

```
In [32]: import pandas as pd
import xlrd
```

```
In [33]: workbook = pd.read_stata('lawschs1_1.dta')
```

```
In [34]: workbook
```

Out[34]:

	lsat	gpa	race	resident	college	year	gender	admit	black	hispanic	asian
0	156.0	3.71	White	0.0	Arizona State	2006	0.0	1.0	0.0	0.0	0
1	161.0	3.85	White	0.0	Arizona State	2006	0.0	1.0	0.0	0.0	0
2	160.0	3.20	White	0.0	Arizona State	2006	1.0	0.0	0.0	0.0	0
3	132.0	2.95		1.0	Arizona State	2006	1.0	0.0	0.0	0.0	0
4	159.0	3.49	White	0.0	Arizona State	2006	1.0	0.0	0.0	0.0	0
...
124552	179.0	3.72	White	1.0	Washington	2006	0.0	1.0	0.0	0.0	0
124553	179.0	3.96	Asian	1.0	Washington	2006	0.0	1.0	0.0	0.0	1
124554	179.0	3.97	White	0.0	Washington	2006	0.0	1.0	0.0	0.0	0
124555	180.0	3.29	White	0.0	Washington	2006	1.0	1.0	0.0	0.0	0
124556	180.0	3.53	White	1.0	Washington	2006	1.0	1.0	0.0	0.0	0

124557 rows × 15 columns

```
In [35]: workbook = workbook.replace(r'^\s*$', '*', regex=True)
```

```
In [36]: workbook = workbook.drop(['black', 'hispanic', 'asian', 'white', 'missingr
```

```
In [37]: workbook.fillna('*').to_csv('lawschs1_1.csv')
```

In [38]: workbook

Out[38]:

	lsat	gpa	race	resident	college	year	gender	admit
0	156.0	3.71	White	0.0	Arizona State	2006	0.0	1.0
1	161.0	3.85	White	0.0	Arizona State	2006	0.0	1.0
2	160.0	3.20	White	0.0	Arizona State	2006	1.0	0.0
3	132.0	2.95	*	1.0	Arizona State	2006	1.0	0.0
4	159.0	3.49	White	0.0	Arizona State	2006	1.0	0.0
...
124552	179.0	3.72	White	1.0	Washington	2006	0.0	1.0
124553	179.0	3.96	Asian	1.0	Washington	2006	0.0	1.0
124554	179.0	3.97	White	0.0	Washington	2006	0.0	1.0
124555	180.0	3.29	White	0.0	Washington	2006	1.0	1.0
124556	180.0	3.53	White	1.0	Washington	2006	1.0	1.0

124557 rows × 8 columns

```
/usr/local/lib/python3.7/site-packages/numpy/lib/histograms.py:839: RuntimeWarning: invalid value encountered in greater_equal
  keep = (tmp_a >= first_edge)
/usr/local/lib/python3.7/site-packages/numpy/lib/histograms.py:840: RuntimeWarning: invalid value encountered in less_equal
  keep &= (tmp_a <= last_edge)
```

Number of Clusters	Frequency
0.0	~88000
1.0	~32000

```
def nonparametric_fcit_test(X, Y, Z, data):
    """
    X and Y are names of variables.
    Z is a list of names of variables.
    data is a pandas data frame.

    Return a float corresponding to the p-value computed from FCIT.
    """

    # implement code here
    data_X = np.asmatrix(data[[X]].to_numpy())
    data_Y = np.asmatrix(data[[Y]].to_numpy())
    data_Z = np.asmatrix(data[Z].to_numpy())
    return fcit.test(data_X, data_Y, data_Z)
```

```
In [41]: import numpy as np
```

```
In [42]: import statsmodels.api as sm
import pandas as pd
import numpy as np
from scipy.special import expit

def odds_ratio(X, Y, Z, data):
    """
    Compute the odds ratio OR(X, Y | Z).
    X, Y are names of variables
    in the data frame. Z is a list of names of variables.

    Return float OR for the odds ratio OR(X, Y | Z)
    """

    # Implement your code here:
    Xtrain = data[[Y] + Z]
    Xtrain.insert(0, 'Ones', 1)
    ytrain = data[[X]]
    log_reg = sm.Logit(ytrain, Xtrain).fit(dis=0)
    beta_1 = log_reg.params.values[1]
    OR = np.exp(beta_1)

    return OR
```

```
In [134]: race = list(workbook[['race']])
admit = list(workbook[['admit']])
lsat = list(workbook[['lsat']])
gpa = list(workbook[['gpa']])
```

```
In [130]: for i in range(len(race)):
    if i == len(race):
        break

    if race[i] == "White":
        race[i] = 1
    elif race[i] == '*':
        race[i] = 0
    elif race[i] == "Asian":
        race[i] = 2
    elif race[i] == "Black":
        race[i] = 3
    elif race[i] == "Hispanic":
        race[i] = 4
```

```
In [131]: i = 0
while i < len(race):
    if pd.isna(admit[i][0]):
        print()
        del admit[i]
        del race[i]
        del lsat[i]
        del gpa[i]
    else:
        i = i+1
```

```
In [162]: import math
data = {'lsat': [], 'gpa': [], 'race':[], 'admit':[]}
data = pd.DataFrame(columns=('lsat', 'gpa', 'race', 'admit'))

for index, row in workbook.iterrows():
    if math.isnan(row[0]) or math.isnan(row[1]) or math.isnan(row[7]):
        continue
    else:
        new_row = row
        if row[2] == '*':
            new_row[2] = 0
        elif row[2] == 'White':
            new_row[2] = 1
        elif row[2] == 'Asian':
            new_row[2] = 2
        elif row[2] == 'Black':
            new_row[2] = 3
        elif row[2] == 'Hispanic':
            new_row[2] = 4
        data.loc[index] = new_row
```

In [163]: data

Out[163]:

	lsat	gpa	race	admit
0	156.0	3.71	1	1.0
1	161.0	3.85	1	1.0
2	160.0	3.20	1	0.0
3	132.0	2.95	0	0.0
4	159.0	3.49	1	0.0
...
124552	179.0	3.72	1	1.0
124553	179.0	3.96	2	1.0
124554	179.0	3.97	1	1.0
124555	180.0	3.29	1	1.0
124556	180.0	3.53	1	1.0

118246 rows x 4 columns

In [175]: data['race'] = data['race'] * 0.25

In [176]: data

Out[176]:

	lsat	gpa	race	admit
0	156.0	3.71	0.25	1.0
1	161.0	3.85	0.25	1.0
2	160.0	3.20	0.25	0.0
3	132.0	2.95	0	0.0
4	159.0	3.49	0.25	0.0
...
124552	179.0	3.72	0.25	1.0
124553	179.0	3.96	0.5	1.0
124554	179.0	3.97	0.25	1.0
124555	180.0	3.29	0.25	1.0
124556	180.0	3.53	0.25	1.0

118246 rows × 4 columns

In [178]: odds_ratio("race", "admit", [], data.astype(float))

Out[178]: 0.9059681854213831

In [179]: odds_ratio("race", "admit", ["gpa"], data.astype(float))

Out[179]: 1.0151255557984287

In [180]: odds_ratio("race", "admit", ["lsat"], data.astype(float))

Out[180]: 1.1871617843528481

In [181]: odds_ratio("race", "admit", ["lsat", "gpa"], data.astype(float))

Out[181]: 1.2294002430115953

```
In [182]: def compute_confidence_intervals(X, Y, Z, data, num_bootstraps=200, alpha=0.05):
    """
    Compute confidence intervals through bootstrap

    Returns tuple (q_low, q_up) for the lower and upper quantiles of the distribution
    """

    Ql = alpha/2
    Qu = 1 - alpha/2
    estimates = []
    data_length = data.shape[0]

    for i in range(num_bootstraps):

        # Implement your code here:
        resampled_data = data.sample(n=data_length, replace=True)
        estimates.append(odds_ratio(X, Y, Z, resampled_data))

    q_low = np.quantile(estimates, Ql)
    q_up = np.quantile(estimates, Qu)

    return q_low, q_up
```

```
In [185]: print("OR(race, admit)", odds_ratio("race", "admit", [], data.astype(float)))
print("OR(race, admit | gpa)", odds_ratio("race", "admit", ["gpa"], data))
print("OR(race, admit | lsat)", odds_ratio("race", "admit", ["lsat"], data))
print("OR(race, admit | gpa,lsat)", odds_ratio("race", "admit", ["gpa", "lsat"], data))
```

```
OR(race, admit) 0.9059681854213831 (0.8930397941261121, 0.9166569347790962)
OR(race, admit | gpa) 1.0151255557984287 (1.0019035147089632, 1.0287907321584313)
OR(race, admit | lsat) 1.1871617843528481 (1.1690079026808833, 1.2051835872100738)
OR(race, admit | gpa,lsat) 1.2294002430115951 (1.209370420517068, 1.24554553624103)
```