## **Chapter 1**

## A real fluid-structure interaction problem: Finite Reynolds number flow in an oscillating elastic ring.

Our first "real" fluid-structure interaction problem: We study the finite-Reynolds number internal flow generated by the motion of an oscillating elastic ring and compare the results against asymptotic predictions.

```
//LIC// This file forms part of oomph-lib, the object-oriented,
//LIC// multi-physics finite-element library, available
//LIC// at http://www.oomph-lib.org.
//LIC//
//LIC//
            Version 1.0; svn revision $LastChangedRevision$
//T.TC//
//LIC// $LastChangedDate$
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//LIC// Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA //LIC// 02110-1301 USA.
//LIC// The authors may be contacted at oomph-lib@maths.man.ac.uk.
//LIC//===
// Driver for 2D Navier Stokes flow interacting with an elastic ring
// Oomph-lib include files
#include "generic.h"
#include "generic.n"
#include "navier_stokes.h"
#include "beam.h"
//Need to include templated meshes, so that all functions
//are instantiated for our particular element types.
#include "meshes/quarter_circle_sector_mesh.h"
#include "meshes/one_d_lagrangian_mesh.h"
using namespace std;
using namespace oomph;
/// Namespace for physical parameters
namespace Global_Physical_Variables
 // Independent parameters:
 /// Square of Womersly number (a frequency parameter)
 double Alpha_sq=50.0;
 /// Density ratio of the solid and the fluid
 double Density_ratio=1.0;
```

```
/// External Pressure
double Pext=0.0;
 /// Poisson ratio
double Nu=0.49:
 /// Nondimensional thickness of the beam
double H=0.05;
 /// Perturbation pressure
double Pcos=0.0;
 // Dependent parameters:
 /// Reynolds number
double Re;
 /// Reynolds x Strouhal number
double ReSt;
 /// Timescale ratio (non-dimensation density)
double Lambda_sq;
 /// Stress ratio
double Q;
 /// \ short Set the parameters that are used in the code as a function
 /// of the Womersley number, the density ratio and {\tt H}
 void set_params()
 cout « "\n\n======= " «std::endl;
 cout « "\nSetting parameters. \n\n";
 cout « "Prescribed: Square of Womersley number: Alpha_sq = "
      « Alpha_sq « std::endl;
      " Density ratio: Density_ratio = "
" Density_ratio « std::endl;
" "
 cout « "
 cout « "
                    Wall thickness:
                                                    H = "
     « H « std::endl;
 « Nu « std::endl; cout « "
                    Poisson ratio:
                   Pressure perturbation: Pcos = "
      « Pcos « std::endl;
 Q=1.0/12.0*pow(H,3)/Alpha_sq;
 cout « "\nDependent: Stress ratio: « Q « std::endl;
                                                       0 = "
 Lambda_sq=1.0/12.0*pow(H,3)*Density_ratio;
                                           Lambda_sq = "
 cout « "
                    Timescale ratio:
      « Lambda_sq « std::endl;
 Re=Alpha_sq;
cout « " Reynolds number:
                                                   Re = "
      « Re « std::endl;
 ReSt=Re;
cout « "
                   Womersley number:
                                                  ReSt = "
 « ReSt « std::endl; cout « "\n======\n\n"
      «std::endl;
 /// Non-FSI load function, a constant external pressure plus
 \ensuremath{///} a (small) sinusoidal perturbation of wavenumber two.
for(unsigned i=0;i<2;i++)</pre>
  \{load[i] = (Pext - Pcos*cos(2.0*xi[0]))*N[i];\}
 }
//----
/// FSI Ring problem: a fluid-structure interaction problem in which
/// a viscous fluid bounded by an initially circular beam is set into motion
/// by a small sinusoidal perturbation of the beam (the domain boundary).
class FSIRingProblem : public Problem
 /// \short There are very few element types that will work for this problem.
/// Rather than passing the element type as a template parameter to the
 /// problem, we choose instead to use a typedef to specify the
 /// particular element fluid used.
typedef AlgebraicElement<RefineableQCrouzeixRaviartElement<2> > FLUID_ELEMENT;
 /// \short Typedef to specify the solid element used
typedef FSIHermiteBeamElement SOLID_ELEMENT;
 /// Constructor: Number of elements in wall mesh, amplitude of the
/// initial wall deformation, amplitude of pcos perturbation and its duration. FSIRingProblem(const unsigned &nelement_wall,
```

```
const double& eps_ampl, const double& pcos_initial,
                            const double& pcos_duration);
/// Update after solve (empty)
void actions_after_newton_solve() {}
/// \short Update before solve (empty)
void actions_before_newton_solve() {
/// \ short Update the problem specs before checking Newton
/// convergence
void actions before newton convergence check()
  // Update the fluid mesh -- auxiliary update function for algebraic
  // nodes automatically updates no slip condition.
 Fluid_mesh_pt->node_update();
/// \short Update the problem specs after adaptation:
void actions_after_adapt()
    \ensuremath{//} The functions used to update the no slip boundary conditions
    \ensuremath{//} must be set on any new nodes that have been created during the
    \ensuremath{//} mesh adaptation process.
    // There is no mechanism by which auxiliary update functions
    // are copied to newly created nodes.
    // (because, unlike boundary conditions, they don't occur exclusively
           at boundaries)
    // The no-slip boundary is boundary 1 of the mesh
    // Loop over the nodes on this boundary and reset the auxilliary
    // node update function
    unsigned n_node = Fluid_mesh_pt->nboundary_node(1);
    for (unsigned n=0;n<n_node;n++)</pre>
       {\tt Fluid\_mesh\_pt->boundary\_node\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)->set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_update\_fct\_pt\,(1,n)-set\_auxiliary\_node\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_update\_
         FSI_functions::apply_no_slip_on_moving_wall);
    // (Re-)setup fsi: Work out which fluid dofs affect wall elements
    // the correspondance between wall dofs and fluid elements is handled // during the remeshing, but the "reverse" association must be done
    // separately.
    // We need to set up the interaction every time because the fluid element
    // me head to be given interfaces. Very time because the filtrate element // adjacent to a given solid element s integration point may have changed // We pass the boundary between the fluid and solid meshes and pointers
    // to the meshes. The interaction boundary is boundary 1 of the 2D
     // fluid mesh.
    FSI_functions::setup_fluid_load_info_for_solid_elements<FLUID_ELEMENT,2>
      (this,1,Fluid_mesh_pt,Wall_mesh_pt);
/// \backslashshort Doc solution: Pass number of timestep, i (we append to tracefile
/// after every timestep but do a full doc only at certain intervals),
/// DocInfo object and tracefile
void doc_solution(const unsigned& i, DocInfo& doc_info, ofstream& trace_file);
/// Do dynamic run
void dynamic_run();
/// Setup initial condition for both domains
void set_initial_condition();
/// Setup initial condition for wall
void set_wall_initial_condition();
/// Setup initial condition for fluid
void set_fluid_initial_condition();
/// \short Element used for documenting displacement
SOLID_ELEMENT* Doc_displacement_elem_pt;
/// Pointer to wall mesh
OneDLagrangianMesh<SOLID_ELEMENT> *Wall_mesh_pt;
 /// Pointer to fluid mesh
AlgebraicRefineableQuarterCircleSectorMesh<FLUID_ELEMENT> *Fluid_mesh_pt;
/// Pointer to geometric object that represents the undeformed wall shape
GeomObject* Undef_geom_pt;
/// Pointer to wall timestepper
Newmark<2>* Wall_time_stepper_pt;
 /// Pointer to fluid timestepper
BDF<2>* Fluid_time_stepper_pt;
/// Pointer to node on coarsest mesh on which velocity is traced
```

```
Node* Veloc_trace_node_pt;
 /// Amplitude of initial deformation
double Eps_ampl;
 /// Initial pcos
double Pcos_initial;
 /// Duration of initial pcos
double Pcos_duration;
};
/// Setup initial condition: When we're done here, all variables
/// represent the state at the initial time.
void FSIRingProblem::set_initial_condition()
cout « "Setting wall ic" « std::endl;
set_wall_initial_condition();
cout « "Setting fluid ic" « std::endl;
 set_fluid_initial_condition();
/// Setup initial condition for fluid: Impulsive start
void FSIRingProblem::set_fluid_initial_condition()
 // Update fluid domain: Careful!!! This also applies the no slip conditions
 // on all nodes on the wall! Since the wall might have moved since
 // we created the mesh; we're therefore imposing a nonzero
 // velocity on these nodes. Must wipe this afterwards (done
 // by setting *all* velocities to zero) otherwise we get
 // an impulsive start from a very bizarre initial velocity
 // field! [Yes, it took me a while to figure this out...]
Fluid_mesh_pt->node_update();
 // Assign initial values for the velocities;
// pressures don't carry a time history and can be left alone.
//Find number of nodes in fluid mesh
 unsigned n_node = Fluid_mesh_pt->nnode();
 // Loop over the nodes to set initial guess everywhere
 for(unsigned n=0;n<n_node;n++)</pre>
  // Loop over velocity directions: Impulsive initial start from
   // zero velocity!
  for (unsigned i=0; i<2; i++)
     Fluid_mesh_pt->node_pt(n)->set_value(i,0.0);
    }
 // Do an impulsive start with the assigned velocity field
Fluid_mesh_pt->assign_initial_values_impulsive();
/// Setup initial condition: Impulsive start either from
/// deformed or undeformed wall shape.
void FSIRingProblem::set_wall_initial_condition()
 // Geometric object that specifies the initial conditions:
 // A ring that is bucked in a 2-lobed mode
GeomObject* ic_geom_object_pt=
 new PseudoBucklingRing(Eps_ampl,Global_Physical_Variables::H,2,2,
                         Wall_time_stepper_pt);
// Assign period of oscillation of the geometric object
static_cast<PseudoBucklingRing*>(ic_geom_object_pt)->set_T(1.0);
 //Set initial time (to deform wall into max. amplitude)
double time=0.25;
 // Assign initial radius of the object
 static_cast<PseudoBucklingRing*>(ic_geom_object_pt)->set_R_0(1.00);
 // Setup object that specifies the initial conditions:
SolidInitialCondition* IC_pt = new SolidInitialCondition(ic_geom_object_pt);
 // Assign values of positional data of all elements on wall mesh
 // so that the wall deforms into the shape specified by IC object.
{\tt SolidMesh::Solid\_IC\_problem.set\_static\_initial\_condition()}
 this, Wall_mesh_pt, IC_pt, time);
/// Document solution: Pass number of timestep, i; we append to trace file
/// at every timestep and do a full doc only after a certain number
/// of steps.
```

```
void FSIRingProblem::doc_solution(const unsigned& i,
    DocInfo& doc_info, ofstream& trace_file)
     // Full doc every nskip steps
     unsigned nskip=1; // ADJUST
      // If we at an integer multiple of nskip, full documentation.
      if (i%nskip==0)
          //Otherwise, just output the trace file
      else
           doc_info.disable_doc();
          cout « "Only trace for time "
                        « time_stepper_pt()->time_pt()->time() « std::endl;
      // If we are at a full documentation step, output the fluid solution
     if (doc_info.is_doc_enabled())
           //Variables used in the output file.
           ofstream some_file; char filename[100];
           //Construct the output filename from the doc_info number and the
          //output directory
sprintf(filename, "%s/soln%i.dat", doc_info.directory().c_str(),
                                doc info.number());
           //Open the output file
           some_file.open(filename);
            ///Output the solution using 5x5 plot points
           Fluid_mesh_pt->output(some_file,5);
           //Close the output file
          some_file.close();
      //Temporary vector to give the local coordinate at which to document
      //the wall displacment
     Vector<double> s(1,1.0);
      // Write to the trace file:
     trace_file « time_pt()->time()
        //Document the displacement at the end of the the chosen element
                                                " « Doc_displacement_elem_pt->interpolated_x(s,1)
                                     « " " « Veloc_trace_node_pt->x(0)
                                     « " " « Veloc_trace_node_pt->x(1)
                                     « " " « Veloc_trace_node_pt->value(0)
                                          " " « Veloc_trace_node_pt->value(1)
                                     « " " « Fluid_mesh_pt->nelement()
                                     « " " « ndof()
                                     « " " « Fluid_mesh_pt->nrefinement_overruled()
                                     " " « Fluid_mesh_pt->max_error()
                                     « " " « Fluid_mesh_pt->min_error()
                                          " " « Fluid_mesh_pt->max_permitted_error()
                                          " " « Fluid_mesh_pt->min_permitted_error()
                                     « " " « Fluid_mesh_pt->max_keep_unrefined();
     // Output the number of the corresponding full documentation // file number (or -1 if no full doc was made)
     if (doc_info.is_doc_enabled())
{trace_file « " " «doc_info.number() « " ";}
     else {trace_file « " " «-1 « "
     //End the trace file
     trace_file « std::endl;
      // Increment counter for full doc
     if (doc info.is doc enabled()) {doc info.number()++;}
/// Constructor for FSI ring problem. Pass number of wall elements
/// and length of wall (in Lagrangian coordinates) amplitude of
/// initial deformation, pcos perturbation and duration.
FSIRingProblem::FSIRingProblem(const unsigned& N,
                                             const double& eps_ampl, const double& pcos_initial,
                                             const double& pcos_duration) :
  Eps_ampl(eps_ampl), Pcos_initial(pcos_initial),
  Pcos_duration(pcos_duration)
   // Create timesteppers
   // Allocate the wall timestepper and add it to the problem's vector % \left( 1\right) =\left( 1\right) \left( 1\right)
  // of timesteppers
```

```
Wall_time_stepper_pt = new Newmark<2>;
add_time_stepper_pt(Wall_time_stepper_pt);
// Allocate the fluid timestepper and add it to the problem's Vector
// of timesteppers
Fluid_time_stepper_pt = new BDF<2>;
add_time_stepper_pt(Fluid_time_stepper_pt);
// Create the wall mesh
// Undeformed wall is an elliptical ring
Undef_geom_pt = new Ellipse(1.0,1.0);
//Length of wall in Lagrangian coordinates
double L = 2.0*atan(1.0);
//Now create the (Lagrangian!) mesh
Wall_mesh_pt = new
 OneDLagrangianMesh<SOLID_ELEMENT>(N,L,Undef_geom_pt,Wall_time_stepper_pt);
// Set the boundary conditions for wall mesh (problem)
// Bottom boundary: (Boundary 0)
// No vertical displacement
\label{lem:wall_mesh_pt-boundary_node_pt(0,0)->pin_position(1);} \\
// Zero slope: Pin type 1 dof for displacement direction 0 \,
Wall_mesh_pt->boundary_node_pt(0,0)->pin_position(1,0);
// Top boundary: (Boundary 1)
// No horizontal displacement
Wall_mesh_pt->boundary_node_pt(1,0)->pin_position(0);
// Zero slope: Pin type 1 dof for displacement direction 1
Wall_mesh_pt->boundary_node_pt(1,0)->pin_position(1,1);
// Fluid mesh is suspended from wall between the following Lagrangian
// coordinates:
double xi_lo=0.0;
double xi_hi=L;
// Fractional position of dividing line for two outer blocks in mesh
double fract_mid=0.5;
//Create a geometric object that represents the wall geometry from the
//wall mesh (one Lagrangian, two Eulerian coordinates).
MeshAsGeomObject *wall_mesh_as_geometric_object_pt
 = new MeshAsGeomObject(Wall_mesh_pt);
// Build fluid mesh using the wall mesh as a geometric object
Fluid_mesh_pt = new AlgebraicRefineableQuarterCircleSectorMesh<FLUID_ELEMENT >
 (wall_mesh_as_geometric_object_pt,
  xi_lo,fract_mid,xi_hi,Fluid_time_stepper_pt);
// Set the error estimator
Z2ErrorEstimator* error_estimator_pt=new Z2ErrorEstimator;
Fluid_mesh_pt->spatial_error_estimator_pt()=error_estimator_pt;
// Extract pointer to node at center of mesh
unsigned nnode=Fluid_mesh_pt->finite_element_pt(0)->nnode();
Veloc_trace_node_pt=Fluid_mesh_pt->finite_element_pt(0)->node_pt(nnode-1);
// Set the fluid boundary conditions
// Bottom boundary (boundary 0):
 unsigned n_node = Fluid_mesh_pt->nboundary_node(0);
 for (unsigned n=0;n<n_node;n++)</pre>
   // Pin vertical velocity
   {\tt Fluid\_mesh\_pt->boundary\_node\_pt(0,n)->pin(1);}
// Ring boundary (boundary 1):
// No slip; this also implies that the velocity needs
// to be updated in response to wall motion
 unsigned n_node = Fluid_mesh_pt->nboundary_node(1);
 for (unsigned n=0;n<n_node;n++)</pre>
   // Which node are we dealing with?
   Node* node_pt=Fluid_mesh_pt->boundary_node_pt(1,n);
   // Set auxiliary update function pointer node_pt->set_auxiliary_node_update_fct_pt(
    FSI_functions::apply_no_slip_on_moving_wall);
   // Pin both velocities
   for(unsigned i=0;i<2;i++) {node_pt->pin(i);}
}
```

```
// Left boundary (boundary 2):
        unsigned n_node = Fluid_mesh_pt->nboundary_node(2);
        for (unsigned n=0;n<n_node;n++)</pre>
              // Pin horizontal velocity
                  Fluid_mesh_pt->boundary_node_pt(2,n)->pin(0);
          }
   // Add the submeshes and build global mesh
   // Wall mesh
   add_sub_mesh(Wall_mesh_pt);
   //Fluid mesh
   add_sub_mesh(Fluid_mesh_pt);
   // Combine all submeshes into a single Mesh
  build_global_mesh();
   // Finish problem setup
   //Find number of elements in fluid mesh
  unsigned n_element = Fluid_mesh_pt->nelement();
   // Loop over the fluid elements to set up element-specific
   // things that cannot be handled by constructor
   for(unsigned e=0;e<n_element;e++)</pre>
        // Upcast from FiniteElement to the present element
        FLUID_ELEMENT *el_pt
          = dynamic_cast<FLUID_ELEMENT*>(Fluid_mesh_pt->element_pt(e));
        //Set the Reynolds number, etc
el_pt->re_pt() = &Global_Physical_Variables::Re;
        el_pt->re_st_pt() = &Global_Physical_Variables::ReSt;
        el_pt->evaluate_shape_derivs_by_direct_fd();
             el_pt->evaluate_shape_derivs_by_chain_rule();
             el_pt->enable_always_evaluate_dresidual_dnodal_coordinates_by_fd();
//
//
//
//
                      el_pt->disable_always_evaluate_dresidual_dnodal_coordinates_by_fd();
                else
                      el_pt->enable_always_evaluate_dresidual_dnodal_coordinates_by_fd();
        //el_pt->evaluate_shape_derivs_by_direct_fd();
   //Loop over the solid elements to set physical parameters etc.
   unsigned n_wall_element = Wall_mesh_pt->nelement();
   for (unsigned e=0;e<n_wall_element;e++)</pre>
        //Cast to proper element type
SOLID_ELEMENT *el_pt = dynamic_cast<SOLID_ELEMENT*>(
          Wall_mesh_pt->element_pt(e));
        //Set physical parameters for each element:
        el_pt->h_pt() = &Global_Physical_Variables::H;
        el_pt->lambda_sq_pt() = &Global_Physical_Variables::Lambda_sq;
        //Function that specifies the external load Vector
        el_pt->load_vector_fct_pt() = &Global_Physical_Variables::pcos_load;
        // Function that specifies the load ratios
        el_pt->q_pt() = &Global_Physical_Variables::Q;
        //Assign the undeformed beam shape
        el_pt->undeformed_beam_pt() = Undef_geom_pt;
   // Establish control displacment: (even if no displacement control is applied
   // we still want to doc the displacement at the same point)
   // Choose element: (This is the last one)
  Doc_displacement_elem_pt = dynamic_cast<SOLID_ELEMENT*>(
     Wall_mesh_pt->element_pt(n_wall_element-1));
   // Setup fsi: Work out which fluid dofs affect the wall elements
   // the correspondance between wall dofs and fluid elements is handled // during the remeshing, but the "reverse" association must be done
   // separately.
   // We pass the boundary between the fluid and solid meshes and pointers % \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) 
   // to the meshes. The interaction boundary is boundary 1 of the
    // 2D fluid mesh.
   FSI_functions::setup_fluid_load_info_for_solid_elements<FLUID_ELEMENT,2>
      (this, 1, Fluid_mesh_pt, Wall_mesh_pt);
  // Do equation numbering
cout « "# of dofs " « assign_eqn_numbers() « std::endl;
```

```
/// Solver loop to perform unsteady run
void FSIRingProblem::dynamic run()
 // Setup documentation
 /// Label for output
 DocInfo doc_info;
 // Output directory
 doc_info.set_directory("RESLT");
 // Step number
 doc_info.number()=0;
//Open a trace file
ofstream trace_file("RESLT/trace_ring.dat");
// Write header for trace file
trace_file « "VARIABLES=\"time\",\"V_c_t_r_l\"";
trace_file « ",\"x<sub>!</sub><sup>(track)</sup>\"";
trace_file « ",\"u<sub>2</sub><sup>(track)</sup>\"";
trace_file « ",\"u<sub>2</sub><sup>(track)</sup>\"";
trace_file « ",\"u<sub>2</sub><sup>(track)</sup>\"";
trace_file « ",\"u<sub>2</sub><sup>(track)</sup>\"";
trace_file « ",\"N<sub>element</sub>\"";
trace_file « ",\"N<sub>dof</sub>\"";
trace_file « ",\"# of under-refined elements\"";
trace_file « ",\"max. error\"";
trace_file « ",\"min. error\"";
trace_file « ",\"min. permitted error\"";
trace_file « ",\"min. permitted error\"";
trace_file « ",\"max. permitted # of unrefined elements\"";
trace_file « ",\"max. permitted # of unrefined elements\"";
trace_file « ",\"doc number\"";
trace_file « std::endl;
 // Write header for trace file
 trace_file « std::endl;
 // Initialise timestepping
 // Number of steps
 unsigned nstep=300;
 // Nontrivial command line input: validation: only do three steps
 if (CommandLineArgs::Argc>1)
   nstep=1:
    cout « "Only doing nstep steps for validation: " « nstep « std::endl;
 }
// Set initial timestep
 double dt=0.004;
 // Set initial value for dt -- also assigns weights to the timesteppers
 initialise_dt(dt);
 // Set physical parameters
 using namespace Global_Physical_Variables;
 // Set Womersley number
 Alpha_sq=100.0; // 50.0; // ADJUST
 // Set density ratio
 Density_ratio=10.0; // 0.0; ADJUST // Wall thickness
 H=1.0/20.0;
 // Set external pressure
 Pext=0.0:
 /// Perturbation pressure
 Pcos=Pcos_initial;
 // Assign/doc corresponding computational parameters
 set_params();
 // Refine uniformly and assign initial conditions
 // Refine the problem uniformly
 refine_uniformly();
 refine_uniformly();
 // This sets up the solution at the initial time
 set_initial_condition();
 // Set targets for spatial adptivity
 // Max. and min. error for adaptive refinement/unrefinement
 Fluid_mesh_pt->max_permitted_error()=1.0e-2;
 Fluid_mesh_pt->min_permitted_error()=1.0e-3;
 // Don't allow refinement to drop under given level
 Fluid_mesh_pt->min_refinement_level()=2;
 // Don't allow refinement beyond given level
 Fluid mesh pt->max refinement level()=6;
 // Don't bother adapting the mesh if no refinement is required
  // and if less than \dots elements are to be merged.
 Fluid_mesh_pt->max_keep_unrefined()=20;
 // Doc refinement targets
 Fluid_mesh_pt->doc_adaptivity_targets(cout);
 // Do the timestepping
```

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```
// Reset initial conditions after refinement for first step only
bool first=true;
//Output initial data
doc_solution(0,doc_info,trace_file);
     unsigned nel=Fluid_mesh_pt->nelement();
     for (unsigned e=0; e<nel; e++)
       std::cout « "\n\nEl: " « e « std::endl « std::endl;
       FiniteElement* el_pt=Fluid_mesh_pt->finite_element_pt(e);
unsigned n_dof=el_pt->ndof();
Vectorsdoubles
       Vector<double> residuals(n_dof);
       DenseDoubleMatrix jacobian(n_dof,n_dof);
       el_pt->get_jacobian(residuals, jacobian);
     exit(0);
// Time integration loop
 for (unsigned i=1;i<=nstep;i++)</pre>
   // Switch doc off during solve
   doc_info.disable_doc();
   // Solve
   unsigned max_adapt=1;
   unsteady_newton_solve(dt,max_adapt,first);
   // Now we've done the first step
   first=false;
   // Doc solution
   doc solution (i, doc info, trace file);
   /// Switch off perturbation pressure
   if (time_pt()->time()>Pcos_duration) {Pcos=0.0;}
/// Driver for fsi ring test problem
int main(int argc, char* argv[])
 // Store command line arguments
CommandLineArgs::setup(argc,argv);
 // Number of elements
unsigned nelem = 13;
 /// Perturbation pressure
double pcos_initial=1.0e-6; // ADJUST
/// Duration of initial pcos perturbation double pcos_duration=0.3; // ADJUST
/// Amplitude of initial deformation double eps_ampl=0.0; // ADJUST
 //Set up the problem
 FSIRingProblem problem (nelem, eps_ampl, pcos_initial, pcos_duration);
 // Do parameter study
 problem.dynamic_run();
```

## 1.1 PDF file

A pdf version of this document is available.