

# ECS 170 Homework 3

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1. Consider the figure

(a) Which of the following (if any) are asserted by the network structure?

i.  $P(B, I, M) = P(B)P(I)P(M)$

This is not asserted because  $B, I, M$  are not independent.

ii.  $P(J|G) = P(J|G, I)$

This is asserted because  $J$  is conditionally independent of  $I$  given  $G$ .

iii.  $P(M|G, B, I) = P(M|G, B, I, J)$

This is asserted because  $J$  is conditionally independent of  $M$  given  $G$ .

(b) Calculate the value of  $P(b, i, m, \neg g, j)$ .

$$\begin{aligned} P(b, i, m, \neg g, j) &= P(b)P(i|b, m)P(m)P(\neg g|b, i, m)P(j|\neg g) \\ &= (0.9)(0.9)(0.1)(0.9)(0.0) \\ &= 0.0 \end{aligned}$$

2. Consider the figure.

(a) Give one example of conditional independence and another of unconditional independence.

**JohnCalls** is conditionally independent of **Burglary** given **Alarm**.

**Burglary** is unconditionally independent of **Earthquake**.

(b) Write completely the general expression to calculate

$P(\text{Burglary}, \text{Earthquake}, \text{Alarm}, \text{JohnCalls}, \text{MaryCalls})$

Abbreviating

Burglary      B

Earthquake   E

Alarm         A

JohnCalls     J

MaryCalls     M

$$P(B, E, A, J, M) = P(B)P(E)P(A|B, E)P(J|A)P(M|A)$$