

Dynamic Models in Biology

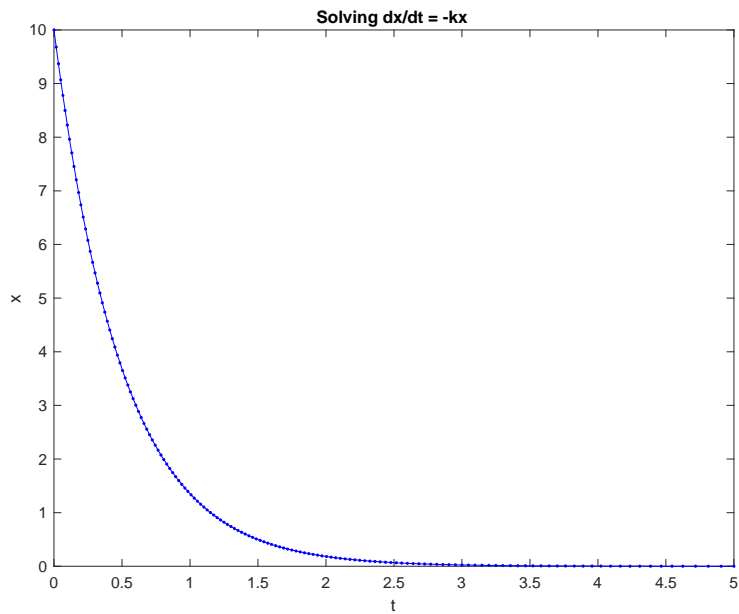
Lab 1 Report

Jonathan Levine

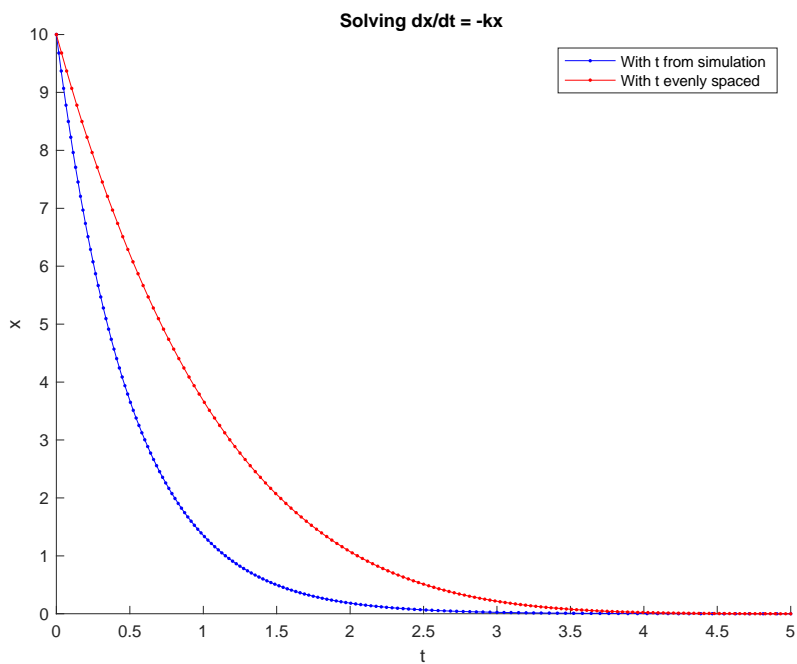
Fall 2023

Part 1 Simulating exponential decay

Decay with $k=2$

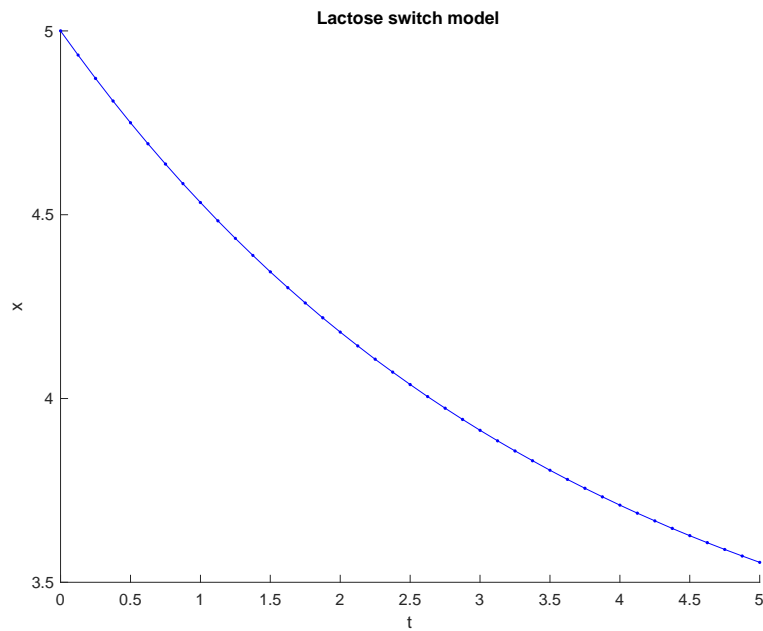


Using the incorrect t values changes the solution:

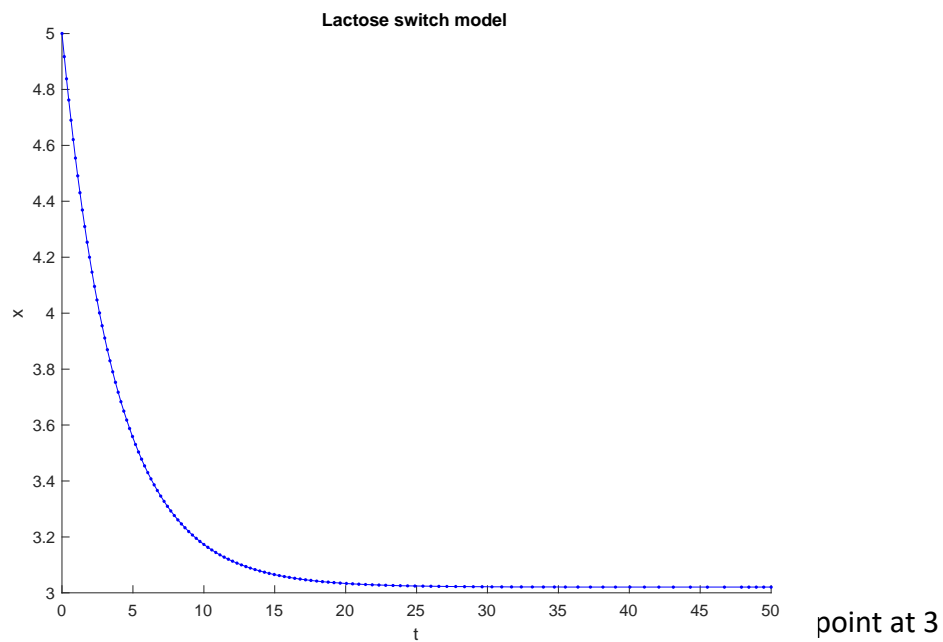


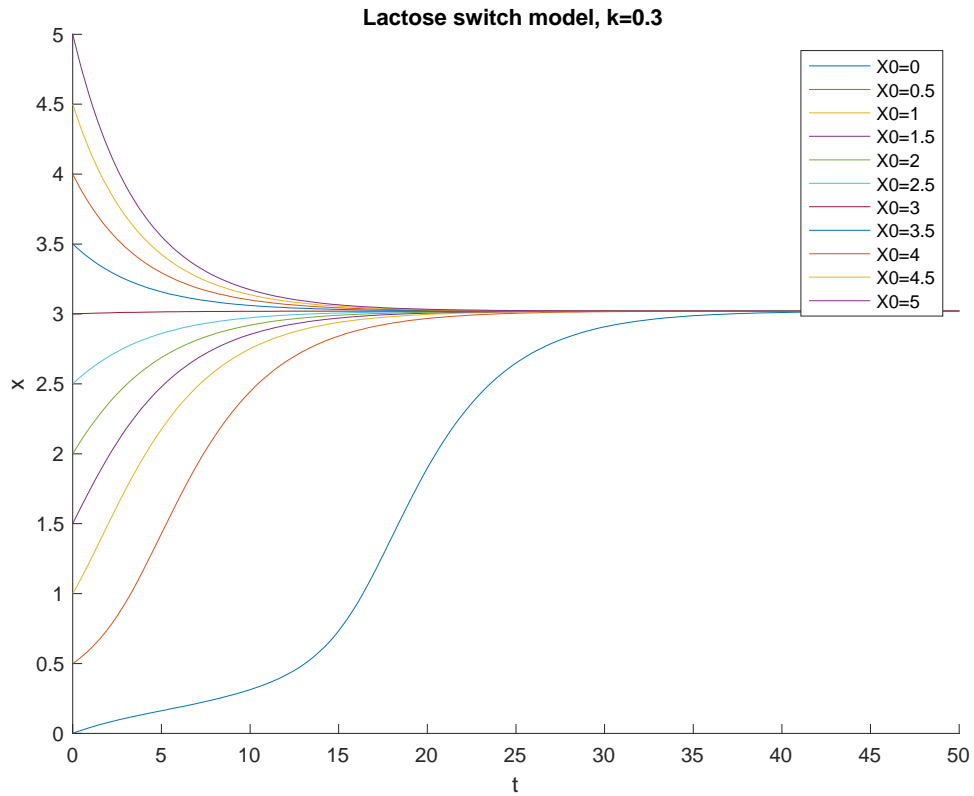
Part 2 Simulating the lactose switch model

If t only goes until 5, then it does not reach steady-state ($a=0.05$, $k=0.3$, and an initial condition of $x_0=5$, $t:0:5$)

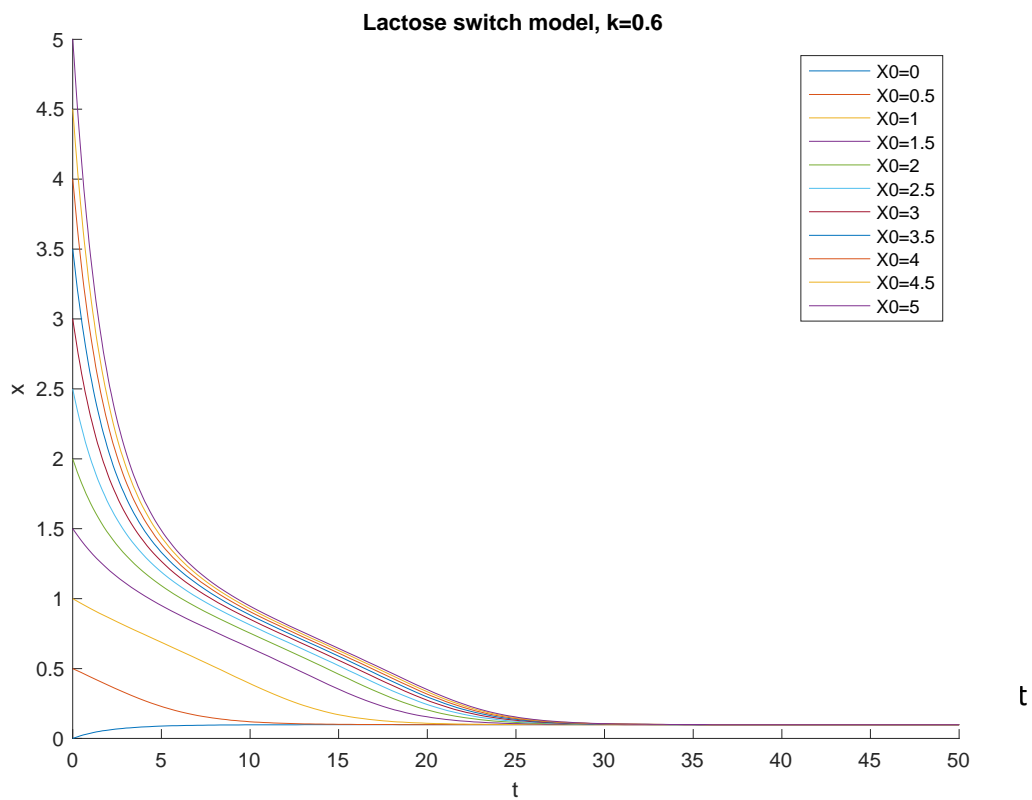


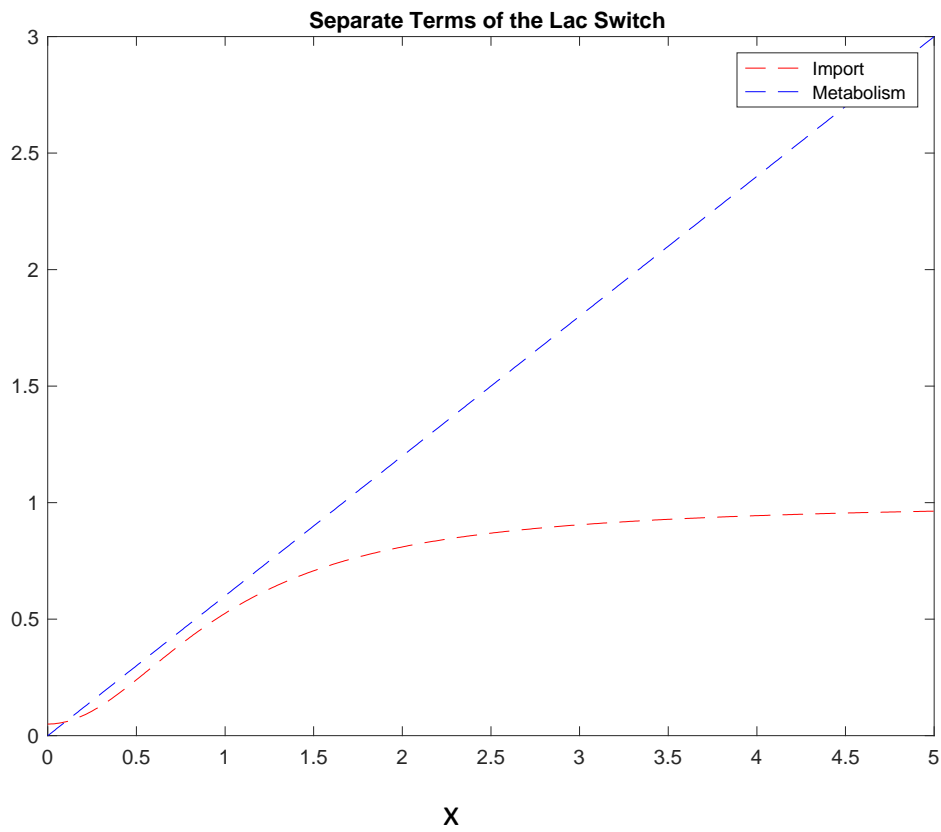
Increasing t will allow it to reach steady-state ($a=0.05$, $k=0.3$, and an initial condition of $x_0=5$, $t:0:50$)



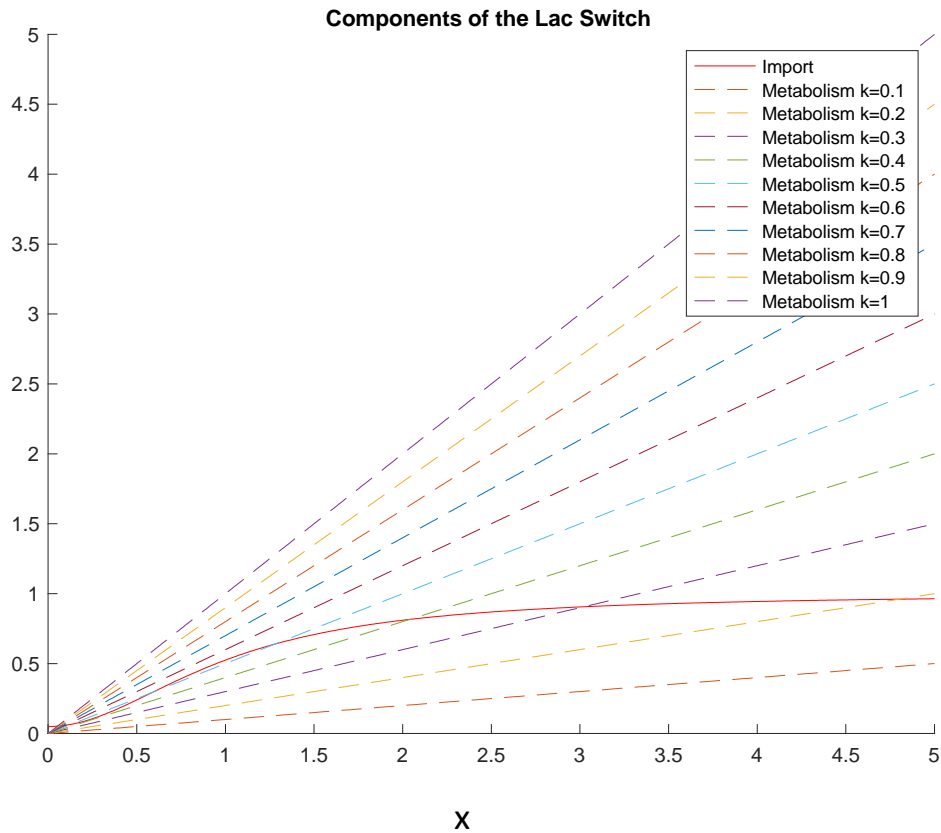


Now with k at 0.6, the steady-state approaches a different fixed point (around 0.1)

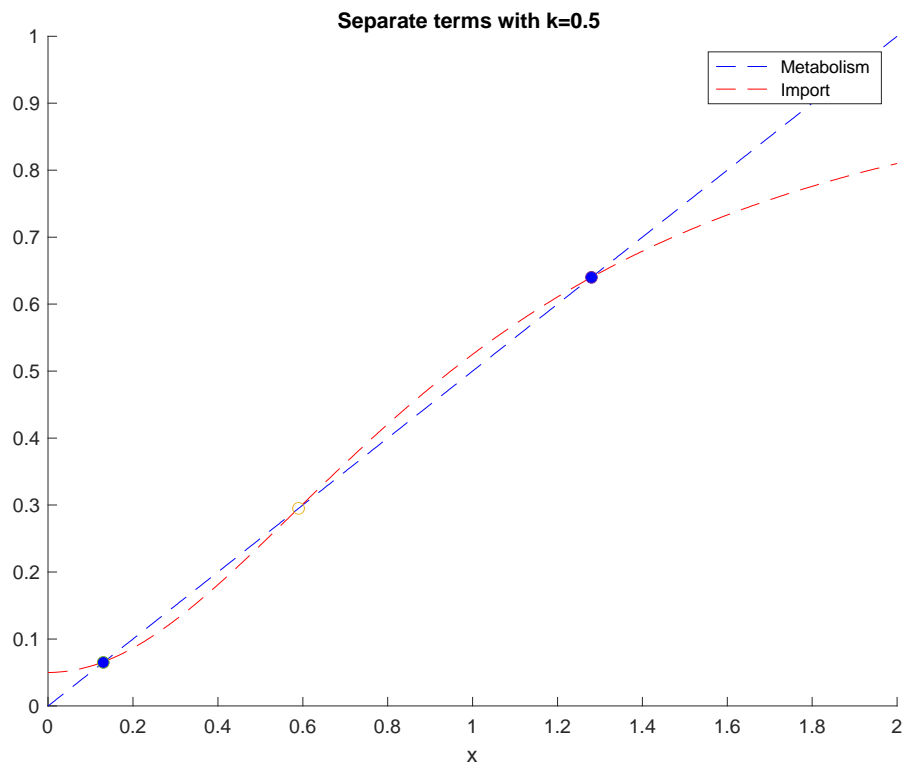




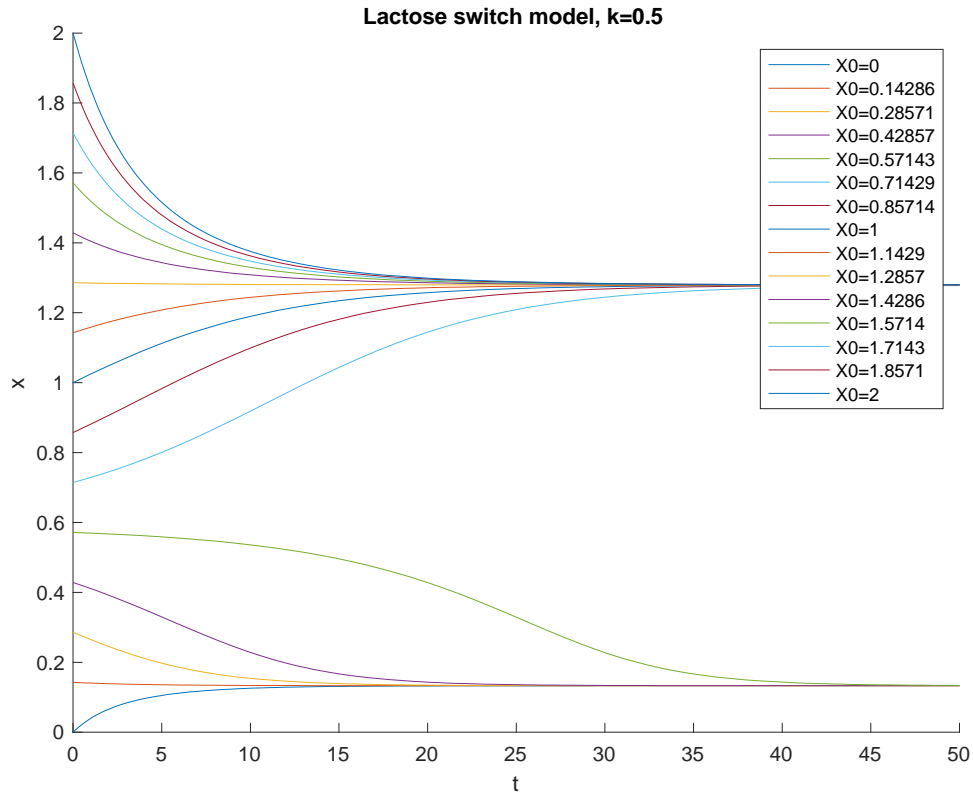
With that value of k , we only get one fixed point. If we want to find values of k for which there exist more fixed points, we vary k and re-run:



The light blue curve ($k=0.5$) looks like a good candidate. Plotting that one and zooming in a bit more, we do see there are 3 fixed points for the system with $k=0.5$. If we solve the equations, we can get the exact fixed points, $x^* \approx \{0.13, 0.59, 1.28\}$

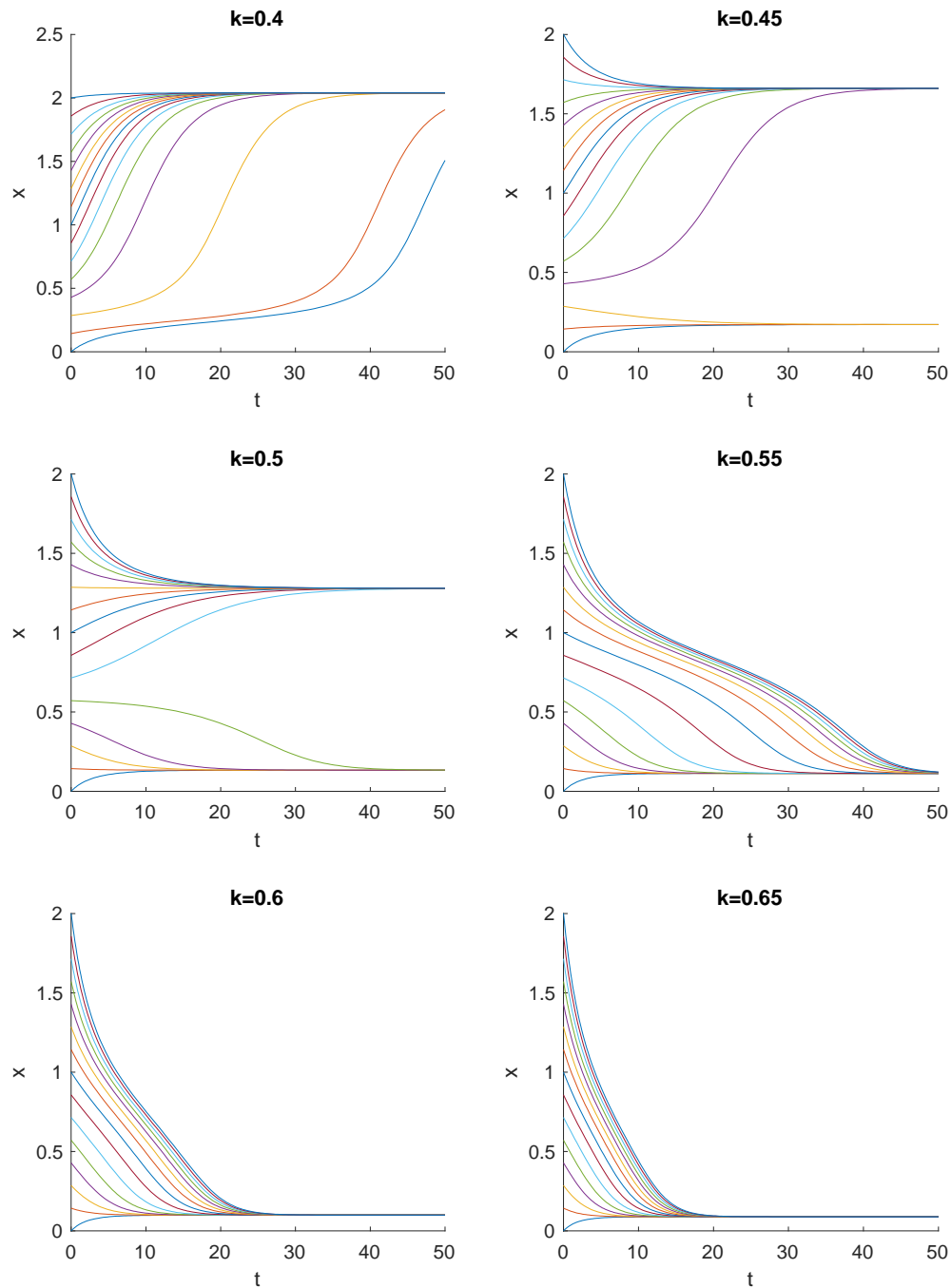


Running the simulation for $k=0.5$, we can see there are two basins of attraction, depending on the initial condition x_0 . In this figure, the basin of attraction changes around $x_0 = 0.6$ which corresponds to the unstable fixed point where the red and blue curve meet in the figure before this one (unfilled orange circle)



The basin of attraction for the k values in the top half is convergent on the fixed point at $x \approx 1.28$ while the basin of attraction for the k values in the bottom half goes to the stable fixed point at $x \approx 0.13$.

We can now vary the parameter k , and see for which values of k there exists a bifurcation with 2 basins based on initial conditions:



Here we can see that only k values of 0.45 and 0.5 lead to bifurcation based on initial conditions.

If we want to zoom in with a bit more granularity, this becomes $0.42 < k < 0.54$. (Obviously you can find more granularity by simulating more precise k values in the range around those edges)

