

$$\text{Var}(\hat{\beta}) = \text{Var}((X^T X)^{-1} X^T y)$$

$$= (X^T X)^{-2} X^T X \text{Var}(y)$$

$$= \underline{\underline{(X^T X)^{-1} \sigma_y^2}}$$