

§ 3.7 Technology Highlight: Polynomial and Rational Inequalities

Example: Solve the inequality $t^5 - 10t^4 + 35t^3 - 50t^2 + 24t > 0$.

This can be done by hand (see Example 8 in Coburn), but not all quintic polynomials can be approached this way, so let's explore the situation with a graphing calculator.

Press $\boxed{\text{Y=}}$ and enter the left-hand-side as Y_1 . Set the $\boxed{\text{WINDOW}}$ to $x \in [0, 4.7]$, $y \in [-5, 5]$, and $\boxed{\text{GRAPH}}$. Use $\boxed{\text{TRACE}}$ to find the solution:

$$t \in (0, 1) \cup (2, 3) \cup (4, \infty)$$

To help us visualize this, we can use the Shade function:

DRAW $\left(\boxed{2\text{nd}} \boxed{\text{PRGM}}\right)$, 7:Shade *or* CATALOG $\left(\boxed{2\text{nd}} \boxed{0}\right)$, Shade(

The arguments of the Shade function are

lower function, upper function, left endpoint, right endpoint, pattern,
density

Here, we try $\text{Shade}(0, Y_1, 0, 5, 1, 2)$

To clear the shading, use the ClrDraw command from the DRAW menu or CATALOG.

Exercise: Do Technology Highlight Exercise 1, pg. 311