

$$y_0 = f(x_0) + \varepsilon_0 \quad (3.21)$$

$$\hat{f}(x_0) = x_0^T \hat{\beta}$$

$$\begin{aligned} E(y_0 - \hat{f}(x_0))^2 &= E((y_0 - E(y_0)) - (\hat{f}(x_0) - E(y_0)))^2 \\ &= E(y_0 - E(y_0))^2 - 2E((y_0 - E(y_0))(\hat{f}(x_0) - E(y_0))) + E(\hat{f}(x_0) - E(y_0))^2 \\ &= \sigma^2 - \cancel{2E(y_0)\hat{f}(x_0)} + \cancel{2E(y_0)E(y_0)} + \cancel{2E(y_0)\hat{f}(x_0)} - \cancel{2E(y_0)E(y_0)} + E(\hat{f}(x_0) - f(x_0))^2 \\ &= \sigma^2 + E(x_0^T \hat{\beta} - f(x_0))^2 \\ &= \sigma^2 + \text{MSE}(\hat{f}(x_0)) \quad (3.22) \end{aligned}$$