MAT 167 HW 1

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§ 1.4 2 • After reducing to a triangle system we have:

$$2x + 3y = 1$$
$$-6y = 6$$

So y = -1, back-substituting and solving for x we get

$$2x + 3(-1) = 1 \implies 2x - 3 = 1 \implies 2x = 4 \implies x = 2.$$

So we have x = 2, y = -1.

• We verify that

$$2\begin{bmatrix}2\\10\end{bmatrix} + (-1)\begin{bmatrix}3\\9\end{bmatrix} = \begin{bmatrix}4\\20\end{bmatrix} + \begin{bmatrix}-3\\-9\end{bmatrix} = \begin{bmatrix}1\\11\end{bmatrix}$$

• If the right hand side changed to $\begin{bmatrix} 4 \\ 44 \end{bmatrix} = 4 \begin{bmatrix} 1 \\ 11 \end{bmatrix}$, then the x and y values increase accordingly.

That is
$$x = 4(2) = 8, y = 4(-1) = -4$$

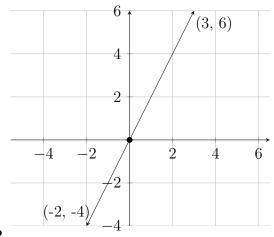
- 7 i. If a=2, then elimination breaks down permanently. As we will end up in an inconsistent system.
 - ii. If a=0, then elimination breaks down temporarily until the first equation is swapped for the second.

We can solve by elimination if we swap the equations

$$\begin{cases}
4x + 6y = 6 \\
3y = -3
\end{cases} \implies \begin{cases}
4x + 6y = 6 \\
y = -1
\end{cases} \implies \begin{cases}
4x = 12 \\
y = -1
\end{cases} \implies \begin{cases}
x = 3 \\
y = -1
\end{cases}$$

So, x = 3, y = -1.

- 9 These two equations have a solution only when $2b_1 = b_2$.
 - There are infinitely many solutions.



§ 1.5 11

§ 1.6 2