

# ECS 154A Homework 4

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1. Implement the following D flipflop as a JK flipflop.

D

		$QX$			
		00	01	11	10
$YZ$	00	1	0	0	1
	01	1	1	1	0
	11	1	1	1	1
	10	0	1	0	0

J

		$QX$			
		00	01	11	10
$YZ$	00	1	0	$d$	$d$
	01	1	1	$d$	$d$
	11	1	1	$d$	$d$
	10	0	1	$d$	$d$

$$J = Z + \overline{X} \overline{Y} + XY$$

K

		$QX$			
		00	01	11	10
$YZ$	00	$d$	$d$	1	0
	01	$d$	$d$	0	1
	11	$d$	$d$	0	0
	10	$d$	$d$	1	1

$$K = X\overline{Z} + Y\overline{Z} + \overline{X} \overline{Y}Z$$

2. Implement the following D flipflop as a T flipflop.

D

		$QX$			
		00	01	11	10
$YZ$	00	0	0	1	1
	01	1	1	0	0
	11	1	1	0	0
	10	0	0	1	1

T

		$QX$			
		00	01	11	10
$YZ$	00	0	0	0	0
	01	1	1	1	1
	11	1	1	1	1
	10	0	0	0	0

$T = Z$

3. Implement the state diagram using D flipflops. Show the state transition table, state encoding, k-maps, and equations.

(a) State transitions

Current	$X_1$	$X_0$	Next
A	d	0	B
A	d	1	A
B	0	0	B
B	0	1	D
B	1	0	D
B	1	1	B
C	0	0	C
C	d	1	D
C	1	0	A
D	0	D	C
D	1	D	D

Output

State	$Z_1$	$Z_0$
A	0	0
B	0	1
C	1	0
D	0	0

(b) State encoding

State	$S_1$	$S_0$
A	0	0
B	0	1
C	1	0
D	1	1

Encoded state transitions

Current		Input		Next	
$S_1$	$S_0$	$X_1$	$X_0$	$S'_1$	$S'_0$
0	0	d	0	0	1
0	0	d	1	0	0
0	1	0	0	0	1
0	1	0	1	1	1
0	1	1	0	1	1
0	1	1	1	0	1
1	0	0	0	1	0
1	0	d	1	1	1
1	0	1	0	0	0
1	1	0	d	1	0
1	1	1	d	1	1

Encoded output

$S_1$	$S_0$	$Z_1$	$Z_0$
0	0	0	0
0	1	0	1
1	0	1	0
1	1	0	0

$S'_1$		$S_1 S_0$			
		00	01	11	10
$X_1 X_0$	00	0	0	1	1
	01	0	1	1	1
	11	0	0	1	1
	10	0	1	0	1

$S'_0$		$S_1 S_0$			
		00	01	11	10
$X_1 X_0$	00	1	1	0	0
	01	0	1	0	1
	11	0	1	1	1
	10	1	1	1	0

$$S'_1 = (S_1 + S_0)(S_1 + \overline{X_1} + \overline{X_0})(S_1 + X_1 + X_0)(\overline{S_1} + \overline{S_0} + \overline{X_1} + X_0)$$

$$S'_0 = (S_1 + S_0 + \overline{X_0})(\overline{S_1} + \overline{S_0} + X_1)(\overline{S_1} + S_0 + X_0)$$

$$Z_1 = S_1 \overline{S_0}$$

$$Z_0 = \overline{S_1} S_0$$