

a) Problem formulation and mathematical modelling.

- Mathematical translation.

The aim is to describe the vertical motion of a ball dropped from a height subject to

→ Gravitational force

→ Elastic collision with the ground.

- Complete mathematical model.

Acceleration of the ball at initial height

$$a(t) = g \quad \text{where } g = \text{gravitational force}$$

From Newton's second law.

Therefore, velocity

$$v(t) = \int a \, dt = \int g \, dt = gt + C = gt + v_0$$

So, ball position,

$$y(t) = \int v(t) \, dt = \int (gt + v_0) \, dt = \frac{1}{2}gt^2 + v_0t + C$$
$$= \frac{1}{2}gt^2 + v_0t + y_0$$

Including the coefficient of restitution, e ,

e = Measure of how bouncy the collision is.

$$e = \frac{v_{\text{after}}}{v_{\text{before}}} \quad (\text{ratio between } 0-1)$$

Velocity after collision,

$$v_{\text{new}} = v_{\text{old}} * -e$$

~~where~~ → Constraints

$$y \rightarrow y(t) \geq 0$$

→ Bounces occur at $y=0$

→ Stop simulation when kinetic energy is zero.