

Crypto Dark Matter++

Abstract

Abstract goes here.

1 Introduction

1.1 Applications

2 Background

3 Related Work

4 Technical Overview of Results

4.1 Protocols Implemented

In this work we implemented a few distributed protocols of the PRF introduced by Boneh et. Al [1]:

$$PRF_k(x) = R \times (K \times x \bmod 2) \bmod 3$$

where R is a randomization matrix in Z_3 , K is an $m \times n$ key and x is an n -length vector. Specifically, we present a new protocol for implementing this PRF. The protocol uses a shared input and output which provides improved performance over the original protocol described in [1]. For context, we also implement the original protocol [1]. We also introduce an improved OPRF (Oblivious PRF) protocol, in which one party has the input and one has the key. Below are details of the protocols.

4.1.1 PRF

notations: below are the notations we use to describe the protocols:

K is the key, represented by an $m \times n$ matrix

x is the input, represented by an n size vector

R_x, r_k - pre-shared randomness for key K and input x

r - random vector in Z_3] We use capital letters for matrices, and \vec{x} notation for vectors

Original Distributed Input Distributed Output (DIDO) PRF Protocol The protocol was introduced in [1]. The main details of the protocols are described below (1). In this setting, both the input and the key are secret shared additively between the two parties. Both the protocol presented in this paper and the original protocol are two-party PRFs.

Algorithm 1 2-Party dark matter PRF

Input: $K_{m \times n}(i)$ and $\vec{Inp}(i_n)$ key and user input of each user,
($i = 1 \dots 2, n, m = 256$)

Output: user 1: $\vec{K} \times x + \vec{r}$

user2: $\neg \vec{r}$

Preprocessing:

Output: user 1: \vec{R}_a, \vec{r}_b - pre-shared randomness

user 2: \vec{r}_x - pre-share randomness

Stage 1: calculate $a \times b + c$

input: user 1: $\vec{A}, \vec{b}, \vec{R}_a, \vec{r}_b$

user 2: $\vec{x}, \vec{r}_x, \vec{z}$

1. user 2 $\vec{m}_x = \vec{x} - \vec{r}_x \rightarrow$ user 1

2. user 1 $\leftarrow \vec{M}_a = \vec{A} - \vec{r}_A$ user 2

3. user 2 $\vec{m}_b = \vec{R}_a \times \vec{m}_x + \vec{b} - \vec{r}_b \rightarrow$ user 1

Output: user1 : $\neg \vec{b}$

user2 : $\vec{M}_a \times \vec{x} + \vec{m}_b + \vec{z} = \vec{A}\vec{x} + \vec{b}$

Stage 2: Oblivious Transfer input: user 1: $\vec{r}_1, \vec{r}_2, \vec{r}_a, \vec{r}_b$ - vectors in Z_3 user 2: \vec{x}, \vec{r}_x - vectors in Z_2 , \vec{z} - vector in Z_3

1. user 1 $\leftarrow \vec{m}_x = \vec{x} \oplus \vec{r}_x$ user 2

2. user 1: $\vec{m}_1 = (\neg m_x) \vec{r}_a + \vec{m}_x \vec{r}_b + \vec{r}_1 \rightarrow$ user 2

3. user 1: $\vec{m}_2 = (\vec{m}_x) \vec{r}_a + \neg \vec{m}_x \vec{r}_b + \vec{r}_2 \rightarrow$ user 2

output: user 2: $\vec{w} := \vec{x} \times \vec{m}_2 + \neg \vec{x} \times \vec{m}_1 - \vec{z}$

stage 3: Z_3 randomization

Algorithm 2 2-Party DSISK PRF

Preprocessing
 Stage 1: calculate $a \times b+c$
 Stage 2: Oblivious Transfer
 stage 3: Z_3 randomization

Our improved (DIDO) PRF protocol**4.2 OPRF**

This is a new OPRF protocol, which improved the performance over the original OPRF protocol described in [1]. In this setting, one party has the input and another party has the key.

Algorithm 3 2-Party oPRF

Preprocessing
 Stage 1: calculate $a \times b+c$
 Stage 2: Oblivious Transfer
 stage 3: Z_3 randomization

4.3 Parameters

The input variable to the PRF functions are the key K which is of size $m \times n$ and each input is a vector of size n . To save storage space, the key was implemented as a Toeplitz matrix, requiring $2 \cdot n$ bits of storage space. In phase 3 of the algorithm, a randomization matrix is used which is of size $r \times n = 81 \times 256$, resulting in entropy of 128 bits.

4.4 Optimizations**4.4.1 packing in Z_2**

Bit slicing: this bit-wise packing technique was used to optimize the run-time, each 64 bits were represented by a word. Since each key is of size $m \times n$ and each input is a vector of size n , it is possible to pack each 64 rows into m words. This may result in time saving of up to $\times 64$ of the run-time.

4.4.2 Packing in Z_3

To optimize the randomization in Z_3 , which requires a matrix-vector multiplication in the last phase of the PRF calculation, we implement two optimization methods:

Bit slicing: this was done by representing a vector over Z_3 as two binary vectors - one LSB's and one MSB's.

A few operations, such as addition, subtraction and multiplication mod 3 required extra calculations. One of the properties that were utilized to implement this was:

mult-by-2 mod 3 \leftrightarrow negation mod 3 \leftrightarrow swap the MSB and LSB

Such a vector is sometimes being represented as a vector of $2 \times n$ bits. One example is when this vector is sent as an input to the Oblivious Transfer mechanism. The algorithms can be found in Algorithms 4 to 7.

Algorithm 4 Addition in Z_3

Item 1: input: \vec{l}_1, \vec{m}_1 - LSB and MSB vectors of value 1
 \vec{l}_2, \vec{m}_2 - LSB and MSB vectors of value 2

1. $\vec{T} = (\vec{l}_1 \vee \vec{m}_2) \oplus (\vec{l}_2 | \vec{m}_1);$
 2. $MSB_{res} = (\vec{l}_1 \vee \vec{l}_2) \oplus \vec{T};$
 3. $LSB_{res} = (\vec{m}_1 \vee \vec{m}_2) \oplus \vec{T};$
-

Algorithm 5 Subtraction in Z_3

Item 2:
input: \vec{l}_1, \vec{m}_1 - LSB and MSB vectors of value 1
 \vec{l}_2, \vec{m}_2 - LSB and MSB vectors of value 2

1. $\vec{T} = (\vec{l}_1 | \vec{l}_2) \wedge (\vec{m}_2 | \vec{m}_1);$
 2. $MSB_{res} = (\vec{l}_1 | \vec{m}_2) \wedge \vec{T};$
 3. $LSB_{res} = (\vec{m}_1 | \vec{l}_2) \wedge \vec{T};$
-

Algorithm 6 Multiplication of two trinary vectors Z_3

Item 3:
input: \vec{l}_1, \vec{m}_1 - LSB and MSB vectors of value 1
 \vec{l}_2, \vec{m}_2 - LSB and MSB vectors of value 2

1. $LSB_{res} = ((\vec{l}_1 \wedge \vec{l}_2) \wedge ((\vec{m}_1 \wedge \vec{m}_2)$
 2. $MSB_{res} = ((\vec{l}_1 \wedge \vec{m}_2) \wedge ((\vec{m}_1 \wedge \vec{l}_2)$
-

Integer packing: this was explored as an alternative to the bit slicing. Since each number is a trinary number, the multiplication of each row by the output vector can be any number between -256 to 256. To explore this option, we represented each number by 9 bits, and packed 7 numbers into each word. This was expected to result in time saving of up to $\times 7$. Testing this option indeed proved to be significantly slower than the first method of packing. We therefore continued using the first packing method of packing instead. Note: Since each trinary number can be either 0,1 or 2, we can add up to 255 numbers and never exceed 510. Moreover, if we take a random sample,

Algorithm 7 Mux implementation of two trinary vectors Z_3

input: \vec{l}_1, \vec{m}_1 - LSB and LSB vectors of value 1

\vec{l}_2, \vec{m}_2 - LSB and LSB vectors of value 2 \vec{select} - binary vector

1. for each word i
 2. $LSB[i] = (\vec{l}_2 \wedge s[i]) | (\vec{l}_1 \wedge \neg s[i])$
 3. $MSB[i] = (\vec{m}_2 \wedge s[i]) | (\vec{m}_1 \wedge \neg s[i])$
-

we can add 256 numbers and the probability of carryover is negligible. We use this to multiply a packed trinary vector with a trinary matrix with 256 columns (see algorithm below).

$$x_0 \dots x_6 \in Z_3 = 0, 1, 2$$
$$\rightarrow x = \sum_{i=0}^6 (512^i) \times c_i, x_i \in [0 \dots (2^{64} - 1)]$$

Using a lookup table: To further optimize the run-time, we created a lookup table to replace the matrix-vector multiplication. To this end, the randomization matrix is assumed to be constant and divided into 16 matrices of size 81×16 . A lookup table of size 16×2^{256} is created during the pre-processing stage. During runtime, the input is divided to MSB and LSB, and each consecutive 16 bits (16 rows in the matrix) are used as separate input to the lookup table.

5 Analysis

Table 5 includes the computation and communication results for the different protocol.

Protocol	Packed	Z_3 lookup table	Computation	Communication Costs
Centralized	N	N		0
Centralized	Y	N		
Original (DIDO) PRF protocol	Y	N		
Our (DIDO) PRF algorithm	Y	N		
Our (DIDO) PRF algorithm	Y	Y		
Our OPRF	Y	N		
Our OPRF	Y	Y		
Discrete log-based PRF	-	-		

Table 1: Run-time of different protocols

6 Benchmarking

We compare our run-time to discrete-log based PRFs. To this end, we use the lib sodium library [2]. The library uses elliptic curve 252 bits, and includes a function that performs scalar multiplication ('crypto_scalarmult_ed25519').

7 Experimental Results

The system was tested on AWS environment, on Ubuntu Server 18.04 with t2.medium. For testing, the code was run in a loop 1000 times. Below are run-time results. The results include both centralized and distributed version. The packing indicates both the Z_2 and Z_3 packing.

Protocol	Packed	Z_3 lookup table	Rounds/sec	Runtime(μ sec)
Centralized	N	N	50K	20.2
Centralized	Y	N	65.4K	18.5
Original distributed dark matter	Y	N	24K	40.56
This protocol	Y	N	49K	20.20
This protocol	Y	Y	83K	12.00
oPRF	Y	N	53K	18.66
oPRF	Y	Y	11.76K	8.50
Discrete log-based PRF	-	-	34K	29.56

Table 2: Run-time of different protocols

8 Conclusion and Future Work

9 Acknowledgement

10 References

References

- [1] Dan Boneh et al. *Exploring Crypto Dark Matter: New Simple PRF Candidates and Their Applications*. Cryptology ePrint Archive, Report 2018/1218. <https://eprint.iacr.org/2018/1218>. 2018.
- [2] *libsodium 1.0.18-stable*. <https://libsodium.gitbook.io/doc/>. Online; December 31 2020. 2020.