

Briefing Document: Fundamentals of Database Searching

1. Searching as a Fundamental Database Function

Searching is the most frequently executed operation within a database system, making efficient search techniques crucial for database performance.

- "Searching is the most common operation performed by a database system."
- SQL's **SELECT** statement is one of the most complex and versatile commands, often involving searches.
- "In SQL, the SELECT statement is arguably the most versatile / complex."

2. Linear Search: The Baseline Algorithm

Linear search serves as the foundational method for evaluating search efficiency. It operates by sequentially examining each element in a dataset until the target value is found or the dataset is exhausted.

- "Baseline for efficiency is Linear Search."
- The process involves:
 - Starting at the first element and checking each sequentially.
 - Stopping when the target value is found or the end of the dataset is reached.

The worst-case scenario involves examining every element, leading to a time complexity of $O(n)$.

- "Worst case: target is not in the array; n comparisons."
- "Therefore, in the worst case, linear search is $O(n)$ time complexity."

3. Impact of Data Storage Structures on Search Performance

Databases rely on two primary data storage methods, each with distinct advantages and drawbacks:

Arrays (Contiguously Allocated Lists):

- Enable fast random access since elements are stored sequentially in memory.
- Slow insertion performance due to the need to shift elements when inserting in the middle.
- "Arrays are faster for random access, but slow for inserting anywhere but the end."
- Example: Inserting an element may require shifting multiple records.

Linked Lists:

- Facilitate quick insertion and deletion at any position, as they only require pointer updates.

- Slower random access because traversal must begin at the head of the list.
- "Linked Lists are faster for inserting anywhere in the list, but slower for random access."
- Example: Extra memory is needed to store pointers.

Comparison Summary:

- Arrays: Fast for random access but slow for insertions.
- Linked Lists: Efficient for insertions but slow for random access.

4. Binary Search: A More Efficient Searching Method

Binary search provides a significant improvement over linear search but requires a sorted dataset, typically stored in an array or a structure supporting rapid access.

- "Input: array of values in sorted order, target value."

The algorithm reduces the search space by half in each step, adjusting **left** and **right** pointers accordingly.

- "Worst case: target is not in the array; $\log_2 n$ comparisons."
- "Therefore, in the worst case, binary search is $O(\log_2 n)$ time complexity."

Since binary search exhibits logarithmic time complexity, search performance improves drastically for large datasets compared to linear search.

5. Complexities of Searching in Database Systems

Searching in databases stored on disk presents additional challenges. Data is often stored by column IDs and values.

- "Assume data is stored on disk by column id's value."

Efficient ID-based searches are possible, but searching by non-key attributes (e.g., **specialVal**) requires a full column scan.

- "Searching for a specific id = fast."
- "But what if we want to search for a specific specialVal?"
- "Only option is a linear scan of that column."

A key limitation is that physical sorting on disk cannot accommodate multiple attributes without duplicating data, which is space-inefficient.

- "Can't store data on disk sorted by both id and specialVal (at the same time)."
- "Data would have to be duplicated → space inefficient."

6. The Role of Indexing in Enhancing Search Performance

To address the inefficiencies of linear scans for non-key attributes, external data structures—indexes—are necessary.

- "We need an external data structure to support faster searching by specialVal than a linear scan."

Two initial indexing approaches are explored:

Sorted Array of Tuples:

- Enables binary search for efficient lookups.
- However, insertions are slow due to the need to maintain order.
- "An array of tuples (specialVal, rowNum) sorted by specialVal."
- "Binary Search allows quick lookup, but insertions are slow."

Sorted Linked List of Tuples:

- Provides quick insertions but requires a full scan for searches.
- "A linked list of tuples (specialVal, rowNum) sorted by specialVal."
- "Search is slow (linear scan), but insertions are fast."

7. Advancing Towards More Efficient Data Structures: Binary Search Trees

A well-designed indexing structure should optimize both search and insertion performance. This leads to the consideration of **Binary Search Trees (BSTs)**.

- "Something with Fast Insert and Fast Search?"
- "Binary Search Tree: A binary tree where every node in the left subtree is smaller than its parent, and every node in the right subtree is greater."