3 firms, $\frac{4}{3}b$	0.042 (0.279)	0.245 (0.467)	0.367 (0.347)	0.385 (0.279)	0.354 (0.250)
	4 firms, $b$	0.085 (0.688)	0.386 (0.468)	0.432 (0.338)	0.294 (0.250)	-0.416 (0.365)
0.2	3 firms, $\frac{4}{3}b$	0.094 (0.415)	0.331 (0.482)	0.449 (0.350)	0.453 (0.280)	0.385 (0.281)
	4 firms, $b$	0.202 (0.691)	0.492 (0.488)	0.535 (0.344)	0.382 (0.249)	-0.372 (0.391)
0.4	3 firms, $\frac{4}{3}b$	0.191 (0.510)	0.446 (0.480)	0.555 (0.335)	0.539 (0.270)	0.423 (0.317)
	4 firms, $b$	0.363 (0.664)	0.629 (0.489)	0.669 (0.329)	0.496 (0.235)	-0.309 (0.429)
0.6	3 firms, $\frac{4}{3}b$	0.337 (0.573)	0.588 (0.483)	0.682 (0.323)	0.637 (0.271)	0.462 (0.373)
	4 firms, $b$	0.568 (0.633)	0.794 (0.496)	0.828 (0.319)	0.632 (0.239)	-0.223 (0.519)
0.8	3 firms, $\frac{4}{3}b$	0.513 (0.743)	0.739 (0.595)	0.812 (0.394)	0.730 (0.374)	0.487 (0.553)
	4 firms, $b$	0.789 (0.768)	0.970 (0.636)	0.992 (0.416)	0.775 (0.378)	-0.109 (0.871)
0.9	3 firms, $\frac{4}{3}b$	0.427 (0.750)	0.665 (0.688)	0.776 (0.418)	0.676 (0.423)	0.345 (0.670)
	4 firms, $b$	0.712 (0.852)	0.896 (0.839)	0.966 (0.577)	0.745 (0.586)	-0.278 (1.422)

Table 45: Impact of Adding Additional Bandwidth on Consumer Surplus by Income Level  $E = -1.8$   
(fixed cost specification)

Nesting Parameter	Market	$\Delta$ 10 %ile	$\Delta$ 30 %ile	$\Delta$ 50 %ile	$\Delta$ 70 %ile	$\Delta$ 90 %ile
0.0	3 firms, $\frac{4}{3}b$	-0.001 (0.070)	-0.027 (0.067)	0.013 (0.085)	0.063 (0.102)	0.318 (0.116)
	4 firms, $b$	-0.119 (1.144)	0.908 (0.030)	1.016 (0.152)	0.980 (0.156)	0.829 (0.125)
0.2	3 firms, $\frac{4}{3}b$	-0.009 (0.014)	0.013 (0.085)	0.057 (0.096)	0.105 (0.114)	0.348 (0.142)
	4 firms, $b$	0.200 (1.020)	0.970 (0.141)	1.071 (0.060)	1.048 (0.046)	0.928 (0.045)
0.4	3 firms, $\frac{4}{3}b$	0.004 (0.046)	0.055 (0.107)	0.102 (0.113)	0.147 (0.131)	0.381 (0.170)
	4 firms, $b$	0.544 (0.789)	1.054 (0.272)	1.153 (0.228)	1.152 (0.199)	1.098 (0.130)
0.6	3 firms, $\frac{4}{3}b$	0.037 (0.095)	0.097 (0.141)	0.145 (0.143)	0.187 (0.160)	0.417 (0.196)
	4 firms, $b$	0.863 (0.606)	1.151 (0.413)	1.252 (0.383)	1.284 (0.335)	1.358 (0.179)
0.8	3 firms, $\frac{4}{3}b$	0.076 (0.168)	0.135 (0.217)	0.182 (0.210)	0.221 (0.225)	0.455 (0.192)
	4 firms, $b$	1.087 (0.707)	1.243 (0.713)	1.357 (0.669)	1.437 (0.579)	1.726 (0.159)
0.9	3 firms, $\frac{4}{3}b$	0.016 (0.010)	0.054 (0.009)	0.096 (0.008)	0.161 (0.015)	0.341 (0.063)
	4 firms, $b$	0.120 (0.091)	0.233 (0.058)	0.301 (0.049)	0.383 (0.043)	0.613 (0.034)

Figure 23: Monthly usage of voice, SMS and data per subscriber



Note: Monthly usage is estimated as quarterly volume divided by 3. This monthly volume is divided by the number of active SIM cards (postpaid and prepaid excluding MtoM) at the end of the quarter.

Source: Own computations using data released by the regulator (ARCEP) - Series Chronologiques

Table 46: Impact of Adding Additional Bandwidth on Consumer Surplus by Income Level  $E = -2.5$   
(fixed cost specification)

Nesting Parameter	Market	$\Delta$ 10 %ile	$\Delta$ 30 %ile	$\Delta$ 50 %ile	$\Delta$ 70 %ile	$\Delta$ 90 %ile
0.0	3 firms, $\frac{4}{3}b$	-0.031 (0.082)	-0.030 (0.135)	0.054 (0.164)	0.237 (0.170)	0.961 (0.090)
	4 firms, $b$	0.023 (0.771)	0.521 (0.186)	0.562 (0.124)	0.522 (0.106)	0.386 (0.107)
0.2	3 firms, $\frac{4}{3}b$	-0.014 (0.042)	0.049 (0.142)	0.137 (0.165)	0.315 (0.181)	1.018 (0.074)
	4 firms, $b$	0.207 (0.709)	0.624 (0.256)	0.673 (0.192)	0.628 (0.170)	0.467 (0.180)
0.4	3 firms, $\frac{4}{3}b$	0.042 (0.130)	0.147 (0.146)	0.239 (0.164)	0.410 (0.187)	1.094 (0.073)
	4 firms, $b$	0.430 (0.603)	0.755 (0.303)	0.811 (0.236)	0.766 (0.213)	0.592 (0.245)
0.6	3 firms, $\frac{4}{3}b$	0.141 (0.181)	0.258 (0.162)	0.352 (0.173)	0.517 (0.198)	1.188 (0.073)
	4 firms, $b$	0.676 (0.511)	0.904 (0.360)	0.968 (0.285)	0.929 (0.263)	0.771 (0.314)
0.8	3 firms, $\frac{4}{3}b$	0.258 (0.269)	0.368 (0.243)	0.461 (0.241)	0.621 (0.246)	1.290 (0.140)
	4 firms, $b$	0.895 (0.607)	1.054 (0.549)	1.125 (0.446)	1.100 (0.425)	1.012 (0.445)
0.9	3 firms, $\frac{4}{3}b$	0.157 (0.155)	0.255 (0.184)	0.353 (0.167)	0.504 (0.107)	1.440 (0.740)
	4 firms, $b$	0.655 (0.540)	0.778 (0.598)	0.910 (0.553)	0.922 (0.552)	0.967 (0.407)

Table 47: Impact of Adding Additional Bandwidth on Consumer Surplus by Income Level  $E = -3.2$   
(fixed cost specification)

Nesting Parameter	Market	$\Delta$ 10 %ile	$\Delta$ 30 %ile	$\Delta$ 50 %ile	$\Delta$ 70 %ile	$\Delta$ 90 %ile
0.0	3 firms, $\frac{4}{3}b$	-0.101 (0.132)	-0.054 (0.148)	0.144 (0.235)	0.531 (0.230)	1.625 (0.144)
	4 firms, $b$	0.118 (0.641)	0.371 (0.257)	0.384 (0.222)	0.379 (0.196)	0.409 (0.123)
0.2	3 firms, $\frac{4}{3}b$	-0.056 (0.057)	0.034 (0.158)	0.232 (0.258)	0.609 (0.271)	1.680 (0.105)
	4 firms, $b$	0.246 (0.608)	0.479 (0.293)	0.493 (0.248)	0.473 (0.225)	0.466 (0.177)
0.4	3 firms, $\frac{4}{3}b$	0.029 (0.070)	0.152 (0.155)	0.350 (0.266)	0.718 (0.300)	1.764 (0.106)
	4 firms, $b$	0.416 (0.550)	0.619 (0.307)	0.634 (0.252)	0.602 (0.238)	0.558 (0.234)
0.6	3 firms, $\frac{4}{3}b$	0.162 (0.086)	0.298 (0.154)	0.495 (0.271)	0.855 (0.317)	1.883 (0.122)
	4 firms, $b$	0.627 (0.497)	0.788 (0.324)	0.804 (0.259)	0.762 (0.258)	0.697 (0.301)
0.8	3 firms, $\frac{4}{3}b$	0.327 (0.137)	0.456 (0.217)	0.648 (0.331)	0.997 (0.342)	2.018 (0.172)
	4 firms, $b$	0.850 (0.592)	0.968 (0.450)	0.984 (0.364)	0.939 (0.376)	0.887 (0.430)
0.9	3 firms, $\frac{4}{3}b$	0.362 (0.271)	0.474 (0.279)	0.637 (0.343)	0.980 (0.253)	2.127 (0.713)
	4 firms, $b$	0.804 (0.736)	0.935 (0.649)	0.975 (0.528)	0.929 (0.545)	0.896 (0.510)

### C.1.2 Market structure

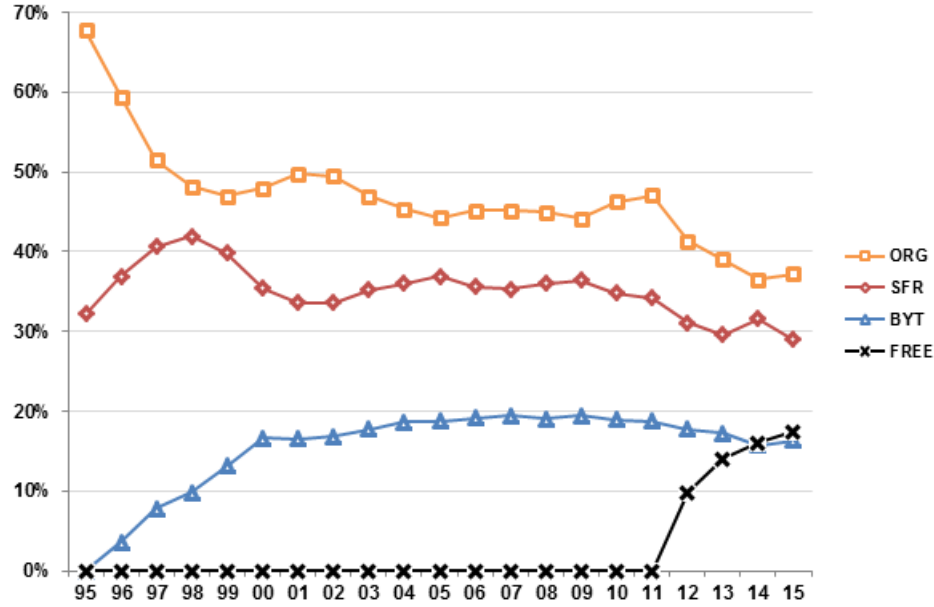
During the period we study, the French mobile industry comprised four mobile network operators (MNO): Orange (ORG), SFR-Numericable (SFR), Bouygues Telecom (BYT) and Free Mobile (FREE). FREE entered the market in January 2012 and experienced a sharp increase in market share, up to 16% in four years (see figure 24). Right before FREE's entry, the three incumbents operators introduced their own low-cost brands: SOSH for ORG, RED for SFR and B&YOU for BYT. Contracts sold under these brands are postpaid without commitment.

MNOs own their networks contrary to mobile virtual network operators (MVNO) who typically rent access to MNOs' networks. Providing network access to MVNO is mandatory and enforced by regulation, but the access charge is freely negotiated with the MNO. According to figures from the national regulator ARCEP, there are more than 30 MVNOs in France in 2015, representing 10.6% of the mobile

market, hosted by ORG, SFR and BYT.

On top of hosting MVNOs, MNOs also share their network infrastructure, particularly in less dense areas. The next section presents the features of network sharing among MNOs.

Figure 24: Evolution of postpaid residential market shares



Source: World Cellular Information Services (Ovum).

### C.1.3 Network sharing

Network sharing occurs when a network operator shares a part or the whole of its network resources with a retail competitor. These resources can be passive network elements, such as antenna supports, masts, or active network elements, such as frequency bandwidths. Passive network sharing affects coverage differentiation but not necessarily quality differentiation. It typically consists of operators sharing the same tower or the cost of electricity. In general, it is any agreement between MNOs that do not involve the sharing of available frequency bandwidths.

In contrast, under active network sharing (Radio Access Network-Sharing), operators cannot differentiate in terms of quality, defined as the frequency bandwidth available per customer. Typically, it consists of the sharing of frequency bands and core network elements. Roaming agreements, whereby an operator's customers rely on the network of a host operator to communicate, is the highest level of active network sharing. It does not offer any possibility for quality or coverage differentiation.

Table 48 below presents the network sharing agreements reached between 2012 and 2015. These agreements apply to two types of areas according to their population density. "White Areas" or "Zones Blanches" correspond to areas where population density is so low that network deployment by

several operators is not profitable. They are identified by the regulator on the basis of criteria which can change. These areas are typically rural, and represent roughly 1% of the population and 10% of the national surface. Only ORG, SFR and BYT have invested in these areas.

The most widespread network technologies in the White Areas are 2G, EDGE and GPRS.<sup>36</sup> However, 3G technology has been recently deployed. As of the end of December 2015, half of ORG and BYT's networks in these areas were covered by 3G, compared to 35% for SFR. In general, only one operator invests in a given White Area, and 64% of antennas in these areas are involved in a roaming agreement. Rival operators roam over the network of the only operator which invests in the area. As a result, there is no quality differentiation. For the remaining 36% of antennas, operators share passive network elements.

At the national level, FREE's customers can roam over ORG's 2G and 3G networks as long as there is no FREE antenna nearby. As a result, FREE cannot differentiate from ORG on 2G and 3G technologies, except when a FREE antenna is nearby its customer. In addition, FREE does not have access to networks in ZBs where BYT or SFR is the leader. MVNOs have roaming agreements with their hosts and therefore cannot differentiate in terms of quality or coverage.

Our model focuses on high-density areas to avoid the need to explicitly model network sharing.

Table 48: Network sharing agreements 2012-2015

		FREE	ORG	SFR	BYT
Zone Blanche	Roaming: 64% of 2G & 3G antenna			↔	
	Passive sharing: 36% of antenna			↔	
Low Density	2G and 3G RAN-Sharing	✗	✗		↔
	4G Roaming	✗	✗		→
High Density		✗	✗	✗	✗
National	Passive sharing			↔	
	2G and 3G Roaming		→	✗	✗

Source: Summary from discussions with ORG's experts (HOSPITAL Jean-Jacques).

Note: ↔: two-way (reciprocal) sharing,  $A \rightarrow B$  one-way sharing hosted by operator B.

#### C.1.4 Infrastructure data

Operators are likely to worry less about providing high-quality coverage to sparsely populated areas. As some municipalities have large unpopulated areas, using raw land area might overstate the land area that operators need to cover (at least, with high quality service). Thus, we use an adjusted measure of land area for each municipality.

Our adjusted land area is based on the contraharmonic mean of population density (integrating across space) within each commune. Equivalently, we can consider the population density in the neighborhood of an individual resident, and then we average over residents.

<sup>36</sup>EDGE and GPRS are suitable for low speed mobile data services.

A commune’s effective land area is defined as its population divided by this contraharmonic mean population density.

The population density source was the Gridded Population of the World, v4 (<https://sedac.ciesin.columbia.edu/data/collection/gpw-v4>). Municipality (commune) borders were obtained from [www.data.gouv.fr](http://www.data.gouv.fr).

## C.2 Tariff data

### C.2.1 Characteristics of Mobile Contracts

Mobile operators offer a variety of contracts that rely on voice and data services that can be bundled with fixed telephony, fixed broadband or television. A typical mobile contract comprises a fixed price (prepaid or postpaid) for given allowances (data, voice and SMS), prices per unit above allowances, commitment duration and handset subsidy.

Mobile contracts typically involve a fixed price for a given allowance, and may involve charges per unit for usage above allowances. Such extra charges are typically associated with plans with small allowances. Some contracts include unlimited SMS and voice allowances, and for contracts with large data allowances, further consumption may be blocked or throttled as consumers hit the limit of their data allowance. In these cases, customers willing to continue data consumption beyond their allowance have to purchase add-ons as one-shot data packages, valid until the end of the contract, or recurrent data packages with a price discount.

For contracts with a data throttling limit, the download speed is reduced for usage above allowance if no add-on is purchased. The maximal download speed under throttling is typically 128 Kbps. With this download speed, it would take over half an hour to download a 30 MB file, compared to 2 minutes under a theoretical unthrottled speed of 2 Mbps in a 3G network, and 24 seconds given a moderate 4G download speed of 10 Mbps. Basically, only emails and light web pages can be opened under throttling. As presented in table 49 below, this download speed is not always specified by operators in their contracts. When it is, it may depend on the location of the usage (local or abroad). The actual download speed experienced by customers is function of the number of simultaneous users, its location and handset. In our demand model, however, we assume that any data consumption over the data limit yields a speed of exactly 128 Kbps.

Mobile tariffs may include a discount for multi-month commitments, a premium for handset subsidy and additional discounts for purchasing fixed or television services on top of mobile services. Customers under commitment can terminate their contracts pursuant to a 2008 act labeled “*Loi Chatel*.” According to this act, customers that have been under commitment for more than 12 months can terminate their contract by paying a penalty equal to the quarter of the bill over the remaining commitment period. If the customer has spent less than 12 months, she has to pay the whole remaining bill until the twelfth month, and the quarter of the remaining.

There is no penalty for changing contract with the same brand. However, customers switching between two brands of the same operator may incur a penalty if they were initially under commitment. This is typically the case for ORG’s customers switching from standard ORG contracts to the low-cost brand

SOSH. Operators introduced contracts without commitment in 2011. FREE does not offer long term commitment contracts, nor handset subsidy.

Table 49: Maximal download speed under throttling (Kbps)

Operator	National	Roaming
ORG	128*	ns
SFR	ns	ns
BYT	128	32
FREE	ns	ns

\*:except video streaming.  
ns  $\equiv$  not specified.  
Source: operators' contracts

### C.2.2 Tariff dataset

We collected data on contracts released between November 2013 and October 2015 along with their characteristics. It includes postpaid contracts from the four MNOs and the largest MVNO (EI Telecom) as well as their prepaid contracts.<sup>37</sup> Promotional contracts, typically released during summer and Christmas, are not included in the dataset.

Characteristics of contracts have been retrieved from operators' quarterly catalogues. Contract characteristics include tariff, voice and data limits, price per unit of consumption above allowance, international voice or data roaming, handset subsidy, length of commitment, bundling with fixed services.

## C.3 Customer data

### C.3.1 Choice and usage data

Contract choice and usage data come from ORG's customer database. We therefore only observe choice and usage data for ORG and not customers of the other firms, an issue we address in Section 5. This database contains observations of all postpaid residential customer choices and data/voice usage in October 2015. Customers can cancel, keep, renew or choose a new contract with ORG. Table 50 presents the number of subscribers according to their status.

Table 50: Number of subscribers

Subscribers	cancel (%)	keep (%)	renew (%)	new (%)	Total (%)
14 992 631	0.9	94.5	3.6	1.1	100

<sup>37</sup>ORG's contracts include not only those that are sold through its main brand, but also others sold under alternative brands such as SOSH, BNP Paribas Mobile, FNAC Mobile, Click Mobile, Carrefour Mobile, etc.



The contract data contain information on the contract and handset characteristics,<sup>38</sup> as well as customer characteristics, including the residence of the customer, which we use to construct market shares. Usage data include SMS, voice, and data consumption.

### C.3.2 Socio-economic data

Socio-economic characteristics are generated from the 2011's population census conducted by the French office of statistics (INSEE). These statistics include the deciles of income at municipality level. Income is measured as the fiscal revenue of households living in a given municipality in 2011.

## C.4 Quality data

Quality measures are constructed using download speed test results provided by Ookla. Test results come from users who use Ookla's free Internet speed test, called simply "Speedtest," using a web browser or within an app. Using speed tests in France in the fourth quarter of 2015 yields 1 056 285 individual speed tests. Each speed test records the download speed, mobile network operator, and the user's location. We aggregate speed tests by averaging measured download speeds over tests for a given operator and geographic market, yielding an operator-market quality measure. An operator-market quality measure is, on average, an average of 284 test results.

## C.5 Statistical inputs

This section presents the main statistical inputs of the estimation procedure: market characteristics and the choice set.

### C.5.1 Market characteristics

This section starts with the definition of markets, and then presents the construction of market size and income distribution within markets. A market is defined as the geographical level at which quality measures can be reliable. Specifically, we need a market definition that yields sufficient speed tests to construct accurate measures of quality. As a result, we define market as either a large (urban) municipality, that is with more than 10 000 inhabitants. This definition collapses the initial 36 664 municipalities into 592 markets, and we discard three of these markets due to insufficient speed test results for at least one operator in the market.

Market size is defined as the population above 12 years old using mobile communications. Table 51 reports the share of mobile users in the population above age 12 according the size of their municipalities of residence. Monthly population size is estimated using the geometric mean of the annual population growth rates obtained from INSEE population data.

Income distribution within markets was presented in section C.3.2. This distribution corresponds to income per capita in 2011.

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<sup>38</sup>In some cases, information on prices, voice and data limits is not consistent with our data from tariffs catalogues. We change these characteristics to be in line with those from tariffs catalogues.

Table 51: Share of mobile users among population above 12

	2011	2012	2013	2014	2015
< 2 000 inhab.	82	85	85	86	91
2 000 - 20 000 inhab.	83	85	87	84	89
20 - 100 000 inhab.	81	89	87	90	91
> 100 000 inhab.	87	89	90	92	93
Paris	88	91	94	92	96
<b>France</b>	<b>84</b>	<b>89</b>	<b>89</b>	<b>89</b>	<b>92</b>

Source: CREDOC Surveys

### C.5.2 Choice set

We use tariff data presented in section C.2.2 to construct the choice set which includes the postpaid contracts of each MNO, the postpaid contracts of the largest MVNO (El Telecom), or the outside option of not using mobile communications.

Table 52 presents the market shares of the alternatives in the choice set during our sample period. Contracts included in the choice set are available in all markets; however, quality differs across markets. We construct market-specific choice sets by adding the quality data measured in each market. Quality of postpaid MVNO offers is estimated as the simple average of the quality of the hosts (BYT, ORG and SFR).

Table 52: Aggregate market shares of alternatives (%)

market size (millions)	Alternatives							Total
	ORG	SFR	BYT	FREE	MVNO	Prepaid	Non-users	
56.5	26.7	20.9	11.7	12.4	13.0	7.2	8.0	100

As noted previously, the choice set would consist of more than 1 700 alternatives if we included all contracts listed in the tariffs catalog, making the demand estimation cumbersome. We overcome this hurdle by focusing on data limits as the most important attribute. Indeed, recent investment in mobile networks in France are primarily made in order to improve the supply of mobile data services. Therefore, we employ a size reduction strategy that removes the less relevant contract's components and focus on the most significant variation in data limits.

Specifically, we define categories of contracts according to their level of data limits: less than 500 MB, 500–3 000 MB, 3 000–7 000 MB and more than 7 000 MB. These thresholds have been chosen following discussions with the industry experts and the statistical distribution of chosen contracts. The second data limit category—that is, contracts with 500–3 000 MB—have been further split according to their voice allowance: unlimited or not, making a total of five categories of contracts. Low data limit contracts typically do not have unlimited voice, and high data limit contracts typically come with

unlimited voice allowance, so we do not split these categories by the voice limit.

Next, we exclude contracts bundled with fixed broadband or television, as they generally come with their mobile standalone version. We then choose the least expensive contract per category as the category’s representative contract. Some customers keep old contracts that are no longer available, so we fill these missing data by using the most chosen old contracts within the same category. While some contracts with handset subsidies have corresponding standalone versions, some do not. We adjust the prices of these latter contracts using data on the price of handsets and the upfront cost required by Orange. These data were collected for both iPhone and Samsung, the two most popular handsets. We then distribute the handset cost over 24 months, and update the monthly contract price by subtracting off the monthly cost of the handset. In addition, we assume that Orange’s handset subsidies apply to other operators because we do not observed their upfront costs.

### **C.5.3 Mean data consumption**

We use the Orange customer data presented in section C.3.1 to construct market-level measures of mean data consumption for each Orange contract. Note that because we only observe data consumption for consumers of Orange contracts, we cannot construct these measures for contracts of other firms. Contracts are aggregated based on the associated data limit and whether or not the voice allowance is unlimited, as detailed in section C.5.2. Constructing market-contract-level measures of mean data consumption is complicated by the fact that the aggregated contracts in the choice set incorporate contracts with different data limits. For example, the Orange 4 000 MB data limit contract in the choice set incorporates contracts in the customer data with data limits ranging from 3 000 MB to 7 000 MB.

Since we use the mean data consumption in the data to discipline the predicted data consumption in our demand model, which is based on the data limit from the choice set, simply averaging the data consumption observed in the customer data can lead to biased estimates in the data consumption coefficients. For example, using the same 4 000 MB aggregated contract as before, if many customers in this category have contracts with data limits above 4 000 MB, they may consume well above 4 000 MB without hitting their data limit. Simply averaging data consumption for this category might give mean data consumption above 4 000 MB, which our demand estimation would interpret as either being insensitive to download speeds (because they are willing to consume even at the very slow throttled speed) or heavily weight the amount of data consumed (because they are consuming large amounts of data despite the slow throttled speed). In fact, it might be that neither of those conclusions is consistent with consumers’ data consumption decisions under their actual data limit.

In order to account for the fact that realized data consumption decisions reflect heterogeneous data limits within a single data limit category, we construct the following measure of mean market shares,

$\bar{x}_{jm}$ ,<sup>39</sup>

$$\bar{x}_{jm} = \frac{1}{|\mathcal{I}_j|} \sum_{i \in \mathcal{I}_j} \min \left\{ \frac{x_i}{\bar{x}_i}, 1 \right\} \bar{x}_j + \max \{0, x_i - \bar{x}_i\},$$

where  $\mathcal{I}_j$  is the set of consumers with contracts that aggregate to  $j$ ,  $x_i$  is consumer  $i$ 's data consumption, and  $\bar{x}_i$  is her data limit. The value  $\bar{x}_j$  is the data limit associated with the aggregate contract  $j$ . We separate these two terms rather than simply using the fraction of the data limit consumed times the aggregated contract's data limit because, conditional on bypassing the data limit, the data limit is irrelevant for further data consumption.

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<sup>39</sup>For contracts belonging to the group characterized by data limits of less than 500 MB, we impose that consumption cannot be greater than the data limit. For this category of contracts, add-on data packages are a common way of increasing one's data limit. Since we do not observe data package purchases, we simply assume that any consumer that consumed above the data limit did so with a purchased data package and that without one, he would have consumed as much as the data limit allowed. Our demand model reflects this, imposing that contracts in this category cannot consume above the data limit at a reduced speed (as they are able to do for high data limit contracts).

Table 53: Notation

Symbol	Description
$B$	bandwidth (hertz)
$c_u$	cost per user
$c_{fc,m}$	cost per base station at zero bandwidth
$c_{bw}$	cost per base station per unit of bandwidth operated
$D$	mass of consumers per unit area that are downloading
$f$	indexes firms
$F$	used for CDFs
$g$	density of consumers at given radius
$i$	indexes consumers
$j$	indexes products
$\mathcal{J}$	product set
$m$	indexes markets
$p_j$	price of contract $j$
$\bar{Q}$	channel capacity (Mbits/second)
$q$	data transmission speed as function of distance
$Q$	download speed (Mbits/second)
$Q^L$	throttled download speed
$Q^D$	demand requests (Mbits/second)
$r$	distance from antenna (km)
$R$	radius of area served by one base station (km)
$s_j$	market share
$\mathbf{s}$	vector of market shares
$u$	utility from data consumption over course of month
$v$	utility of a contract
$x$	monthly data consumption
$\gamma_m$	data transmission efficiency in market $m$
$\varepsilon_{ij}$	idiosyncratic, consumer-contract-level demand shock
$\theta$	demand parameters
$\sigma$	nesting parameter
$\theta_{pi}$	price coefficient
$\theta_{p0}$	parameter controlling the mean of the price coefficient
$\theta_{pz}$	parameter controlling the heterogeneity in the price coefficient
$\theta_v$	coefficient on dummy for unlimited voice
$\theta_O$	coefficient on dummy for Orange products
$\theta_c$	opportunity cost of time spent downloading data coefficient
$\theta_{di}$	parameter of log-normal distribution that defines distribution from which a consumer's utility of data consumption is drawn
$\theta_{d0}$	parameter controlling the mean of $\theta_{di}$
$\theta_{dz}$	parameter controlling the heterogeneity in $\theta_{di}$
$\vartheta_i$	random shock to consumer's utility of data consumption, distributed exponentially with parameter $\theta_{di}$
$\xi_{jm}$	market-level demand shock