MAT 167 Homework 8

Hardy Jones 999397426 Professor Cheer Winter 2014

6.1

5

a We have $f = x^2 + 2bxy + 81y^2$. So a = 1 and c = 81. We need $ac > b^2$ or $81 > b^2$. So A is positive definite when -3 < b < 3.

b

$$\begin{bmatrix} 1 & b \\ b & 9 \end{bmatrix} = \begin{bmatrix} 1 & b \\ 0 & 9 - b^2 \end{bmatrix}$$

So we have

$$A = \begin{bmatrix} 1 & 0 \\ b & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 9 - b^2 \end{bmatrix} \begin{bmatrix} 1 & b \\ 0 & 1 \end{bmatrix}$$

6.2

6.3

6.4