

# A Novel Filtering Approach for Robust and Fast Keypoint Matching in Mobile Environment

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**Abstract**—The abstract goes here.

**Index Terms**—IEEEtran, journal, LATEX, paper, template.

## I. INTRODUCTION

IMAGE matching is at the core of many interesting computer vision applications including simultaneous localization and mapping [1], [2], object recognition [3], panorama stitching [4], [5], augmented reality [6], [7], and visual odometry [8], [9]. To resolve this problem, there are several techniques researched. Interest point recognition is a key technique to resolve the problem, because it can provide robust matching quality against occlusion or transformation.

This interest point recognition works as shown in fig. 1. 사전에 오프라인 학습 단계에서 미리 학습 영상을 분석하여 데이터베이스를 생성하고, 이를 이용하여 온라인 인식 단계에서 입력된 영상을 데이터베이스와 비교하여 가장 근접한 결과를 검색한다. 이 때 각 단계는, detection, description, matching의 세 가지 단계를 통하여 수행된다. 먼저, 인식의 대상이 되는 train object(reference object)를 분석하여 keypoint database를 만들게 된다. 이를 위하여 train object image에서 검출이 잘 되는 점들을 detect 한다. 이렇게 검출된 특징점들에서 local texture 특징을 이용하여 descriptor를 생성한다. 이 단계에서는 rotation, scale, perspective transform 등 다양한 변환에 강인하게 매칭이 수행될 수 있도록 descriptor를 계산한다. 이렇게 계산된 descriptor 집합을 online matching 과정에서 효율적으로 matching이 이루어질 수 있도록 tree나 hashing과 같은 efficient matching structure를 만들어 database로 저장한다. 이후 이렇게 만들어진 database를 이용하여 online matching 과정에서는 입력된 query 영상에서 corresponding keypoint pair를 찾게 된다. 이를 위하여 입력된 query 영상에서 특징점을 검출하고, 검출된 특징점의 descriptor를 생성하여 database에 저장된 descriptor와 가장 유사한 특징점을 계산한다.

본 논문에서는 database에 저장되는 keypoint들을 평가하여 matching 성능이 높은 점들만 filtering하여 저장함으로써 matching 성능을 향상시키고 빠른 인식 성능을 제공하는 방법을 제안한다. 기존의 특징점 매칭 방법에서는 일반적으로 keypoint detection process에서 geometrical 특성에 의하여 저장하고자 하는 특징점들을 filter하였다. 하지만, 특징점 검출 단계는 영상 변환에도 반복적으로 강인하게 특징점이 검출되는 것을 목표로 설계되었다. 따라서 이렇게 검출된 특징점은 이후의 매칭 단계와는 독립적인 연산이 수행되고, 이에

따라 매칭 퀄리티를 보장할 수 없는 문제가 있다. 이에 따라, 특정 특징점들은 distinguishability가 떨어지는 점들이 학습되는 경우가 많고, 이러한 점들은 miss matching을 유발하여 인식의 정확도를 떨어뜨리게 된다. (bad keypoint 이미지 추가) 또한, 이러한 점들이 포함된 database는 비교 대상이 되는 특징점의 개수가 증가되므로 인식의 속도 또한 저하시키게 된다. 본 논문에서는 이러한 문제점을 극복하기 위하여 오프라인 학습 단계에서 검출된 특징점의 매칭 성능을 평가하고, 이 평가에 의하여 특징점을 필터링하는 기법을 제안한다. 이를 통하여 매칭 품질이 높은 특징점만을 저장하고 비교함으로써, 강인한 인식 성능을 제공하면서도 인식의 속도를 향상시킬 수 있는 방법을 제안한다.

이후의 논문은 다음과 같이 구성된다. 먼저 2장에서는 기존의 특징점 기반 매칭 연구들을 정리하고, 이러한 연구 중 기존의 특징점 필터 방법을 설명한다. 3장에서는 제안하는 keypoint score function을 정의하고, 이를 ground truth와 비교하여 유사도를 보여준다. 그리고 이렇게 측정된, 매칭에 유리한 특징점과 그렇지 않은 특징점을 영상 패치로 비교하여 어떤 특징점들이 매칭에 유리한지 설명한다. 이후 4장에서는 다양한 환경에서 실험을 수행하고, 제안하는 방법과 기존의 일반적인 database 방식의 속도 및 인식율, 특징점의 매치 정확도를 비교한다. 이후 5장에서 본론을 정리한다.

## II. RELATED WORKS

### A. Interest Point Detectors

1) *Geometry based Detectors*: 영상에서 다양한 방향에서의 gradient의 변화량을 측정함으로써 corner, edge, region을 구분하는 방법을 통하여 Interest Point를 검출하는 방법들이 제안되었다. 이러한 방법은 Repeatability가 높은 점을 검출할

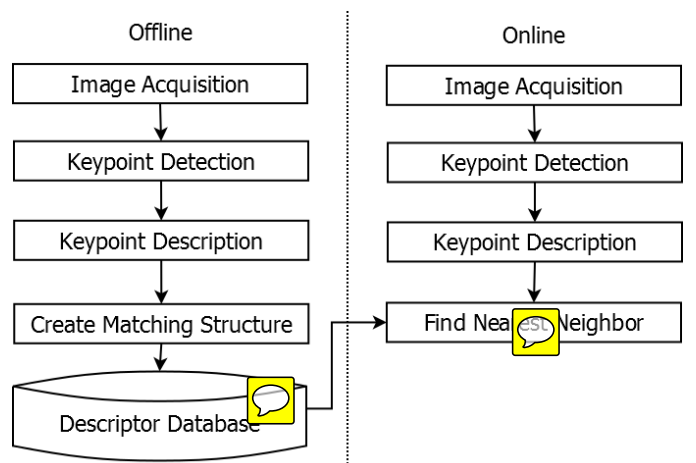


Fig. 1. Process of Feature Matching

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수 있다는 장점이 있으나, Image derivation이 필요하여 연산량이 높고, 노이즈에 취약하다는 한계가 있었다. 가장 먼저 Harris and Stephan [10] 은 SSD의 Hessian Matrix를 계산하고, 이 행렬을 eigen decomposition 하여 corner, edge, flat을 판별하였다. 이러한 연산을 전체 영상에 걸쳐 sliding window 방식으로 연산하여야 하기 때문에 연산량이 높은 문제가 존재하였다. Mikolajczyk and Schmid

2) *Template based Detectors*: 많은 연산량을 필요로 하는 Geometry based Detector 를 대신하여 영상에서 간단한 연산만으로 특징점을 검출할 수 있는 Template based Detector 들이 개발되고 있다. 가장 먼저

## B. Keypoint Descriptors

1) *Vector-Value based Descriptors*: 기존의 SIFT [11]나 SURF [12]와 같은 vector value-based description 방법은 높은 인식율을 제공해 주었지만, orientation과 scale 등의 distortion에 robust한 descriptor를 생성하기 위하여 복잡한 연산을 수행하여야 하기 때문에 연산이 복잡하게 수행되었다.

2) *Binary-Value based Descriptors*: 최근에는 BRIEF [13], ORB [14], BRISK [15], FREAK [16]과 같은 다양한 Binary value-based descriptor들이 개발되고 있다. 이러한 Binary descriptor들은 그림 ??와 같이 특징점을 중심으로 다양한 형태의 패턴을 이용하여 두 점 사이의 밝기 값을 비교하여 binary code로 표현하는 방법이다. 단순 비교 연산만으로 descriptor를 계산하기 때문에 vector-based descriptor에 비하여 연산 속도가 상당히 빠르며, 최근에는 생성 패턴을 기준으로 orientation이나 scale 등을 normalize 하기 때문에 다양한 distortion에서도 상당히 강인한 성능을 보여주고 있다. 특히 smart space와 같이 제한된 성능의 환경에서는 vector-value descriptor 기반의 복잡한 연산 보다는 단순 비교연산만으로도 처리가 가능한 binary descriptor를 사용하는 연구가 많아지고 있다.

## C. Keypoint Matching

다음 방법은 matching data structure를 효율적으로 설계하여 nearest neighbor match를 빠르게 수행하도록 하고 있다. 기존의 brute force matching 방법은 query image의 모든 keypoint들을 reference image의 모든 keypoint들과 비교하는 방식으로 가장 속도가 오래 걸리지만, 가장 정확한 nearest neighbor를 검출할 수 있다는 장점이 있다.

1) *Partitioning Trees*: [17]에서는 kD tree 기반의 approximation 방법이 제안되었다. 이 방법은 특징의 차원이 비교적 적은 SIFT나 SURF와 같은 vector-value description 방식에서는 좋은 성능을 보여주지만, 최근에 사용되는 binary descriptor에서는 dimension이 높아 성능향상을 기대하기 어렵다는 문제가 있다. 또한, Random Forest [18] 또는 Random Fern [19]은 Binary Description 방식을 Tree 구조 또는 List 구조에 적용하여 matching structure를 구성하였다. 이러한 매칭 방식들은 인식의 속도를 향상시키고, 좀 더 정확한 approximation 값을 얻기 위하여 일반적으로 offline training 단계에서 계산된 descriptor들을 이용하여 추가의 연산을 적용하여 효율적인 matching structure를 생성한다. 하지만, 이러한 방법들을 사용한 추가적인 구조체가 상당히 복잡하고 용량이 크기 때문에 모바일 환경에서 사용하기에 매칭 구조체가 과도하게 무거워진다는 문제점이 존재한다.

2) *Hashing*: 가장 많이 알려진 Hashing 기반의 Nearest Neighbor 검색 기법은 Locality Sensitive Hashing [20]이다. 이 방법은 많은 수의 해쉬 함수를 이용하여 특징점을 저장하고, 같은 bucket에 저장된 특징점에 한하여 Linear Search를 수행하기 때문에 비교 연산의 횟수를  $O(N)$ 에서  $O(k)$ 로 감소시키는 장점이 있다. LSH [21]와 같은 Hashing 기반의 structure를 이용하여 matching 을 가속화하는 방법도 제안되었다 [14]. 이러한 방법은 offline training 단계에서 적절히 특징점들이 고르게 분포하도록 적절한 hash function set을 구성하는 것이 중요하다.

3) *Nearest Neighbor Graph Techniques*:

4) *Automatic Configuration of NN Algorithms*:

## D. Keypoint Filtering

학습 과정에서 특징점을 평가하여 저장하는 특징점 필터링 방식은 활발하게 연구되지는 않았다. 이러한 기법은 일반적으로 특징점 검출 알고리즘에서 수행되었다.

1) *Thresholding*: Harris score 나 Hessian score 등을 이용하여 특징점의 강인한 검출 정도를 측정하여 필터하는 방법이 사용되었다.

2) *Non-maximum Suppression*: Spatial relation을 고려하여 non-maximum suppression이 수행되었다.

3) *Distinctiveness*: 특징점의 distinctiveness를 고려한 필터방법이 몇가지 제안되었다.

## III. PROPOSED METHOD

본 논문에서는 matching quality 를 기준으로 detected keypoint 를 evaluate하여 filtering하는 방법을 제안한다. 이를 통하여 matching quality가 높은 점들만을 학습함으로써 online matching 과정에서 높은 matching preciseness와 빠른 속도를 얻을 수 있다. 본 장에서는 matching quality 에 따라서 keypoint를 evaluation 하기 위한 criteria 를 정의하고, ground truth data 를 기준으로 이러한 criteria 가 동작됨을 증명한다. 또한, 이러한 기준에 의하여 분류된 keypoint 들의 image patch 를 비교하여 matching에 좋은 특징점과 그렇지 않은 특징점의 xxx 측면에서의 차이점을 비교하였다.

### A. Assumption

### B. Keypoint Score Function

~~Feature matching based augmented reality system generates the feature database, the subjects of comparison, by way of the offline training of the reference images before online process. In particular, as shown in the foregoing study of matching data structure, a method that composes a matching structure by applying a various computations to offline process to increase the online recognition speed and recognition rate is proposed.~~ Such established keypoints matching methods ~~used simply~~ all of the keypoints detected in feature detection module for training. However, since the feature detection algorithm is performed independently from the description algorithm, the descriptor is not able to ensue the matching performance for the detected feature.

Thus, in this paper, the keypoints of the subjects of training in the offline training process were assessed ~~and only the keypoints providing rigid real-time recognition performance were selected. As a result, a method to increase the recognition speed by saving these features only while maintaining the quality of recognition was proposed.~~

TABLE I  
KEYPOINTBASED IMAGE MATCHING SYSTEMS

Reference	Detector	Descriptor	Matching
Bleser and Stricker (2008) [22]	FAST	patch, warped	
Carrera et al. (2007) [23]	Harris	SURF	
Chekhlov et al. (2007) [24]	Shi-Tomasi	SIFT-like	
Cheng et al. (2006) [8]	Harris	patch	
Davison et al. (2007) [2]	Shi-Tomasi	patch, warped	
DiVerdi et al. (2008) [25]	Shi-Tomasi	Optical flow & SURF	
Eade and Drummond (2006) [26]	FAST	patch, warped	
Klein and Murray (2007) [6]	FAST	patch, warped	
Lee and Höllerer (2008) [27]	DoG	Optical flow & SIFT	
Lepetit and Fua (2006) [18]		Randomized Trees	Randomized Trees
Muja and Lowe (2012) [28]	DoG	SIFT	FLANN
Nistér et al. (2004) [9]	Harris	patch	
Özuysal et al. (2007) [29]		Ferns	Ferns
Park et al. (2008) [30]		Ferns	Ferns
Se et al. (2002) [31]	DoG	scale, orientation	
Skrypnik and Lowe (2004) [32]	DoG	SIFT	kD Tree
Taylor et al. (2009) [33]	FAST	trained histograms	
Wagner et al. (2009) [34]	FAST	patch & reduced SIFT	
Wagner et al. (2010) [5]	FAST	patch, warped	
Williams et al. (2007) [35]	FAST	Randomized lists	

1) *Definition of Good Keypoints:* The proposed method filters only good keypoints by analyzing the detected keypoints and measuring the degree of the effectiveness of them on recognition. To this effect, good keypoints were defined.

The conditions of good keypoints for recognition are as follows:

First, good keypoints need to be stably detected as good points in an environment where targeted images change in various ways. In fact, a wide range of form transformation, such as the rotation, size, perspective, noise and lighting of the targeted images, are applied to the camera images used in the actual matching process. The good keypoints for recognition are detected stably in the converted images, generating descriptors.

The detection of stable keypoints can be measured by *Repeatability* condition. *Repeatability* is calculated by the ratio between the total number of converted images and the number of cases where the converted keypoints are existent in the converted images.

$$Prepeatability(p_i) = \frac{n_i^{overlap}}{N} \quad (1)$$

where  $n_i^{overlap}$  is calculated by the frequency of the existence of converted keypoint( $p_i$ ) in the set of keypoints( $T(p_i) \in K'_t$ ) of converted images  $T_t(I)$ ;  $N$  is the total number of converted images; and all keypoints have single value.

Second, Good keypoints need to be well-matched with identical keypoints even though targeted images change in various ways(*Similarity* condition). With regard to a certain keypoint( $p_i$ ) of reference images, genuine distribution' and imposter distribution' for the corresponding keypoint can be measured by calculating the matching between the descriptors of all the sets of keypoints( $p_i$ ) in images( $T_t(I)$ ) converted in various ways during the training process. At this time, to reduce the failure in matching the corresponding keypoints and the descriptors in the converted images, the genuine distribution needs to have small value, being far enough away

from match distance threshold. To this effect, it was measured using the mean of genuine distribution. As shown in Equation (2), the keypoints with the decreasing the genuine distribution are better, so the evaluation function was calculated by normalizing the mean of the genuine distribution and subtracting its value from 1.

$$p_{similarity}(p_i) = 1 - \frac{\mu_{gen,i} - \min_i \mu_{gen,i}}{\max_i \mu_{gen,i} - \min_i \mu_{gen,i}} \quad (2)$$

Third, the trained keypoints and other keypoints shall not be matched(*Separability*), which is associated with the imposter distribution of each keypoint. Of the keypoints extracted from the images converted in various images, the distribution of the matching with other keypoints rather than the converted keypoints themselves are referred to as imposter distribution. Thus for a specific keypoint to show the low success rate of matching with other keypoints rather than themselves, it is necessary that the genuine distribution and imposter distribution are well classified. To this effect, in this paper, *Fisher's Discriminant Ratio* [36] was used. It measures the distance between two classes by the mean and distribution of sample in 1-dimensional, two class problems. Since the second Similarity condition ensures the genuine distribution is small enough, the nonexistence of the matching with the keypoints in the imposter distribution is ensured if the importer distribution is far enough away compared with the genuine distribution. Separability value also requires the normalization process as shown in equation (4).

$$FDR(p_i) = \frac{(\mu_{gen,i} - \mu_{imp,i})^2}{\sigma_{gen,i}^2 + \sigma_{imp,i}^2} \quad (3)$$

$$p_{separability}(p_i) = \frac{FDR(p_i) - \min_i FDR(p_i)}{\max_i s_i} \quad (4)$$

The score functions of each keypoint can be defined using 3 criteria calculated as above. The 3 conditions are dependent, so can be defined as shown in Equation (5).



$$gf(p_i) = Prepeatability(p_i)Psimilarity(p_i)Pseparability(p_i) \quad (5)$$

### C. Proof of Criteria

1) *Validation Design*: To validate the proposed keypoint evaluation criteria, we examined a relationship between criteria and correct matching count of each keypoints. At first, to provide robust image matching, we synthesized image dataset by various image transformation. Then, based on this dataset, we counted correct matching count for each keypoint, and this correct matching count is a basis of matching quality. 이러한 correct matching count가 높은 특징점은 fixed image dataset에서 더 높은 matching quality를 보여준다고 볼 수 있기 때문에 본 논문에서 제안하는 Matching에 더 적합한 keypoint로 볼 수 있다. 반대로 correct matching count가 낮은 특징점은 특징점이 반복적으로 검출되지 않거나, 모호성이 높아 inter-keypoint miss-match가 많이 발생하는 특징점으로 matching에 적합하지 못한 keypoint로 볼 수 있다. 따라서, 이러한 correct match count와 제안하는 keypoint evaluation score function (see, Eq. 5) 간의 상관관계를 관찰함으로써 제안하는 score function의 적절성을 검증할 수 있다.

2) *Dataset*: 검증에 사용된 이미지는 서울 관광 가이드북 [37]의 *Seoul Tour Map* 16장을 사용하였다. 우리는 이러한 이미지를 대상으로 rotate(0.5 – 2.0-folds, at the interval of 0.1-fold), scaling(0° – 360°, at the interval of 10 intervals), and blurring (Gaussian blur,  $r \in \{0, 3, 5, 7\}$  pixels)의 transform을 적용하여 총 36,864 장의 dataset을 생성하였다. 이 중 랜덤으로 training Set 16,114 장, Test set 16,142 장을 선택하여 실험을 진행하였다.

3) *Images Patches*: 그림 2와 같이, correct matching count를 기준으로 상위 10개의 keypoint와 하위 10개의 keypoint들의 특징을 비교하였다. 상위 10개에 대한 패치는 비교적 단순한 사각형 형태에서 많이 검출되었다. Genuine과 Impostor Histogram의 값을 정규화하여 표현된 Normal Distribution의 분포를 보면 Genuine과 Impostor 분포가 확연하게 구분되는 것을 확인할 수 있다. 반면, 하위 10개에 대한 패치는 글자 또는 단순한 패턴이 반복되는 형태에서 많이 검출되었다. Genuine과 Impostor Histogram의 값을 정규화하여 표현된 Normal Distribution의 분포를 보면 Genuine과 Impostor 분포가 많은 부분 겹쳐있어 구분이 어려운 것을 확인할 수 있다. 인식에 좋은 특징점은 큰 숫자 패치와 같이 단순한 색상으로 패턴이 큰 숫자 표시와 같은 특징점이 인식에 좋은 성능을 보여주었으며, 반대로 작은 설명 글씨와 같은 특징점들은 인식 성능이 좋지 못하였으며, 이러한 점들을 제거하고 학습을 수행하는 것이 좋다.

## IV. EXPERIMENTS

The improvement of recognition performance after the training using the keypoints filtering algorithm proposed earlier was measured. As for the experimental images, 16 images of Seoul Guide Map Pamphlet was selected. These images were deformed by way of rotating(0.5 ~ 2.0-folds, at the interval of 0.1-fold) scaling (0° ~ 360°, at the interval of 10 intervals) and blurring (Gaussian blur,  $r = 0, 3, 5, 7$  pixels). As a result, 32,256 images were obtained. Of them, 16,114 training images



(a) the best 100-images



(b) the worst 100-images

Fig. 2. The Best/Worst 100-Images with Regard to Correct Matching Count

and 16,142 test images were selected at random. First, the keypoints of training images were detected and then the score function( $gf(p_i)$ ) was calculated using the detected keypoints.

The keypoints database is composed of the set of all keypoints( $K_{all}, n(K_{all}) = 3000$ ) that did not consider the score function and the set of the keypoints( $K_{50}, K_{100}, K_{300}, K_{500}$ ) composed of top 50, 100, 300 and 500 keypoints filtered in the score function.

First the improvement of recognition speed was measured. As for the proposed method, since the keypoints were reduced to be saved in the training phase, the number of the keypoints, the subjects of comparison, decreases, which in turn increases the computing speed.

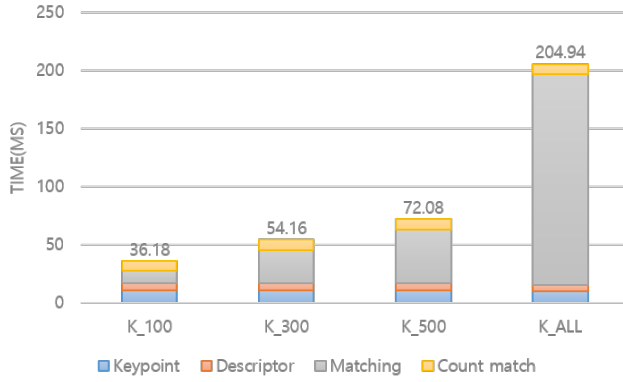


Fig. 3. Time Comparison Among Conventional Full Database and Proposed Filtered Database

As shown in Figure ??, the computing speed improves in proportion to the number of the set of keypoints. In particular, the time spent for training decreases to  $1/n$  compared to the training of whole keypoints when training was performed with 100 keypoints. In a lightweight implementation environment like smartphone, the reduction of computation provides rapid interaction. The proposed method is expected to increase the speed and to improve the overall recognition performance. The test image recognition performance was measured using keypoints database. As for the match method for measuring recognition performance, we used the match method [38] which prevent false matches.

The results of the measurement of recognition rate using the above method were demonstrated in Figure 4. In comparison with the keypoints database using the whole of keypoint sets ( $K_{all}$ ),  $K_{500}$  and  $K_{300}$  showed slight degradation of recognition rate whereas  $K_{100}$  and  $K_{50}$  showed the improvement of performance.

When performing keypoint filtering, the bad keypoints causing miss-match are eliminated, which in turn increases the reliability of the match results. To prove this, the precision [39] in the feature-level was calculated. The precision can be calculated as the ratio between the number of the correspondence pairs obtained after matching and the correct matches, indicating the insignificant proportion of mass-match and significant proportion of correction match in the match results. The increase of the ratio between correct match and match results subsequently affects the performance of robust pose estimation.

The results of precision are demonstrated in Table II and Table 5. The filtered keypoints sets showed higher precision compared to the whole of keypoints set ( $K_{all}$ ). The number of the detected keypoints decreased but the ratio of correct

TABLE II  
PRECISION OF FILTERED MATCHING

	$K_{50}$	$K_{100}$	$K_{300}$	$K_{500}$	$K_{all}$
Avg. Match Result	10.098	15.618	26.747	31.409	44.859
Avg. Correct Match	7.759	11.747	18.705	21.033	26.326
Precision	76.8%	75.2%	69.9%	67.0%	58.7%

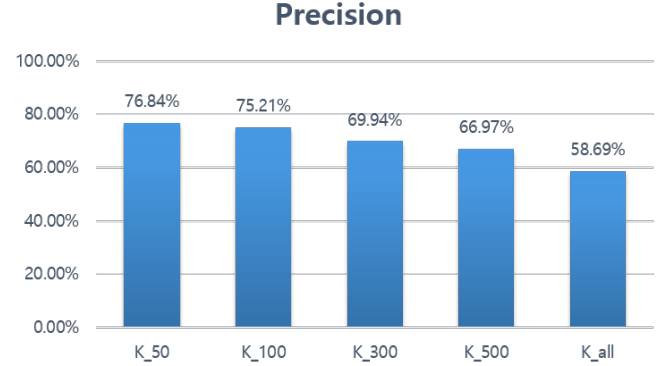


Fig. 5. Precision of filtered keypoint database

match increased, which showed high precision. Such results are able to improve the speed and performance of robust pose estimation.

## V. CONCLUSION

The conclusion goes here.

## APPENDIX A

### PROOF OF THE FIRST ZONKLAR EQUATION

Appendix one text goes here.

## APPENDIX B

Appendix two text goes here.

## ACKNOWLEDGMENT

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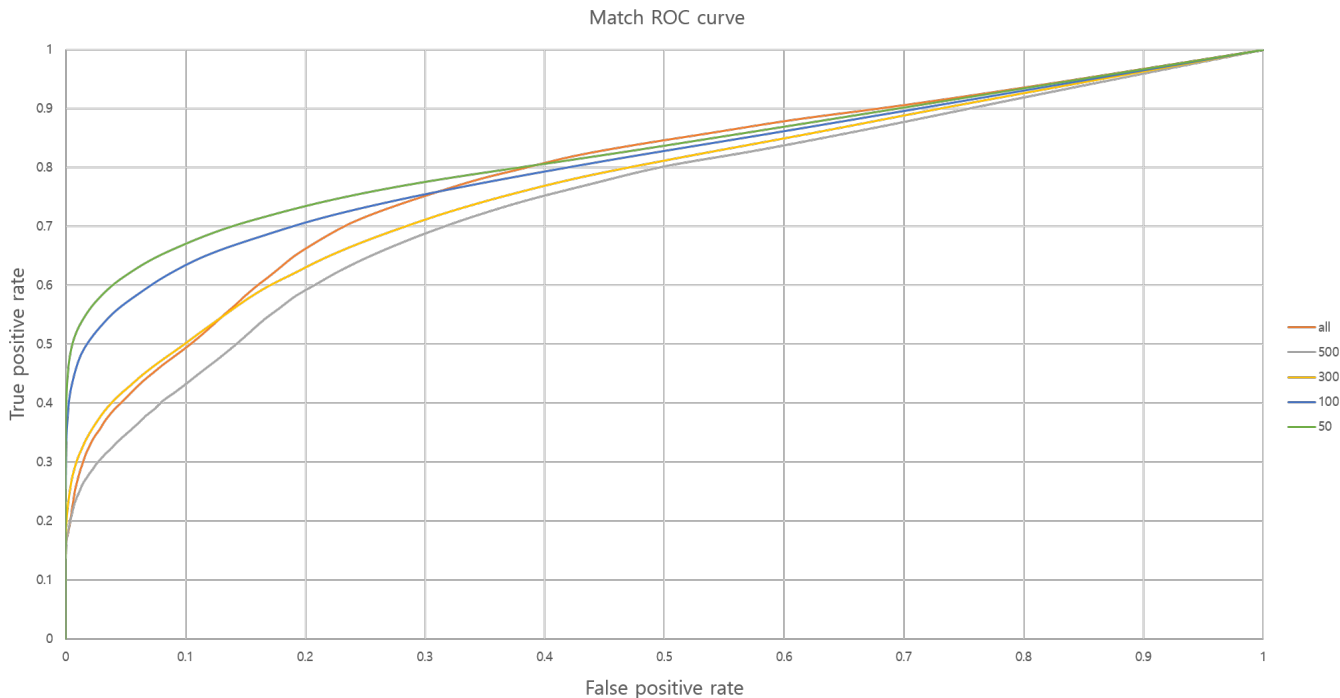


Fig. 4. ROC curve for match rate

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**Michael Shell** Biography text here.

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