# Regression Models Project

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#### **Executive Summary**

In this report, we examine the mtcars dataset as provided by R. The mtcars data was extracted from the 1974 Motor Trend US magazine, and comprises fuel consumption and 10 aspects of automobile design and performance for 32 automobiles. Using linear regression models and t.test we can form some conclusions on the relationships between Miles/gallon mtcars\$mpg and all the other variables in the dataset. Based on the analysis in the report we can summarize the following:

- Manual cars on average give higher MPG of 7.245 when we exclude all other variables.
- The final model using a mix of the step() model and intution is:  $mpg_e = 30.947 + 11.555 * am 0.027 * hp 2.516 * wt 3.578 * wt * am$ .
- Results show the possibility of one outlier in the 'Maserati Bora' model which dents the effectiveness of the above model.

#### Exploring the Data

We first need to understand the data before we perform any sort of linear regression. Fig 1.1 (appendix) section shows pair graphs between all the variables. Using this plot in conjunction with ?mtcars one can argue that some of the variables should be factorized. However, given the limited amount of observations along with the reasoning that for a varible like cyl, the number of cylinders can be different from observed of just 4, 6 or 8 (i.e. we can technically have 5 or 7 cylinders) then the only variables we factorize() are vs & am - whether engine is v-shaped (1 or 0) or whether car is automatic or manual (0 or 1) respectively.

#### Is an automatic or manual transmission better for MPG?

We perform basic exploratory data analysis via a boxplot for the two different types of transmission (0 = automatic, 1 = manual). Figure 2.1 (appendix) shows that there is a significant difference in mpg between 2 types of transmissions with manual cars having a higher mean MPG over that of automatic cars. We can take this a step further by conducting a Welch Two Sample t-test below (results in appendix Figure 2.2):

```
test <- t.test(mpg~am, data=mtcars)</pre>
```

We find that test\$p.value = 0.0014, therefore we can reject null hyptothesis that the means are the same. Furthermore, the difference in means between the two types of transmissions is 7.245, and we can conclude that manual transmission has on average higher MPG.

#### Quantifying MPG difference between transmissions

In order to quantify the difference in MPG between transmission and its significance we look to linearly regress mtcars\$mpg against mtcars\$am with the following model (results in appendix Figure 3.1):

```
fit_am <- lm(mpg~am, data=mtcars)
summary(fit_am)$coef</pre>
```

Although the coefficient of am is significant in explaining mpg, the R-squared is only 0.3598, and consequently is not enough to explain the variation in mpg. Therefore we have to explore the other variables in the dataset to see if we can come up with a more viable model

#### Model Building

We start off by regressing MPG against all the other variables:

```
fit_all <- lm(mpg~., data=mtcars)
summary(fit_all)</pre>
```

From Figure 3.2 we see that by including all the variables, the **r-squared** is 0.869, however now none of the coefficients are significant resulting in a poor model.

Instead we look to build a model using the backwards step() function (which removes the least significant variables one by one) as a building block, then use a little bit of intuition and understanding of cars to finalize and make sense of the model

```
fit_step <- step(fit_all)
summary(fit_step)</pre>
```

Results from the step() algorithm show that the optimal model is:  $mpg_e = b_0 + b_1 * wt + b_2 * qsec + b_3 * am$ , with **R-squared** of 0.8497, however the problem with using quarter mile time (qsec) as a predictor is that this variable is actually an outcome of the parts that make a car rather than what explains the MPG for a particular model. So instead we substitute qsec with hp with the intuitive reasoning that higher horsepower may affect mpg, but higher horsepower usually means lower quarter mile times; this can be confirmed by looking at the correlation between the two variables which consequently is -0.708.

Now we analyze the model with qsec replaced:  $mpg_e = b_0 + b_1 * wt + b_2 * hp + b_3 * am$ 

```
fit1 <- lm(mpg ~ wt + am + hp, data = mtcars)
summary(fit1)</pre>
```

Results in Fig 3.4, show a pretty good  $\mathbf{R}$ -squared = 0.8399 and with the exception of  $\mathbf{am}$  all coefficients are significant giving us a pretty good final model.

#### Interactions

Before finalizing the model and reporting results, we look at the different variables for possible interactions. Fig 4.1 & Fig 4.2 are plots of mpg against wt and vs respectively with transmission type in different colors. We see that there is a significantly different slope in Fig 4.1 with the different transmission types, but not in Fig 4.2 suggesting an interaction of wt \* am to explore:

```
fit_final <- lm(mpg ~ am + hp + wt + wt:am, mtcars)
summary(fit_final)</pre>
```

Fig 4.3 shows this model has an **R-squared** = 0.8696 with all coefficients stastically significant. We can therefore conclude using anova() in fig 4.4 that fit\_final is the best model given the level of significance for each additional variable:

```
mpg_e = 30.947 + 11.555 * am - 0.027 * hp - 2.516 * wt - 3.578 * am * wt
```

- Therefore, a manual car that has weight = 1000lbs will have a higher mpg of 11.555 -3.578 = 7.977 higher mpg given same hp.
- A manual car that weighs 5000lbs will have a lower mpg of -6.335.

#### Residual Plot & Diagnostics

Fig 5.1 shows the residual plot & diagnostic:

- Residual plot shows no obvious pattern
- Q-Q plot shows for the most part that standardized residuals lie on the line.
- Scale-Location plot shows random distribution of points.
- Residual vs leverage for the most part has no outliers with exception of the 'Maserati Bora'. We show the influence in fig 4.4 using dfbetas(fit\_final)["Maserati Bora",1]. This unfortunately shows some weakness in the model that should be pointed out despite other criterias being met.

# **Appendix**

pairs(mtcars, main="Fig 1.1: Pair Graph of mtcars")

Fig 1.1: Pair Graph of mtcars

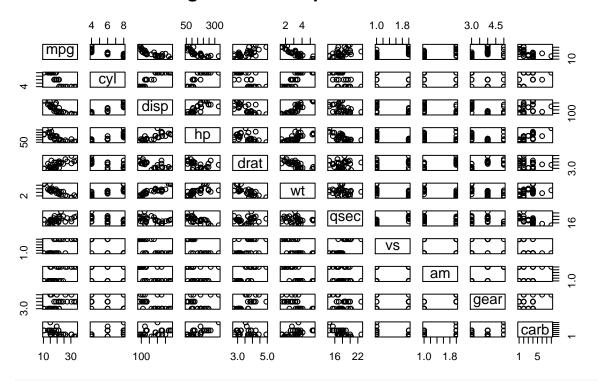
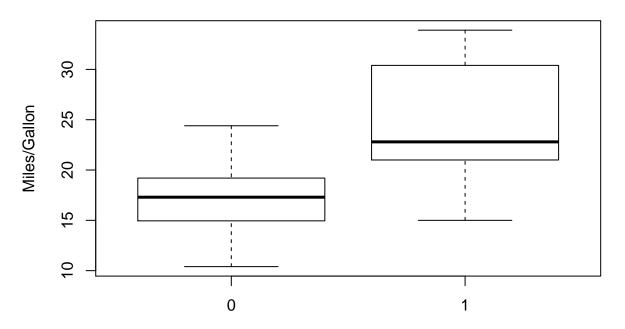


Fig 2.1 MPG v Transmission



Transmission, 0 = Automatic, 1 = Manual

Figure 2.2

```
t.test(mpg~am, data=mtcars)
##
   Welch Two Sample t-test
##
##
## data: mpg by am
## t = -3.7671, df = 18.332, p-value = 0.001374
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -11.280194 -3.209684
## sample estimates:
## mean in group 0 mean in group 1
          17.14737
                          24.39231
##
Figure 3.1
```

#### rigure 3.1

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 17.147368 1.124603 15.247492 1.133983e-15
## am1 7.244939 1.764422 4.106127 2.850207e-04
```

## Figure 3.2

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 12.30337416 18.71788443 0.6573058 0.51812440
## cyl -0.11144048 1.04502336 -0.1066392 0.91608738
## disp 0.01333524 0.01785750 0.7467585 0.46348865
```

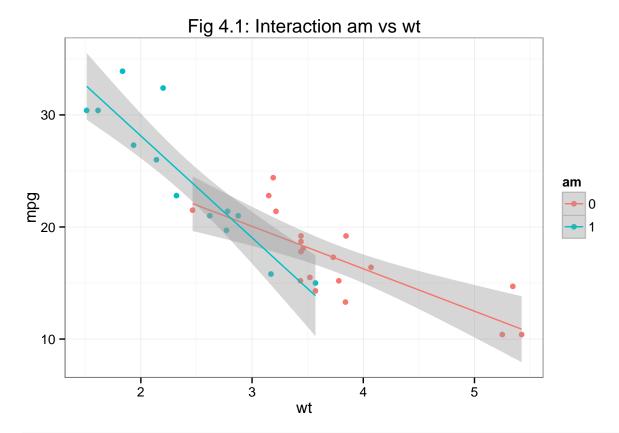
```
## hp
          0.78711097 1.63537307 0.4813036 0.63527790
## drat
## wt
          -3.71530393 1.89441430 -1.9611887 0.06325215
## qsec
          0.82104075 0.73084480 1.1234133 0.27394127
## vs1
          0.31776281 2.10450861 0.1509915 0.88142347
          2.52022689 2.05665055 1.2254035 0.23398971
## am1
## gear
          0.65541302 1.49325996 0.4389142 0.66520643
          ## carb
```

## Figure 3.3

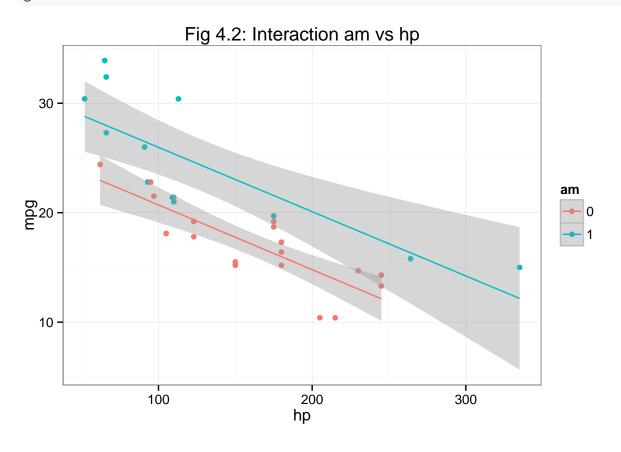
```
fit_step <- step(fit_all)
summary(fit_step)$coef</pre>
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 9.617781 6.9595930 1.381946 1.779152e-01
## wt -3.916504 0.7112016 -5.506882 6.952711e-06
## qsec 1.225886 0.2886696 4.246676 2.161737e-04
## am1 2.935837 1.4109045 2.080819 4.671551e-02
```

## Figure 3.4



g1 <- ggplot(data=mtcars, aes(x=hp, y=mpg, colour=am)) +
geom\_point() + stat\_smooth(method="lm") + labs(title="Fig 4.2: Interaction am vs hp") + theme\_bw()
g1</pre>



#### Figure 4.3

```
##
                  Estimate Std. Error
                                         t value
                                                     Pr(>|t|)
## (Intercept) 30.94733319 2.723410935 11.363446 8.546944e-12
               11.55481296 4.023276579 2.871991 7.844579e-03
## am1
## hp
               -0.02694935 0.009795903 -2.751084 1.047673e-02
## wt
               -2.51558550 0.844496532 -2.978799 6.051842e-03
## am1:wt
               -3.57790980 1.442795585 -2.479845 1.967639e-02
```

Figure 4.4

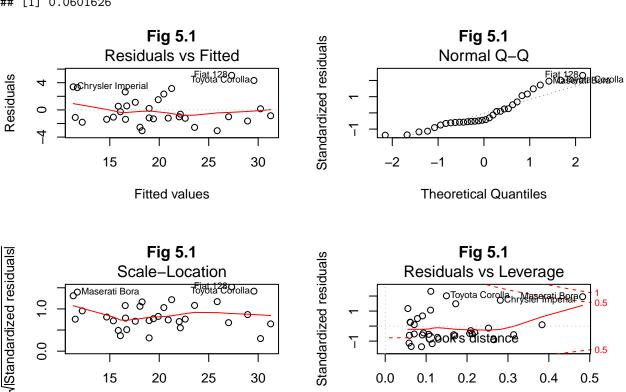
```
anova(fit_am, fit1, fit_final)
```

```
## Analysis of Variance Table
##
## Model 1: mpg ~ am
## Model 2: mpg ~ wt + am + hp
## Model 3: mpg ~ am + hp + wt + wt:am
              RSS Df Sum of Sq
##
     Res.Df
                                          Pr(>F)
## 1
        30 720.90
## 2
         28 180.29
                   2
                        540.61 49.6998 8.909e-10 ***
## 3
        27 146.85
                   1
                         33.45 6.1496
                                          0.01968 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

dfbetas(fit\_final)["Maserati Bora",1]

Fitted values

## [1] 0.0601626



Leverage