

# STA 032 Homework 8

Hardy Jones  
999397426  
Professor Melcon  
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§ 6.1    5 We have  $n = 80$ ,  $\bar{X} = 4.5$  and  $s = 2.7$ .

i. We have our hypotheses:

$$H_0 : \mu \geq 5.4$$

$$H_A : \mu < 5.4$$

ii. The test statistic is:

$$Z_s = \frac{\bar{X} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{4.5 - 5.4}{\frac{2.7}{\sqrt{80}}} = -2.98$$

iii. The corresponding p-value is: 0.00140

iv. Since the p-value is so small, we reject the null hypothesis.

(1) See part iii above.

(2) I am convinced the mean number of sick days is less than 5.4 after allowing telecommuting. The probability that the sample was from a population where the mean number of sick days was greater than 5.4 is exceedingly small. It is much more likely that the sample was taken from a population with a mean number of sick days less than 5.4.

8 We have  $n = 100$ ,  $\bar{X} = 25$  and  $s = 60$ .

i. We have our hypotheses:

$$H_0 : \mu = 0$$

$$H_A : \mu \neq 0$$

ii. The test statistic is:

$$Z_s = \frac{\bar{X} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{25 - 0}{\frac{60}{\sqrt{100}}} = 4.17$$

iii. The corresponding p-value is: 1

iv. Since the p-value is large, we assume the null hypothesis is true.

(1) See part iii above.

- (2) I am convinced that the laser is properly calibrated. Since the probability that the sample was from a population with 0 mean error is effectively 1, it makes sense that the laser is properly calibrated.

§ 6.2 9 (1) The null hypothesis should be:

$$H_0 : \mu \leq 8 \text{ years}$$

If  $H_0$  is rejected, then it is known that the batteries will have a mean lifetime of more than 8 years and so can be installed in pacemakers.

If  $H_0$  is not rejected, then the batteries might have a mean lifetime less than 8 years and so cannot be installed in pacemakers.

- (2) The null hypothesis should be:

$$H_0 : \mu \leq 60\,000 \text{ miles}$$

If  $H_0$  is rejected, then it is known that the tires will have a mean lifetime more than 60 000 miles and so the new material can be used to make tires.

If  $H_0$  is not rejected, then the tires might have a mean lifetime less than 60 000 miles and so the new material cannot be used to make tires.

- (3) The null hypothesis should be:

$$H_0 : \mu = 10 \text{ mL s}^{-1}$$

If  $H_0$  is rejected, then it is known that the flow rate will be  $10 \text{ mL s}^{-1}$  and so the flowmeter should be recalibrated.

If  $H_0$  is not rejected, then the flow rate might not be  $10 \text{ mL s}^{-1}$  and so the flowmeter should not be recalibrated.

14 i. Greater than 0.05.

We can compute the necessary values from the information given.

With the interval from 1.2 to 2.0, we can compute  $\bar{X} = \frac{1.2+2.0}{2} = 1.6$ .

We also know that

$$\begin{aligned} 1.2 &= 1.6 - 1.96 \frac{s}{\sqrt{n}} \\ 1.96 \frac{s}{\sqrt{n}} &= 0.4 \\ \frac{s}{\sqrt{n}} &= \frac{0.4}{1.96} \\ \frac{s}{\sqrt{n}} &= 0.204 \end{aligned}$$

So, we can compute a z-score

$$Z = \frac{\bar{X} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{1.6 - 1.4}{0.204} = 0.98$$

The corresponding p-value is 0.8365, which much greater than 0.05.

§ 6.3 7 We want the hypotheses:

$$H_0 : \mu \leq 0.7$$

$$H_A : \mu > 0.7$$

So  $n = 150$  and  $p = 0.7$ .

Thus,  $\hat{p} \sim N(150, \frac{0.7(1-0.7)}{150}) = N(150, 0.00140)$ .

This lets us compute  $\sigma_{\hat{p}} = \sqrt{0.00140} = 0.0374$ , and an observed  $\hat{p} = \frac{110}{150} = 0.733$ .

So we have a z-score of  $Z = \frac{0.733-0.7}{0.0374} = 0.8913$ .

The corresponding p-value is  $1 - 0.8133 = 0.1867$ .

Since this value is much higher than 0.05, we do not reject the null hypothesis. We cannot conclude that more than 70% of the households in the city have high-speed internet access.

8 We want the hypotheses:

$$H_0 : \mu \geq 0.08$$

$$H_A : \mu < 0.08$$

So  $n = 300$  and  $p = 0.08$ .

Thus,  $\hat{p} \sim N(300, \frac{0.08(1-0.08)}{300}) = N(300, 0.000245)$ .

This lets us compute  $\sigma_{\hat{p}} = \sqrt{0.000245} = 0.0157$ , and an observed  $\hat{p} = \frac{12}{300} = 0.0400$ .

So we have a z-score of  $Z = \frac{0.0400-0.08}{0.0157} = -2.55$ .

The corresponding p-value is 0.0054.

Since this value is very small, we reject the null hypothesis. We can conclude that less than 8% of the produced parts are defective.

§ 6.4 3 We have  $n = 8$ ,  $\bar{X} = 6.5$  and  $s = 1.9$ .

i. We have our hypotheses:

$$H_0 : \mu \leq 5$$

$$H_A : \mu > 5$$

ii. The test statistic is:

$$t = \frac{\bar{X} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{6.5 - 5}{\frac{1.9}{\sqrt{8}}} = 2.23$$

- iii. The corresponding p-value is:  $0.025 < P < 0.050$
- iv. Since the p-value is less than 0.050, we reject the null hypothesis.
- (1) See part i above.
- (2) See part iii above.
- (3) Since we reject the null hypothesis, the alternative hypothesis states that the mean flow rate is more than 5 gpm.  
So, the pumps should be put into service.

4 We have  $n = 10$ ,  $\bar{X} = 23.2$  and  $s = 0.2$ .

- i. We have our hypotheses:

$$H_0 : \mu = 23$$

$$H_A : \mu \neq 23$$

- ii. The test statistic is:

$$t = \frac{\bar{X} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{23.2 - 23}{\frac{0.2}{\sqrt{10}}} = 3.16$$

- iii. The corresponding p-value is:  $0.01 < P < 0.005$
- iv. Since the p-value is less than 0.050, we reject the null hypothesis.
- (1) See part i above.
- (2) See part iii above.
- (3) Since we reject the null hypothesis, the alternative hypothesis states that the mean percentage of potassium by weight is not 23%.  
So, the process should be recalibrated.

§ 6.5    7 (1)  
(2)

§ 6.6    12

§ 6.7    13

§ 6.12    4 (1)  
(2)  
(3)  
(4)  
5 (1)  
(2)  
(3)  
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