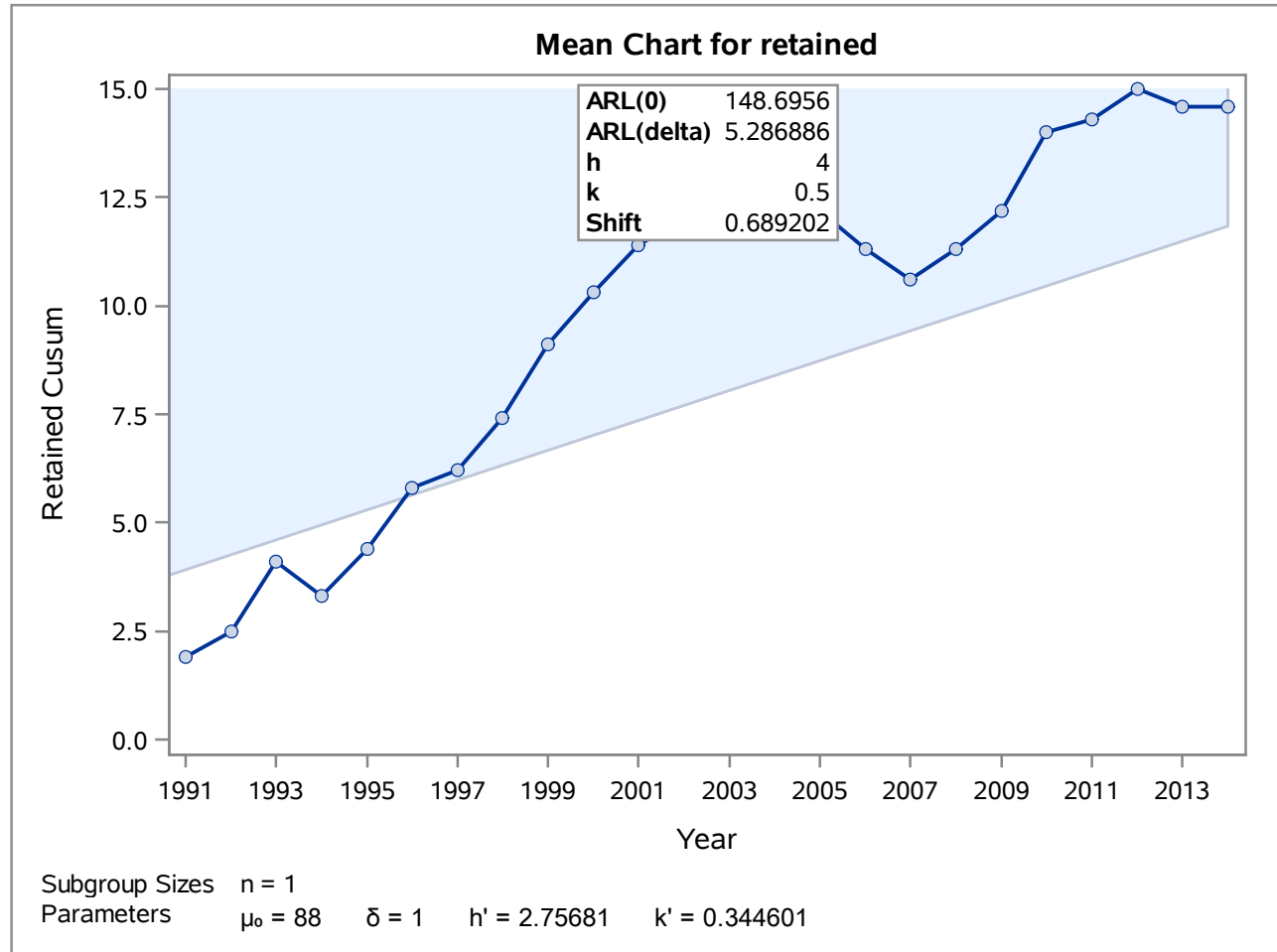


**CUSUM for Retention Rate (sigma unknown)****The CUSUM Procedure**

**CUSUM for Retention Rate (sigma unknown)****The CUSUM Procedure**

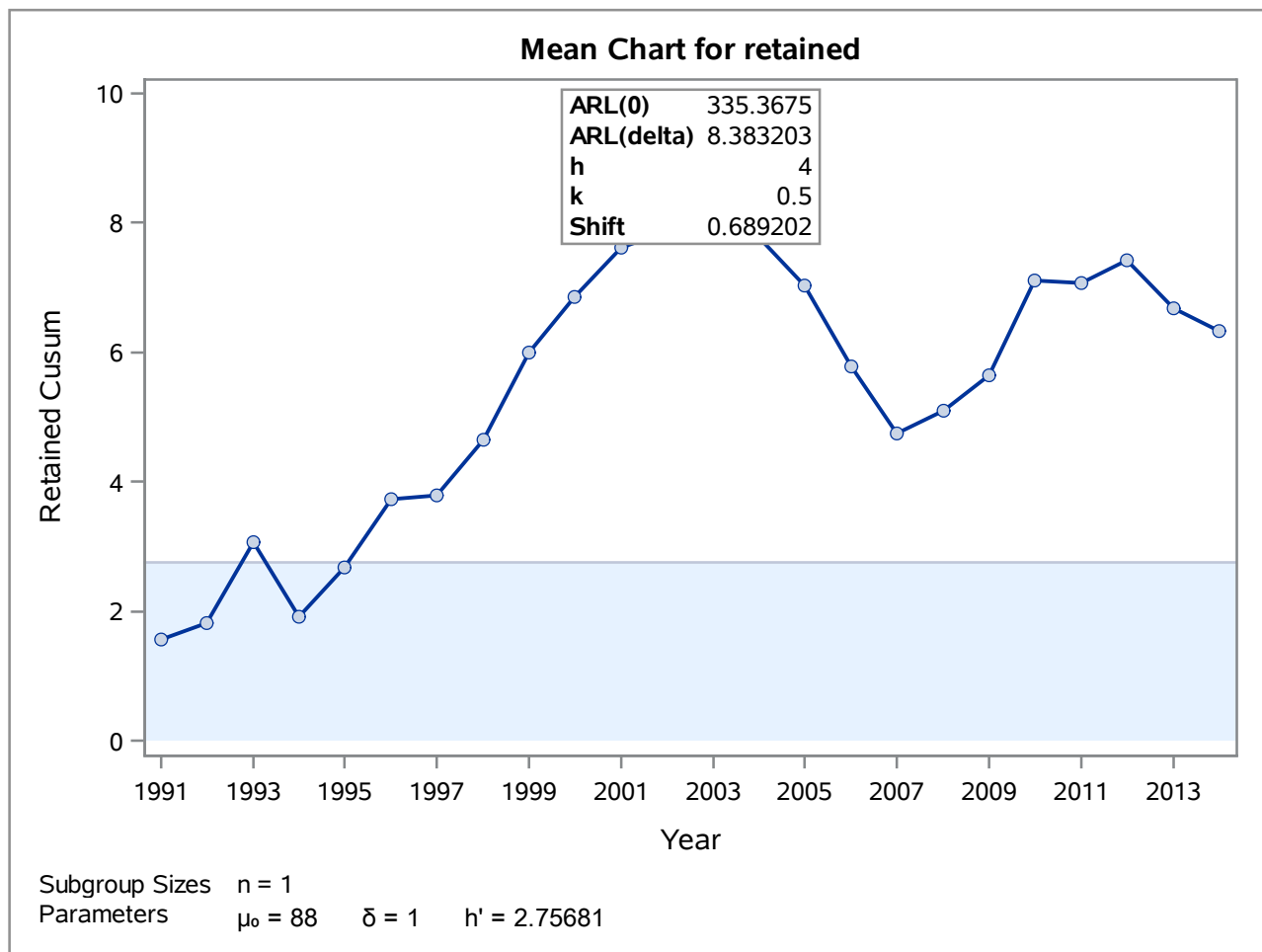
Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	Two-Sided
Target Mean ( $\mu_0$ )	88
Standard Deviation	0.68920244
Delta	1
Nominal Sample Size	1
h	4
h' (Data Units)	2.75680975
k	0.5
k' (Data Units)	0.34460122
Head Start	2
Average Run Length (Delta)	5.28688613
Average Run Length (0)	148.695619

**CUSUM for Retention Rate (sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for retained						
year	Subgroup Sample Size	Individual Value	V-Mask Lower Limit	Cusum	V-Mask Upper Limit	V-Mask Limit Exceeded
1991	1	89.900000	3.9174	1.900000	25.2826	Lower
1992	1	88.600000	4.2620	2.500000	24.9380	Lower
1993	1	89.600000	4.6066	4.100000	24.5934	Lower
1994	1	87.200000	4.9512	3.300000	24.2488	Lower
1995	1	89.100000	5.2958	4.400000	23.9042	Lower
1996	1	89.400000	5.6404	5.800000	23.5596	
1997	1	88.400000	5.9850	6.200000	23.2150	
1998	1	89.200000	6.3296	7.400000	22.8704	
1999	1	89.700000	6.6742	9.100000	22.5258	
2000	1	89.200000	7.0188	10.300000	22.1812	
2001	1	89.100000	7.3634	11.400000	21.8366	
2002	1	88.600000	7.7080	12.000000	21.4920	
2003	1	88.500000	8.0526	12.500000	21.1474	
2004	1	88.100000	8.3972	12.600000	20.8028	
2005	1	87.600000	8.7418	12.200000	20.4582	
2006	1	87.100000	9.0864	11.300000	20.1136	
2007	1	87.300000	9.4310	10.600000	19.7690	
2008	1	88.700000	9.7756	11.300000	19.4244	
2009	1	88.900000	10.1202	12.200000	19.0798	
2010	1	89.800000	10.4648	14.000000	18.7352	
2011	1	88.300000	10.8094	14.300000	18.3906	
2012	1	88.700000	11.1540	15.000000	18.0460	
2013	1	87.600000	11.4986	14.600000	17.7014	
2014	1	88.000000	11.8432	14.600000	17.3568	

# UPPER ONE-SIDED CUSUM for Retention Rate(sigma unknown)

## The CUSUM Procedure



**UPPER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

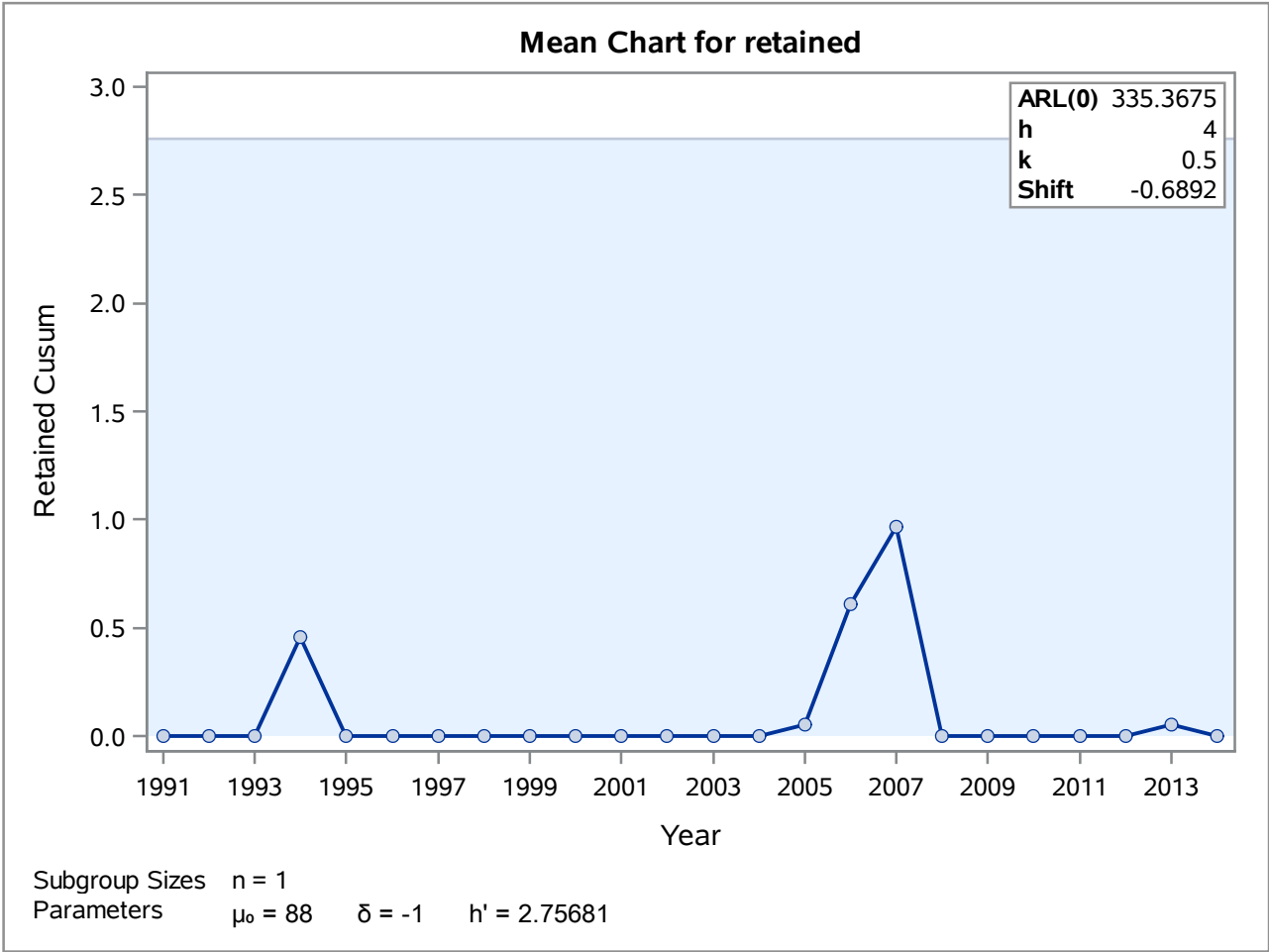
Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	88
Standard Deviation	0.68920244
Delta	1
Nominal Sample Size	1
h	4
h' (Data Units)	2.75680975
k	0.5
k' (Data Units)	0.34460122
Average Run Length (Delta)	8.38320257
Average Run Length (0)	335.367498

**UPPER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for retained					
year	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
1991	1	89.900000	1.5553988	2.7568	
1992	1	88.600000	1.8107976	2.7568	
1993	1	89.600000	3.0661963	2.7568	Upper
1994	1	87.200000	1.9215951	2.7568	
1995	1	89.100000	2.6769939	2.7568	
1996	1	89.400000	3.7323927	2.7568	Upper
1997	1	88.400000	3.7877915	2.7568	Upper
1998	1	89.200000	4.6431902	2.7568	Upper
1999	1	89.700000	5.9985890	2.7568	Upper
2000	1	89.200000	6.8539878	2.7568	Upper
2001	1	89.100000	7.6093866	2.7568	Upper
2002	1	88.600000	7.8647854	2.7568	Upper
2003	1	88.500000	8.0201842	2.7568	Upper
2004	1	88.100000	7.7755829	2.7568	Upper
2005	1	87.600000	7.0309817	2.7568	Upper
2006	1	87.100000	5.7863805	2.7568	Upper
2007	1	87.300000	4.7417793	2.7568	Upper
2008	1	88.700000	5.0971781	2.7568	Upper
2009	1	88.900000	5.6525768	2.7568	Upper
2010	1	89.800000	7.1079756	2.7568	Upper
2011	1	88.300000	7.0633744	2.7568	Upper
2012	1	88.700000	7.4187732	2.7568	Upper
2013	1	87.600000	6.6741720	2.7568	Upper
2014	1	88.000000	6.3295707	2.7568	Upper

LOWER ONE-SIDED CUSUM for Retention Rate(sigma unknown)

The CUSUM Procedure



**LOWER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	88
Standard Deviation	0.68920244
Delta	-1
Nominal Sample Size	1
h	4
h' (Data Units)	2.75680975
k	0.5
k' (Data Units)	0.34460122
Average Run Length (Delta)	973907.392
Average Run Length (0)	335.367498

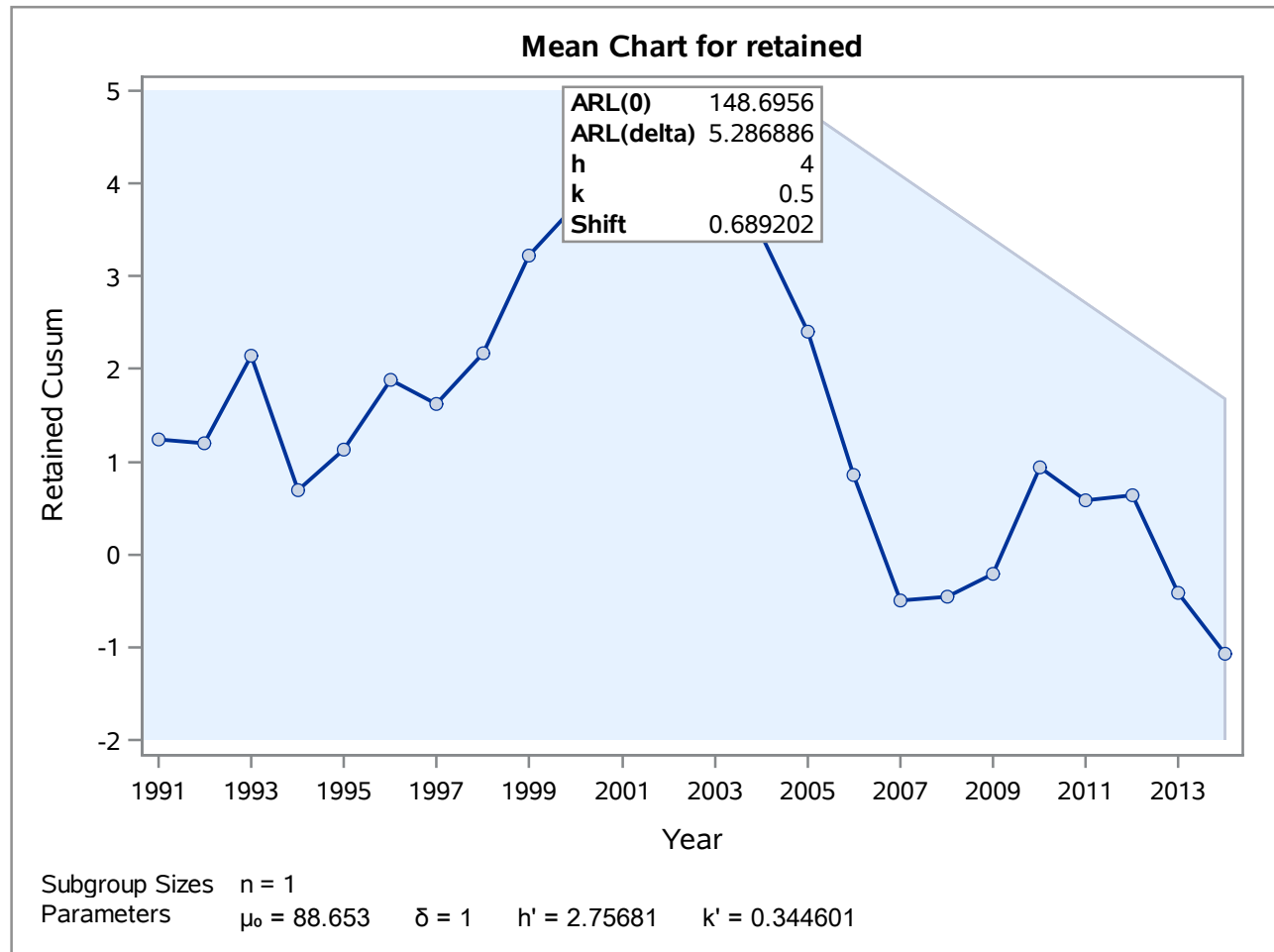


**LOWER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for retained					
year	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
1991	1	89.900000	0.00000000	2.7568	
1992	1	88.600000	0.00000000	2.7568	
1993	1	89.600000	0.00000000	2.7568	
1994	1	87.200000	0.45539878	2.7568	
1995	1	89.100000	0.00000000	2.7568	
1996	1	89.400000	0.00000000	2.7568	
1997	1	88.400000	0.00000000	2.7568	
1998	1	89.200000	0.00000000	2.7568	
1999	1	89.700000	0.00000000	2.7568	
2000	1	89.200000	0.00000000	2.7568	
2001	1	89.100000	0.00000000	2.7568	
2002	1	88.600000	0.00000000	2.7568	
2003	1	88.500000	0.00000000	2.7568	
2004	1	88.100000	0.00000000	2.7568	
2005	1	87.600000	0.05539878	2.7568	
2006	1	87.100000	0.61079756	2.7568	
2007	1	87.300000	0.96619634	2.7568	
2008	1	88.700000	0.00000000	2.7568	
2009	1	88.900000	0.00000000	2.7568	
2010	1	89.800000	0.00000000	2.7568	
2011	1	88.300000	0.00000000	2.7568	
2012	1	88.700000	0.00000000	2.7568	
2013	1	87.600000	0.05539878	2.7568	
2014	1	88.000000	0.00000000	2.7568	

**CUSUM with Reset after Signal (sigma unknown)**

year	xbar	n	cusum_l	hsigma	cusum_h	flag
1991	89.9	1	0.0000	2.756	1.5555	
1992	88.6	1	0.0000	2.756	1.8110	
1993	89.6	1	0.0000	2.756	3.0665	upper
1994	87.2	1	0.4555	2.756	0.0000	
1995	89.1	1	0.0000	2.756	0.7555	
1996	89.4	1	0.0000	2.756	1.8110	
1997	88.4	1	0.0000	2.756	1.8665	
1998	89.2	1	0.0000	2.756	2.7220	
1999	89.7	1	0.0000	2.756	4.0775	upper
2000	89.2	1	0.0000	2.756	0.8555	
2001	89.1	1	0.0000	2.756	1.6110	
2002	88.6	1	0.0000	2.756	1.8665	
2003	88.5	1	0.0000	2.756	2.0220	
2004	88.1	1	0.0000	2.756	1.7775	
2005	87.6	1	0.0555	2.756	1.0330	
2006	87.1	1	0.6110	2.756	0.0000	
2007	87.3	1	0.9665	2.756	0.0000	
2008	88.7	1	0.0000	2.756	0.3555	
2009	88.9	1	0.0000	2.756	0.9110	
2010	89.8	1	0.0000	2.756	2.3665	
2011	88.3	1	0.0000	2.756	2.3220	
2012	88.7	1	0.0000	2.756	2.6775	
2013	87.6	1	0.0555	2.756	1.9330	
2014	88.0	1	0.0000	2.756	1.5885	

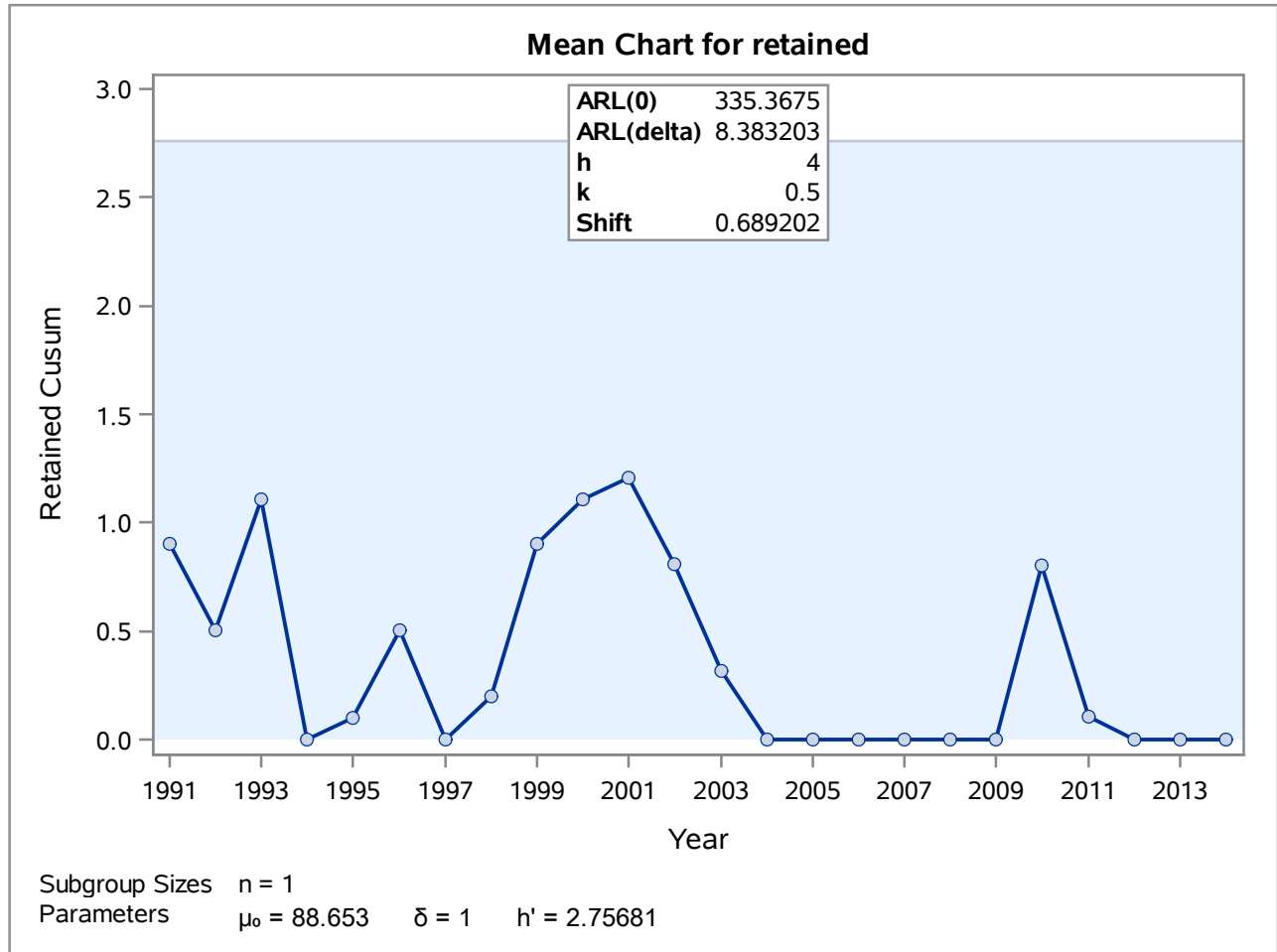
**CUSUM for Retention Rate (sigma unknown)****The CUSUM Procedure**

**CUSUM for Retention Rate (sigma unknown)****The CUSUM Procedure**

Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	Two-Sided
Target Mean ( $\mu_0$ )	88.653
Standard Deviation	0.68920244
Delta	1
Nominal Sample Size	1
h	4
h' (Data Units)	2.75680975
k	0.5
k' (Data Units)	0.34460122
Head Start	2
Average Run Length (Delta)	5.28688613
Average Run Length (0)	148.695619

**CUSUM for Retention Rate (sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for retained						
year	Subgroup Sample Size	Individual Value	V-Mask Lower Limit	Cusum	V-Mask Upper Limit	V-Mask Limit Exceeded
1991	1	89.900000	-11.7546	1.2470000	9.6106	
1992	1	88.600000	-11.4100	1.1940000	9.2660	
1993	1	89.600000	-11.0654	2.1410000	8.9214	
1994	1	87.200000	-10.7208	0.6880000	8.5768	
1995	1	89.100000	-10.3762	1.1350000	8.2322	
1996	1	89.400000	-10.0316	1.8820000	7.8876	
1997	1	88.400000	-9.6870	1.6290000	7.5430	
1998	1	89.200000	-9.3424	2.1760000	7.1984	
1999	1	89.700000	-8.9978	3.2230000	6.8538	
2000	1	89.200000	-8.6532	3.7700000	6.5092	
2001	1	89.100000	-8.3086	4.2170000	6.1646	
2002	1	88.600000	-7.9640	4.1640000	5.8200	
2003	1	88.500000	-7.6194	4.0110000	5.4754	
2004	1	88.100000	-7.2748	3.4580000	5.1308	
2005	1	87.600000	-6.9302	2.4050000	4.7862	
2006	1	87.100000	-6.5856	0.8520000	4.4416	
2007	1	87.300000	-6.2410	-0.5010000	4.0970	
2008	1	88.700000	-5.8964	-0.4540000	3.7524	
2009	1	88.900000	-5.5518	-0.2070000	3.4078	
2010	1	89.800000	-5.2072	0.9400000	3.0632	
2011	1	88.300000	-4.8626	0.5870000	2.7186	
2012	1	88.700000	-4.5180	0.6340000	2.3740	
2013	1	87.600000	-4.1734	-0.4190000	2.0294	
2014	1	88.000000	-3.8288	-1.0720000	1.6848	

**UPPER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

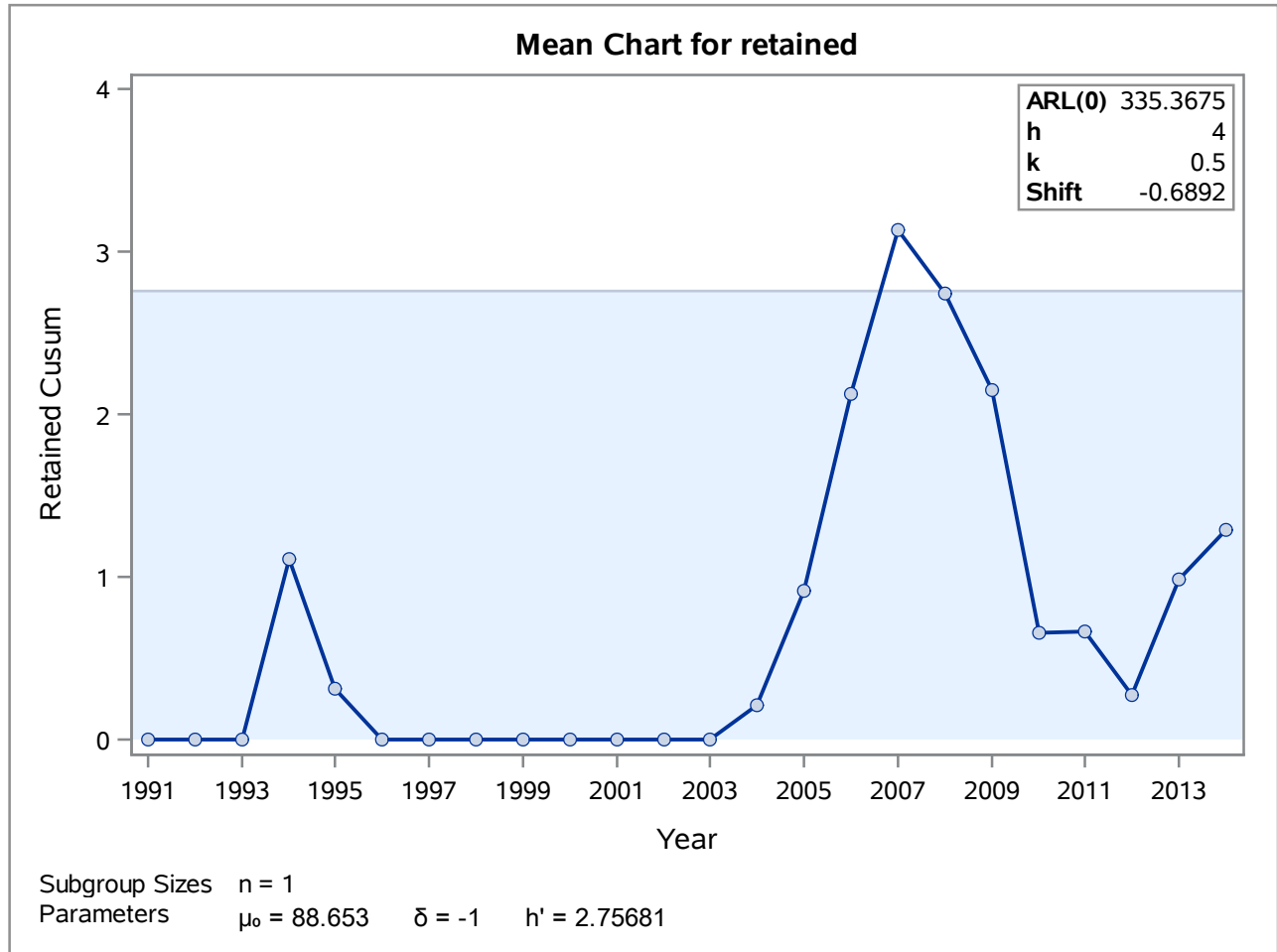
**UPPER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	88.653
Standard Deviation	0.68920244
Delta	1
Nominal Sample Size	1
h	4
h' (Data Units)	2.75680975
k	0.5
k' (Data Units)	0.34460122
Average Run Length (Delta)	8.38320257
Average Run Length (0)	335.367498

**UPPER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for retained					
year	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
1991	1	89.900000	0.9023988	2.7568	
1992	1	88.600000	0.5047976	2.7568	
1993	1	89.600000	1.1071963	2.7568	
1994	1	87.200000	0.0000000	2.7568	
1995	1	89.100000	0.1023988	2.7568	
1996	1	89.400000	0.5047976	2.7568	
1997	1	88.400000	0.0000000	2.7568	
1998	1	89.200000	0.2023988	2.7568	
1999	1	89.700000	0.9047976	2.7568	
2000	1	89.200000	1.1071963	2.7568	
2001	1	89.100000	1.2095951	2.7568	
2002	1	88.600000	0.8119939	2.7568	
2003	1	88.500000	0.3143927	2.7568	
2004	1	88.100000	0.0000000	2.7568	
2005	1	87.600000	0.0000000	2.7568	
2006	1	87.100000	0.0000000	2.7568	
2007	1	87.300000	0.0000000	2.7568	
2008	1	88.700000	0.0000000	2.7568	
2009	1	88.900000	0.0000000	2.7568	
2010	1	89.800000	0.8023988	2.7568	
2011	1	88.300000	0.1047976	2.7568	
2012	1	88.700000	0.0000000	2.7568	
2013	1	87.600000	0.0000000	2.7568	
2014	1	88.000000	0.0000000	2.7568	



**LOWER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

**LOWER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	88.653
Standard Deviation	0.68920244
Delta	-1
Nominal Sample Size	1
h	4
h' (Data Units)	2.75680975
k	0.5
k' (Data Units)	0.34460122
Average Run Length (Delta)	973907.392
Average Run Length (0)	335.367498

**LOWER ONE-SIDED CUSUM for Retention Rate(sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for retained					
year	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
1991	1	89.900000	0.0000000	2.7568	
1992	1	88.600000	0.0000000	2.7568	
1993	1	89.600000	0.0000000	2.7568	
1994	1	87.200000	1.1083988	2.7568	
1995	1	89.100000	0.3167976	2.7568	
1996	1	89.400000	0.0000000	2.7568	
1997	1	88.400000	0.0000000	2.7568	
1998	1	89.200000	0.0000000	2.7568	
1999	1	89.700000	0.0000000	2.7568	
2000	1	89.200000	0.0000000	2.7568	
2001	1	89.100000	0.0000000	2.7568	
2002	1	88.600000	0.0000000	2.7568	
2003	1	88.500000	0.0000000	2.7568	
2004	1	88.100000	0.2083988	2.7568	
2005	1	87.600000	0.9167976	2.7568	
2006	1	87.100000	2.1251963	2.7568	
2007	1	87.300000	3.1335951	2.7568	Upper
2008	1	88.700000	2.7419939	2.7568	
2009	1	88.900000	2.1503927	2.7568	
2010	1	89.800000	0.6587915	2.7568	
2011	1	88.300000	0.6671902	2.7568	
2012	1	88.700000	0.2755890	2.7568	
2013	1	87.600000	0.9839878	2.7568	
2014	1	88.000000	1.2923866	2.7568	

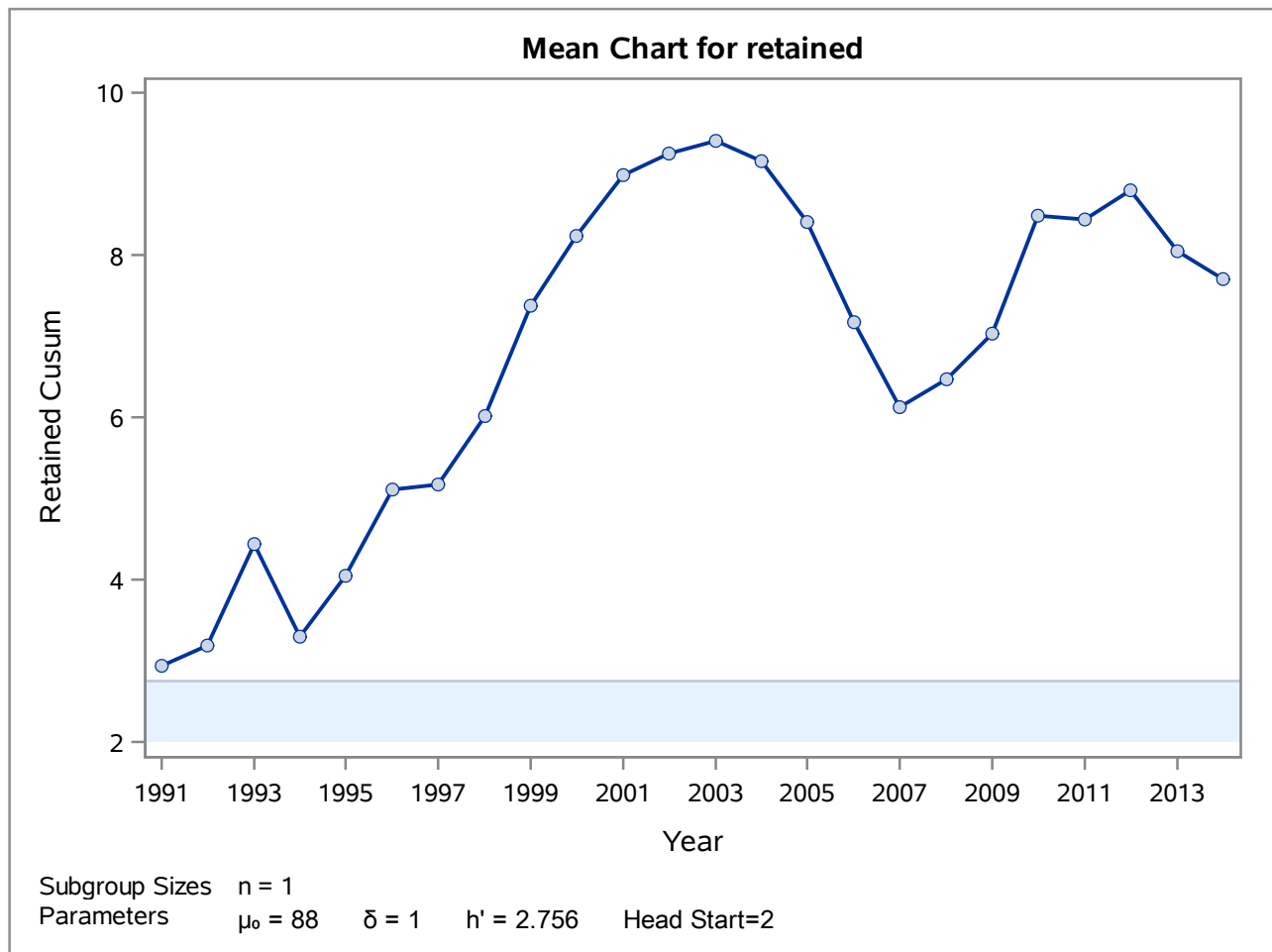
**CUSUM with Reset after Signal (sigma unknown)**

year	xbar	n	cusum_l	hsigma	cusum_h	flag
1991	89.9	1	0.0000	2.756	0.9025	
1992	88.6	1	0.0000	2.756	0.5050	
1993	89.6	1	0.0000	2.756	1.1075	
1994	87.2	1	1.1085	2.756	0.0000	
1995	89.1	1	0.3170	2.756	0.1025	
1996	89.4	1	0.0000	2.756	0.5050	
1997	88.4	1	0.0000	2.756	0.0000	
1998	89.2	1	0.0000	2.756	0.2025	
1999	89.7	1	0.0000	2.756	0.9050	
2000	89.2	1	0.0000	2.756	1.1075	
2001	89.1	1	0.0000	2.756	1.2100	
2002	88.6	1	0.0000	2.756	0.8125	
2003	88.5	1	0.0000	2.756	0.3150	
2004	88.1	1	0.2085	2.756	0.0000	
2005	87.6	1	0.9170	2.756	0.0000	
2006	87.1	1	2.1255	2.756	0.0000	
2007	87.3	1	3.1340	2.756	0.0000	lower
2008	88.7	1	0.0000	2.756	0.0000	
2009	88.9	1	0.0000	2.756	0.0000	
2010	89.8	1	0.0000	2.756	0.8025	
2011	88.3	1	0.0085	2.756	0.1050	
2012	88.7	1	0.0000	2.756	0.0000	
2013	87.6	1	0.7085	2.756	0.0000	
2014	88.0	1	1.0170	2.756	0.0000	

**FIR CUSUM with Reset after Signal**

year	xbar	n	fir	cusum_l	hsigma	cusum_h	flag
1991	89.9	1	0.01	0.0000	0.02	1.5555	upper
1992	88.6	1	0.01	0.0000	0.02	1.8110	upper
1993	89.6	1	0.01	0.0000	0.02	3.0665	upper
1994	87.2	1	0.01	0.4555	0.02	0.0000	lower
1995	89.1	1	0.01	0.0000	0.02	0.7555	upper
1996	89.4	1	0.01	0.0000	0.02	1.8110	upper
1997	88.4	1	0.01	0.0000	0.02	1.8665	upper
1998	89.2	1	0.01	0.0000	0.02	2.7220	upper
1999	89.7	1	0.01	0.0000	0.02	4.0775	upper
2000	89.2	1	0.01	0.0000	0.02	0.8555	upper
2001	89.1	1	0.01	0.0000	0.02	1.6110	upper
2002	88.6	1	0.01	0.0000	0.02	1.8665	upper
2003	88.5	1	0.01	0.0000	0.02	2.0220	upper
2004	88.1	1	0.01	0.0000	0.02	1.7775	upper
2005	87.6	1	0.01	0.0555	0.02	1.0330	lower
2005	87.6	1	0.01	0.0555	0.02	1.0330	upper
2006	87.1	1	0.01	0.6110	0.02	0.0000	lower
2007	87.3	1	0.01	0.9665	0.02	0.0000	lower
2008	88.7	1	0.01	0.0000	0.02	0.3555	upper
2009	88.9	1	0.01	0.0000	0.02	0.9110	upper
2010	89.8	1	0.01	0.0000	0.02	2.3665	upper
2011	88.3	1	0.01	0.0000	0.02	2.3220	upper
2012	88.7	1	0.01	0.0000	0.02	2.6775	upper
2013	87.6	1	0.01	0.0555	0.02	1.9330	lower
2013	87.6	1	0.01	0.0555	0.02	1.9330	upper
2014	88.0	1	0.01	0.0000	0.02	1.5885	upper

## The CUSUM Procedure



## The CUSUM Procedure

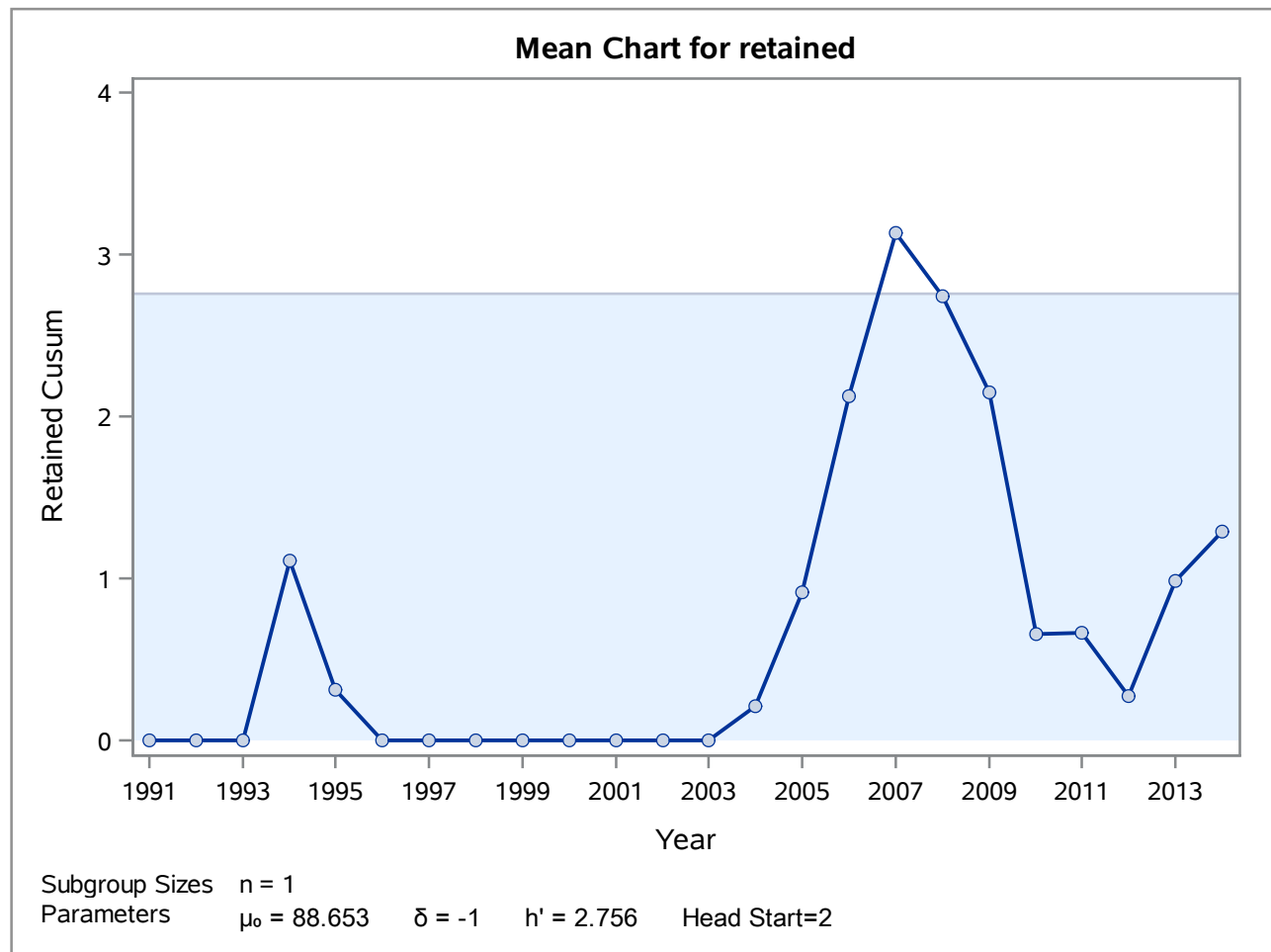
Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	88
Sigma0	0.689
Delta	1
Nominal Sample Size	1
h	4
h' (Data Units)	2.756
k	0.5
k' (Data Units)	0.3445
Head Start	2
Average Run Length (Delta)	5.29102011
Average Run Length (0)	316.379368

## The CUSUM Procedure

Computational Cumulative Sum for retained				
year	Subgroup Sample Size	Individual Value	Upper Cusum	Number of Consecutive Upper Sums > 0
1991	1	89.900000	2.9335000	1
1992	1	88.600000	3.1890000	2
1993	1	89.600000	4.4445000	3
1994	1	87.200000	3.3000000	4
1995	1	89.100000	4.0555000	5
1996	1	89.400000	5.1110000	6
1997	1	88.400000	5.1665000	7
1998	1	89.200000	6.0220000	8
1999	1	89.700000	7.3775000	9
2000	1	89.200000	8.2330000	10
2001	1	89.100000	8.9885000	11
2002	1	88.600000	9.2440000	12
2003	1	88.500000	9.3995000	13
2004	1	88.100000	9.1550000	14
2005	1	87.600000	8.4105000	15
2006	1	87.100000	7.1660000	16
2007	1	87.300000	6.1215000	17
2008	1	88.700000	6.4770000	18
2009	1	88.900000	7.0325000	19
2010	1	89.800000	8.4880000	20
2011	1	88.300000	8.4435000	21
2012	1	88.700000	8.7990000	22
2013	1	87.600000	8.0545000	23
2014	1	88.000000	7.7100000	24



## The CUSUM Procedure

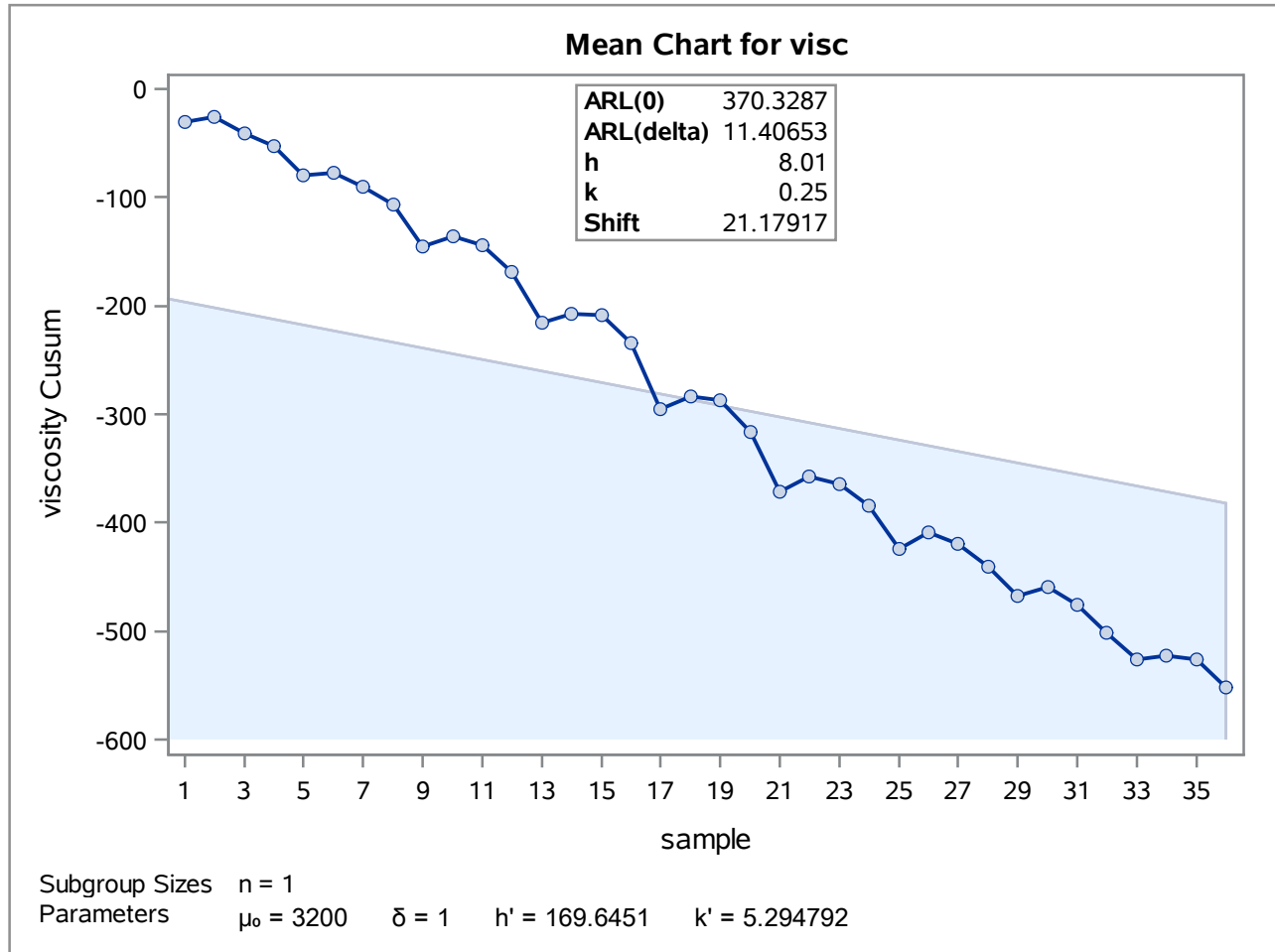


## The CUSUM Procedure

Cusum Parameters	
Process Variable	retained (Retained Cusum)
Subgroup Variable	year (Year)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	88.653
Sigma0	0.689
Delta	-1
Nominal Sample Size	1
h	4
h' (Data Units)	2.756
k	0.5
k' (Data Units)	0.3445
Head Start	2
Average Run Length (Delta)	973432.42
Average Run Length (0)	316.379368

## The CUSUM Procedure

Computational Cumulative Sum for retained				
year	Subgroup Sample Size	Individual Value	Lower Cusum	Number of Consecutive Lower Sums > 0
1991	1	89.900000	0.0000000	0
1992	1	88.600000	0.0000000	0
1993	1	89.600000	0.0000000	0
1994	1	87.200000	1.1085000	1
1995	1	89.100000	0.3170000	2
1996	1	89.400000	0.0000000	0
1997	1	88.400000	0.0000000	0
1998	1	89.200000	0.0000000	0
1999	1	89.700000	0.0000000	0
2000	1	89.200000	0.0000000	0
2001	1	89.100000	0.0000000	0
2002	1	88.600000	0.0000000	0
2003	1	88.500000	0.0000000	0
2004	1	88.100000	0.2085000	1
2005	1	87.600000	0.9170000	2
2006	1	87.100000	2.1255000	3
2007	1	87.300000	3.1340000	4
2008	1	88.700000	2.7425000	5
2009	1	88.900000	2.1510000	6
2010	1	89.800000	0.6595000	7
2011	1	88.300000	0.6680000	8
2012	1	88.700000	0.2765000	9
2013	1	87.600000	0.9850000	10
2014	1	88.000000	1.2935000	11

**CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

**CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

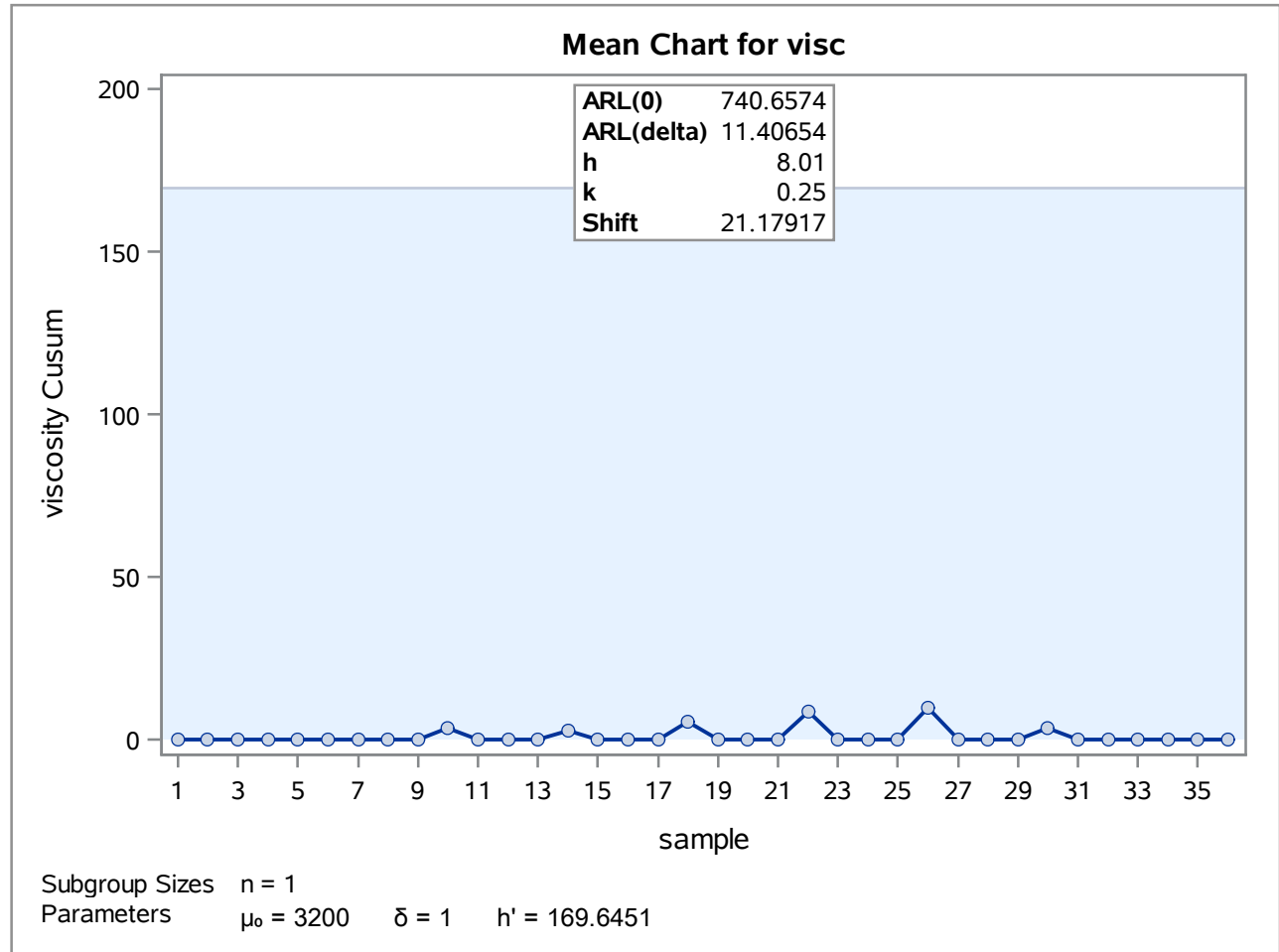
Cusum Parameters	
Process Variable	visc (viscosity Cusum)
Subgroup Variable	sample (sample)
Scheme	Two-Sided
Target Mean ( $\mu_0$ )	3200
Standard Deviation	21.1791677
Delta	1
Nominal Sample Size	1
h	8.01
h' (Data Units)	169.645133
k	0.25
k' (Data Units)	5.29479192
Average Run Length (Delta)	11.4065336
Average Run Length (0)	370.328713

**CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for visc						
sample	Subgroup Sample Size	Individual Value	V-Mask Lower Limit	Cusum	V-Mask Upper Limit	V-Mask Limit Exceeded
1	1	3169.0000	-906.9629	-31.00000	-197.0371	Upper
2	1	3205.0000	-901.6681	-26.00000	-202.3319	Upper
3	1	3185.0000	-896.3733	-41.00000	-207.6267	Upper
4	1	3188.0000	-891.0785	-53.00000	-212.9215	Upper
5	1	3173.0000	-885.7837	-80.00000	-218.2163	Upper
6	1	3203.0000	-880.4889	-77.00000	-223.5111	Upper
7	1	3187.0000	-875.1941	-90.00000	-228.8059	Upper
8	1	3183.0000	-869.8993	-107.00000	-234.1007	Upper
9	1	3162.0000	-864.6045	-145.00000	-239.3955	Upper
10	1	3209.0000	-859.3097	-136.00000	-244.6903	Upper
11	1	3192.0000	-854.0149	-144.00000	-249.9851	Upper
12	1	3175.0000	-848.7201	-169.00000	-255.2799	Upper
13	1	3154.0000	-843.4253	-215.00000	-260.5747	Upper
14	1	3208.0000	-838.1306	-207.00000	-265.8694	Upper
15	1	3199.0000	-832.8358	-208.00000	-271.1642	Upper
16	1	3174.0000	-827.5410	-234.00000	-276.4590	Upper
17	1	3139.0000	-822.2462	-295.00000	-281.7538	
18	1	3211.0000	-816.9514	-284.00000	-287.0486	Upper
19	1	3197.0000	-811.6566	-287.00000	-292.3434	Upper
20	1	3171.0000	-806.3618	-316.00000	-297.6382	
21	1	3145.0000	-801.0670	-371.00000	-302.9330	
22	1	3214.0000	-795.7722	-357.00000	-308.2278	
23	1	3193.0000	-790.4774	-364.00000	-313.5226	
24	1	3180.0000	-785.1826	-384.00000	-318.8174	
25	1	3160.0000	-779.8878	-424.00000	-324.1122	
26	1	3215.0000	-774.5931	-409.00000	-329.4069	
27	1	3190.0000	-769.2983	-419.00000	-334.7017	
28	1	3179.0000	-764.0035	-440.00000	-339.9965	
29	1	3172.0000	-758.7087	-468.00000	-345.2913	
30	1	3209.0000	-753.4139	-459.00000	-350.5861	
31	1	3183.0000	-748.1191	-476.00000	-355.8809	
32	1	3175.0000	-742.8243	-501.00000	-361.1757	
33	1	3175.0000	-737.5295	-526.00000	-366.4705	
34	1	3203.0000	-732.2347	-523.00000	-371.7653	

**CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for visc						
sample	Subgroup Sample Size	Individual Value	V-Mask Lower Limit	Cusum	V-Mask Upper Limit	V-Mask Limit Exceeded
35	1	3197.0000	-726.9399	-526.00000	-377.0601	
36	1	3174.0000	-721.6451	-552.00000	-382.3549	

**UPPER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**



**UPPER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

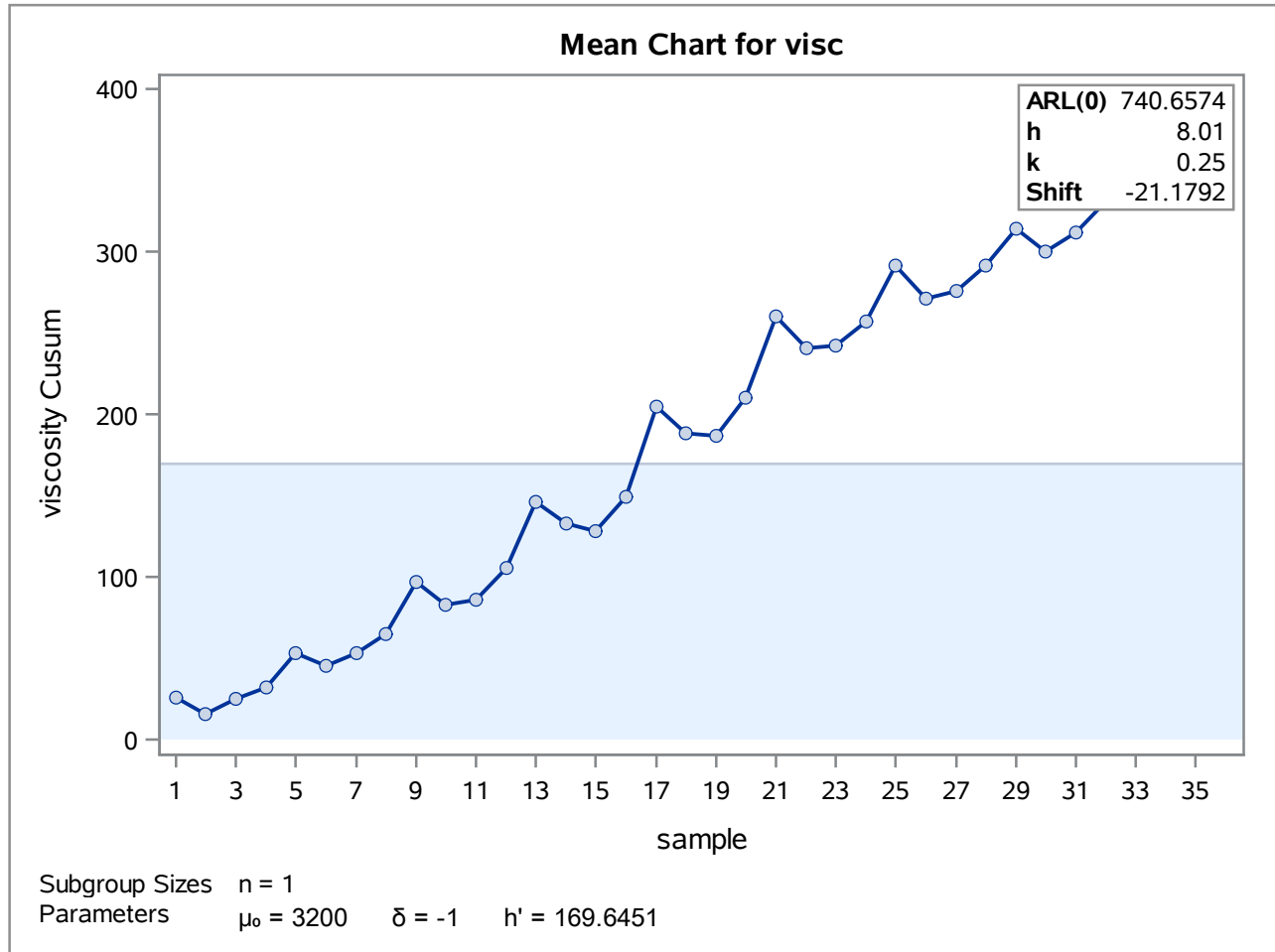
Cusum Parameters	
Process Variable	visc (viscosity Cusum)
Subgroup Variable	sample (sample)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	3200
Standard Deviation	21.1791677
Delta	1
Nominal Sample Size	1
h	8.01
h' (Data Units)	169.645133
k	0.25
k' (Data Units)	5.29479192
Average Run Length (Delta)	11.4065412
Average Run Length (0)	740.657426

**UPPER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for visc					
sample	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
1	1	3169.0000	0.0000000	169.6451	
2	1	3205.0000	0.0000000	169.6451	
3	1	3185.0000	0.0000000	169.6451	
4	1	3188.0000	0.0000000	169.6451	
5	1	3173.0000	0.0000000	169.6451	
6	1	3203.0000	0.0000000	169.6451	
7	1	3187.0000	0.0000000	169.6451	
8	1	3183.0000	0.0000000	169.6451	
9	1	3162.0000	0.0000000	169.6451	
10	1	3209.0000	3.7052081	169.6451	
11	1	3192.0000	0.0000000	169.6451	
12	1	3175.0000	0.0000000	169.6451	
13	1	3154.0000	0.0000000	169.6451	
14	1	3208.0000	2.7052081	169.6451	
15	1	3199.0000	0.0000000	169.6451	
16	1	3174.0000	0.0000000	169.6451	
17	1	3139.0000	0.0000000	169.6451	
18	1	3211.0000	5.7052081	169.6451	
19	1	3197.0000	0.0000000	169.6451	
20	1	3171.0000	0.0000000	169.6451	
21	1	3145.0000	0.0000000	169.6451	
22	1	3214.0000	8.7052081	169.6451	
23	1	3193.0000	0.0000000	169.6451	
24	1	3180.0000	0.0000000	169.6451	
25	1	3160.0000	0.0000000	169.6451	
26	1	3215.0000	9.7052081	169.6451	
27	1	3190.0000	0.0000000	169.6451	
28	1	3179.0000	0.0000000	169.6451	
29	1	3172.0000	0.0000000	169.6451	
30	1	3209.0000	3.7052081	169.6451	
31	1	3183.0000	0.0000000	169.6451	
32	1	3175.0000	0.0000000	169.6451	
33	1	3175.0000	0.0000000	169.6451	
34	1	3203.0000	0.0000000	169.6451	

**UPPER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for visc					
sample	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
35	1	3197.0000	0.0000000	169.6451	
36	1	3174.0000	0.0000000	169.6451	

**LOWER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

**LOWER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

Cusum Parameters	
Process Variable	visc (viscosity Cusum)
Subgroup Variable	sample (sample)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	3200
Standard Deviation	21.1791677
Delta	-1
Nominal Sample Size	1
h	8.01
h' (Data Units)	169.645133
k	0.25
k' (Data Units)	5.29479192
Average Run Length (Delta)	17287591.2
Average Run Length (0)	740.657426

**LOWER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

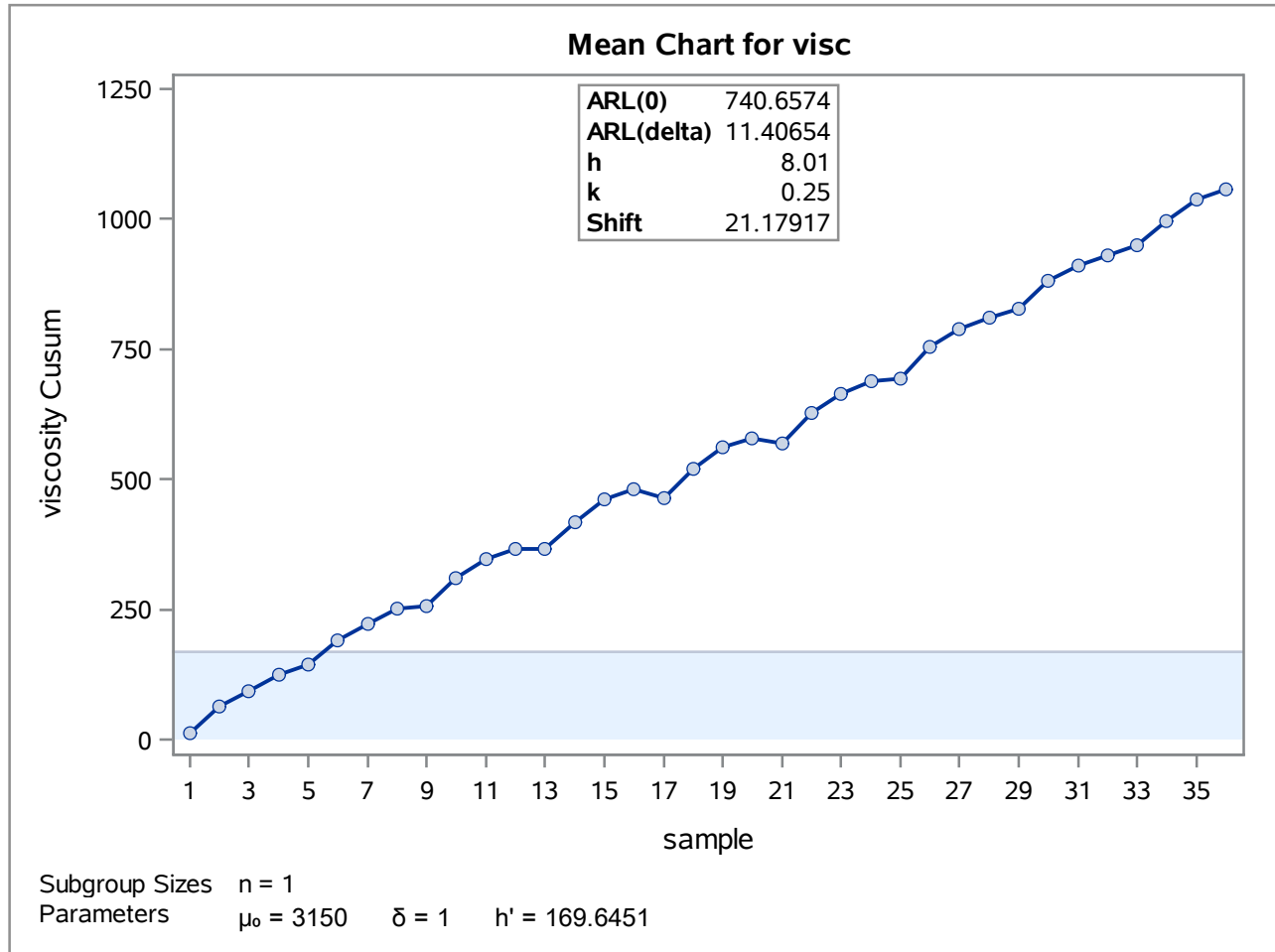
Cumulative Sum Chart Summary for visc					
sample	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
1	1	3169.0000	25.70521	169.6451	
2	1	3205.0000	15.41042	169.6451	
3	1	3185.0000	25.11562	169.6451	
4	1	3188.0000	31.82083	169.6451	
5	1	3173.0000	53.52604	169.6451	
6	1	3203.0000	45.23125	169.6451	
7	1	3187.0000	52.93646	169.6451	
8	1	3183.0000	64.64166	169.6451	
9	1	3162.0000	97.34687	169.6451	
10	1	3209.0000	83.05208	169.6451	
11	1	3192.0000	85.75729	169.6451	
12	1	3175.0000	105.46250	169.6451	
13	1	3154.0000	146.16771	169.6451	
14	1	3208.0000	132.87291	169.6451	
15	1	3199.0000	128.57812	169.6451	
16	1	3174.0000	149.28333	169.6451	
17	1	3139.0000	204.98854	169.6451	Upper
18	1	3211.0000	188.69375	169.6451	Upper
19	1	3197.0000	186.39895	169.6451	Upper
20	1	3171.0000	210.10416	169.6451	Upper
21	1	3145.0000	259.80937	169.6451	Upper
22	1	3214.0000	240.51458	169.6451	Upper
23	1	3193.0000	242.21979	169.6451	Upper
24	1	3180.0000	256.92499	169.6451	Upper
25	1	3160.0000	291.63020	169.6451	Upper
26	1	3215.0000	271.33541	169.6451	Upper
27	1	3190.0000	276.04062	169.6451	Upper
28	1	3179.0000	291.74583	169.6451	Upper
29	1	3172.0000	314.45103	169.6451	Upper
30	1	3209.0000	300.15624	169.6451	Upper
31	1	3183.0000	311.86145	169.6451	Upper
32	1	3175.0000	331.56666	169.6451	Upper
33	1	3175.0000	351.27187	169.6451	Upper
34	1	3203.0000	342.97707	169.6451	Upper

**LOWER ONE-SIDED CUSUM for viscosity (sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for visc					
sample	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
35	1	3197.0000	340.68228	169.6451	Upper
36	1	3174.0000	361.38749	169.6451	Upper

# UPPER ONE-SIDED CUSUM for viscosity ( $\mu = 3150$ )(sigma unknown)

## The CUSUM Procedure





**UPPER ONE-SIDED CUSUM for viscosity ( $\mu = 3150$ )(sigma unknown)****The CUSUM Procedure**

Cusum Parameters	
Process Variable	visc (viscosity Cusum)
Subgroup Variable	sample (sample)
Scheme	One-Sided
Target Mean ( $\mu_0$ )	3150
Standard Deviation	21.1791677
Delta	1
Nominal Sample Size	1
h	8.01
h' (Data Units)	169.645133
k	0.25
k' (Data Units)	5.29479192
Average Run Length (Delta)	11.4065412
Average Run Length (0)	740.657426

**UPPER ONE-SIDED CUSUM for viscosity ( $\mu = 3150$ )( $\sigma$  unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for visc					
sample	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
1	1	3169.0000	13.7052	169.6451	
2	1	3205.0000	63.4104	169.6451	
3	1	3185.0000	93.1156	169.6451	
4	1	3188.0000	125.8208	169.6451	
5	1	3173.0000	143.5260	169.6451	
6	1	3203.0000	191.2312	169.6451	Upper
7	1	3187.0000	222.9365	169.6451	Upper
8	1	3183.0000	250.6417	169.6451	Upper
9	1	3162.0000	257.3469	169.6451	Upper
10	1	3209.0000	311.0521	169.6451	Upper
11	1	3192.0000	347.7573	169.6451	Upper
12	1	3175.0000	367.4625	169.6451	Upper
13	1	3154.0000	366.1677	169.6451	Upper
14	1	3208.0000	418.8729	169.6451	Upper
15	1	3199.0000	462.5781	169.6451	Upper
16	1	3174.0000	481.2833	169.6451	Upper
17	1	3139.0000	464.9885	169.6451	Upper
18	1	3211.0000	520.6937	169.6451	Upper
19	1	3197.0000	562.3990	169.6451	Upper
20	1	3171.0000	578.1042	169.6451	Upper
21	1	3145.0000	567.8094	169.6451	Upper
22	1	3214.0000	626.5146	169.6451	Upper
23	1	3193.0000	664.2198	169.6451	Upper
24	1	3180.0000	688.9250	169.6451	Upper
25	1	3160.0000	693.6302	169.6451	Upper
26	1	3215.0000	753.3354	169.6451	Upper
27	1	3190.0000	788.0406	169.6451	Upper
28	1	3179.0000	811.7458	169.6451	Upper
29	1	3172.0000	828.4510	169.6451	Upper
30	1	3209.0000	882.1562	169.6451	Upper
31	1	3183.0000	909.8615	169.6451	Upper
32	1	3175.0000	929.5667	169.6451	Upper
33	1	3175.0000	949.2719	169.6451	Upper
34	1	3203.0000	996.9771	169.6451	Upper

**UPPER ONE-SIDED CUSUM for viscosity ( $\mu = 3150$ )(sigma unknown)****The CUSUM Procedure**

Cumulative Sum Chart Summary for visc					
sample	Subgroup Sample Size	Individual Value	Cusum	Decision Interval	Decision Interval Exceeded
35	1	3197.0000	1038.6823	169.6451	Upper
36	1	3174.0000	1057.3875	169.6451	Upper