

# Are Uncertainty Capabilities of Evidential Deep Learning a Mirage?

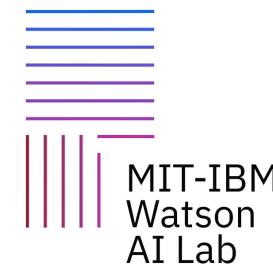
Maohao Shen<sup>1\*</sup>, J. Jon Ryu<sup>1\*</sup>, Soumya Ghosh<sup>2</sup>,

Yuheng Bu<sup>3</sup>, Prasanna Sattigeri<sup>2</sup>, Subhro Das<sup>2</sup>, Gregory W. Wornell<sup>1</sup>

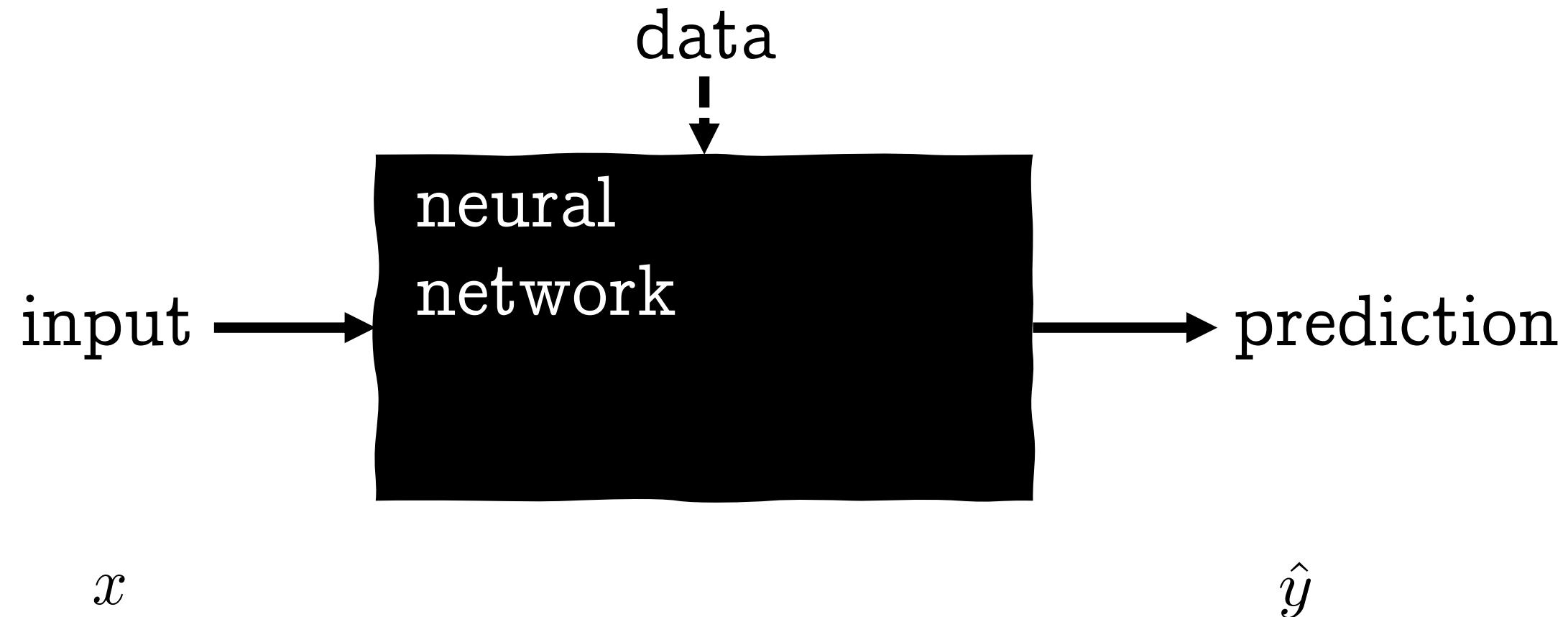
<sup>1</sup>MIT

<sup>2</sup>MIT-IBM Watson AI Lab, IBM Research

<sup>3</sup>University of Florida

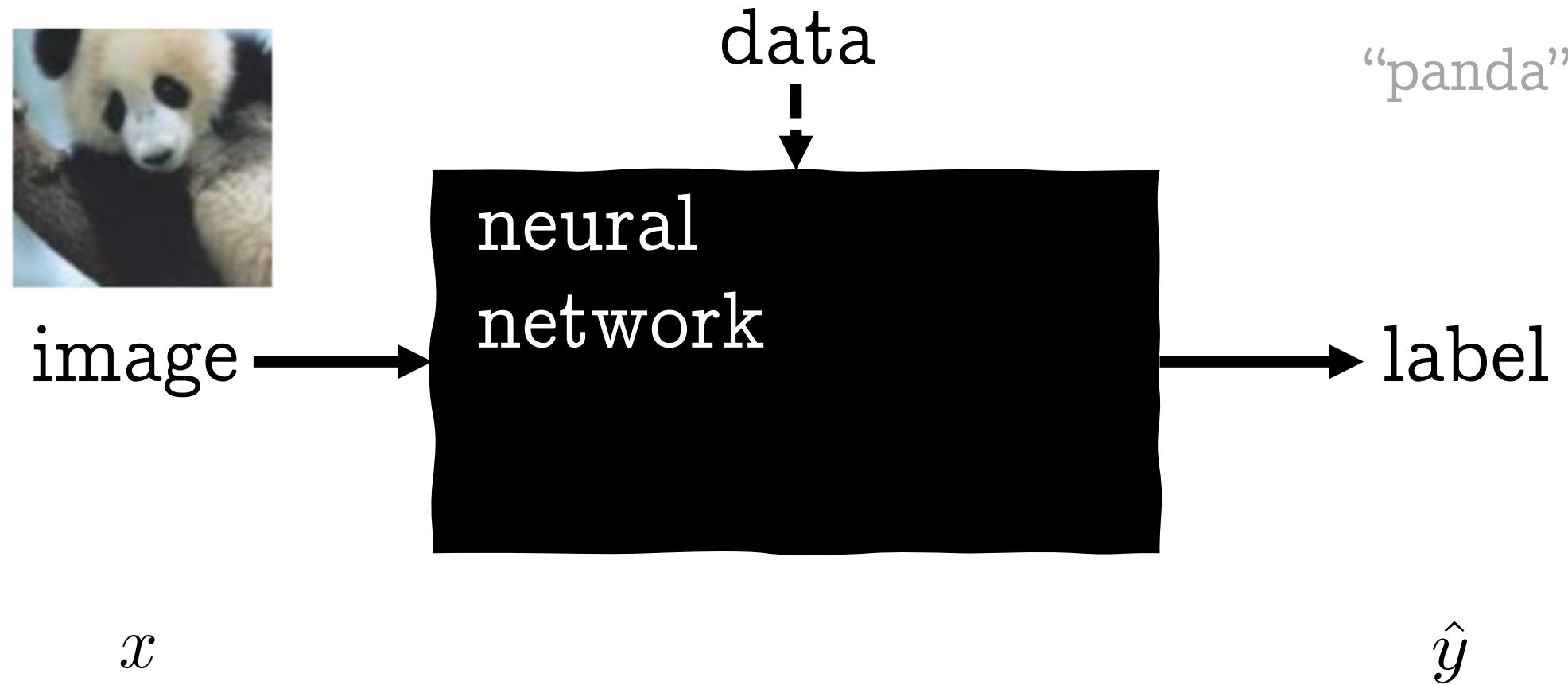


# Black-Box Prediction is Unreliable



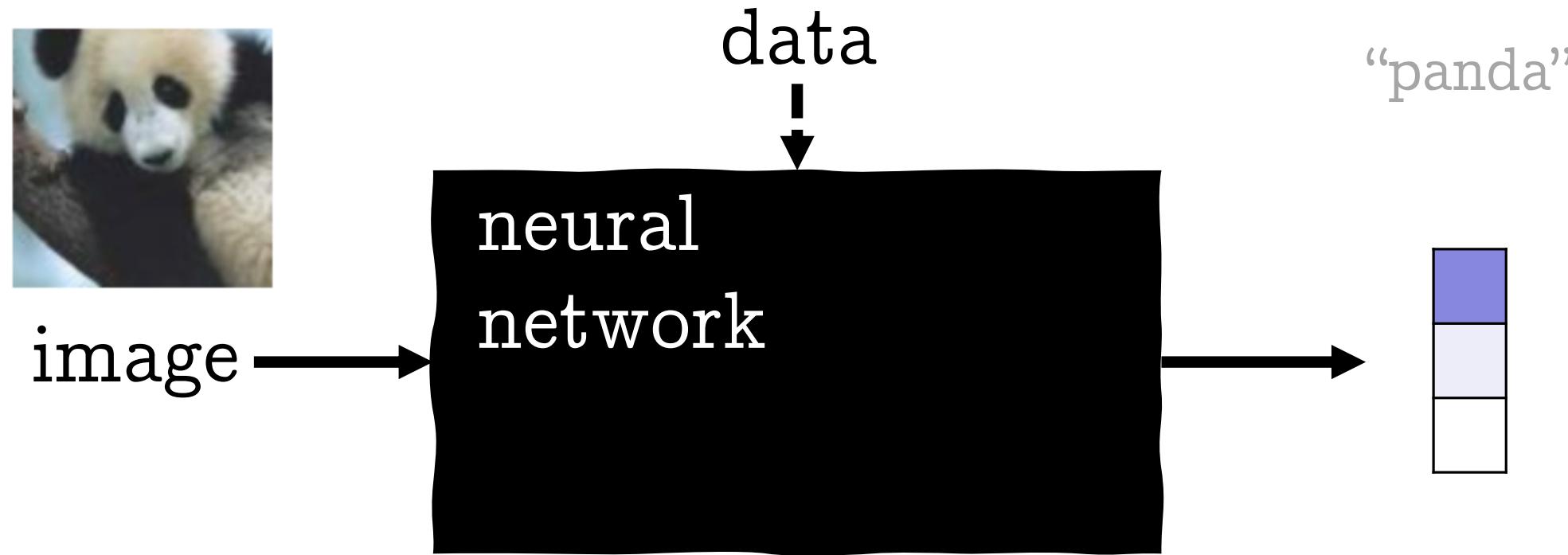
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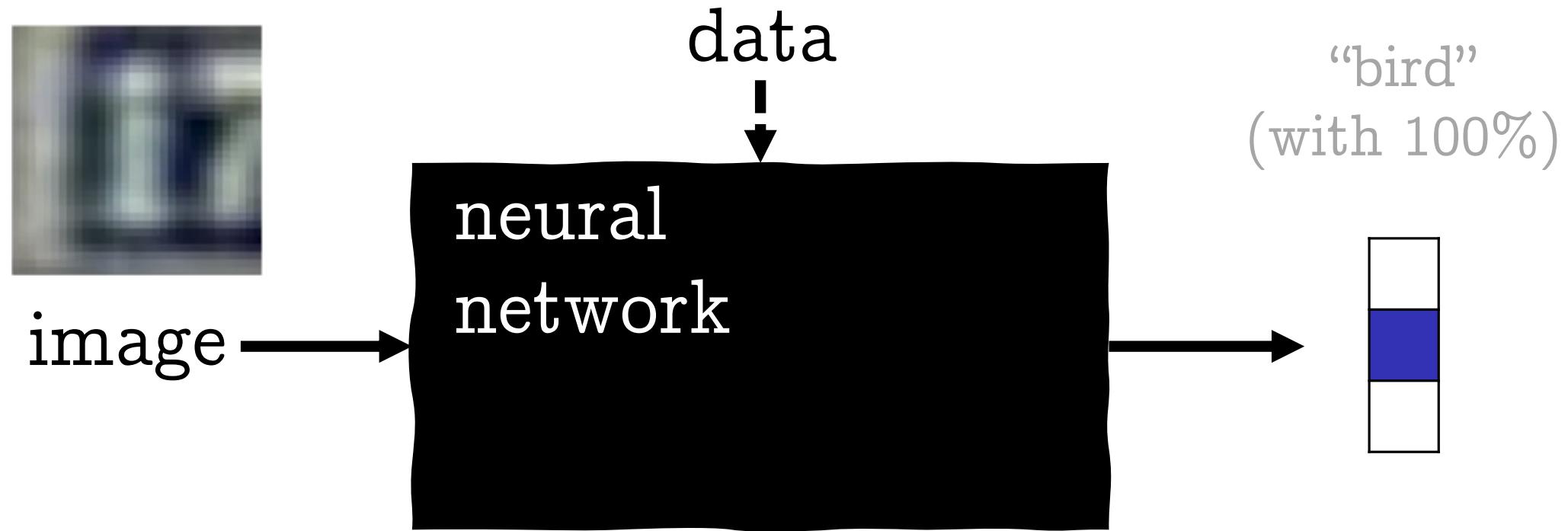


$x$

$$\pi_{\psi}(x) = (p_{\psi}(y|x))_{y=1}^C$$

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# Black-Box Prediction is Unreliable

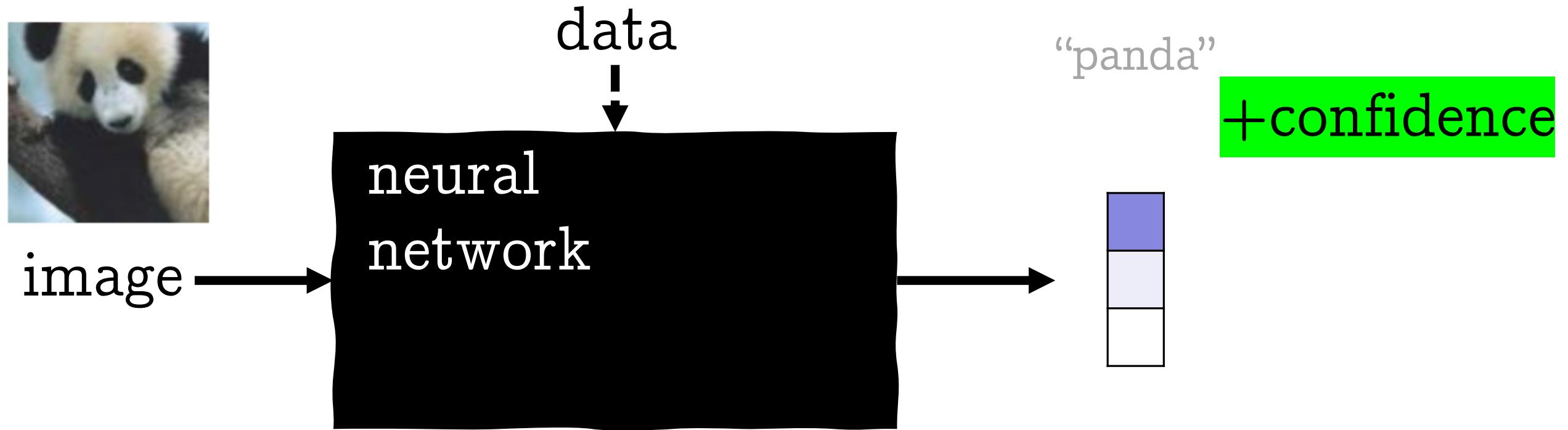


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$$\pi_{\psi}(x) = (p_{\psi}(y|x))_{y=1}^C$$

- Neural-network predictors are highly accurate...
- But often **overconfident** for out-of-distribution (OOD) data

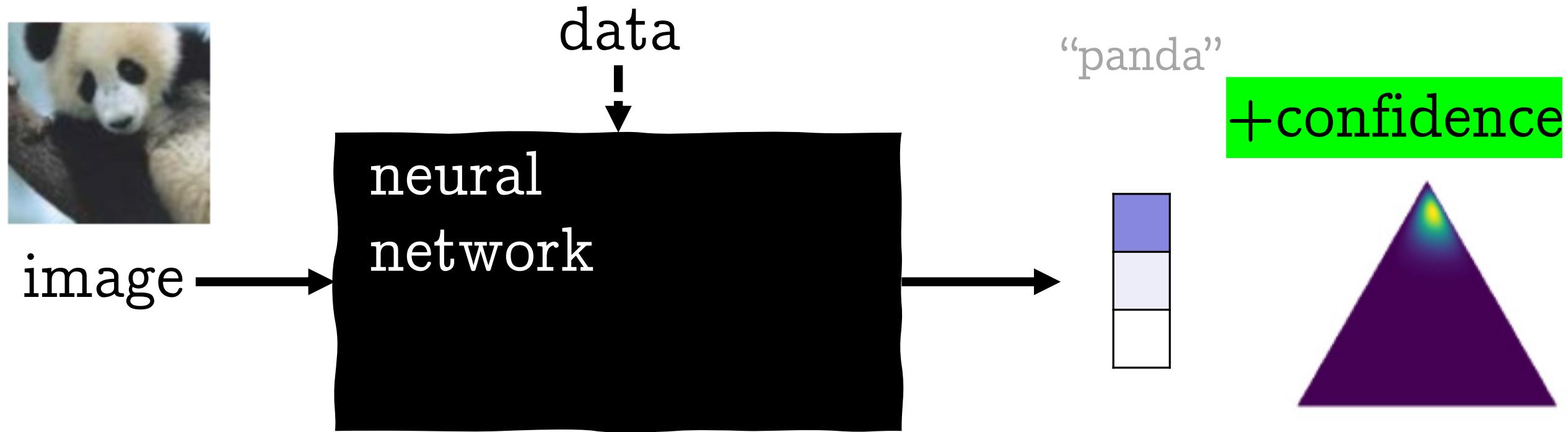
# We Need Uncertainty Quantification!



$x$

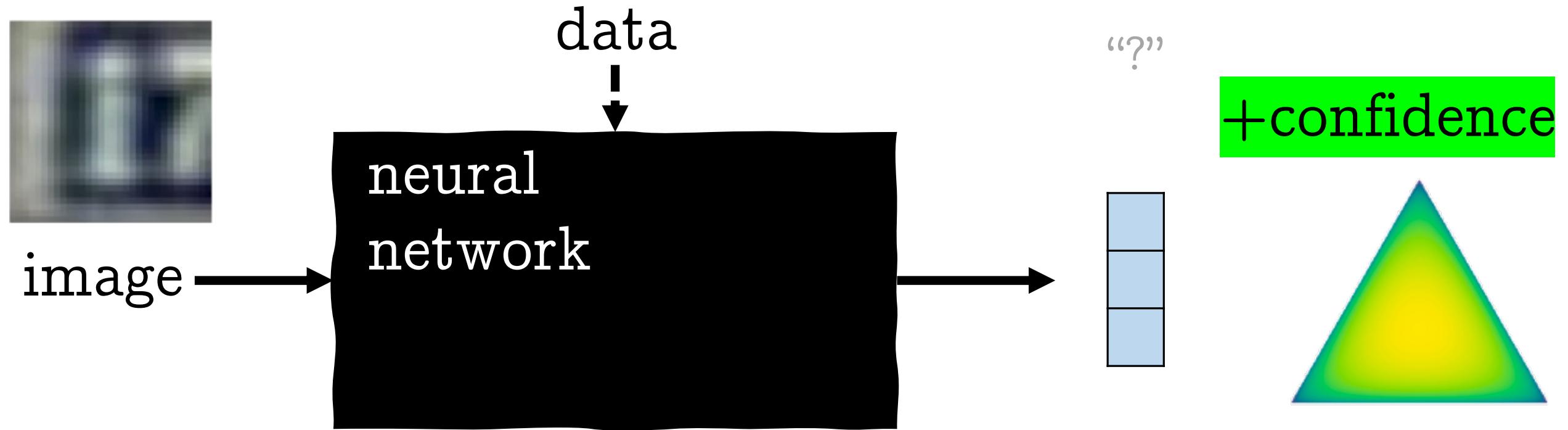
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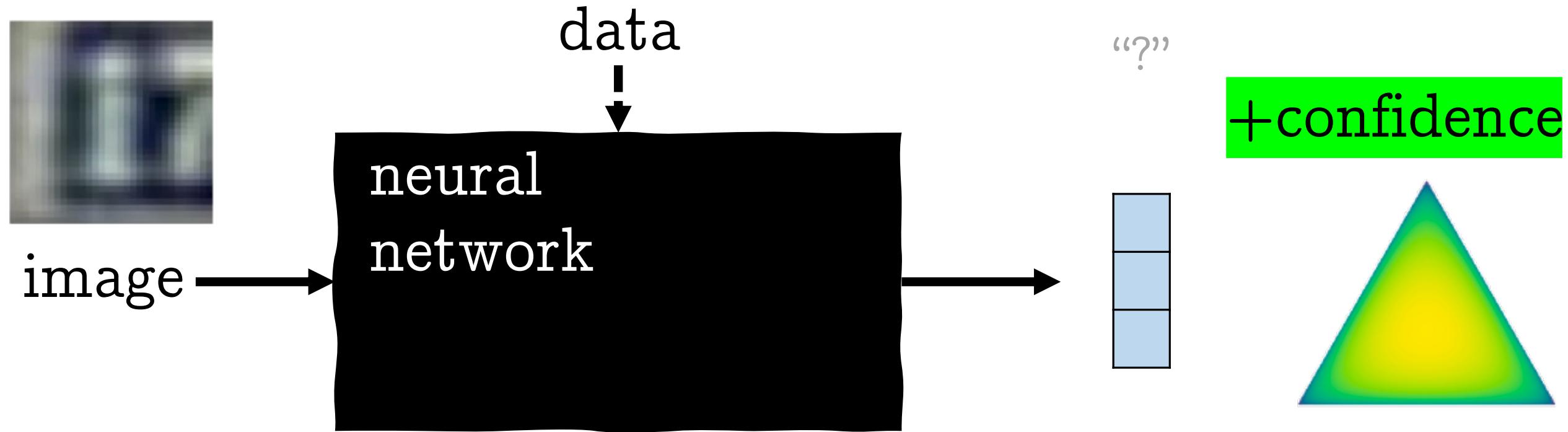
$$\pi_\psi(x) = (p_\psi(y|x))_{y=1}^C \ p_\psi(\pi|x)$$

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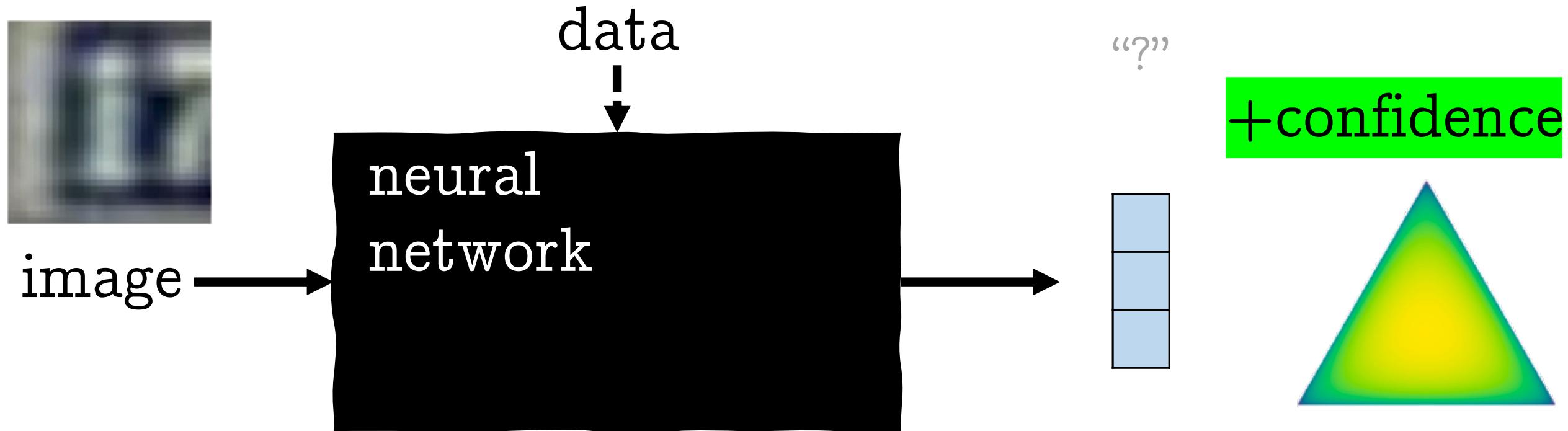
# We Need Uncertainty Quantification!



Different ways of inducing  $p_\psi(\pi|x)$

- Bayesian methods: variational inference, MCMC, Monte Carlo Dropout, ...
- Frequentist methods: jackknife, bootstrap, ...
- Ensemble methods

# We Need Uncertainty Quantification!



$x$

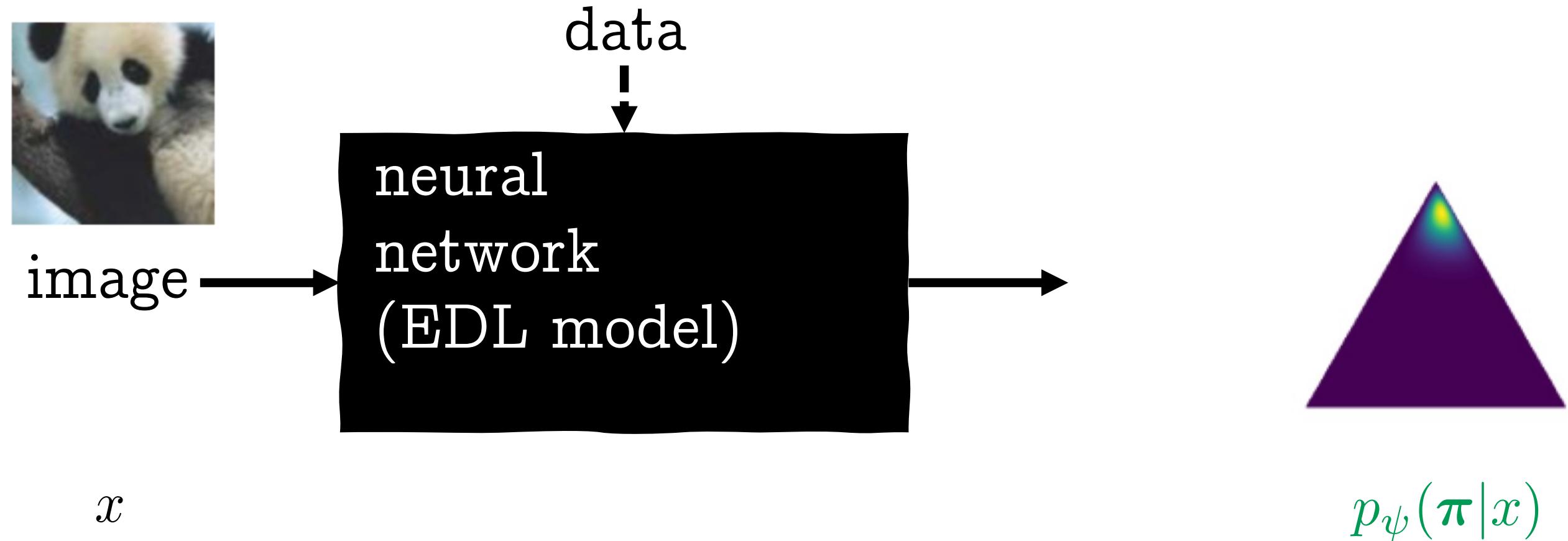
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- Bayesian methods: variational inference, MCMC, Monte Carlo Dropout, ...
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**Computationally Inefficient!**

# Evidential Deep Learning (EDL)



- Directly train a **single** neural network that outputs  $p_\psi(\pi|x)$
- Empirical successes for downstream tasks (e.g., OOD detection)
- Lack of theoretical understanding
- Recent works have reported spurious behaviors

# Demystifying EDL Methods

- Q1. What do EDL methods learn as **uncertainty**?
- Q2. **Why** are the EDL methods **successful**?
- Q3. How can we **make** EDL methods **more reliable**?

# Unifying EDL Objectives: A New Taxonomy

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## Method (name of loss)

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FPriorNet (F-KL loss) [7]

RPriorNet (R-KL loss) [8]

EDL (MSE loss) [10]

Belief Matching (VI loss) [12, 13]

PostNet (UCE loss) [15]

NatPN (UCE loss) [20]

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What's the common principle  
behind all these objectives?

$$\mathcal{L}(\psi) := \mathbb{E}_{p(x,y)}[D(p^{(\nu)}(\pi|y), p_\psi(\pi|x))] + \gamma_{\text{ood}} \mathbb{E}_{p_{\text{ood}}(x)}[D(p(\pi), p_\psi(\pi|x))]$$

“fixed”  
uncertainty target

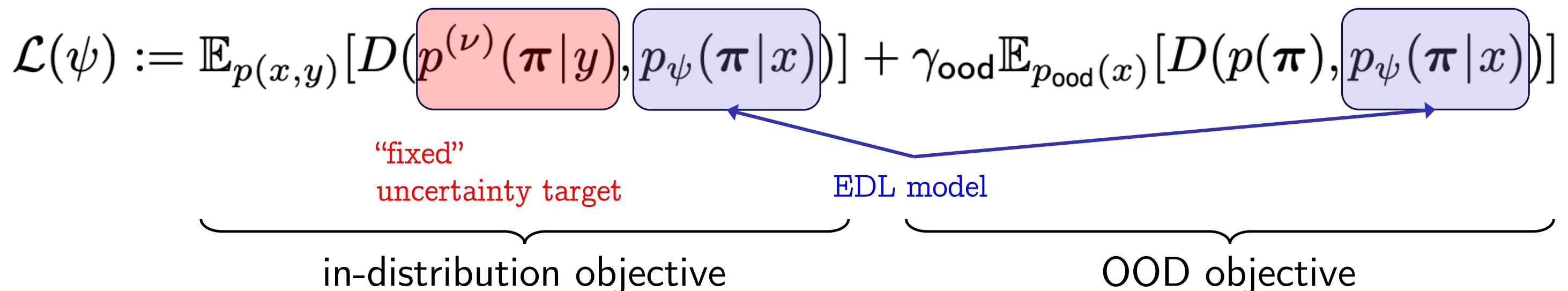
EDL model

in-distribution objective      OOD objective

The diagram illustrates the decomposition of the EDL loss function. The total loss  $\mathcal{L}(\psi)$  is the sum of two terms. The first term,  $\mathbb{E}_{p(x,y)}[D(p^{(\nu)}(\pi|y), p_\psi(\pi|x))]$ , is highlighted with a red box and labeled "fixed uncertainty target". The second term,  $\gamma_{\text{ood}} \mathbb{E}_{p_{\text{ood}}(x)}[D(p(\pi), p_\psi(\pi|x))]$ , is highlighted with a blue box and labeled "EDL model". Brackets below the terms group them into "in-distribution objective" and "OOD objective". Arrows point from the labels "fixed uncertainty target" and "EDL model" to their respective highlighted terms.

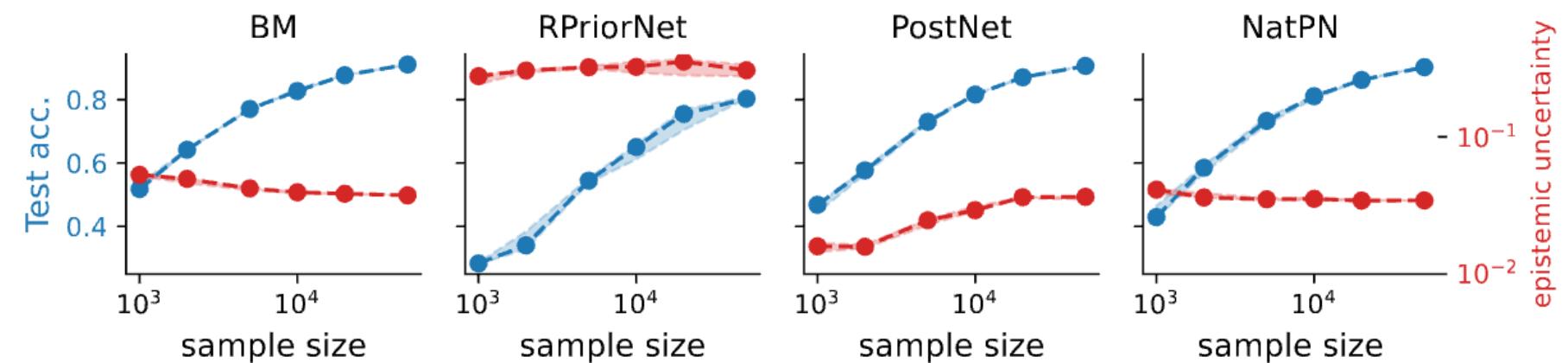
# Unifying EDL Objectives: A New Taxonomy

Method (name of loss)	likelihood	$D(\cdot, \cdot)$	prior $\alpha_0$	$\gamma_{\text{ood}}$	$\alpha_\psi(x)$ parameterization
FPriorNet (F-KL loss) [7]	categorical	fwd. KL	$= \mathbf{1}_C$	$> 0$	direct
RPriorNet (R-KL loss) [8]	categorical	rev. KL	$= \mathbf{1}_C$	$> 0$	direct
EDL (MSE loss) [10]	Gaussian	rev. KL	$= \mathbf{1}_C$	$= 0$	direct
Belief Matching (VI loss) [12, 13]	categorical	rev. KL	$\in \mathbb{R}_{>0}^C$	$= 0$	direct
PostNet (UCE loss) [15]	categorical	rev. KL	$= \mathbf{1}_C$	$= 0$	density w/ single flow
NatPN (UCE loss) [20]	categorical	rev. KL	$= \mathbf{1}_C$	$= 0$	density w/ multiple flows



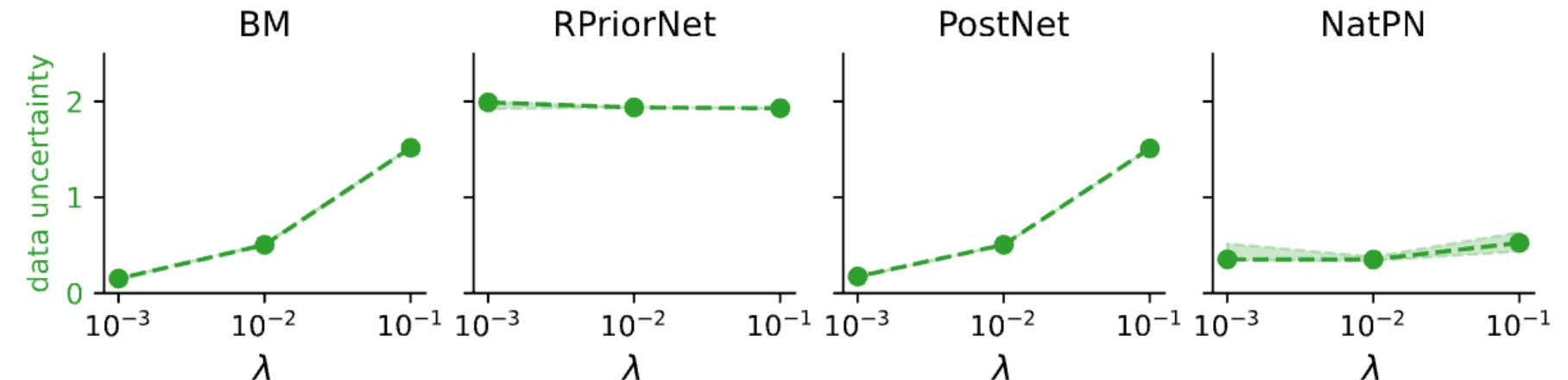
# Explain Spurious Behaviors of Learned Uncertainties

Non-vanishing  
learned epistemic uncertainty



(a) Epistemic Uncertainty: CIFAR10

Hyperparameter sensitive  
learned aleatoric uncertainty



(b) Aleatoric Uncertainty: CIFAR10

# Explain Success of EDL Methods

$$\mathcal{L}(\psi) := \mathbb{E}_{p(x,y)}[D(p^{(\nu)}(\boldsymbol{\pi}|y), p_\psi(\boldsymbol{\pi}|x))] + \gamma_{\text{ood}} \mathbb{E}_{p_{\text{ood}}(x)}[D(p(\boldsymbol{\pi}), p_\psi(\boldsymbol{\pi}|x))]$$

“fixed”  
uncertainty target

EDL model

in-distribution objective

OOD objective



$$-\mathbb{E}_{p(x,y)}[\log p_\psi(y|x)] + \tau \left\{ \mathbb{E}_{p(x)}[\max(0, E_\phi(x) - m_{\text{id}})^2] + \mathbb{E}_{p_{\text{ood}}(x)}[\max(0, m_{\text{ood}} - E_\phi(x))^2] \right\},$$

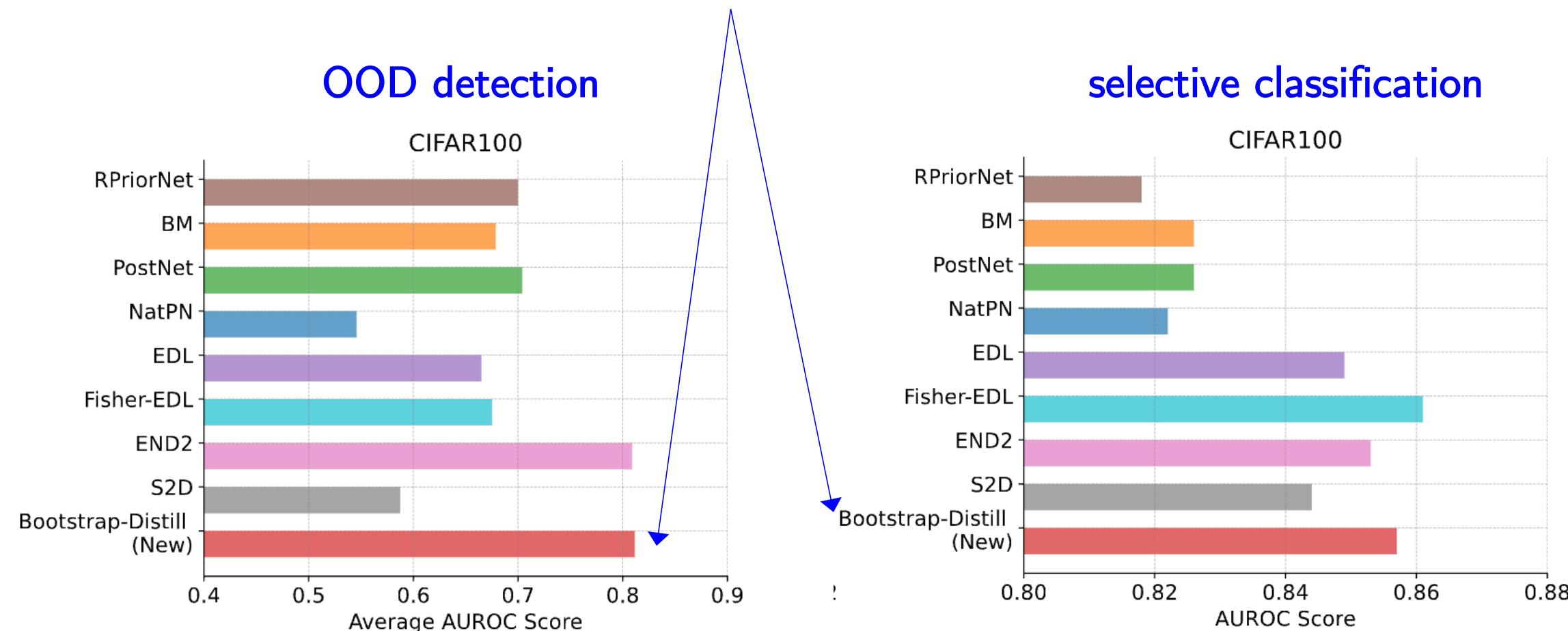
in-distribution objective

OOD objective

- EDL methods can be better understood as **EBM-based OOD detector**

# How to Improve EDL?

- All the issues of EDL arise from **the ignorance of model stochasticity**
- **Conjecture:** Incorporating external stochasticity is the key for meaningful UQ and EDL should be used for “distillation” for fast inference
- Show **distilling** randomness in **Bootstrap** can achieve SOTA performance



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