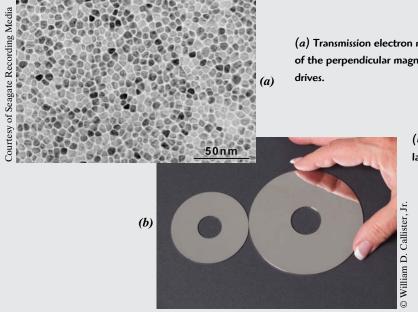
# Chapter 20 Magnetic Properties

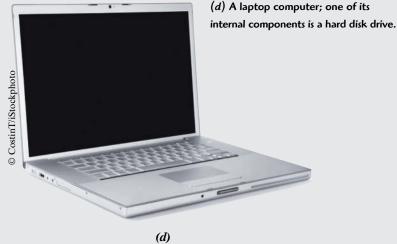


(a) Transmission electron micrograph showing the microstructure of the perpendicular magnetic recording medium used in hard disk drives.

(b) Magnetic storage hard disks used in laptop (left) and desktop (right) computers.



(c) The inside of a hard disk drive. The circular disk will typically spin at a rotational velocity of 5400 or 7200 revolutions per minute.



## WHY STUDY the Magnetic Properties of Materials?

An understanding of the mechanism that explains the permanent magnetic behavior of some materials may allow us to alter and in some cases tailor the magnetic properties. For example, in Design Example 20.1 we note how the behavior of a ceramic magnetic material may be enhanced by changing its composition.

## Learning Objectives

After studying this chapter, you should be able to do the following:

- Determine the magnetization of some material given its magnetic susceptibility and the applied magnetic field strength.
- From an electronic perspective, note and briefly explain the two sources of magnetic moments in materials.
- Briefly explain the nature and source of

   (a) diamagnetism, (b) paramagnetism, and
   (c) ferromagnetism.
- **4.** In terms of crystal structure, explain the source of ferrimagnetism for cubic ferrites.
- **5.** (a) Describe magnetic hysteresis; (b) explain why ferromagnetic and ferrimagnetic materials experience magnetic hysteresis; and (c) explain why these materials may become permanent magnets.
- Note the distinctive magnetic characteristics for both soft and hard magnetic materials.
- **7.** Describe the phenomenon of *superconductivity*.

#### **20.1 INTRODUCTION**

Magnetism—the phenomenon by which materials exert an attractive or repulsive force or influence on other materials—has been known for thousands of years. However, the underlying principles and mechanisms that explain magnetic phenomena are complex and subtle, and their understanding has eluded scientists until relatively recent times. Many modern technological devices rely on magnetism and magnetic materials, including electrical power generators and transformers, electric motors, radio, television, telephones, computers, and components of sound and video reproduction systems.

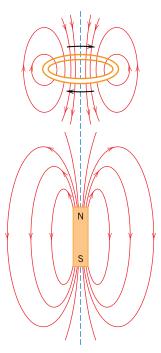
Iron, some steels, and the naturally occurring mineral lodestone are well-known examples of materials that exhibit magnetic properties. Not so familiar, however, is the fact that all substances are influenced to one degree or another by the presence of a magnetic field. This chapter provides a brief description of the origin of magnetic fields and discusses magnetic field vectors and magnetic parameters; diamagnetism, paramagnetism, ferromagnetism, and ferrimagnetism; different magnetic materials; and superconductivity.

#### 20.2 BASIC CONCEPTS

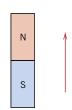
## Magnetic Dipoles

Magnetic forces are generated by moving electrically charged particles; these magnetic forces are in addition to any electrostatic forces that may exist. Often it is convenient to think of magnetic forces in terms of fields. Imaginary lines of force may be drawn to indicate the direction of the force at positions in the vicinity of the field source. The magnetic field distributions as indicated by lines of force are shown for a current loop and a bar magnet in Figure 20.1.

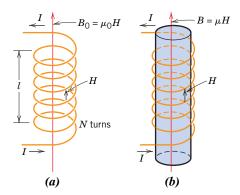
Magnetic dipoles are found to exist in magnetic materials, which, in some respects, are analogous to electric dipoles (Section 18.19). Magnetic dipoles may be thought of as small bar magnets composed of north and south poles instead of positive and negative



**Figure 20.1** Magnetic field lines of force around a current loop and a bar magnet.



**Figure 20.2** The magnetic moment as designated by an arrow.



**Figure 20.3** (a) The magnetic field H as generated by a cylindrical coil is dependent on the current I, the number of turns N, and the coil length l, according to Equation 20.1. The magnetic flux density  $B_0$  in the presence of a vacuum is equal to  $\mu_0 H$ , where  $\mu_0$  is the permeability of a vacuum,  $4\pi \times 10^{-7}$  H/m. (b) The magnetic flux density B within a solid material is equal to  $\mu H$ , where  $\mu$  is the permeability of the solid material. (Adapted from A. G. Guy, Essentials of Materials Science, McGraw-Hill Book Company, New York, 1976.)

electric charges. In our discussion, magnetic dipole moments are represented by arrows, as shown in Figure 20.2. Magnetic dipoles are influenced by magnetic fields in a manner similar to the way in which electric dipoles are affected by electric fields (Figure 18.30). Within a magnetic field, the force of the field exerts a torque that tends to orient the dipoles with the field. A familiar example is the way in which a magnetic compass needle lines up with the Earth's magnetic field.

## **Magnetic Field Vectors**

Before discussing the origin of magnetic moments in solid materials, we describe magnetic behavior in terms of several field vectors. The externally applied magnetic field, sometimes called the **magnetic field strength**, is designated by H. If the magnetic field is generated by means of a cylindrical coil (or solenoid) consisting of N closely spaced turns having a length l and carrying a current of magnitude I, then

$$H = \frac{NI}{l} \tag{20.1}$$

A schematic diagram of such an arrangement is shown in Figure 20.3a. The magnetic field that is generated by the current loop and the bar magnet in Figure 20.1 is an H field. The units of H are ampere-turns per meter, or just amperes per meter.

The **magnetic induction**, or **magnetic flux density**, denoted by B, represents the magnitude of the internal field strength within a substance that is subjected to an H

## magnetic field strength

Magnetic field strength within a coil—dependence on number of turns, applied current, and coil length

magnetic induction
magnetic flux density

field. The units for B are teslas [or webers per square meter (Wb/m<sup>2</sup>)]. Both B and H are field vectors, being characterized not only by magnitude, but also by direction in space.

Magnetic flux density in a materialdependence on permeability and magnetic field strength

The magnetic field strength and flux density are related according to

$$B = \mu H \tag{20.2}$$

## permeability

The parameter  $\mu$  is called the **permeability**, which is a property of the specific medium through which the H field passes and in which B is measured, as illustrated in Figure 20.3b. The permeability has dimensions of webers per ampere-meter (Wb/A·m) or henries per meter (H/m).

In a vacuum,

Magnetic flux density in a vacuum

$$B_0 = \mu_0 H \tag{20.3}$$

where  $\mu_0$  is the permeability of a vacuum, a universal constant, which has a value of  $4\pi \times 10^{-7}$  (1.257  $\times$  10<sup>-6</sup>) H/m. The parameter  $B_0$  represents the flux density within a vacuum as demonstrated in Figure 20.3a.

Several parameters may be used to describe the magnetic properties of solids. One of these is the ratio of the permeability in a material to the permeability in a vacuum, or

Definition of relative permeability

$$\mu_r = \frac{\mu}{\mu_0} \tag{20.4}$$

where  $\mu_r$  is called the *relative permeability*, which is unitless. The permeability or relative permeability of a material is a measure of the degree to which the material can be magnetized, or the ease with which a B field can be induced in the presence of an external H field.

Another field quantity, M, called the **magnetization** of the solid, is defined by the expression

$$B = \mu_0 H + \mu_0 M \tag{20.5}$$

In the presence of an H field, the magnetic moments within a material tend to become aligned with the field and to reinforce it by virtue of their magnetic fields; the term  $\mu_0 M$ in Equation 20.5 is a measure of this contribution.

The magnitude of *M* is proportional to the applied field as follows:

$$M = \chi_m H \tag{20.6}$$

and  $\chi_m$  is called the magnetic susceptibility, which is unitless. The magnetic susceptibility and the relative permeability are related as follows:

$$\chi_m = \mu_r - 1 \tag{20.7}$$

#### Magnetic flux density—as a function of magnetic field strength and magnetization of a material

magnetization

Magnetization of a materialdependence on susceptibility and magnetic field strength

## magnetic susceptibility

Relationship between magnetic susceptibility and relative permeability

<sup>&</sup>lt;sup>1</sup>This  $\chi_m$  is taken to be the volume susceptibility in SI units, which, when multiplied by H, yields the magnetization per unit volume (cubic meter) of material. Other susceptibilities are also possible; see Problem 20.3.

| · ·                               |                                   |   | J                   | •                       |   |
|-----------------------------------|-----------------------------------|---|---------------------|-------------------------|---|
|                                   |                                   | SI Units                                |                     |                         |   |
| Quantity                          | Symbol                            | Derived                                 | Primary             | cgs-emu Unit            | Conversion  |
| Magnetic induction (flux density) | В                                 | Tesla (Wb/m <sup>2</sup> ) <sup>a</sup> | kg/s•C              | Gauss                   | $1 \text{ Wb/m}^2 = 10^4 \text{ gauss}$               |
| Magnetic field strength           | H                                 | Amp·turn/m                              | C/m·s               | Oersted                 | 1 amp·turn/m = $4\pi \times 10^{-3}$ oersted          |
| Magnetization                     | M (SI) I (cgs-emu)                | Amp·turn/m                              | C/m·s               | Maxwell/cm <sup>2</sup> | $1 \text{ amp-turn/m} = 10^{-3} \text{ maxwell/cm}^2$ |
| Permeability of a vacuum          | $\mu_0$                           | Henry/m <sup>b</sup>                    | kg·m/C <sup>2</sup> | Unitless (emu)          | $4\pi \times 10^{-7} \text{ henry/m} = 1 \text{ emu}$ |
| Relative permeability             | $\mu_r$ (SI) $\mu'$ (cgs-emu)     | Unitless                                | Unitless            | Unitless                | $\mu_r = \mu'$  |
| Susceptibility                    | $\chi_m$ (SI) $\chi'_m$ (cgs-emu) | Unitless                                | Unitless            | Unitless                | $\chi_m = 4\pi\chi_m^{\prime}$                        |

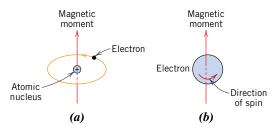
Table 20.1 Magnetic Units and Conversion Factors for the SI and cgs-emu Systems

There is a dielectric analogue for each of the foregoing magnetic field parameters. The B and H fields are, respectively, analogous to the dielectric displacement D and the electric field  $\mathscr E$ , whereas the permeability  $\mu$  is analogous to the permittivity  $\epsilon$  (cf. Equations 20.2 and 18.30). Furthermore, the magnetization M and polarization P are correlates (Equations 20.5 and 18.31).

Magnetic units may be a source of confusion because there are really two systems in common use. The ones used thus far are SI [rationalized *MKS* (meter-kilogram-second)]; the others come from the *cgs-emu* (centimeter-gram-second-electromagnetic unit) system. The units for both systems as well as the appropriate conversion factors are given in Table 20.1.

#### Origins of Magnetic Moments

The macroscopic magnetic properties of materials are a consequence of *magnetic moments* associated with individual electrons. Some of these concepts are relatively complex and involve some quantum mechanical principles beyond the scope of this discussion; consequently, simplifications have been made and some of the details omitted. Each electron in an atom has magnetic moments that originate from two sources. One is related to its orbital motion around the nucleus; because it is a moving charge, an electron may be considered to be a small current loop, generating a very small magnetic field and having a magnetic moment along its axis of rotation, as schematically illustrated in Figure 20.4a.



**Figure 20.4** Demonstration of the magnetic moment associated with (a) an orbiting electron and (b) a spinning electron.

<sup>&</sup>lt;sup>a</sup>Units of the weber (Wb) are volt-seconds.

<sup>&</sup>lt;sup>b</sup>Units of the henry are webers per ampere.

Each electron may also be thought of as spinning around an axis; the other magnetic moment originates from this electron spin, which is directed along the spin axis as shown in Figure 20.4b. Spin magnetic moments may be only in an "up" direction or in an antiparallel "down" direction. Thus each electron in an atom may be thought of as being a small magnet having permanent orbital and spin magnetic moments.

**Bohr magneton** 

The most fundamental magnetic moment is the **Bohr magneton**  $\mu_{\rm B}$ , which is of magnitude  $9.27 \times 10^{-24}~{\rm A\cdot m^2}$ . For each electron in an atom, the spin magnetic moment is  $\pm \mu_{\rm B}$  (plus for spin up, minus for spin down). Furthermore, the orbital magnetic moment contribution is equal to  $m_l \mu_{\rm B}$ ,  $m_l$  being the magnetic quantum number of the electron, as mentioned in Section 2.3.

In each atom, orbital moments of some electron pairs cancel each other; this also holds true for the spin moments. For example, the spin moment of an electron with spin up cancels that of one with spin down. The net magnetic moment, then, for an atom is just the sum of the magnetic moments of each of the constituent electrons, including both orbital and spin contributions, and taking into account moment cancellation. For an atom having completely filled electron shells or subshells, when all electrons are considered, there is total cancellation of both orbital and spin moments. Thus, materials composed of atoms having completely filled electron shells are not capable of being permanently magnetized. This category includes the inert gases (He, Ne, Ar, etc.) as well as some ionic materials. The types of magnetism include diamagnetism, paramagnetism, and ferromagnetism; in addition, antiferromagnetism and ferrimagnetism are considered to be subclasses of ferromagnetism. All materials exhibit at least one of these types, and the behavior depends on the response of electron and atomic magnetic dipoles to the application of an externally applied magnetic field.

#### 20.3 DIAMAGNETISM AND PARAMAGNETISM

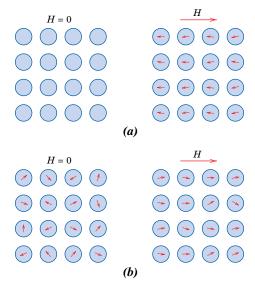
diamagnetism

**Diamagnetism** is a very weak form of magnetism that is nonpermanent and persists only while an external field is being applied. It is induced by a change in the orbital motion of electrons due to an applied magnetic field. The magnitude of the induced magnetic moment is extremely small and in a direction opposite to that of the applied field. Thus, the relative permeability  $\mu_r$  is less than unity (however, only very slightly), and the magnetic susceptibility is negative—that is, the magnitude of the B field within a diamagnetic solid is less than that in a vacuum. The volume susceptibility  $\chi_m$  for diamagnetic solid materials is on the order of  $-10^{-5}$ . When placed between the poles of a strong electromagnet, diamagnetic materials are attracted toward regions where the field is weak.

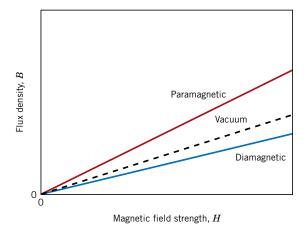
Figure 20.5a illustrates schematically the atomic magnetic dipole configurations for a diamagnetic material with and without an external field; here, the arrows represent atomic dipole moments, whereas for the preceding discussion, arrows denoted only electron moments. The dependence of B on the external field H for a material that exhibits diamagnetic behavior is presented in Figure 20.6. Table 20.2 gives the susceptibilities of several diamagnetic materials. Diamagnetism is found in all materials, but because it is so weak, it can be observed only when other types of magnetism are totally absent. This form of magnetism is of no practical importance.

For some solid materials, each atom possesses a permanent dipole moment by virtue of incomplete cancellation of electron spin and/or orbital magnetic moments. In the absence of an external magnetic field, the orientations of these atomic magnetic moments are random, such that a piece of material possesses no net macroscopic magnetization. These atomic dipoles are free to rotate, and **paramagnetism** results when they preferentially align, by rotation, with an external field as shown in Figure 20.5b. These magnetic dipoles are acted on individually with no mutual interaction between

paramagnetism



**Figure 20.5** (a) The atomic dipole configuration for a diamagnetic material with and without a magnetic field. In the absence of an external field, no dipoles exist; in the presence of a field, dipoles are induced that are aligned opposite to the field direction. (b) Atomic dipole configuration with and without an external magnetic field for a paramagnetic material.



**Figure 20.6** Schematic representation of the flux density B versus the magnetic field strength H for diamagnetic and paramagnetic materials.

adjacent dipoles. Inasmuch as the dipoles align with the external field, they enhance it, giving rise to a relative permeability  $\mu_r$  that is greater than unity and to a relatively small but positive magnetic susceptibility. Susceptibilities for paramagnetic materials range from about  $10^{-5}$  to  $10^{-2}$  (Table 20.2). A schematic B-versus-H curve for a paramagnetic material is shown in Figure 20.6.

Both diamagnetic and paramagnetic materials are considered nonmagnetic because they exhibit magnetization only when in the presence of an external field. Also, for both, the flux density B within them is almost the same as it would be in a vacuum.

**Table 20.2** Room-Temperature Magnetic Susceptibilities for Diamagnetic and Paramagnetic **Materials** 

| Diamag          | netics  | Paramagnetics     |   |  |
|-----------------|---|-------------------|---|--|
| Material        | Susceptibility<br>χ <sub>m</sub> (volume)<br>(SI units) | Material          | Susceptibility<br>\(\chi_m\) (volume)<br>(SI units) |  |
| Aluminum oxide  | $-1.81 \times 10^{-5}$                                  | Aluminum          | $2.07 \times 10^{-5}$                               |  |
| Copper          | $-0.96 \times 10^{-5}$                                  | Chromium          | $3.13 \times 10^{-4}$                               |  |
| Gold            | $-3.44 \times 10^{-5}$                                  | Chromium chloride | $1.51 \times 10^{-3}$                               |  |
| Mercury         | $-2.85 \times 10^{-5}$                                  | Manganese sulfate | $3.70 \times 10^{-3}$                               |  |
| Silicon         | $-0.41 \times 10^{-5}$                                  | Molybdenum        | $1.19 \times 10^{-4}$                               |  |
| Silver          | $-2.38 \times 10^{-5}$                                  | Sodium            | $8.48 \times 10^{-6}$                               |  |
| Sodium chloride | $-1.41 \times 10^{-5}$                                  | Titanium          | $1.81 \times 10^{-4}$                               |  |
| Zinc            | $-1.56 \times 10^{-5}$                                  | Zirconium         | $1.09 \times 10^{-4}$                               |  |

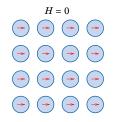
#### **20.4 FERROMAGNETISM**

ferromagnetism

domain

saturation magnetization

For a ferromagnetic material, relationship between magnetic flux density and magnetization



## Figure 20.7

Schematic illustration of the mutual alignment of atomic dipoles for a ferromagnetic material, which will exist even in the absence of an external magnetic field.

Certain metallic materials possess a permanent magnetic moment in the absence of an external field and manifest very large and permanent magnetizations. These are the characteristics of **ferromagnetism**, and they are displayed by the transition metals iron (as BCC  $\alpha$ -ferrite), cobalt, nickel, and some rare earth metals such as gadolinium (Gd). Magnetic susceptibilities as high as  $10^6$  are possible for ferromagnetic materials. Consequently,  $H \ll M$ , and from Equation 20.5 we write

$$B \cong \mu_0 M \tag{20.8}$$

Permanent magnetic moments in ferromagnetic materials result from atomic magnetic moments due to uncanceled electron spins as a consequence of the electron structure. There is also an orbital magnetic moment contribution that is small in comparison to the spin moment. Furthermore, in a ferromagnetic material, coupling interactions cause net spin magnetic moments of adjacent atoms to align with one another, even in the absence of an external field. This is schematically illustrated in Figure 20.7. The origin of these coupling forces is not completely understood, but they are thought to arise from the electronic structure of the metal. This mutual spin alignment exists over relatively large-volume regions of the crystal called **domains** (see Section 20.7).

The maximum possible magnetization, or **saturation magnetization**,  $M_s$ , of a ferromagnetic material represents the magnetization that results when all the magnetic dipoles in a solid piece are mutually aligned with the external field; there is also a corresponding saturation flux density,  $B_s$ . The saturation magnetization is equal to the product of the net magnetic moment for each atom and the number of atoms present. For each of iron, cobalt, and nickel, the net magnetic moments per atom are 2.22, 1.72, and 0.60 Bohr magnetons, respectively.

## **EXAMPLE PROBLEM 20.1**

## Saturation Magnetization and Flux Density Computations for Nickel

Calculate (a) the saturation magnetization and (b) the saturation flux density for nickel, which has a density of 8.90 g/cm<sup>3</sup>.

#### Solution

(a) The saturation magnetization is the product of the number of Bohr magnetons per atom (0.60, as given above), the magnitude of the Bohr magneton  $\mu_B$ , and the number N of atoms per cubic meter, or

$$M_s = 0.60 \,\mu_{\rm B} N \tag{20.9}$$

The number of atoms per cubic meter is related to the density  $\rho$ , the atomic weight  $A_{\text{Ni}}$ , and Avogadro's number  $N_{\text{A}}$ , as follows:

$$N = \frac{\rho N_{\rm A}}{A_{\rm Ni}}$$

$$= \frac{(8.90 \times 10^6 \,\mathrm{g/m^3})(6.022 \times 10^{23} \,\mathrm{atoms/mol})}{58.71 \,\mathrm{g/mol}}$$

$$= 9.13 \times 10^{28} \,\mathrm{atoms/m^3}$$
(20.10)

Saturation magnetization for nickel

For nickel, computation of the number of atoms per unit volume Finally,

$$M_s = \left(\frac{0.60 \text{ Bohr magneton}}{\text{atom}}\right) \left(\frac{9.27 \times 10^{-24} \text{ A} \cdot \text{m}^2}{\text{Bohr magneton}}\right) \left(\frac{9.13 \times 10^{28} \text{ atoms}}{\text{m}^3}\right)$$
$$= 5.1 \times 10^5 \text{ A/m}$$

**(b)** From Equation 20.8, the saturation flux density is

$$\begin{split} B_s &= \mu_0 M_s \\ &= \bigg(\frac{4\pi \times 10^{-7} \,\mathrm{H}}{\mathrm{m}}\bigg) \bigg(\frac{5.1 \times 10^5 \,\mathrm{A}}{\mathrm{m}}\bigg) \\ &= 0.64 \,\mathrm{tesla} \end{split}$$

## 20.5 ANTIFERROMAGNETISM AND FERRIMAGNETISM

## Antiferromagnetism

antiferromagnetism

Magnetic moment coupling between adjacent atoms or ions also occurs in materials other than those that are ferromagnetic. In one such group, this coupling results in an antiparallel alignment; the alignment of the spin moments of neighboring atoms or ions in exactly opposite directions is termed **antiferromagnetism**. Manganese oxide (MnO) is one material that displays this behavior. Manganese oxide is a ceramic material that is ionic in character, having both Mn<sup>2+</sup> and O<sup>2-</sup> ions. No net magnetic moment is associated with the O<sup>2-</sup> ions because there is a total cancellation of both spin and orbital moments. However, the Mn<sup>2+</sup> ions possess a net magnetic moment that is predominantly of spin origin. These Mn<sup>2+</sup> ions are arrayed in the crystal structure such that the moments of adjacent ions are antiparallel. This arrangement is represented schematically in Figure 20.8. The opposing magnetic moments cancel one another, and, as a consequence, the solid as a whole possesses no net magnetic moment.

## **Ferrimagnetism**

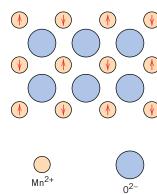
ferrimagnetism

Some ceramics also exhibit a permanent magnetization, termed **ferrimagnetism.** The macroscopic magnetic characteristics of ferromagnets and ferrimagnets are similar; the distinction lies in the source of the net magnetic moments. The principles of ferrimagnetism are illustrated with the cubic ferrites. These ionic materials may be represented by the chemical formula  $MFe_2O_4$ , in which M represents any one of several metallic elements. The prototype ferrite is  $Fe_3O_4$ —the mineral magnetite, sometimes called lodestone.

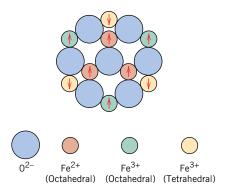
The formula for  $Fe_3O_4$  may be written as  $Fe^{2+}O^{2-}(Fe^{3+})_2(O^{2-})_3$ , in which the Fe ions exist in both +2 and +3 valence states in the ratio of 1:2. A net spin magnetic moment exists for each  $Fe^{2+}$  and  $Fe^{3+}$  ion, which corresponds to 4 and 5 Bohr magnetons, respectively, for the two ion types. Furthermore, the  $O^{2-}$  ions are magnetically neutral. There are antiparallel spin-coupling interactions between the Fe ions, similar in character to antiferromagnetism. However, the net ferrimagnetic moment arises from the incomplete cancellation of spin moments.

Cubic ferrites have the inverse spinel crystal structure, which is cubic in symmetry and is similar to the spinel structure (Section 12.2). The inverse spinel crystal structure might be thought of as having been generated by the stacking of close-packed planes

<sup>&</sup>lt;sup>2</sup>Ferrite in the magnetic sense should not be confused with the ferrite  $\alpha$ -iron discussed in Section 9.18; in the remainder of this chapter, the term **ferrite** indicates the magnetic ceramic.



**Figure 20.8** Schematic representation of antiparallel alignment of spin magnetic moments for antiferromagnetic manganese oxide.



**Figure 20.9** Schematic diagram showing the spin magnetic moment configuration for Fe<sup>2+</sup> and Fe<sup>3+</sup> ions in Fe<sub>3</sub>O<sub>4</sub>. (From Richard A. Flinn and Paul K. Trojan, *Engineering Materials and Their Applications*, 4th edition. Copyright © 1990 by John Wiley & Sons, Inc. Adapted by permission of John Wiley & Sons, Inc.)



WileyPLUS: VMSE Spinel/Inverse Spinel

of O<sup>2-</sup> ions. Again, there are two types of positions that may be occupied by the iron cations, as illustrated in Figure 12.7. For one, the coordination number is 4 (tetrahedral coordination)—that is, each Fe ion is surrounded by four oxygen nearest neighbors. For the other, the coordination number is 6 (octahedral coordination). With this inverse spinel structure, half the trivalent (Fe<sup>3+</sup>) ions are situated in octahedral positions and the other half in tetrahedral positions. The divalent Fe<sup>2+</sup> ions are all located in octahedral positions. The critical factor is the arrangement of the spin moments of the Fe ions, as represented in Figure 20.9 and Table 20.3. The spin moments of all the Fe<sup>3+</sup> ions in the octahedral positions are aligned parallel to one another; however, they are directed oppositely to the Fe<sup>3+</sup> ions disposed in the tetrahedral positions, which are also aligned. This results from the antiparallel coupling of adjacent iron ions. Thus, the spin moments of all Fe<sup>3+</sup> ions cancel one another and make no net contribution to the magnetization of the solid. All the Fe<sup>2+</sup> ions have their moments aligned in the same direction; this total moment is responsible for the net magnetization (see Table 20.3). Thus, the saturation magnetization of a ferrimagnetic solid may be computed from the product of the net spin magnetic moment for each Fe<sup>2+</sup> ion and the number of Fe<sup>2+</sup> ions; this corresponds to the mutual alignment of all the Fe<sup>2+</sup> ion magnetic moments in the Fe<sub>3</sub>O<sub>4</sub> specimen.

Cubic ferrites having other compositions may be produced by adding metallic ions that substitute for some of the iron in the crystal structure. Again, from the ferrite chemical formula  $M^{2+}O^{2-}-(Fe^{3+})_2(O^{2-})_3$ , in addition to  $Fe^{2+}$ ,  $M^{2+}$  may represent

Table 20.3

The Distribution of Spin Magnetic Moments for Fe<sup>2+</sup> and Fe<sup>3+</sup> lons in a Unit Cell of Fe<sub>3</sub>O<sub>4</sub><sup>a</sup>

| Cation           | Octahedral<br>Lattice Site | Tetrahedral<br>Lattice Site                | Net Magnetic<br>Moment                |
|------------------|----------------------------|--|---------------------------------------|
| Fe <sup>3+</sup> | ↑↑↑↑<br>↑↑↑↑               | $\downarrow\downarrow\downarrow\downarrow$ | Complete cancellation                 |
| Fe <sup>2+</sup> | ^ ^ ^ ^<br>^ ^ ^ ^         | _  | 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 |

<sup>&</sup>lt;sup>a</sup>Each arrow represents the magnetic moment orientation for one of the cations.

## **Table 20.4 Net Magnetic** Moments for Six **Cations**

| Cation           | Net Spin Magnetic Moment<br>(Bohr Magnetons) |  |  |
|------------------|--|--|--|
| Fe <sup>3+</sup> | 5  |  |  |
| Fe <sup>2+</sup> | 4  |  |  |
| Mn <sup>2+</sup> | 5  |  |  |
| Co <sup>2+</sup> | 3  |  |  |
| Ni <sup>2+</sup> | 2  |  |  |
| Cu <sup>2+</sup> | 1  |  |  |

divalent ions such as Ni<sup>2+</sup>, Mn<sup>2+</sup>, Co<sup>2+</sup>, and Cu<sup>2+</sup>, each of which possesses a net spin magnetic moment different from 4; several are listed in Table 20.4. Thus, by adjustment of composition, ferrite compounds having a range of magnetic properties may be produced. For example, nickel ferrite has the formula NiFe<sub>2</sub>O<sub>4</sub>. Other compounds may also be produced containing mixtures of two divalent metal ions such as (Mn, Mg)Fe<sub>2</sub>O<sub>4</sub>, in which the  $Mn^{2+}$ : $Mg^{2+}$  ratio may be varied; these are called *mixed ferrites*.

Ceramic materials other than the cubic ferrites are also ferrimagnetic and include the hexagonal ferrites and garnets. Hexagonal ferrites have a crystal structure similar to the inverse spinel crystal structure, with hexagonal symmetry rather than cubic. The chemical formula for these materials may be represented by AB<sub>12</sub>O<sub>19</sub>, in which A is a divalent metal such as barium, lead, or strontium, and B is a trivalent metal such as aluminum, gallium, chromium, or iron. The two most common examples of the hexagonal ferrites are PbFe<sub>12</sub>O<sub>19</sub> and BaFe<sub>12</sub>O<sub>19</sub>.

The garnets have a very complicated crystal structure, which may be represented by the general formula M<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>; here, M represents a rare earth ion such as samarium, europium, gadolinium, or yttrium. Yttrium iron garnet (Y<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>), sometimes denoted YIG, is the most common material of this type.

The saturation magnetizations for ferrimagnetic materials are not as high as for ferromagnets. However, ferrites, being ceramic materials, are good electrical insulators. For some magnetic applications, such as high-frequency transformers, a low electrical conductivity is most desirable.



**Concept Check 20.1** Cite the major similarities and differences between ferromagnetic and ferrimagnetic materials.

**Concept Check 20.2** What is the difference between the spinel and inverse spinel crystal structures? Hint: You may want to consult Section 12.2.

[The answers may be found at www.wiley.com/college/callister (Student Companion Site.)]

## **EXAMPLE PROBLEM 20.2**

## Saturation Magnetization Determination for Fe<sub>3</sub>O<sub>4</sub>

Calculate the saturation magnetization for Fe<sub>3</sub>O<sub>4</sub>, given that each cubic unit cell contains 8 Fe<sup>2+</sup> and 16 Fe<sup>3+</sup> ions and that the unit cell edge length is 0.839 nm.

#### Solution

This problem is solved in a manner similar to Example Problem 20.1, except that the computational basis is per unit cell as opposed to per atom or ion.

Saturation magnetization for a ferrimagnetic material (Fe<sub>3</sub>O<sub>4</sub>)

Computation of the number of Bohr magnetons per unit cell The saturation magnetization is equal to the product of the number N' of Bohr magnetons per cubic meter of Fe<sub>3</sub>O<sub>4</sub> and the magnetic moment per Bohr magneton  $\mu_B$ ,

$$M_s = N' \mu_{\rm B} \tag{20.11}$$

Now, N' is just the number of Bohr magnetons per unit cell  $n_B$  divided by the unit cell volume  $V_C$ , or

$$N' = \frac{n_{\rm B}}{V_C} \tag{20.12}$$

Again, the net magnetization results from the Fe<sup>2+</sup> ions only. Because there are 8 Fe<sup>2+</sup> ions per unit cell and 4 Bohr magnetons per Fe<sup>2+</sup> ion,  $n_{\rm B}$  is 32. Furthermore, the unit cell is a cube, and  $V_C = a^3$ , a being the unit cell edge length. Therefore.

$$M_s = \frac{n_{\rm B}\mu_{\rm B}}{a^3}$$

$$= \frac{(32 \text{ Bohr magnetons/unit cell})(9.27 \times 10^{-24} \text{ A·m²/Bohr magneton})}{(0.839 \times 10^{-9} \text{ m})^3/\text{unit cell}}$$

$$= 5.0 \times 10^5 \text{ A/m}$$
(20.13)



## **DESIGN EXAMPLE 20.1**

#### **Design of a Mixed Ferrite Magnetic Material**

Design a cubic mixed-ferrite magnetic material that has a saturation magnetization of  $5.25 \times 10^5 \, \text{A/m}$ .

#### Solution

According to Example Problem 20.2, the saturation magnetization for Fe<sub>3</sub>O<sub>4</sub> is  $5.0 \times 10^5$  A/m. In order to increase the magnitude of  $M_s$ , it is necessary to replace some fraction of the Fe<sup>2+</sup> with a divalent metal ion that has a greater magnetic moment—for example, Mn<sup>2+</sup>; from Table 20.4, note that there are 5 Bohr magnetons/Mn<sup>2+</sup> ion as compared to 4 Bohr magnetons/Fe<sup>2+</sup>. Let us first use Equation 20.13 to compute the number of Bohr magnetons per unit cell ( $n_B$ ), assuming that the Mn<sup>2+</sup> addition does not change the unit cell edge length (0.839 nm). Thus,

$$n_{\rm B} = \frac{M_{\rm s} a^3}{\mu_{\rm B}}$$
=\frac{(5.25 \times 10^5 \text{ A/m})(0.839 \times 10^{-9} \text{ m})^3/\text{unit cell}}{9.27 \times 10^{-24} \text{ A·m}^2/\text{Bohr magneton}}
= 33.45 \text{ Bohr magnetons/unit cell}

If we let x represent the fraction of  $Mn^{2+}$  that substitute for  $Fe^{2+}$ , then the remaining unsubstituted  $Fe^{2+}$  fraction is equal to (1 - x). Furthermore, inasmuch as there are 8 divalent ions per unit cell, we may write the following expression:

$$8[5x + 4(1 - x)] = 33.45$$

which leads to x = 0.181. Thus, if 18.1 at% of the Fe<sup>2+</sup> in Fe<sub>3</sub>O<sub>4</sub> are replaced with Mn<sup>2+</sup>, the saturation magnetization will be increased to  $5.25 \times 10^5$  A/m.

# 20.6 THE INFLUENCE OF TEMPERATURE ON MAGNETIC BEHAVIOR

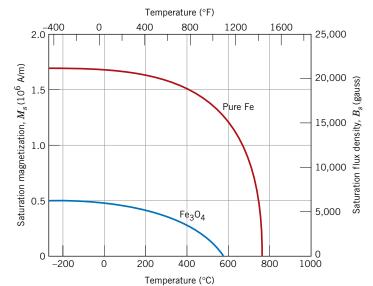
Temperature can also influence the magnetic characteristics of materials. Recall that raising the temperature of a solid increases the magnitude of the thermal vibrations of atoms. The atomic magnetic moments are free to rotate; hence, with rising temperature, the increased thermal motion of the atoms tends to randomize the directions of any moments that may be aligned.

For ferromagnetic, antiferromagnetic, and ferrimagnetic materials, the atomic thermal motions counteract the coupling forces between the adjacent atomic dipole moments, causing some dipole misalignment, regardless of whether an external field is present. This results in a decrease in the saturation magnetization for both ferro- and ferrimagnets. The saturation magnetization is a maximum at 0 K, at which temperature the thermal vibrations are at a minimum. With increasing temperature, the saturation magnetization decreases gradually and then abruptly drops to zero at what is called the **Curie temperature**  $T_c$ . The magnetization–temperature behavior for iron and Fe<sub>3</sub>O<sub>4</sub> is represented in Figure 20.10. At  $T_c$ , the mutual spin-coupling forces are completely destroyed, such that for temperatures above  $T_c$ , both ferro- and ferrimagnetic materials are paramagnetic. The magnitude of the Curie temperature varies from material to material; for example, for iron, cobalt, nickel, and Fe<sub>3</sub>O<sub>4</sub>, the respective values are 768°C, 1120°C, 335°C, and 585°C.

Antiferromagnetism is also affected by temperature; this behavior vanishes at what is called the *Néel temperature*. At temperatures above this point, antiferromagnetic materials also become paramagnetic.

**Concept Check 20.3** Explain why repeatedly dropping a permanent magnet on the floor causes it to become demagnetized.

[The answer may be found at www.wiley.com/college/callister (Student Companion Site.)]



**Figure 20.10** Plot of saturation magnetization as a function of temperature for iron and  $Fe_3O_4$ .

(Adapted from J. Smit and H. P. J. Wijn, Ferrites. Copyright © 1959 by N. V. Philips Gloeilampenfabrieken, Eindhoven (Holland). Reprinted by permission.)

#### **Curie temperature**

#### 20.7 DOMAINS AND HYSTERESIS

Any ferro- or ferrimagnetic material at a temperature below  $T_c$  is composed of small-volume regions in which there is a mutual alignment in the same direction of all magnetic dipole moments, as illustrated in Figure 20.11. Such a region is called a *domain*, and each one is magnetized to its saturation magnetization. Adjacent domains are separated by domain boundaries or walls across which the direction of magnetization gradually changes (Figure 20.12). Normally, domains are microscopic in size, and for a polycrystalline specimen, each grain may consist of more than a single domain. Thus, in a macroscopic piece of material, there are a large number of domains, and all may have different magnetization orientations. The magnitude of the M field for the entire solid is the vector sum of the magnetizations of all the domains, each domain contribution being weighted by its volume fraction. For an unmagnetized specimen, the appropriately weighted vector sum of the magnetizations of all the domains is zero.

Flux density B and field intensity H are not proportional for ferro- and ferrimagnets. If the material is initially unmagnetized, then B varies as a function of H, as shown in Figure 20.13. The curve begins at the origin, and as H is increased, the B field begins to increase slowly, then more rapidly, finally leveling off and becoming independent of H. This maximum value of B is the saturation flux density  $B_s$ , and the corresponding magnetization is the saturation magnetization  $M_s$  mentioned previously. Because the permeability  $\mu$  from Equation 20.2 is the slope of the B-versus-H curve, note from Figure 20.13 that the permeability is dependent on H. On occasion, the slope of the

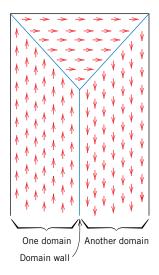
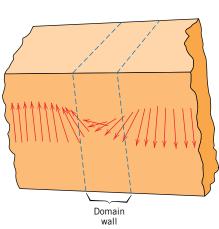


Figure 20.11 Schematic depiction of domains in a ferromagnetic or ferrimagnetic material; arrows represent atomic magnetic dipoles. Within each domain, all dipoles are aligned, whereas the direction of alignment varies from one domain to another.



**Figure 20.12** The gradual change in magnetic dipole orientation across a domain wall. (From W. D. Kingery, H. K. Bowen, and D. R.

(From W. D. Kingery, H. K. Bowen, and D. R Uhlmann, *Introduction to Ceramics*, 2nd edition. Copyright © 1976 by John Wiley & Sons, New York. Reprinted by permission of John Wiley & Sons, Inc.)

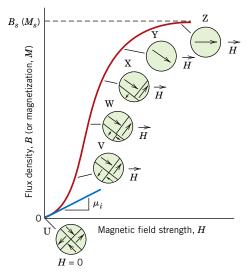
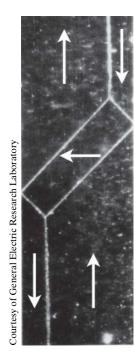


Figure 20.13 The *B*-versus-*H* behavior for a ferro- or ferrimagnetic material that was initially unmagnetized. Domain configurations during several stages of magnetization are represented. Saturation flux density  $B_s$ , magnetization  $M_s$ , and initial permeability  $\mu_i$  are also indicated. (Adapted from O. H. Wyatt and D. Dew-Hughes, *Metals, Ceramics and Polymers*, Cambridge University Press, Cambridge, 1974. Reprinted with the permission of the Cambridge University Press.)



Photomicrograph showing the domain structure of an iron single crystal (arrows indicate directions of magnetization).

hysteresis remanence coercivity

B-versus-H curve at H=0 is specified as a material property, which is termed the *initial* permeability  $\mu_i$ , as indicated in Figure 20.13.

As an H field is applied, the domains change shape and size by the movement of domain boundaries. Schematic domain structures are represented in the insets (labeled U through Z) at several points along the B-versus-H curve in Figure 20.13. Initially, the moments of the constituent domains are randomly oriented such that there is no net B (or M) field (inset U). As the external field is applied, the domains that are oriented in directions favorable to (or nearly aligned with) the applied field grow at the expense of those that are unfavorably oriented (insets V through X). This process continues with increasing field strength until the macroscopic specimen becomes a single domain, which is nearly aligned with the field (inset Y). Saturation is achieved when this domain, by means of rotation, becomes oriented with the H field (inset Z).

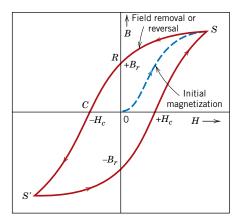
From saturation—point S in Figure 20.14—as the H field is reduced by reversal of field direction, the curve does not retrace its original path. A hysteresis effect is produced in which the B field lags behind the applied H field, or decreases at a lower rate. At zero H field (point R on the curve), there exists a residual B field called the remanence, or remanent flux density,  $B_r$ , the material remains magnetized in the absence of an external H field.

Hysteresis behavior and permanent magnetization may be explained by the motion of domain walls. Upon reversal of the field direction from saturation (point S in Figure 20.14), the process by which the domain structure changes is reversed. First, there is a rotation of the single domain with the reversed field. Next, domains having magnetic moments aligned with the new field form and grow at the expense of the former domains. Critical to this explanation is the resistance to movement of domain walls that occurs in response to the increase of the magnetic field in the opposite direction; this accounts for the lag of B with H, or the hysteresis. When the applied field reaches zero, there is still some net volume fraction of domains oriented in the former direction, which explains the existence of the remanence  $B_r$ .

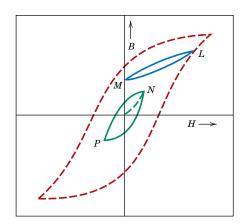
To reduce the B field within the specimen to zero (point C on Figure 20.14), an H field of magnitude  $-H_c$  must be applied in a direction opposite to that of the original field;  $H_c$  is called the **coercivity**, or sometimes the *coercive force*. Upon continuation of the applied field in this reverse direction, as indicated in the figure, saturation is ultimately achieved in the opposite sense, corresponding to point S'. A second reversal of the field to the point of the initial saturation (point S) completes the symmetrical hysteresis loop and also yields both a negative remanence  $(-B_r)$  and a positive coercivity  $(+H_c)$ .

The B-versus-H curve in Figure 20.14 represents a hysteresis loop taken to saturation. It is not necessary to increase the H field to saturation before reversing the field direction; in Figure 20.15, loop NP is a hysteresis curve corresponding to less than saturation. Furthermore, it is possible to reverse the direction of the field at any point along the curve and generate other hysteresis loops. One such loop is indicated on the saturation curve in Figure 20.15: for loop LM, the H field is reversed to zero. One method of demagnetizing a ferro- or ferrimagnet is to repeatedly cycle it in an H field that alternates direction and decreases in magnitude.

At this point, it is instructive to compare the B-versus-H behaviors of paramagnetic, diamagnetic, and ferromagnetic/ferrimagnetic materials; such a comparison is shown in Figure 20.16. The linearity of paramagnetic and diamagnetic materials may be noted in the small inset plot, whereas the behavior of a typical ferromagnetic/ferrimagnetic is nonlinear. Furthermore, the rationale for labeling paramagnetics and diamagnetics as nonmagnetic materials is verified by comparing the B scales on the vertical axes of the two plots—at an H field strength of 50 A/m, the ferromagnetic/ferrimagnetic materials flux density is on the order of 1.5 tesla, whereas for the paramagnetic and diamagnetic materials it is on the order of  $5 \times 10^{-5}$  tesla.



**Figure 20.14** Magnetic flux density versus the magnetic field strength for a ferromagnetic material that is subjected to forward and reverse saturations (points S and S'). The hysteresis loop is represented by the solid curve; the dashed curve indicates the initial magnetization. The remanence  $B_r$  and the coercive force  $H_c$  are also shown.



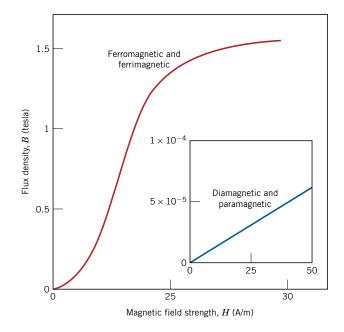
**Figure 20.15** A hysteresis curve at less than saturation (curve NP) within the saturation loop for a ferromagnetic material. The B-H behavior for field reversal at other than saturation is indicated by curve LM.

**Concept Check 20.4** Schematically sketch on a single plot the *B*-versus-*H* behavior for a ferromagnetic material (a) at 0 K, (b) at a temperature just below its Curie temperature, and (c) at a temperature just above its Curie temperature. Briefly explain why these curves have different shapes.

**Concept Check 20.5** Schematically sketch the hysteresis behavior for a ferromagnet that is gradually demagnetized by cycling in an H field that alternates direction and decreases in magnitude.

[The answers may be found at www.wiley.com/college/callister (Student Companion Site.)]

**Figure 20.16** Comparison of *B*-versus-*H* behaviors for ferromagnetic/ferrimagnetic and diamagnetic/paramagnetic materials (inset plot). Note that extremely small *B* fields are generated in materials that experience only diamagnetic/paramagnetic behavior, which is why they are considered nonmagnetics.



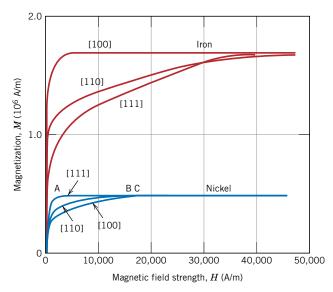
#### 20.8 MAGNETIC ANISOTROPY

The magnetic hysteresis curves discussed in Section 20.7 have different shapes depending on various factors: (1) whether the specimen is a single crystal or polycrystalline; (2) if it is polycrystalline, whether there is any preferred orientation of the grains; (3) the presence of pores or second-phase particles; and (4) other factors such as temperature and, if a mechanical stress is applied, the stress state.

For example, the B (or M) versus H curve for a single crystal of a ferromagnetic material depends on its crystallographic orientation relative to the direction of the applied H field. This behavior is demonstrated in Figure 20.17 for single crystals of nickel (FCC) and iron (BCC), where the magnetizing field is applied in [100], [110], and [111] crystallographic directions, and in Figure 20.18 for cobalt (HCP) in [0001] and  $[10\overline{10}]/[11\overline{20}]$  directions. This dependence of magnetic behavior on crystallographic orientation is termed *magnetic* (or sometimes *magnetocrystalline*) *anisotropy*.

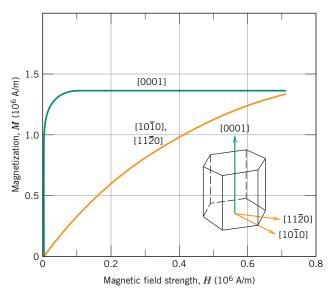
For each of these materials, there is one crystallographic direction in which magnetization is easiest—that is, saturation (of M) is achieved at the lowest H field; this is termed a direction of *easy magnetization*. For example, for Ni (Figure 20.17), this direction is [111] inasmuch as saturation occurs at point A; for [110] and [100] orientations, saturation points correspond, respectively, to points B and C. Correspondingly, easy magnetization directions for Fe and Co are [100] and [0001], respectively (Figures 20.17 and 20.18). Conversely, a *hard* crystallographic direction is that direction for which saturation magnetization is most difficult; hard directions for Ni, Fe, and Co are [100], [111], and  $[10\overline{10}]/[11\overline{20}]$ .

As noted in Section 20.7, the insets of Figure 20.13 represent domain configurations at various stages along the B (or M) versus H curve during the magnetization of a ferromagnetic/ferrimagnetic material. Here, each of the arrows represents a domain's direction of easy magnetization; domains whose directions of easy magnetization are most closely aligned with the H field grow at the expense of the other domains, which shrink (insets V through X). Furthermore, the magnetization of the single domain in inset Y also corresponds to an easy direction. Saturation is achieved as the direction of this domain rotates away from the easy direction into the direction of the applied field (inset Z).



**Figure 20.17** Magnetization curves for single crystals of iron and nickel. For both metals, a different curve was generated when the magnetic field was applied in each of [100], [110], and [111] crystallographic directions.

(Adapted from K. Honda and S. Kaya, "On the Magnetisation of Single Crystals of Iron," *Sci. Rep. Tohoku Univ.*, **15**, 721 (1926); and from S. Kaya, "On the Magnetisation of Single Crystals of Nickel," *Sci. Rep. Tohoku Univ.*, **17**, 639 (1928).)



**Figure 20.18** Magnetization curves for single crystals of cobalt. The curves were generated when the magnetic field was applied in [0001] and  $[10\overline{1}0]/[11\overline{2}0]$  crystallographic directions.

(Adapted from S. Kaya, "On the Magnetisation of Single Crystals of Cobalt," Sci. Rep. Tohoku Univ., 17, 1157 (1928).)

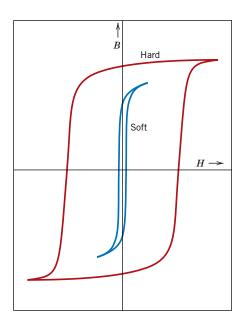


Figure 20.19 Schematic magnetization curves for soft and hard magnetic materials. (From K. M. Ralls, T. H. Courtney, and J. Wulff, *Introduction to Materials Science and Engineering*. Copyright © 1976 by John Wiley & Sons, New York. Reprinted by permission of John Wiley & Sons, Inc.)

## **20.9 SOFT MAGNETIC MATERIALS**

The size and shape of the hysteresis curve for ferro- and ferrimagnetic materials are of considerable practical importance. The area within a loop represents a magnetic energy loss per unit volume of material per magnetization—demagnetization cycle; this energy loss is manifested as heat that is generated within the magnetic specimen and is capable of raising its temperature.

Both ferro- and ferrimagnetic materials are classified as either *soft* or *hard* on the basis of their hysteresis characteristics. **Soft magnetic materials** are used in devices that are subjected to alternating magnetic fields and in which energy losses must be low; one familiar example consists of transformer cores. For this reason, the relative area within the hysteresis loop must be small; it is characteristically thin and narrow, as represented in Figure 20.19. Consequently, a soft magnetic material must have a high initial permeability and a low coercivity. A material possessing these properties may reach its saturation magnetization with a relatively low applied field (i.e., may be easily magnetized and demagnetized) and still have low hysteresis energy losses.

The saturation field or magnetization is determined only by the composition of the material. For example, in cubic ferrites, substitution of a divalent metal ion such as  $\mathrm{Ni^{2+}}$  for  $\mathrm{Fe^{2+}}$  in  $\mathrm{FeO-Fe_2O_3}$  changes the saturation magnetization. However, susceptibility and coercivity ( $H_c$ ), which also influence the shape of the hysteresis curve, are sensitive to structural variables rather than to composition. For example, a low value of coercivity corresponds to the easy movement of domain walls as the magnetic field changes magnitude and/or direction. Structural defects such as particles of a nonmagnetic phase or voids in the magnetic material tend to restrict the motion of domain walls and thus increase the coercivity. Consequently, a soft magnetic material must be free of such structural defects.

soft magnetic material

#### MATERIALS I M

## An Iron-Silicon Alloy Used in Transformer Cores

s mentioned earlier in this section, transformer cores require the use of soft magnetic materials, which are easily magnetized and demagnetized (and also have relatively high electrical resistivities). One alloy commonly used for this application is the iron-silicon alloy listed in Table 20.5 (97 wt% Fe-3 wt% Si). Single crystals of this alloy are magnetically anisotropic, as are also single crystals of iron (as explained previously). Consequently, energy losses of transformers could be minimized if their cores were fabricated from single crystals such that a [100]-type direction [the direction of easy magnetization (Figure 20.17)] is oriented parallel to the direction of an applied magnetic field; this configuration for a transformer core is represented schematically in Figure 20.20. Unfortunately, single crystals are expensive to prepare, and, thus, this is an economically unpractical situation. A better, more economically attractive alternative—one used commercially—is to fabricate cores from polycrystalline sheets of this alloy that are anisotropic.

Often, the grains in polycrystalline materials are oriented randomly, with the result that their properties are isotropic (Section 3.15). However, one way of developing anisotropy in polycrystalline metals is

via plastic deformation, for example by rolling (Section 11.4, Figure 11.9b); rolling is the technique by which sheet transformer cores are fabricated. A flat sheet that has been rolled is said to have a rolling (or sheet) texture, or there is a preferred crystallographic orientation of the grains. For this type of texture, during the rolling operation, for most of the grains in the sheet, a specific crystallographic plane (hkl) becomes aligned parallel (or nearly parallel) to the surface of the sheet, and, in addition a direction [uvw] in that plane lies parallel (or nearly parallel) to the rolling direction. Thus, a rolling texture is indicated by the plane-direction combination, (hkl)[uvw]. For bodycentered cubic alloys (to include the iron-silicon alloy mentioned earlier), the rolling texture is (110)[001], which is represented schematically in Figure 20.21. Thus, transformer cores of this iron-silicon alloy are fabricated so that the direction in which the sheet was rolled (corresponding to a [001]-type direction for most of the grains) is aligned parallel to the direction of the magnetic field application.<sup>3</sup>

The magnetic characteristics of this alloy may be further improved through a series of deformation and heat-treating procedures that produce a (100)[001] texture.

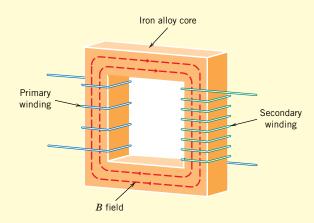


Figure 20.20 Schematic diagram of a transformer core, including the direction of the B field that is generated.

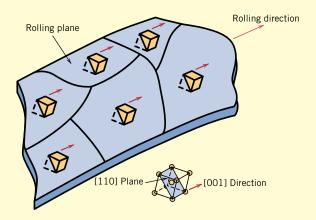


Figure 20.21 Schematic representation of the (110)[001] rolling texture for body-centered cubic iron.

For body-centered cubic metals and alloys, [100] and [001] directions are equivalent (Section 3.9)—that is, both are directions of easy magnetization.

**Table 20.5** Typical Properties for Several Soft Magnetic Materials

| Material                   | Composition (wt%)   | Initial<br>Relative<br>Permeability μ <sub>i</sub> | Saturation Flux  Density B <sub>s</sub> [tesla (gauss)] | Hysteresis<br>Loss/Cycle<br>[J/m³ (erg/cm³)] | Resistivity<br>ρ (Ω·m) |
|----------------------------|---|--|---|--|------------------------|
| Commercial iron ingot      | 99.95 Fe  | 150  | 2.14 (21,400)   | 270 (2,700)                                  | $1.0 \times 10^{-7}$   |
| Silicon-iron<br>(oriented) | 97 Fe, 3 Si   | 1,400  | 2.01 (20,100)   | 40 (400)                                     | $4.7 \times 10^{-7}$   |
| 45 Permalloy               | 55 Fe, 45 Ni  | 2,500  | 1.60 (16,000)   | 120 (1,200)                                  | $4.5 \times 10^{-7}$   |
| Supermalloy                | 79 Ni, 15 Fe, 5 Mo, 0.5 Mn  | 75,000   | 0.80 (8,000)  | _  | $6.0 \times 10^{-7}$   |
| Ferroxcube A               | 48 MnFe <sub>2</sub> O <sub>4</sub> , 52 ZnFe <sub>2</sub> O <sub>4</sub> | 1,400  | 0.33 (3,300)  | ~40 (~400)                                   | 2,000                  |
| Ferroxcube B               | 36 NiFe <sub>2</sub> O <sub>4</sub> , 64 ZnFe <sub>2</sub> O <sub>4</sub> | 650  | 0.36 (3,600)  | ~35 (~350)                                   | $10^{7}$               |

Source: Adapted from *Metals Handbook: Properties and Selection: Stainless Steels, Tool Materials and Special-Purpose Metals,* Vol. 3, 9th edition, D. Benjamin (Senior Editor), 1980. Reproduced by permission of ASM International, Materials Park, OH.

Another property consideration for soft magnetic materials is the electrical resistivity. In addition to the hysteresis energy losses described previously, energy losses may result from electrical currents that are induced in a magnetic material by a magnetic field that varies in magnitude and direction with time; these are called *eddy currents*. It is most desirable to minimize these energy losses in soft magnetic materials by increasing the electrical resistivity. This is accomplished in ferromagnetic materials by forming solid solution alloys; iron–silicon and iron–nickel alloys are examples. The ceramic ferrites are commonly used for applications requiring soft magnetic materials because they are intrinsically electrical insulators. Their applicability is somewhat limited, however, inasmuch as they have relatively small susceptibilities. The properties of some soft magnetic materials are shown in Table 20.5.

The hysteresis characteristics of soft magnetic materials may be enhanced for some applications by an appropriate heat treatment in the presence of a magnetic field. Using such a technique, a square hysteresis loop may be produced, which is desirable in some magnetic amplifier and pulse transformer applications. In addition, soft magnetic materials are used in generators, motors, dynamos, and switching circuits.

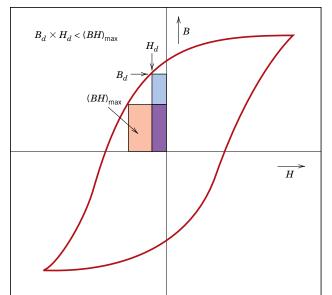
#### 20.10 HARD MAGNETIC MATERIALS

hard magnetic material Hard magnetic materials are used in permanent magnets, which must have a high resistance to demagnetization. In terms of hysteresis behavior, a **hard magnetic material** has high remanence, coercivity, and saturation flux density, as well as low initial permeability and high hysteresis energy losses. The hysteresis characteristics for hard and soft magnetic materials are compared in Figure 20.19. The two most important characteristics relative to applications for these materials are the coercivity and what is termed the *energy product*, designated as  $(BH)_{\rm max}$ . This  $(BH)_{\rm max}$  corresponds to the area of the largest B-H rectangle that can be constructed within the second quadrant of the hysteresis curve, Figure 20.22; its units are kJ/m³ (MGOe). The value of the energy product is

 $1 \text{ MGOe} = 10^6 \text{ gauss-oersted}$ 

Conversion from cgs-emu to SI units is accomplished by the relationship

<sup>&</sup>lt;sup>4</sup>MGOe is defined as



**Figure 20.22** Schematic magnetization curve that displays hysteresis. Within the second quadrant are drawn two B-H energy product rectangles; the area of the rectangle labeled  $(BH)_{max}$  is the largest possible, which is greater than the area defined by  $B_d$ – $H_d$ .

representative of the energy required to demagnetize a permanent magnet—that is, the larger  $(BH)_{\rm max}$ , the harder the material in terms of its magnetic characteristics.

Hysteresis behavior is related to the ease with which the magnetic domain boundaries move; by impeding domain wall motion, the coercivity and susceptibility are enhanced, such that a large external field is required for demagnetization. Furthermore, these characteristics are related to the microstructure of the material.

**Concept Check 20.6** It is possible, by various means (e.g., alteration of microstructure and impurity additions), to control the ease with which domain walls move as the magnetic field is changed for ferromagnetic and ferrimagnetic materials. Sketch a schematic B-versus-H hysteresis loop for a ferromagnetic material, and superimpose on this plot the loop alterations that would occur if domain boundary movement were hindered.

[The answer may be found at www.wiley.com/college/callister (Student Companion Site.)]

## Conventional Hard Magnetic Materials

Hard magnetic materials fall within two main categories-conventional and high energy. The conventional materials have  $(BH)_{max}$  values that range between about 2 and 80 kJ/m<sup>3</sup> (0.25 and 10 MGOe). These include ferromagnetic materials—magnet steels, cunife (Cu-Ni-Fe) alloys, and alnico (Al-Ni-Co) alloys—as well as the hexagonal ferrites (BaO-6Fe<sub>2</sub>O<sub>3</sub>). Table 20.6 presents some critical properties of several of these hard magnetic materials.

The hard magnetic steels are normally alloyed with tungsten and/or chromium. Under the proper heat-treating conditions, these two elements readily combine with carbon in the steel to form tungsten and chromium carbide precipitate particles, which are especially effective in obstructing domain wall motion. For the other metal alloys, an appropriate heat treatment forms extremely small single-domain and strongly magnetic iron-cobalt particles within a nonmagnetic matrix phase.

 Table 20.6
 Typical Properties for Several Hard Magnetic Materials

| Material                             | Composition<br>(wt%)                        | Remanence<br>B, [tesla<br>(gauss)] | Coercivity  H <sub>c</sub> [amp- turn/m (Oe)] | (BH) <sub>max</sub><br>[kJ/m <sup>3</sup><br>(MGOe)] | Curie<br>Temperature<br>T <sub>c</sub><br>[°C (°F)] | Resistivity<br>ρ (Ω·m) |
|--------------------------------------|---|------------------------------------|---|--|---|------------------------|
| Tungsten steel                       | 92.8 Fe, 6 W,<br>0.5 Cr, 0.7 C              | 0.95<br>(9,500)                    | 5,900<br>(74)                                 | 2.6<br>(0.33)  | 760<br>(1,400)                                      | $3.0 \times 10^{-7}$   |
| Cunife                               | 20 Fe, 20 Ni,<br>60 Cu                      | 0.54<br>(5,400)                    | 44,000<br>(550)                               | 12<br>(1.5)  | 410<br>(770)  | $1.8 \times 10^{-7}$   |
| Sintered<br>alnico 8                 | 34 Fe, 7 Al,<br>15 Ni, 35 Co,<br>4 Cu, 5 Ti | 0.76<br>(7,600)                    | 125,000<br>(1,550)                            | 36<br>(4.5)  | 860<br>(1,580)                                      | _                      |
| Sintered ferrite 3                   | BaO-6Fe <sub>2</sub> O <sub>3</sub>         | 0.32<br>(3,200)                    | 240,000<br>(3,000)                            | 20<br>(2.5)  | 450<br>(840)  | ~104                   |
| Cobalt rare earth 1                  | SmCo <sub>5</sub>                           | 0.92<br>(9,200)                    | 720,000<br>(9,000)                            | 170<br>(21)  | 725<br>(1,340)                                      | $5.0 \times 10^{-7}$   |
| Sintered<br>neodymium-<br>iron-boron | $Nd_2Fe_{14}B$                              | 1.16<br>(11,600)                   | 848,000<br>(10,600)                           | 255<br>(32)  | 310<br>(590)  | $1.6 \times 10^{-6}$   |

**Source:** Adapted from ASM Handbook, Vol. 2, Properties and Selection: Nonferrous Alloys and Special-Purpose Materials. Copyright © 1990 by ASM International. Reprinted by permission of ASM International, Materials Park, OH.

## **High-Energy Hard Magnetic Materials**

Permanent magnetic materials having energy products in excess of about  $80 \text{ kJ/m}^3$  (10 MGOe) are considered to be of the high-energy type. These are recently developed intermetallic compounds that have a variety of compositions; the two that have found commercial exploitation are SmCo<sub>5</sub> and Nd<sub>2</sub>Fe<sub>14</sub>B. Their magnetic properties are also listed in Table 20.6.

## Samarium-Cobalt Magnets

Samarium–cobalt,  $SmCo_5$ , is a member of a group of alloys that are combinations of cobalt or iron and a light rare earth element; a number of these alloys exhibit high-energy, hard magnetic behavior, but  $SmCo_5$  is the only one of commercial significance. The energy product of these  $SmCo_5$  materials [between 120 and 240 kJ/m³ (15 and 30 MGOe)] are considerably higher than those of the conventional hard magnetic materials (Table 20.6); in addition, they have relatively large coercivities. Powder metallurgical techniques are used to fabricate  $SmCo_5$  magnets. The appropriately alloyed material is first ground into a fine powder; the powder particles are aligned using an external magnetic field and then pressed into the desired shape. The piece is then sintered at an elevated temperature, followed by another heat treatment that improves the magnetic properties.

## Neodymium-Iron-Boron Magnets

Samarium is a rare and relatively expensive material; furthermore, the price of cobalt is variable, and its sources are unreliable. Consequently, the neodymium–iron–boron, Nd<sub>2</sub>Fe<sub>14</sub>B, alloys have become the materials of choice for a large number and wide diversity of applications requiring hard magnetic materials. Coercivities and energy products of these materials rival those of the samarium–cobalt alloys (Table 20.6).

The magnetization-demagnetization behavior of these materials is a function of domain wall mobility, which is controlled by the final microstructure—that is, the size, shape, and orientation of the crystallites or grains, as well as the nature and distribution of any

second-phase particles that are present. Microstructure depends on how the material is processed. Two different processing techniques are available for the fabrication of Nd<sub>2</sub>Fe<sub>14</sub>B magnets: powder metallurgy (sintering) and rapid solidification (melt spinning). The powder metallurgical approach is similar to that used for the SmCo<sub>5</sub> materials. For rapid solidification, the alloy in molten form is quenched very rapidly such that either an amorphous or very fine-grained and thin solid ribbon is produced. This ribbon material is then pulverized, compacted into the desired shape, and subsequently heat-treated. Rapid solidification is the more involved of the two fabrication processes; nevertheless, it is continuous, whereas powder metallurgy is a batch process, which has its inherent disadvantages.

These high-energy hard magnetic materials are used in a host of different devices in a variety of technological fields. One common application is in motors. Permanent magnets are far superior to electromagnets in that their magnetic fields are maintained continuously and without the necessity to expend electrical power; furthermore, no heat is generated during operation. Motors using permanent magnets are much smaller than their electromagnetic counterparts and are used extensively in fractional horsepower units. Familiar motor applications include cordless drills and screwdrivers; in automobiles (starters; window winders, wipers, and washers; fan motors); in audio and video recorders; clocks; speakers in audio systems, lightweight earphones, and hearing aids; and computer peripherals.

#### 20.11 MAGNETIC STORAGE

Magnetic materials are important in the area of information storage; in fact, magnetic recording<sup>5</sup> has become virtually the universal technology for the storage of electronic information. This is evidenced by the preponderance of disk storage media [e.g., computers (both desktop and laptop), and high-definition camcorder hard drives], credit/ debit cards (magnetic stripes), and so on. Whereas in computers, semiconductor elements serve as primary memory, magnetic hard disks are normally used for secondary memory because they are capable of storing larger quantities of information and at a lower cost; however, their transfer rates are slower. Furthermore, the recording and television industries rely heavily on magnetic tapes for the storage and reproduction of audio and video sequences. In addition, tapes are used with large computer systems to back up and archive data.

In essence, computer bytes, sound, or visual images in the form of electrical signals are recorded magnetically on very small segments of the magnetic storage medium - a tape or disk. Transference to (i.e., "writing") and retrieval from (i.e., "reading") the tape or disk is accomplished by means of a recording system that consists of read and write heads. For hard drives, this head system is supported above and in close proximity to the magnetic medium by a self-generating air bearing as the medium passes beneath at relatively high rotational speeds. In contrast, tapes make physical contact with the heads during read and write operations. Tape velocities run as high as 10 m/s.

As noted previously, there are two principal types of magnetic media— $hard\ disk$ drives (HDDs) and magnetic tapes—both of which we now briefly discuss.

#### **Hard Disk Drives**

Hard disk magnetic storage hard drives consist of rigid circular disks with diameters that range between about 65 mm (2.5 in.) and 95 mm (3.75 in). During read and

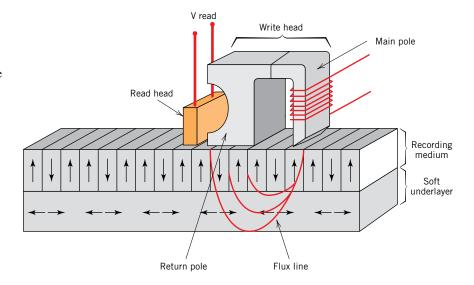
<sup>&</sup>lt;sup>5</sup>The term *magnetic recording* is often used to denote the recording and storage of audio or video and audio signals, whereas in the field of computing, magnetic storage is frequently preferred.

<sup>&</sup>lt;sup>6</sup>It is sometimes stated that the head "flies" over the disk.

Figure 20.23 Schematic diagram of a hard disk drive that uses the perpendicular magnetic recording medium; also shown are inductive write and magnetoresistive read heads.

(Courtesy of HGST, a Western

Digital Company.)



write processes, disks rotate at relatively high velocities—5400 and 7200 revolutions per minute are common. Rapid rates of data storage and retrieval are possible using HDDs, as are high storage densities.

For the current HDD technology, "magnetic bits" point up or down perpendicular to the plane of the disk surface; this scheme is appropriately called *perpendicular magnetic recording (PMR)*, and is represented schematically in Figure 20.23.

Data (or bits) are introduced (written) into the storage medium using an inductive write head. For one head design, shown in Figure 20.23, a time-varying write magnetic flux is generated at the tip of the main pole—a ferromagnetic/ferrimagnetic core material around which a wire coil is wound—by an electric current (also time variable) that passes through the coil. This flux penetrates through the magnetic storage layer into a magnetically soft underlayer and then reenters the head assembly through a return pole (Figure 20.23). A very intense magnetic field is concentrated in the storage layer beneath the tip of the main pole. At this point, data are written as a very small region of the storage layer becomes magnetized. Upon removal of the field (i.e., as the disk continues its rotation), the magnetization remains—that is, the signal (i.e., data) has been stored. Digital data storage (i.e., as 1s and 0s) is in the form of minute magnetization patterns; the 1s and 0s correspond to the presence or absence of magnetic reversal directions between adjacent regions.

Data retrieval from the storage medium is accomplished using a magnetoresistive read head (Figure 20.23). During read-back, magnetic fields from the written magnetic patterns are sensed by this head; these fields produce changes in electrical resistance. The resulting signals are then processed so as to reproduce the original data.

The storage layer is composed of granular media—a thin film (15 to 20 nm thick) consisting of very small (~10-nm diameter) and isolated grains of an HCP cobalt—chromium alloy that are magnetically anisotropic. Other alloying elements (notably Pt and Ta) are added to enhance the magnetic anisotropy as well as to form oxide grain-boundary segregants that isolate the grains. Figure 20.24 is a transmission electron micrograph that shows the grain structure of an HDD storage layer. Each grain is a single domain that is oriented with its c-axis (i.e., [0001] crystallographic direction) perpendicular (or nearly perpendicular) to the disk surface. This [0001] direction is the direction of easy magnetization for Co (Figure 20.18); thus, when magnetized, the direction of magnetization of each grain has this desired perpendicular orientation. Reliable storage of data requires that each bit written on the disk

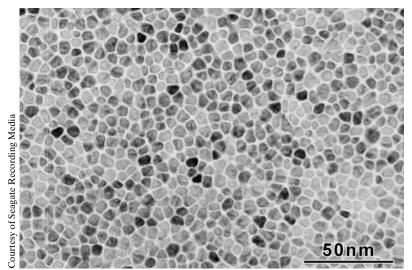


Figure 20.24 Transmission electron micrograph showing the microstructure of the perpendicular magnetic recording medium used in hard disk drives. This "granular medium" consists of small grains of a cobalt—chromium alloy (darker regions) that are isolated from one another by an oxide grain-boundary segregant (lighter regions).

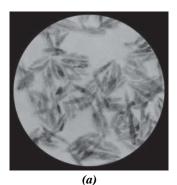
encompasses approximately 100 grains. Furthermore, there is a lower limit to the grain size; for grain sizes below this limit, there is the possibility that the direction of magnetization will spontaneously reverse because of the effects of thermal agitation (Section 20.6), which causes a loss of stored data.

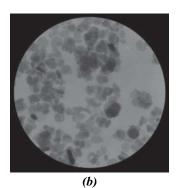
The current storage capacities of perpendicular HDDs are in excess of 100 Gbit/in.<sup>2</sup> (10<sup>11</sup> bit/in.<sup>2</sup>); the ultimate goal for HDDs is a storage capacity of 1 Tbit/in.<sup>2</sup> (10<sup>12</sup> bit/in.<sup>2</sup>).

## **Magnetic Tapes**

The development of magnetic tape storage preceded that for the hard disk drives. Today, tape storage is less expensive than HDD; however, areal storage densities are lower for tape (by a factor of on the order of 100). Tapes [of standard 0.5-in. (12.7-mm) width] are wound onto reels and enclosed within cartridges for protection and to facilitate handling. During operation, a tape drive, using precision-synchronized motors, winds the tape from one reel onto another past a read/write head system in order to access a point of interest. Typical tape speeds are 4.8 m/s; some systems run as high as 10 m/s. Head systems for tape storage are similar to those employed for HDDs, as described previously.

For the latest tape-memory technology, storage media are particulates of magnetic materials that have dimensions on the order of tens of nanometers: ferromagnetic metal particles that are *acicular* (needle-shaped), and hexagonal and *tabular* (plate-shaped) ferrimagnetic barium–ferrite particles. Photomicrographs of both media types are shown in Figure 20.25. Tape products use one particle type or the other (not both





**Figure 20.25** Scanning electron micrographs showing particulate media used in tape-memory storage. (a) Needle-shaped ferromagnetic metal particles. (b) Plate-shaped ferrimagnetic barium-ferrite particles. Magnifications unknown.

(Photographs courtesy of Fujifilm, Inc., Recording Media Division.)

together), depending on application. These magnetic particles are thoroughly and uniformly dispersed in a proprietary high-molecular-weight organic binder material to form a magnetic layer approximately 50 nm thick. Beneath this layer is nonmagnetic thin-film support substrate between about 100 and 300 nm thick that is attached to the tape. Either poly(ethylene naphthalate) (PEN) or poly(ethylene terephthalate) (PET) is used for the tape.

Both particle types are magnetically *anisotropic*—that is, they have an "easy" or preferential direction along which they may be magnetized; for example, for the metal particles, this direction is parallel to their long axes. During manufacture, these particles are aligned such that this direction parallels the direction of motion of the tape past the write head. Inasmuch as each particle is a single domain that may be magnetized only in one direction or its opposite by the write head, two magnetic states are possible. These two states allow for the storage of information in digital form, as 1s and 0s.

Using the plate-shaped barium–ferrite medium, a tape-storage density of 6.7 Gbit/in.<sup>2</sup> has been achieved. For the industry-standard LTO tape cartridge, this density corresponds to a storage capacity of 8 Tbytes of uncompressed data.

#### **20.12 SUPERCONDUCTIVITY**

Superconductivity is basically an electrical phenomenon; however, its discussion has been deferred to this point because there are magnetic implications relative to the superconducting state, and, in addition, superconducting materials are used primarily in magnets capable of generating high fields.

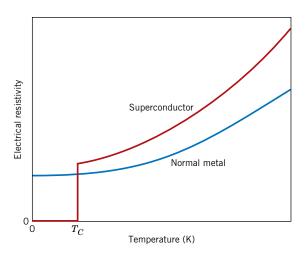
As most high-purity metals are cooled down to temperatures nearing 0 K, the electrical resistivity decreases gradually, approaching some small yet finite value characteristic of the particular metal. There are a few materials, however, for which the resistivity abruptly plunges at a very low temperature, from a finite value to one that is virtually zero and remains there upon further cooling. Materials that display this behavior are called *superconductors*, and the temperature at which they attain **superconductivity** is called the critical temperature  $T_C$ . The resistivity–temperature behaviors for superconductive and nonsuperconductive materials are contrasted in Figure 20.26. The critical temperature varies from superconductor to superconductor but lies between less than 1 K and approximately 20 K for metals and metal alloys. Recently, it has been demonstrated that some complex oxide ceramics have critical temperatures of greater than 100 K.

At temperatures below  $T_C$ , the superconducting state ceases upon application of a sufficiently large magnetic field, termed the *critical field*  $H_C$ , which depends on temperature and decreases with increasing temperature. The same may be said for current density—that is, a critical applied current density  $J_C$  exists below which a material is superconductive. Figure 20.27 shows schematically the boundary in temperature-magnetic field-current density space separating normal and superconducting states. The position of this boundary depends on the material. For temperature, magnetic field, and current density values lying between the origin and this boundary, the material is superconductive; outside the boundary, conduction is normal.

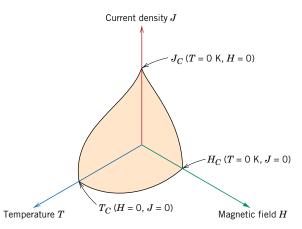
The superconductivity phenomenon has been satisfactorily explained by means of a rather involved theory. In essence, the superconductive state results from attractive interactions between pairs of conducting electrons; the motions of these paired electrons become coordinated such that scattering by thermal vibrations and impurity atoms is

superconductivity

<sup>&</sup>lt;sup>7</sup>The symbol  $T_c$  is used to represent both the Curie temperature (Section 20.6) and the superconducting critical temperature in the scientific literature. They are different entities and should not be confused. In this discussion, they are denoted by  $T_c$  and  $T_c$ , respectively.



**Figure 20.26** Temperature dependence of the electrical resistivity for normally conducting and superconducting materials in the vicinity of 0 K.



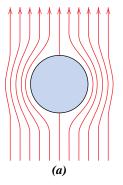
**Figure 20.27** Critical temperature, current density, and magnetic field boundary separating superconducting and normal conducting states (schematic).

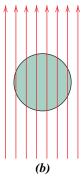
highly inefficient. Thus, the resistivity, being proportional to the incidence of electron scattering, is zero.

On the basis of magnetic response, superconducting materials may be divided into two classifications, type I and type II. Type I materials, while in the superconducting state, are completely diamagnetic—that is, all of an applied magnetic field is excluded from the body of material, a phenomenon known as the *Meissner effect*, which is illustrated in Figure 20.28. As H is increased, the material remains diamagnetic until the critical magnetic field  $H_C$  is reached. At this point, conduction becomes normal, and complete magnetic flux penetration takes place. Several metallic elements, including aluminum, lead, tin, and mercury, belong to the type I group.

Type II superconductors are completely diamagnetic at low applied fields, and field exclusion is total. However, the transition from the superconducting state to the normal state is gradual and occurs between lower critical and upper critical fields, designated  $H_{C1}$  and  $H_{C2}$ , respectively. The magnetic flux lines begin to penetrate into the body of material at  $H_{C1}$ , and with increasing applied magnetic field, this penetration continues; at  $H_{C2}$ , field penetration is complete. For fields between  $H_{C1}$  and  $H_{C2}$ , the material exists in what is termed a *mixed state*—both normal and superconducting regions are present.

Type II superconductors are preferred over type I for most practical applications by virtue of their higher critical temperatures and critical magnetic fields. The three





**Figure 20.28** Representation of the Meissner effect. (a) While in the superconducting state, a body of material (circle) excludes a magnetic field (arrows) from its interior. (b) The magnetic field penetrates the same body of material once it becomes normally conductive.

Table 20.7
Critical Temperatures and Magnetic
Fluxes for Selected
Superconducting
Materials

| Material  | Critical Temperature $T_{C}\left( K ight)$ | Critical Magnetic Flux Density $B_C$ (tesla) <sup>a</sup> |
|---|--|---|
|   | Elements <sup>b</sup>                      |   |
| Tungsten  | 0.02                                       | 0.0001  |
| Titanium  | 0.40                                       | 0.0056  |
| Aluminum  | 1.18                                       | 0.0105  |
| Tin   | 3.72                                       | 0.0305  |
| Mercury (α)   | 4.15                                       | 0.0411  |
| Lead  | 7.19                                       | 0.0803  |
|   | Compounds and Alloys <sup>b</sup>          |   |
| Nb-Ti alloy   | 10.2                                       | 12  |
| Nb–Zr alloy   | 10.8                                       | 11  |
| PbMo <sub>6</sub> S <sub>8</sub>  | 14.0                                       | 45  |
| V <sub>3</sub> Ga   | 16.5                                       | 22  |
| Nb <sub>3</sub> Sn  | 18.3                                       | 22  |
| Nb <sub>3</sub> Al  | 18.9                                       | 32  |
| Nb <sub>3</sub> Ge  | 23.0                                       | 30  |
|   | Ceramic Compounds                          |   |
| YBa <sub>2</sub> Cu <sub>3</sub> O <sub>7</sub>                                 | 92   | _   |
| Bi <sub>2</sub> Sr <sub>2</sub> Ca <sub>2</sub> Cu <sub>3</sub> O <sub>10</sub> | 110  | _   |
| $Tl_2Ba_2Ca_2Cu_3O_{10}$  | 125  | _   |
| HgBa <sub>2</sub> Ca <sub>2</sub> Cu <sub>2</sub> O <sub>8</sub>                | 153  | _   |

<sup>&</sup>quot;The critical magnetic flux density ( $\mu_0H_C$ ) for the elements was measured at 0 K. For alloys and compounds, the flux is taken as  $\mu_0H_{C2}$  (in teslas), measured at 0 K.

most commonly used superconductors are niobium–zirconium (Nb–Zr) and niobium–titanium (Nb–Ti) alloys and the niobium–tin intermetallic compound Nb<sub>3</sub>Sn. Table 20.7 lists several type I and II superconductors, their critical temperatures, and their critical magnetic flux densities.

Recently, a family of ceramic materials that are normally electrically insulative have been found to be superconductors with inordinately high critical temperatures. Initial research has centered on yttrium barium copper oxide, YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub>, which has a critical temperature of about 92 K. This material has a complex perovskite-type crystal structure (Section 12.2). New superconducting ceramic materials reported to have even higher critical temperatures have been and are currently being developed. Several of these materials and their critical temperatures are listed in Table 20.7. The technological potential of these materials is extremely promising because as their critical temperatures are above 77 K, which permits the use of liquid nitrogen, a very inexpensive coolant in comparison to liquid hydrogen and liquid helium. These new ceramic superconductors are not without drawbacks, chief of which is their brittle nature. This characteristic limits the ability of these materials to be fabricated into useful forms such as wires.

The phenomenon of superconductivity has many important practical implications. Superconducting magnets capable of generating high fields with low power consumption are being used in scientific test and research equipment. In addition, they are also used for magnetic resonance imaging (MRI) in the medical field as a diagnostic tool. Abnormalities in body tissues and organs can be detected on the basis of the production of cross-sectional images. Chemical analysis of body tissues is also possible using magnetic

<sup>&</sup>lt;sup>b</sup>**Source:** Adapted from *Materials at Low Temperatures*, R. P. Reed and A. F. Clark (Editors), 1983. Reproduced by permission of ASM International, Materials Park, OH.

resonance spectroscopy (MRS). Numerous other potential applications of superconducting materials also exist. Some of the areas being explored include (1) electrical power transmission through superconducting materials—power losses would be extremely low, and the equipment would operate at low voltage levels; (2) magnets for high-energy particle accelerators; (3) higher-speed switching and signal transmission for computers; and (4) high-speed magnetically levitated trains, for which the levitation results from magnetic field repulsion. The chief deterrent to the widespread application of these superconducting materials is the difficulty in attaining and maintaining extremely low temperatures. It can be hoped that this problem will be overcome with the development of the new generation of superconductors with reasonably high critical temperatures.

#### **SUMMARY**

#### **Basic Concepts**

- The macroscopic magnetic properties of a material are a consequence of interactions between an external magnetic field and the magnetic dipole moments of the constituent atoms.
- The magnetic field strength (H) within a coil of wire is proportional to the number of wire turns and the magnitude of the current and inversely proportional to the coil length (Equation 20.1).
- Magnetic flux density and magnetic field strength are proportional to one another.
  - In a vacuum, the constant of proportionality is the permeability of a vacuum (Equation 20.3).
  - When some material is present, this constant is the permeability of the material (Equation 20.2).
- Associated with each individual electron are both orbital and spin magnetic moments.
   The magnitude of an electron's orbital magnetic moment is equal to the product of the value of the Bohr magneton and the electron's magnetic quantum number.
  - An electron's spin magnetic moment is plus or minus the value of the Bohr magneton (plus for spin up and minus for spin down).
- The net magnetic moment for an atom is the sum of the contributions of each of its electrons, in which there is spin and orbital moment cancellation of electron pairs. When cancellation is complete, the atom possesses no magnetic moment.

#### Diamagnetism and Paramagnetism

- Diamagnetism results from changes in electron orbital motion that are induced by an external field. The effect is extremely small (with susceptibilities on the order of -10<sup>-5</sup>) and in opposition to the applied field. All materials are diamagnetic.
- Paramagnetic materials are those having permanent atomic dipoles, which are acted on individually and aligned in the direction of an external field.
- Diamagnetic and paramagnetic materials are considered nonmagnetic because the magnetizations are relatively small and persist only while an applied field is present.

#### Ferromagnetism

- Large and permanent magnetizations may be established within the ferromagnetic metals (Fe, Co, Ni).
- Atomic magnetic dipole moments are of spin origin, which are coupled and mutually aligned with moments of adjacent atoms.

# Antiferromagnetism and Ferrimagnetism

Antiparallel coupling of adjacent cation spin moments is found for some ionic materials. Those in which there is total cancellation of spin moments are termed antiferromagnetic.

- With ferrimagnetism, permanent magnetization is possible because spin moment cancellation is incomplete.
- For cubic ferrites, the net magnetization results from the divalent ions (e.g., Fe<sup>2+</sup>) that reside on octahedral lattice sites, the spin moments of which are all mutually aligned.

## The Influence of Temperature on Magnetic Behavior

- With rising temperature, increased thermal vibrations tend to counteract the dipole coupling forces in ferromagnetic and ferrimagnetic materials. Consequently, the saturation magnetization gradually decreases with temperature, up to the Curie temperature, at which point it drops to near zero (Figure 20.10).
- Above  $T_c$ , ferromagnetic and ferrimagnetic materials are paramagnetic.

## Domains and Hysteresis

- Below its Curie temperature, a ferromagnetic or ferrimagnetic material is composed of *domains*—small-volume regions in which all net dipole moments are mutually aligned and the magnetization is saturated (Figure 20.11).
- The total magnetization of the solid is just the appropriately weighted vector sum of the magnetizations of all these domains.
- As an external magnetic field is applied, domains having magnetization vectors oriented in the direction of the field grow at the expense of domains that have unfavorable magnetization orientations (Figure 20.13).
- At total saturation, the entire solid is a single domain and the magnetization is aligned with the field direction.
- The change in domain structure with increase or reversal of a magnetic field is accomplished by the motion of domain walls. Both hysteresis (the lag of the *B* field behind the applied *H* field) and permanent magnetization (or *remanence*) result from the resistance to movement of these domain walls.
- From a complete hysteresis curve for a ferromagnetic/ferrimagnetic material, the following may be determined:

Remanence—value of the *B* field when H = 0 ( $B_r$ , Figure 20.14) Coercivity—value of the *H* field when B = 0 ( $H_r$ , Figure 20.14)

## Magnetic Anisotropy

- The *M* (or *B*) versus *H* behavior for a ferromagnetic single crystal is *anisotropic*—that is, it depends on the crystallographic direction along which the magnetic field is applied.
- The crystallographic direction for which  $M_s$  is achieved at the lowest H field is an easy magnetization direction.
- For Fe, Ni, and Co, easy magnetization directions are, respectively, [100], [111], and [0001].
- Energy losses in transformer cores made of magnetic ferrous alloys may be minimized by taking advantage of anisotropic magnetic behavior.

## Soft Magnetic Materials

## Hard Magnetic Materials

- For soft magnetic materials, domain wall movement is easy during magnetization and demagnetization. Consequently, they have small hysteresis loops and low energy losses.
- Domain wall motion is much more difficult for the hard magnetic materials, which results in larger hysteresis loops; because greater fields are required to demagnetize these materials, the magnetization is more permanent.

#### Magnetic Storage

• Information storage is accomplished by using magnetic materials; the two principal types of magnetic media are hard disk drives and magnetic tapes.

- The storage medium for hard disk drives is composed of nanometer-size grains of an HCP cobalt-chromium alloy. These grains are oriented such that their direction of easy magnetization (i.e., [0001]) is perpendicular to the plane of the disk.
- For tape-memory storage, either needle-shape ferromagnetic metal particles or plateshape ferromagnetic barium–ferrite particles are used. Particle size is on the order of tens of nanometers.

#### Superconductivity

- Superconductivity has been observed in a number of materials; upon cooling and in the vicinity of absolute zero temperature, the electrical resistivity vanishes (Figure 20.26).
- The superconducting state ceases to exist if temperature, magnetic field, or current density exceeds a critical value.
- For type I superconductors, magnetic field exclusion is complete below a critical field, and field penetration is complete once  $H_C$  is exceeded. This penetration is gradual with increasing magnetic field for type II materials.
- New complex oxide ceramics are being developed with relatively high critical temperatures that allow inexpensive liquid nitrogen to be used as a coolant.

## **Equation Summary**

| Equation<br>Number | Equation                    | Solving For   | Page<br>Number |
|--------------------|-----------------------------|---|----------------|
| 20.1               | $H = \frac{NI}{l}$          | Magnetic field strength within a coil                 | 805            |
| 20.2               | $B = \mu H$                 | Magnetic flux density in a material                   | 806            |
| 20.3               | $B_0 = \mu_0 H$             | Magnetic flux density in a vacuum                     | 806            |
| 20.4               | $\mu_r = \frac{\mu}{\mu_0}$ | Relative permeability                                 | 806            |
| 20.5               | $B = \mu_0 H + \mu_0 M$     | Magnetic flux density, in terms of magnetization      | 806            |
| 20.6               | $M = \chi_m H$              | Magnetization   | 806            |
| 20.7               | $\chi_m = \mu_r - 1$        | Magnetic susceptibility                               | 806            |
| 20.8               | $B \cong \mu_0 M$           | Magnetic flux density for a ferromagnetic material    | 810            |
| 20.9               | $M_s = 0.60 \mu_{\rm B} N$  | Saturation magnetization for Ni                       | 810            |
| 20.11              | $M_s = N' \mu_{ m B}$       | Saturation magnetization for a ferrimagnetic material | 814            |

## **List of Symbols**

| Symbol       | Meaning   |
|--------------|---|
| I            | Magnitude of current passing through a magnetic coil  |
| l            | Length of magnetic coil   |
| N            | Number of turns in a magnetic coil (Equation 20.1); number of atoms per unit volume (Equation 20.9) |
| N'           | Number of Bohr magnetons per unit cell  |
| $\mu$        | Permeability of a material  |
| $\mu_0$      | Permeability of a vacuum  |
| $\mu_{ m B}$ | Bohr magneton $(9.27 \times 10^{-24} \mathrm{A \cdot m^2})$   |

## **Important Terms and Concepts**

antiferromagnetism Bohr magneton coercivity Curie temperature diamagnetism domain ferrimagnetism ferrite (ceramic)

ferromagnetism hard magnetic material hysteresis magnetic field strength magnetic flux density magnetic induction magnetic susceptibility magnetization
paramagnetism
permeability
remanence
saturation magnetization
soft magnetic material
superconductivity

#### REFERENCES

Brockman, F. G., "Magnetic Ceramics—A Review and Status Report," *American Ceramic Society Bulletin*, Vol. 47, No. 2, February 1968, pp. 186–194.

Coey, J. M. D., Magnetism and Magnetic Materials, Cambridge University Press, Cambridge, 2009.

Cullity, B. D., and C. D. Graham, Introduction to Magnetic Materials, 2nd edition, Wiley, Hoboken, NJ, 2009.

Hilzinger, R., and W. Rodewald, Magnetic Materials: Fundamentals, Products, Properties, Applications, Wiley, Hoboken, NJ, 2013. Jiles, D., Introduction to Magnetism and Magnetic Materials, 2nd edition, CRC Press, Boca Raton, FL, 1998.

Spaldin, N. A., *Magnetic Materials: Fundamentals and Device Applications*, 2nd edition, Cambridge University Press, Cambridge, 2011.

## **QUESTIONS AND PROBLEMS**

1 Problem available (at instructor's discretion) in WileyPLUS

#### **Basic Concepts**

**20.1** A coil of wire 0.25 m long and having 400 turns carries a current of 15 A.

- (a) What is the magnitude of the magnetic field strength *H*?
- **(b)** Compute the flux density *B* if the coil is in a vacuum.
- **(c)** Compute the flux density inside a bar of chromium positioned within the coil. The susceptibility for chromium is given in Table 20.2.
- (d) Compute the magnitude of the magnetization M.
- **20.2** Demonstrate that the relative permeability and the magnetic susceptibility are related according to Equation 20.7.

**20.3** It is possible to express the magnetic susceptibility  $\chi_m$  in several different units. For the discussion in this chapter,  $\chi_m$  is used to designate the volume susceptibility in SI units—that is, the quantity that gives the magnetization per unit volume (m³) of material when multiplied by H. The mass susceptibility  $\chi_m(kg)$  yields the magnetic moment (or magnetization) per kilogram of material when multiplied by H; similarly, the atomic susceptibility  $\chi_m(a)$  gives the magnetization per kilogram-mole. The last two quantities

are related to  $\chi_m$  through the following relationships:

$$\chi_m = \chi_m(\text{kg}) \times \text{mass density (in kg/m}^3)$$
  
 $\chi_m(a) = \chi_m(\text{kg}) \times \text{atomic weight (in kg)}$ 

When using the cgs-emu system, comparable parameters exist that may be designated by  $\chi'_m$ ,  $\chi'_m(g)$ , and  $\chi'_m(a)$ ; the  $\chi_m$  and  $\chi'_m$  are related in accordance with Table 20.1. From Table 20.2,  $\chi_m$  for copper is  $-0.96 \times 10^{-5}$ ; convert this value into the other five susceptibilities.

- **20.4 (a)** Explain the two sources of magnetic moments for electrons.
  - **(b)** Do all electrons have a net magnetic moment? Why or why not?
  - **(c)** Do all atoms have a net magnetic moment? Why or why not?

# Diamagnetism and Paramagnetism Ferromagnetism

20.5 The magnetic flux density within a bar of some material is 0.630 tesla at an *H* field of 5 × 10<sup>5</sup> A/m. Compute the following for this material: (a) the magnetic permeability and (b) the magnetic susceptibility. (c) What type(s) of magnetism would you suggest is (are) being displayed by this material? Why?

- 20.6 The magnetization within a bar of some metal alloy is 1.2 × 10<sup>6</sup> A/m at an *H* field of 200 A/m. Compute the following: (a) the magnetic susceptibility, (b) the permeability, and (c) the magnetic flux density within this material. (d) What type(s) of magnetism would you suggest is (are) being displayed by this material? Why?
- **20.7** Compute (a) the saturation magnetization and **(b)** the saturation flux density for iron, which has a net magnetic moment per atom of 2.2 Bohr magnetons and a density of 7.87 g/cm<sup>3</sup>.
- **20.8** Confirm that there are 1.72 Bohr magnetons associated with each cobalt atom, given that the saturation magnetization is 1.45 × 10<sup>6</sup> A/m, that cobalt has an HCP crystal structure with an atomic radius of 0.1253 nm and a *c/a* ratio of 1.623.
- 20.9 Assume there exists some hypothetical metal that exhibits ferromagnetic behavior and that has (1) a simple cubic crystal structure (Figure 3.3), (2) an atomic radius of 0.125 nm, and (3) a saturation flux density of 0.85 tesla. Determine the number of Bohr magnetons per atom for this material.
- **20.10** A net magnetic moment is associated with each atom in paramagnetic and ferromagnetic materials. Explain why ferromagnetic materials can be magnetized permanently, whereas paramagnetic ones cannot.

#### Antiferromagnetism and Ferrimagnetism

- **20.11** Consult a reference in which Hund's rule is outlined, and on its basis explain the net magnetic moments for each of the cations listed in Table 20.4.
- 20.12 Estimate (a) the saturation magnetization and
  (b) the saturation flux density of cobalt ferrite [(CoFe<sub>2</sub>O<sub>4</sub>)<sub>8</sub>], which has a unit cell edge length of 0.838 nm.
- 20.13 The chemical formula for copper ferrite may

  be written as (CuFe<sub>2</sub>O<sub>4</sub>)<sub>8</sub> because there are eight formula units per unit cell. If this material has a saturation magnetization of 1.35 × 10<sup>5</sup> A/m and a density of 5.40 g/cm³, estimate the number of Bohr magnetons associated with each Cu²+ ion.
- 20.14 The formula for samarium iron garnet (Sm<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>) may be written in the form Sm<sub>3</sub><sup>c</sup>Fe<sub>2</sub><sup>d</sup>Fe<sub>3</sub><sup>d</sup>O<sub>12</sub>, where the superscripts *a*, *c*, and *d* represent different sites on which the Sm<sup>3+</sup> and Fe<sup>3+</sup> ions are located. The spin magnetic moments for the Sm<sup>3+</sup> and Fe<sup>3+</sup> ions positioned in the *a* and *c* sites are oriented parallel to one another and antiparallel to the Fe<sup>3+</sup> ions in *d* sites. Compute the number of Bohr magnetons associated with

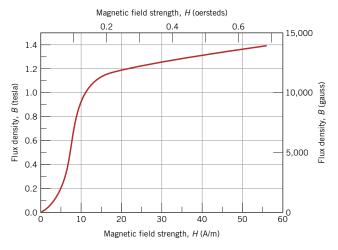
each Sm<sup>3+</sup> ion, given the following information: (1) each unit cell consists of eight formula (Sm<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>) units; (2) the unit cell is cubic with an edge length of 1.2529 nm; (3) the saturation magnetization for this material is  $1.35 \times 10^5$  A/m; and (4) there are 5 Bohr magnetons associated with each Fe<sup>3+</sup> ion.

# The Influence of Temperature on Magnetic Behavior

20.15 Briefly explain why the magnitude of the saturation magnetization decreases with increasing temperature for ferromagnetic materials, and why ferromagnetic behavior ceases above the Curie temperature.

## **Domains and Hysteresis**

- **20.16** Briefly describe the phenomenon of magnetic hysteresis and why it occurs for ferro- and ferrimagnetic materials.
- **20.17** A coil of wire 0.5 m long and having 20 turns carries a current of 1.0 A.
  - (a) Compute the flux density if the coil is within a vacuum.
  - **(b)** A bar of an iron–silicon alloy, the *B–H* behavior for which is shown in Figure 20.29, is positioned within the coil. What is the flux density within this bar?
  - **(c)** Suppose that a bar of molybdenum is now situated within the coil. What current must be used to produce the same *B* field in the Mo as was produced in the iron–silicon alloy (part b) using 1.0 A?



**Figure 20.29** Initial magnetization *B*-versus-*H* curve for an iron–silicon alloy.

- **20.18** A ferromagnetic material has a remanence of 1.0 tesla and a coercivity of 15,000 A/m. Saturation is achieved at a magnetic field strength of 25,000 A/m, at which the flux density is 1.25 teslas. Using these data, sketch the entire hysteresis curve in the range H = -25,000 to +25,000 A/m. Be sure to scale and label both coordinate axes.
- **20.19** The following data are for a plain carbon steel alloy:

| H (A/m) | B (tesla) | H(A/m) | B (tesla) |
|---------|-----------|--------|-----------|
| 0       | 0         | 80     | 0.90      |
| 15      | 0.007     | 100    | 1.14      |
| 30      | 0.033     | 150    | 1.34      |
| 50      | 0.10      | 200    | 1.41      |
| 60      | 0.30      | 300    | 1.48      |
| 70      | 0.63      |        |           |

- (a) Construct a graph of B versus H.
- **(b)** What are the values of the initial permeability and initial relative permeability?
- **(c)** What is the value of the maximum permeability?
- (d) At about what H field does this maximum permeability occur?
- **(e)** To what magnetic susceptibility does this maximum permeability correspond?
- 20.20 An iron bar magnet having a coercivity of 7000 A/m is to be demagnetized. If the bar is inserted within a cylindrical wire coil 0.25 m long and having 150 turns, what electric current is required to generate the necessary magnetic field?
- **20.21** A bar of an iron–silicon alloy having the *B−H* behavior shown in Figure 20.29 is inserted within a coil of wire 0.40 m long and having 50 turns through which passes a current of 0.1 A.
  - (a) What is the B field within this bar?
  - **(b)** At this magnetic field:
    - (i) What is the permeability?
    - (ii) What is the relative permeability?
    - (iii) What is the susceptibility?
    - (iv) What is the magnetization?

#### Magnetic Anisotropy

**20.22** Estimate saturation values of *H* for single-crystal nickel in the [100], [110], and [111] directions.

**20.23** The energy (per unit volume) required to magnetize a ferromagnetic material to saturation  $(E_s)$  is defined by the following equation:

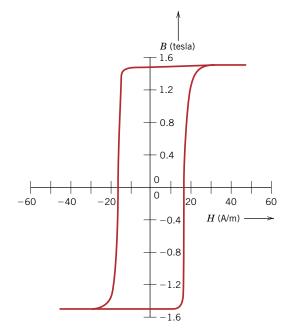
$$E_s = \int_0^{M_s} \mu_0 H dM$$

that is,  $E_s$  is equal to the product of  $\mu_0$  and the area under an M-versus-H curve, to the point of saturation referenced to the ordinate (or M) axis—for example, in Figure 20.17, the area between the vertical axis and the magnetization curve to  $M_s$ . Estimate  $E_s$  values (in  $J/m^3$ ) for single-crystal iron in [100], [110], and [111] directions.

## Soft Magnetic Materials

## Hard Magnetic Materials

- **20.24** Cite the differences between hard and soft magnetic materials in terms of both hysteresis behavior and typical applications.
- 20.25 Assume the silicon–iron (97 Fe, 3 Si) in Table
  20.5 just reaches the point of saturation when inserted within the coil in Problem 20.1. Compute the saturation magnetization.
- **20.26** Figure 20.30 shows the *B*-versus-*H* curve for a nickel–iron alloy.
  - (a) What is the saturation flux density?
  - **(b)** What is the saturation magnetization?



**Figure 20.30** Complete magnetic hysteresis loop for a nickel–iron alloy.

- **(c)** What is the remanence?
- (d) What is the coercivity?
- **(e)** On the basis of data in Tables 20.5 and 20.6, would you classify this material as a soft or a hard magnetic material? Why?

## Magnetic Storage

**20.27** Briefly explain the manner in which information is stored magnetically.

## Superconductivity

- **20.28** For a superconducting material at a temperature T below the critical temperature  $T_C$ , the
- ture T below the critical temperature  $T_C$ , the critical field  $H_C(T)$  depends on temperature according to the relationship

$$H_C(T) = H_C(0) \left(1 - \frac{T^2}{T_C^2}\right)$$
 (20.14)

where  $H_C(0)$  is the critical field at 0 K.

- (a) Using the data in Table 20.7, calculate the critical magnetic fields for lead at 2.5 and 5.0 K.
- **(b)** To what temperature must lead be cooled in a magnetic field of 15,000 A/m for it to be superconductive?
- **20.29** Using Equation 20.14, determine which of the superconducting elements in Table 20.7 are superconducting at 2 K and a magnetic field of 40,000 A/m.
- **20.30** Cite the differences between type I and type II superconductors.
- 20.31 Briefly describe the Meissner effect.
- **20.32** Cite the primary limitation of the new superconducting materials that have relatively high critical temperatures.

#### **DESIGN PROBLEMS**

#### **Ferromagnetism**

**20.D1** A cobalt–iron alloy is desired that has a saturation magnetization of  $1.47 \times 10^6$  A/m. Specify its composition in weight percent iron. Cobalt has an HCP crystal structure with c/a ratio of 1.623. Assume that the unit cell volume for this alloy is the same as for pure Co.

## **Ferrimagnetism**

**20.D2** Design a cubic mixed-ferrite magnetic material that has a saturation magnetization of 4.25 × 10<sup>5</sup> A/m.

# FUNDAMENTALS OF ENGINEERING QUESTIONS AND PROBLEMS

- **20.1FE** The magnetization within a bar of some metal alloy is 4.6 × 10<sup>5</sup> A/m at an *H* field of 52 A/m. What is this alloy's magnetic susceptibility?
  - (A)  $1.13 \times 10^{-4}$
  - (B)  $8.85 \times 10^3$
  - (C)  $1.11 \times 10^{-2} \text{ H/m}$
  - (D)  $5.78 \times 10^{-1}$  tesla
- **20.2FE** Which of the following pairs of materials displays ferromagnetic behavior?
  - (A) Aluminum oxide and copper
  - (B) Aluminum and titanium
  - (C) MnO and Fe<sub>3</sub>O<sub>4</sub>
  - (D) Iron ( $\alpha$ -ferrite) and nickel