

BB512 - Instructor Resources

Owen R. Jones (Course Coordinator)

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Chapter 1

This website and other course materials

This website contains resources for instructors in BB512.

We may not do ALL of these exercises, but you are welcome to do ones we miss in your own time.

1.1 Software

We will use Excel and R/RStudio during this course.

1.1.1 Excel

I expect you will already have Excel installed, so there is not much to say here.

Be aware that Excel differs depending on the language it is localised in. For example, Danish vs. English. This means that some of the commands might differ between version. See [here](#) for examples.

1.1.2 R and RStudio

R and RStudio are two separate pieces of software. RStudio is a user-friendly interface to talk to R, it cannot work if you have not got R installed. So, when you install these two programs, install R first, then RStudio.

Already have them installed? I strongly recommend to update to the latest versions of R, which you can download [here](#) and RStudio Desktop, which you can find [here](#).

Part I

Evolution by Natural Selection

Chapter 2

The Blind Watchmaker

2.1 Introduction

This exercise simulates evolutionary processes using an algorithm inspired by *The Blind Watchmaker*. Students will observe how random mutations and selection pressure shape the evolution of a target phrase from an initial random string. By altering parameters of selection and phrase length, students will explore the balance between randomness (mutation) and determinism (selection) in evolutionary processes. This exercise provides insight into natural selection and highlights the filtering nature of natural selection.

2.2 Key concepts

- **Random Mutation:** Each generation introduces random changes (mutations) in the string.
- **Selection Pressure:** When active, selection favours letters that match the target phrase, simulating the process of natural selection.
- **Stochasticity vs Determinism:** Evolution combines random mutations and deterministic selection, resulting in gradual adaptation toward a specific goal (in this case, a predefined phrase).

2.3 Learning outcomes

- Greater understanding of adaptive evolution via natural selection.
- Understanding that random change does NOT result in disorder, if paired with selection.
- Use of R for exploring biological phenomenon.

2.4 Activity Overview

2.4.1 Time: 30 minutes

1. **Introduction (5-10 min):** Explain the activity, including the basic concepts of natural selection.
2. **Loading RStudio, Script setup (5 min):** Students load RStudio, create a new script and paste the exercise script into it.
3. **Main Activity (15 min):** Students may use their own phrase, they should use the script and then answer the questions.
4. **Discussion and Wrap-Up (5-10 min):** Run through the questions and answers. Reflect on how the simulation demonstrates key concepts of selection, adaptation, and evolution.

2.5 Instructions for facilitating

2.5.1 Code Setup

1. **Preparation:** Ensure students have R and RStudio installed. If needed, provide assistance with installation or setting up the R environment.
2. **Running the Code:** Students open a new R script, paste the provided code, and save it.
 - Explain that the simulation uses random letter generation to mimic mutations, and selection fixes correct letters over time, just as beneficial traits are selected in nature.
3. **Modifying Parameters:** Have students edit parameters like `phrase`, `nGenerations`, and `selection`, observing the effects.

2.5.2 Key Observation

- When **selection is ON**, the phrase gradually becomes more similar to the target, showing how selection can direct random mutations toward a specific outcome.
- When **selection is OFF**, the output remains random, illustrating that random changes without selection do not lead to order or meaningful results.

2.6 Questions and model answers

Question 1: What happens if selection is turned OFF? - Without selection, mutations accumulate randomly without any guidance, resulting in no directional progress toward the target phrase.

Question 2: Does the number of generations affect whether the target phrase is reached? - Yes, more generations allow more opportunities for

mutations and selection to work, increasing the chances of reaching the target phrase, but there is no absolute guarantee.

Question 3: Does the speed of reaching the target phrase depend on the length of the phrase? - Yes, longer phrases require more steps to match each letter, meaning the process takes more time and generations due to the greater complexity.

Question 4: How does this simulation differ from real natural selection? - Real natural selection is not driven by a specific goal. It is shaped by environmental pressures and the organisms' fitness relative to their surroundings, rather than aiming for a specific outcome like in this simulation.

2.7 Teaching Tips

1. **Clarify the Role of Selection:** Emphasise that selection drives the evolutionary process toward the target, while random mutations provide the variation necessary for evolution.
2. **R Programming Guidance:** Assist students in modifying parameters like mutation rate, number of generations, and selection to observe different outcomes.
3. **Link to Real Evolution:** Discuss how real-world evolution is more complex and involves multiple factors such as genetic drift, environmental changes, and does not have a predetermined goal like the target phrase.

2.8 Common Pitfalls to Watch For

- **Misunderstanding Selection:** Students might think that selection always chooses perfect sequences. Clarify that selection favours the closest match, not necessarily perfection.
- **R Script Issues:** Ensure students accurately modify the code to adjust parameters like the mutation rate and number of generations.
- **Misinterpretation of the Target Concept:** Make sure students understand that real natural selection does not work toward a fixed outcome like in this simulation.

Chapter 3

Bug Hunt Camouflage (NetLogo)

3.1 Introduction

This exercise demonstrates adaptive evolution and natural selection using a predator-prey simulation in NetLogo. Students take on the role of a predator (a bird) and hunt bugs to observe how the bug population evolves in response to selective pressures. The key concept is the relationship between camouflage and predator efficiency, mirroring real-world natural selection.

3.2 Key Concepts

- **Natural Selection:** The process where individuals with traits better suited to the environment survive and reproduce, passing those traits to the next generation.
- **Adaptive Evolution:** Changes in populations over time that enhance survival and reproduction in a given environment.
- **Selection Pressure:** The environmental factors that influence which individuals survive and reproduce.
- **Heritability:** A measure of the fraction of phenotype that can be attributed to genetic variation.

3.3 Learning Outcomes

- Understanding adaptive evolution via natural selection.
- Understanding how fitness depends on the environment.
- Understanding the terms adaptation, selection, selection pressure, heritability.

3.4 Activity Overview

3.4.1 Time: 45 minutes

1. **Introduction (5 min):** Explain the activity, including the basic concepts of natural selection and camouflage.
2. **Simulation Setup (5-10 min):** Students log into NetLogo and load the Bug Hunt Camouflage model.
3. **Main Activity (25 min):** Students play the role of a predator, hunting bugs and observing how the bug population evolves over time. Students pause and analyse the graphs to assess hunting efficiency and bug color evolution.
4. **Discussion and Wrap-Up (5-10 min):** Reflect on how the simulation demonstrates key concepts of selection, adaptation, and evolution.

3.5 Instructions for Facilitating

3.5.1 Simulation Setup

1. Guide students to open NetLogo and find the “Bug Hunt Camouflage” model.
 - **Tip:** If using UCloud, ensure students are familiar with the platform steps outlined in the task description.
2. Explain the interface: sliders control population and mutation rates, while the graphs provide real-time feedback on bug traits and hunting efficiency.

3.5.2 Running the Simulation

- Students begin by adjusting the population size to 30 bugs using the “carrying-capacity” slider.
- Students click “set up”, then start the simulation with “Go”. They then hunt bugs by clicking on them. Encourage them to hunt quickly to avoid bias in their selection process.
- Students observe how their hunting impacts the bug population, paying attention to changes in color traits (hue, saturation, brightness) and hunting efficiency (the slope of the graph showing number of bugs caught) over time.
- After 5 minutes of hunting, students should pause the simulation and examine the graphs.
 1. **Bugs Caught vs. Time:** Steep slopes indicate high hunting efficiency.
 2. **Color Distribution:** This will show the shift in color traits due to selective pressures from hunting.
- Encourage students to reflect on how the bug population becomes better adapted to their environment over successive generations.

- After about 10 minutes, get them to pause (by pressing “Go”) and change the background picture.

3.6 Questions & Model Answers

1. What happens to the average color of the bug population with time as you hunt?

Over time, the average color of the bug population tends to shift towards colors that blend in better with the environment. As you hunt, bugs with less effective camouflage are caught more easily, while those that are harder to spot survive and pass on their traits to their offspring. This results in a gradual change in the population’s average color.

2. What happens to your hunting efficiency?

Initially, hunting efficiency is high, as the bugs are easy to spot. However, as the population evolves and the bugs’ colors become better camouflaged with the environment, hunting efficiency decreases. This reflects natural selection, where better-adapted individuals (bugs) are harder to catch.

3. Would you say that the bug population becomes worse or better adapted to their environment?

The bug population becomes better adapted to their environment. As selective pressure is applied (through predation), bugs with colors that offer better camouflage survive and reproduce, increasing the frequency of these adaptive traits in the population.

4. Can you explain how this happens?

This is a result of natural selection. Bugs with colors that provide better camouflage have a higher chance of survival because they are harder to detect by predators. These surviving bugs reproduce, passing on their coloration traits to their offspring. Over generations, the population’s coloration shifts to match the environment better, increasing the population’s overall fitness in that habitat.

5. After simulating in one environment (e.g. poppy field) for a few minutes, pause then switch to another environment. Are the bugs now well- or poorly-adapted to their new environment?

When the environment is changed, the bugs are usually poorly adapted to the new environment initially. The traits that made them well-camouflaged in the previous environment may now stand out, making them more visible to predators. This change highlights the importance of the environment in determining what traits are beneficial for survival.

6. Do the genotypes of individuals change (e.g., with individual age)?

No, the genotypes of individual bugs do not change as they age. The genotypes are fixed at birth and are inherited from their parents. However, the population’s genotype distribution can change over time due to natural selection favoring certain traits (such as better camouflage) and through mutations in the offspring.

7. Increasing the “max-mutation-step” makes bug offspring less like their parents. How do you think this will influence the speed of adaptation of the bugs?

Increasing the mutation step introduces greater genetic variability into the population. This can speed up adaptation by providing more opportunities for new beneficial traits to arise. However, it can also produce non-adaptive traits that may decrease the fitness of individuals. The overall effect on adaptation speed will depend on how many of the mutations are beneficial in the given environment.

3.7 Teaching Tips

- **Concept Reinforcement:** Frequently remind students of the evolutionary principles at play. Point out how the simulation reflects real-world dynamics, such as how organisms evolve to evade predators or increase predation efficiency.
- **Model Flexibility:** Depending on student progress, you may encourage them to modify other sliders (e.g., mutation rate) to explore more complex evolutionary dynamics.
- **Connecting Theory to Simulation:** Help students relate their observations in the simulation to theoretical principles, such as the definition of evolution as “change in heritable traits over generations.”

3.8 Common Pitfalls

- **Misinterpreting Graphs:** Students may struggle to understand the relationship between color changes and hunting efficiency. Emphasise that selection pressure favors bugs that are harder to see, and this trait is passed on to future generations.
- **Technical Issues with NetLogo:** Ensure students are comfortable with the UCloud setup or have downloaded NetLogo in advance.

3.9 Additional Resources

- Read more about the model here: [NetLogo Bug Hunt Camouflage](#).

Part II

Population Growth Models

Chapter 4

Geometric growth

4.1 Introduction

This exercise explores the geometric growth model in discrete time steps, focusing on how different values of λ affect population dynamics. It aims to develop students' understanding of growth models, the effects of log transformations, and the limitations of simple models.

4.2 Key Concepts

- Geometric growth assumes constant λ , leading to exponential growth or decline.
- Plotting log-transformed population sizes allows easier visualisation of trends.
- Limitations of the model include the assumption of infinite resources and lack of environmental constraints.

4.3 Learning outcomes

- Competence in using Excel formulae for mathematical modeling.
- Understanding the parameters of exponential/geometric growth.
- Competence in using mathematical models in Excel to strengthen own understanding of biological processes.
- Awareness of rearranging of mathematical formulae to produce different forms of models.
- Knowing that the slope of the $\ln(N_t)$ vs. t relationship can tell you about population growth rate (it is $\ln(\lambda)$).

4.4 Activity Overview

4.4.1 Time: 40-45 minutes

1. **Introduction (5 min):** Explain the activity, including the basic concepts of geometric growth
2. **Main Activity (25 min):** Students complete the Excel sheet and answer the questions provided.
3. **Discussion and Wrap-Up (5-10 min):** Run through the questions and discuss answers.

4.5 Instructions for Facilitating

4.5.1 Excel Setup

1. **Download File:** Ensure students have downloaded the provided Excel file `GeometricGrowth.xlsx`.
2. **Initial Setup:**
 - Start with an initial population size (N_0) of 10 and a growth rate (λ) of 1.1.
 - Use Excel formulas to calculate population size at each time step from $t = 1$ to $t = 20$.
 - Example formula: `=B8*F8`, where B8 is the population at time t and `F8` is the growth rate λ .
3. **Creating Charts:**
 - Plot the population size against time using an x-y scatterplot.
 - Create a second plot using the natural logarithm of population size ($\ln()$) on the y-axis.

4.5.2 Key Observations

- **Plot Comparison:** The linear plot will show exponential (curved) growth, while the log-transformed plot should display a straight line, where the slope represents $\ln(\lambda)$.
- **Altering λ :** As students experiment with different values for λ (e.g., 0.8, 1, 1.2), they will observe changes in the steepness of the population growth curve. A λ of 1 results in no population growth, while λ values below 1 indicate population decline.
- **Trendline Slope:** Adding a trendline to the log-transformed graph and determining its slope will give $\ln(\lambda)$. Students can use this slope to compute λ using the Excel function `EXP()`.

4.5.3 Geometric Series Calculation

- **Geometric Series Formula:** Introduce students to the geometric series formula, $N_t = N_0\lambda^t$. This formula provides a shortcut to calculate population size at any given time without stepping through each time point manually.
- **Application:** Use this formula to calculate population size for $t = 5$ and compare it to earlier manual calculations. Then extend it to predict population size after a large number of generations (e.g., $t = 900$).
- **Where does that equation come from?**

As a starting point, consider this equation: $N_{t+1} = \lambda N_t$.

If we want to calculate N_{t+2} , we would need to plug in N_{t+1} instead of N_t : $N_{t+2} = \lambda N_{t+1}$,

and, since we know that $N_{t+1} = \lambda N_t$, $N_{t+2} = \lambda\lambda N_t$.

Similarly, if we wanted to calculate N_{t+3} , we'd end up with: $N_{t+3} = \lambda\lambda\lambda N_t$.

This can be simplified by raising λ to a suitable power, and using the starting population at time = 0, N_0 :

eqn. 9. $N_t = \lambda^t N_0$.

This should be familiar to those of you that did (or remember!) the concept of geometric series which you have likely covered in earlier maths classes.

4.6 Questions & Model Answers

1. How does the population size change with time for different values of λ ?

The growth rate λ drives the population's exponential increase or decrease.

- For $\lambda > 1$, the population size increases exponentially.
- For $\lambda = 1$, the population size remains constant.
- For $\lambda < 1$, the population size decreases exponentially.

2. Why is it useful to plot log-transformed population size?

Log-transformations linearise exponential relationships. Therefore, the transformation converts the exponential growth trajectory into a straight line allowing for easier interpretation of the growth rate, as the slope corresponds to $\log(\lambda)$. You can get the λ value by taking the exponential of $\log(\lambda)$ (in Excel =EXP()).

3. What are the limitations of the geometric growth model? - The model assumes infinite resources, no competition, or environmental constraints, making it unrealistic for real-world populations. Real-world populations face density-dependent factors and environmental stochasticity, which the geometric model does not account for.

4. What would happen if we introduced a carrying capacity to this model? - The population would follow a logistic growth model, where growth slows as the population nears the carrying capacity.

4.7 Teaching Tips:

- **Reinforce Mathematical Understanding:** Emphasize how rearranging and transforming formulas, such as logarithmic transformations, are useful tools for interpreting population growth models.
- **Visual Learning:** Encourage students to compare the linear and log-transformed plots side by side to see how exponential growth behaves differently in each case.
- **Connect to Ecology:** When discussing real-world applications, introduce concepts like carrying capacity and logistic growth to contrast with geometric growth. -. **Model limitations:** Engage students in discussions about how the model could be adapted to account for real-world variables like environmental factors or density dependence.

4.8 Additional Resources

- **Excel Tutorial:** If students are unfamiliar with Excel's log transformation and trendline features, provide a walkthrough. They should use natural log (=LN).

Chapter 5

Estimating Population Growth Rate

5.1 Introduction

This exercise allows students to work with real population data to estimate the population growth rate (λ) by applying log transformation and linear regression in Excel. It reinforces concepts of geometric growth, exponential growth, and practical skills in data analysis using Excel. Students will learn how to interpret log-transformed data, calculate the growth rate, and understand model assumptions and real-world factors that may affect population growth.

5.2 Key Concepts

- **Exponential Growth:** Populations grow by a constant rate (λ) each time step, leading to exponential growth. Log-transforming the data linearizes this relationship.
- **Log Transformation:** Applying \log_e to population size makes it possible to fit a linear model to exponential growth data. The slope of this line gives $\log(\lambda)$, and exponentiating this value yields λ , the population growth rate.
- **Limitations of the Model:** The exercise uses a geometric growth model, which assumes a constant growth rate. Real-world populations often deviate from this due to environmental variability, competition, and other factors.

5.3 Learning outcomes

- Competence in using Excel formulae for data transformation and regression analysis.

- Understanding the role of λ in population growth and its estimation through log-transformed data.
- Competence in applying mathematical models in Excel to analyse real biological data.
- Awareness of how log transformations can linearise exponential growth data for easier interpretation.
- Knowing that the slope of the $\ln(N)$ vs. time relationship represents $\ln(\lambda)$ and can be used to estimate population growth rate.

5.4 Activity Overview

5.4.1 Time: 20 minutes

- 1-2 minutes: Introduce the exercise
- 2-3 minutes: Students read the exercise introduction and instructions.
- 10 minutes: Students do the exercise. Check on them as you walk around the class.
- 5 minutes: Wrap up and go through answers to questions.

5.5 Instructions for Facilitating

5.5.1 Step 1: Download and Open the Data

1. Ensure students download the provided Excel file **EstimatingGrowth.xlsx**.
2. Once students open the file, explain that the dataset contains population sizes recorded annually over 25 years.

5.5.2 Step 2: Plot the Population Size Over Time

- In Excel, have students create an x-y scatter plot of **population size** N_t against **time** (Year).
- Ensure students correctly label the axes and choose an appropriate chart type.

5.5.3 Step 3: Log-Transform the Population Size

1. Guide students to create a new column for the **natural logarithm** of the population size by using the Excel formula `=LN(cell)` where `cell` refers to the population size at a specific time step.
2. Students should then create a second scatter plot using the **log-transformed population size** on the y-axis and **time** on the x-axis.

5.5.4 Step 4: Fit a Linear Regression Model

1. In the log-transformed scatter plot, students will add a **linear trendline**.
 - Right-click on the data points and select “Add Trendline.”
 - Choose “Linear” and check the box for “Display Equation on Chart.”
2. Explain that the **slope** of the trendline represents $\log(\lambda)$.

5.5.5 Step 5: Calculate λ

- Once students have the slope from the trendline, they will calculate λ using the formula $\lambda = e^{\text{slope}}$, which can be done in Excel with the formula `=EXP(cell)`.

5.6 Questions & Model Answers

1. Interpret the Plot: What does the log-transformed plot of population size over time tell you about the population’s growth trend? Does the population appear to grow exponentially?

- The log-transformed plot should show a straight line if the population is growing exponentially, because the natural logarithm of an exponentially growing population will linearize the exponential curve. A positively sloped line indicates growth, a flat line suggests stability, and a negatively sloped line indicates population decline.

Estimate Growth Rate: What is the estimated population growth rate (λ) based on your linear regression analysis?

- The slope of the regression line from the log-transformed plot corresponds to $\log(\lambda)$. To find λ , students one can exponentiate the slope: $\lambda = e^{\text{slope}}$.
- Example: If the slope of the regression line is 0.086, then $\lambda = e^{0.086} \approx 1.09$, meaning the population grows by approximately 9% per year.

Model Assumptions: What assumptions does this model make about population growth? Discuss any potential real-world factors that might affect the accuracy of your estimate for λ .

- The model assumes that population growth follows a constant rate (λ) over time, without any external influences such as migration, resource limitations, or environmental changes. In the real world, population growth rates can fluctuate due to factors such as weather, food availability, disease, or human intervention.
- Other factors, like density dependence (competition for resources), may also affect the accuracy of the model. The geometric model does not account for a carrying capacity, which limits population growth in real ecosystems.

5.7 Teaching Tips:

1. **Ensure Students Understand Log Transformations:** Emphasize why log transformation linearises the exponential growth model, making it easier to interpret the population's growth trend. A short explanation of the mathematics behind this is helpful. Explain that exponential growth is linear in log space because $\log(N_t) = \log(N_0) + t \log(\lambda)$, which is analogous to the standard equation for a straight line $y = ax + b$.
2. **Excel Skills:** Ensure students know how to use Excel for log transformations (LN function), plot data, add trendlines, and display the regression equation on their charts. Consider providing a walkthrough if they are not familiar with Excel's plotting tools.
3. **Discuss Model Assumptions:** Encourage students to critically think about the assumptions behind geometric growth models. A good discussion could involve real-world examples where the assumptions break down, such as predator-prey dynamics, food shortages, or disease outbreaks.
4. **Data Quality and Measurement Error:** Highlight how measurement error or random fluctuations can influence data analysis. If measurement noise was introduced in the exercise, this can be a good opportunity to discuss the impact of imperfect data on the accuracy of the estimated growth rate.
5. **Comparing to Year-over-Year Estimates:** Have students compare the growth rate they estimate from the regression model to a simple year-over-year ratio estimate of population growth. Discuss why these values might differ, particularly in the presence of noise or irregularities in the data.

5.8 Common Pitfalls

- **Confusion with Log Transformation:** Students may not understand why log transformation creates a straight line from exponential data.
- **Exponentiating the Slope:** Remind students that the slope of the regression line represents $\log(\lambda)$, and they need to calculate $\lambda = e^{\text{slope}}$ to find the actual growth rate.
- **Interpreting λ :** Make sure students understand that $\lambda > 1$ indicates growth, $\lambda = 1$ indicates a stable population, and $\lambda < 1$ indicates population decline.

Chapter 6

Stochastic population growth

6.1 Introduction

This exercise introduces students to the stochastic version of population growth models, focusing on how randomness and variability can influence population dynamics over time. By working with both Excel and R, students will explore the differences between deterministic and stochastic population models, specifically applying them to geometric (discrete) growth models. The exercise allows students to build skills in mathematical modeling, data analysis, and stochastic simulation, all of which are essential for understanding real-world ecological systems and predicting population trajectories under uncertainty.

6.2 Key Concepts

- **Deterministic vs. Stochastic Models:**
Deterministic models assume a fixed growth rate, while stochastic models incorporate randomness, leading to more realistic projections.
- **Geometric Growth Model:**
The model is expressed as $N_{t+1} = \lambda N_t$, where $\lambda = e^{r_m}$ and $r_m = \ln(\lambda)$. It is used to predict population size in the next generation.
- **Stochasticity:**
Variability in growth rates, often modeled by drawing random values from a normal distribution for r_m . This randomness reflects environmental fluctuations and individual-level variation.
- **Extinction Risk:**
As stochasticity increases, populations are more likely to decline or go extinct. Extinction risk depends on factors such as variance in r_m , initial population size, and mean growth rate.

6.3 Learning Outcomes

- Understand and apply stochastic models to population dynamics.
 - Build competence in using Excel for mathematical modeling and simulations.
 - Grasp the relationship between stochasticity, extinction risk, and environmental variability.
 - Use R to simulate population growth and estimate extinction risk.
-

6.4 Activity Overview

Suggested Timings:

- **5 minutes:** Introduce the concept of stochastic population growth.
 - **5 minutes:** Students read through the background and instructions.
 - **20 minutes:** Students work on Excel-based deterministic and stochastic population growth modeling. Students with R experience may also explore stochastic simulations using R.
 - **10 minutes:** Wrap up discussion and review key takeaways.
-

6.5 Instructions for Facilitating

1. Introduction:

Briefly explain the difference between deterministic and stochastic models, focusing on why stochasticity is more reflective of real-world populations. Emphasize how the exercise will involve building models in Excel (and optionally R).

2. Excel Modeling:

Guide students through calculating deterministic population growth first, then introduce stochastic variation in growth rates by using the provided formula [English Excel: `=NORMINV(RAND(),F10,SQRT(F11))` / Danish Excel: `=NORMINV(SLUMP();F10;KVR0D(F11))`]. If you get errors, check whether Excel is expecting commas or semi-colons].

3. R Simulation:

For the R component, ensure students understand the basic structure of the code and how the simulation works. Encourage them to modify parameters like `mean.r` and `var.r` to observe different outcomes.

4. Discussion:

Facilitate a discussion on extinction risk, the impact of variability, and how different levels of stochasticity affect population trajectories.

6.6 Questions & Model Answers

1. What is the main difference between deterministic and stochastic population growth models? - Deterministic models use fixed growth rates, while stochastic models incorporate random variability, making them more realistic for representing natural populations.

2. Describe how incorporating randomness into the stochastic model makes it more realistic for understanding real-world populations. - Real-world populations face unpredictable environmental conditions and other factors that influence growth. Stochastic models account for these fluctuations, better mimicking actual population dynamics.

3. Simulate a scenario where two populations with identical growth rates experience different outcomes due to stochastic factors. Explain the implications of these findings. - Due to randomness, populations with the same initial conditions can diverge significantly over time. This demonstrates how chance events can lead to different outcomes, including extinction for one population and growth for another.

4. What can this stochastic model tell us about extinction risk and population size? - Smaller populations are more vulnerable to extinction in stochastic models because random negative growth events can have a greater impact.

5. What can this stochastic model tell us about extinction risk and environmental variation? - As environmental variability (represented by increased stochasticity) increases, populations face a higher risk of extinction due to more frequent poor years.

6.7 Teaching Tips

- **Stochasticity:**

Ensure students understand that stochasticity represents environmental and biological variability. Highlight how the normal distribution used to model r_m generates different growth rates across generations.

- **Excel Formulae:**

Some students may struggle with Excel formula syntax, particularly in different language settings. Double-check that students are using the correct formula (e.g., commas vs. semicolons).

- **R Simulations:**

Not all students may be familiar with R, so you may need to provide extra guidance on running the simulations and interpreting results.

- **Comparing Models:**

Emphasize the importance of comparing deterministic and stochastic models using visual charts. This comparison helps students see how randomness impacts long-term population trends.

6.8 Common Pitfalls

- **Formula Errors in Excel:**

Ensure students understand how to use the Excel function to generate stochastic r_m values. Remind them that Excel might expect different delimiters (commas or semicolons).

- **Misinterpreting Stochasticity:**

Students may confuse the effects of stochasticity with systematic trends. Clarify that stochasticity introduces random fluctuations that are just as likely to be negative as positive, not directional trends.

- **R Familiarity:**

If students are unfamiliar with R, they may find the simulation code challenging. Ensure they don't modify critical parts of the script unnecessarily.

““

Chapter 7

Basic logistic population growth

Coming soon. . .

Chapter 8

Deeper into logistic growth

Coming soon. . .

Chapter 9

Life tables and survivorship types

Coming soon. . .

Chapter 10

Matrix population modelling

Coming soon. . .

Chapter 11

Pre- and Post-reproduction census

Coming soon. . .

Chapter 12

Life Table Response Experiments

Coming soon. . .

Chapter 13

How many eggs should a bird lay?

Coming soon. . .

Chapter 14

Trade-offs and the declining force of selection

Coming soon. . .

Part III

Population Genetics and Evolution

Chapter 15

Hardy-Weinberg equilibrium

Coming soon. . .

Chapter 16

The Gene Pool Model

Coming soon...

Chapter 17

Neutral or Adaptive Evolution in Humans: What Drives Evolution of Our Traits?

Coming soon. . .

Chapter 18

Heritability from a linear regression

Coming soon. . .

Part IV

Interactions Between Species and Community Structure

Chapter 19

Lotka-Volterra competition

Coming soon. . .

Chapter 20

Lotka-Volterra predator-prey dynamics

Coming soon. . .

Part V

Animal behaviour, altruism and sexual selection

Chapter 21

Game theory: Hawks and doves

Coming soon. . .

Part VI

Appendix - extras

Chapter 22

Exponential growth in detail

Coming soon. . .

Chapter 23

The legend of Ambalapuzha

Coming soon. . .

Chapter 24

From population biology to fitness

Coming soon. . .