MAT 167 Homework 7

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6.3

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$$A = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix}$$
$$A^{T}A = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 2 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

$$|A^{T}A - \lambda I| = 0$$

$$= \begin{vmatrix} 1 - \lambda & 1 & 0 \\ 1 & 2 - \lambda & 1 \\ 0 & 1 & 1 - \lambda \end{vmatrix}$$

$$= (1 - \lambda)[(2 - \lambda)(1 - \lambda) - 1] - (1 - \lambda)$$

$$= (1 - \lambda)[[(2 - \lambda)(1 - \lambda) - 1] - 1]$$

$$= (1 - \lambda)(\lambda^{2} - 3\lambda)$$

$$= \lambda(1 - \lambda)(\lambda - 3)$$

$$AA^T = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$$

7.3