

$$a_G = \alpha r_{P/G}$$

kinematic relation

$$a_B = 1.5d \quad a_B = a_{Gy}$$

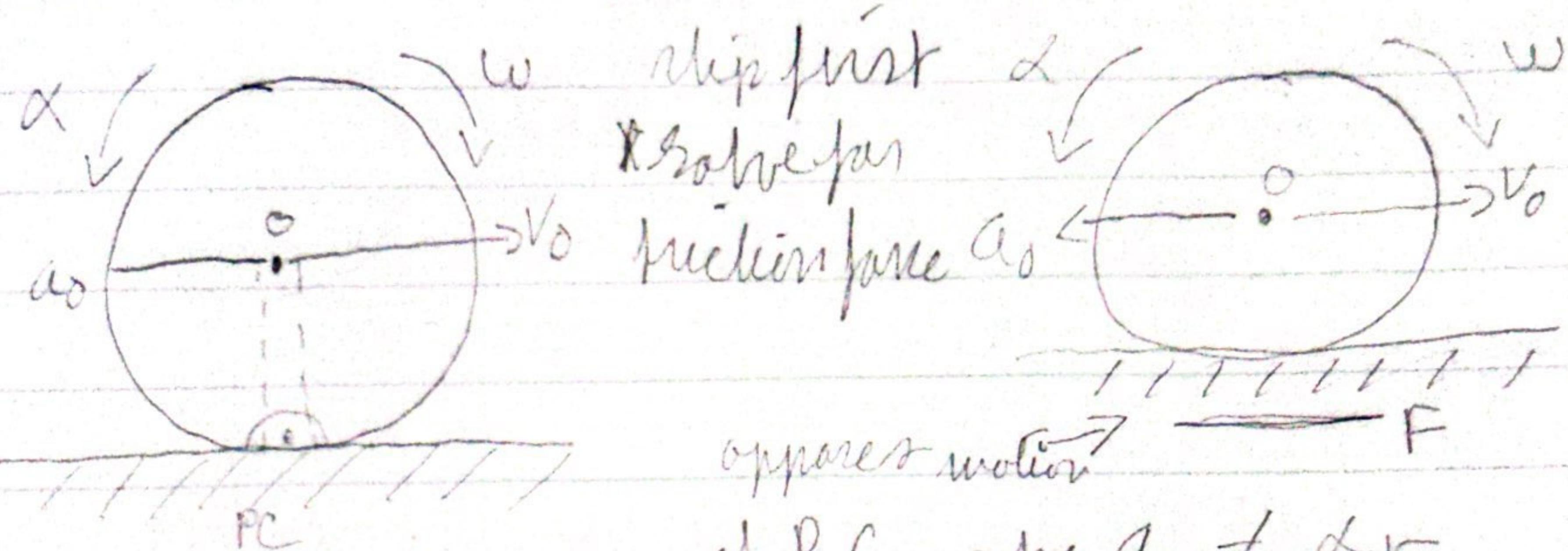
$$a_{Gy} = 1.5d$$

$$v_{aB} = \alpha r_B / 6$$

No slip: kinematic

Slipping:

* Assume no



$$\checkmark * \quad a_0 = \alpha r$$

$$v_0 = \omega r$$

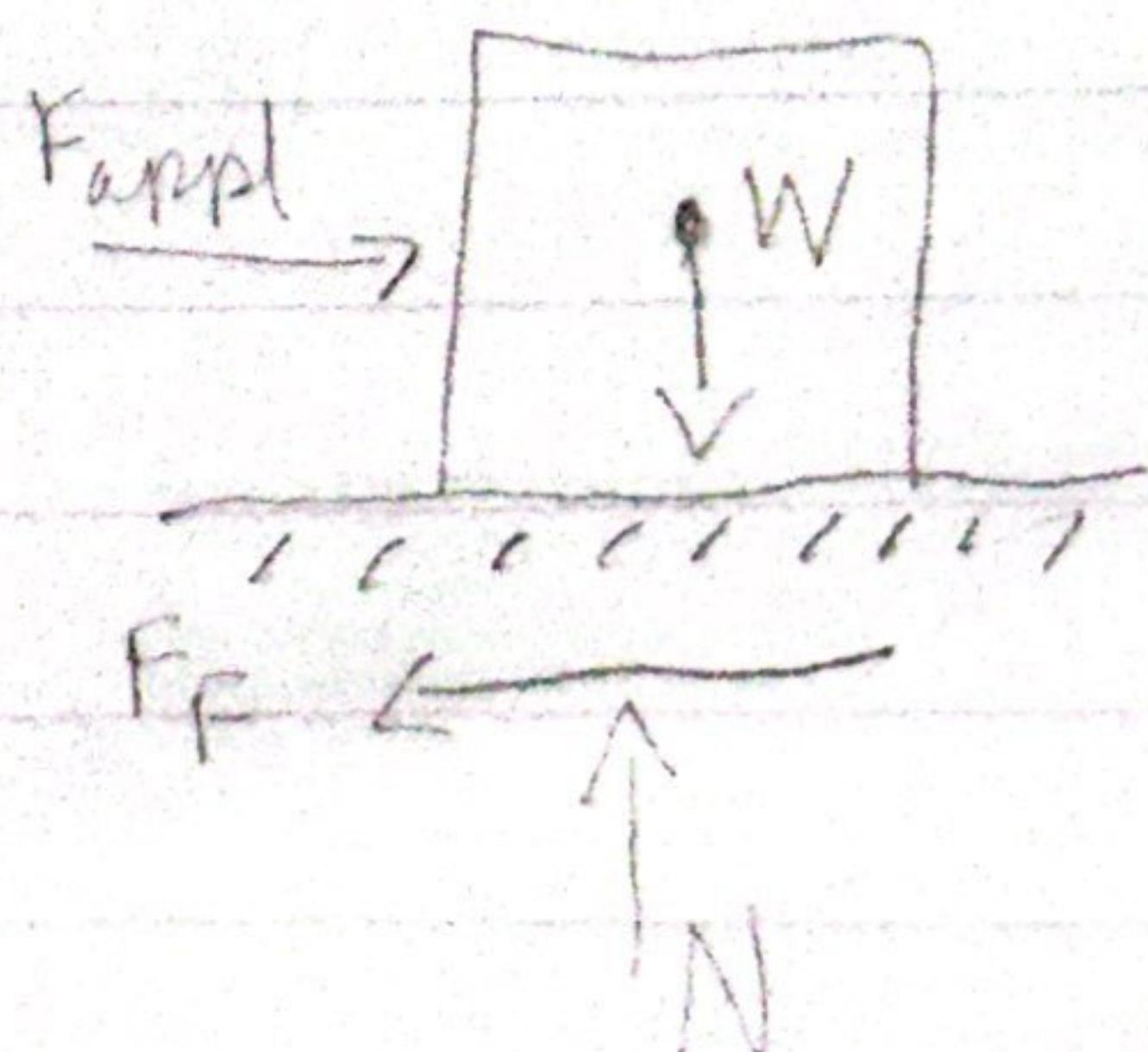
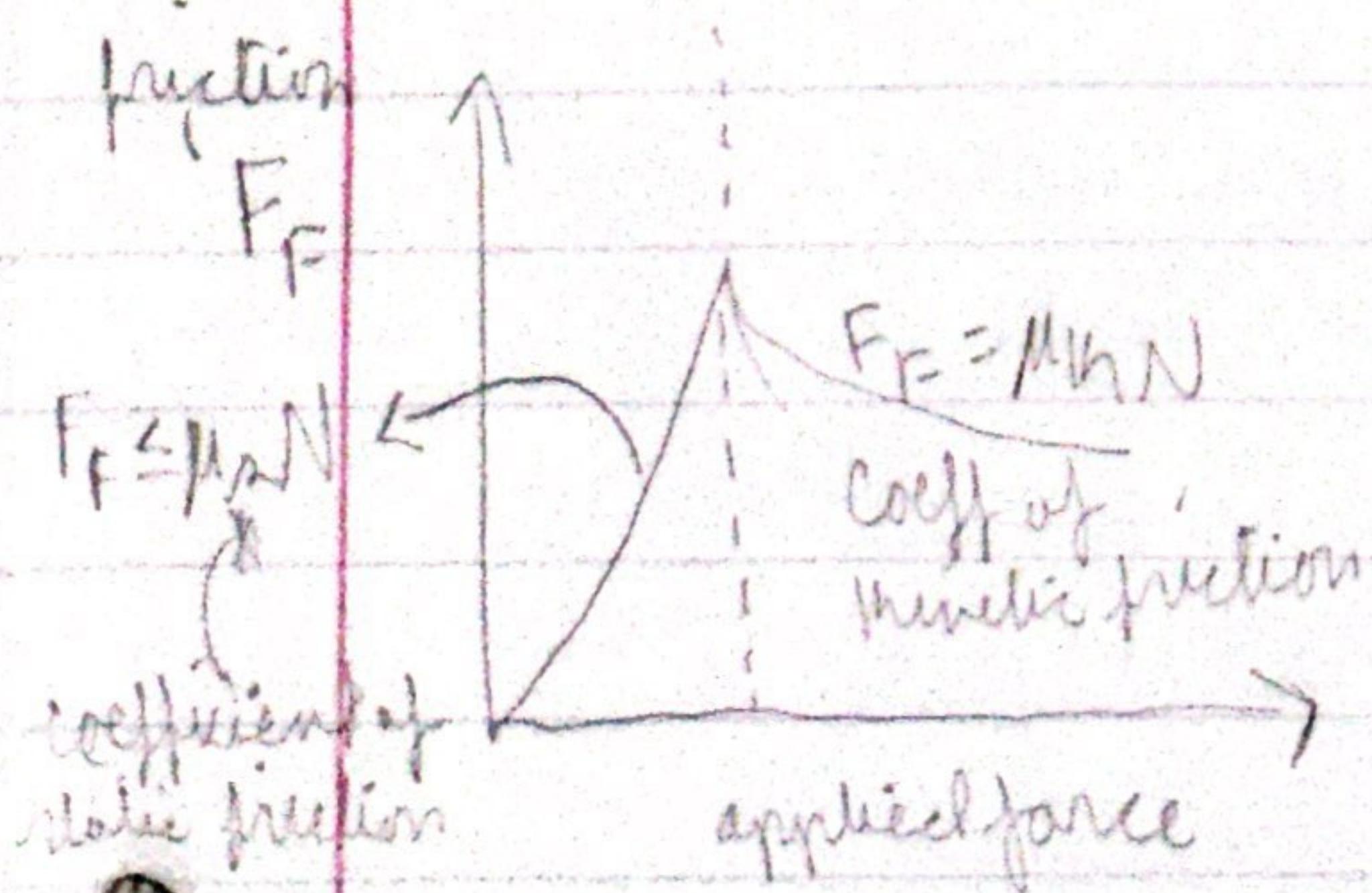
solve $F \leq \mu s N$ if yes
whether

of P.C. note $a_0 \neq \alpha r$

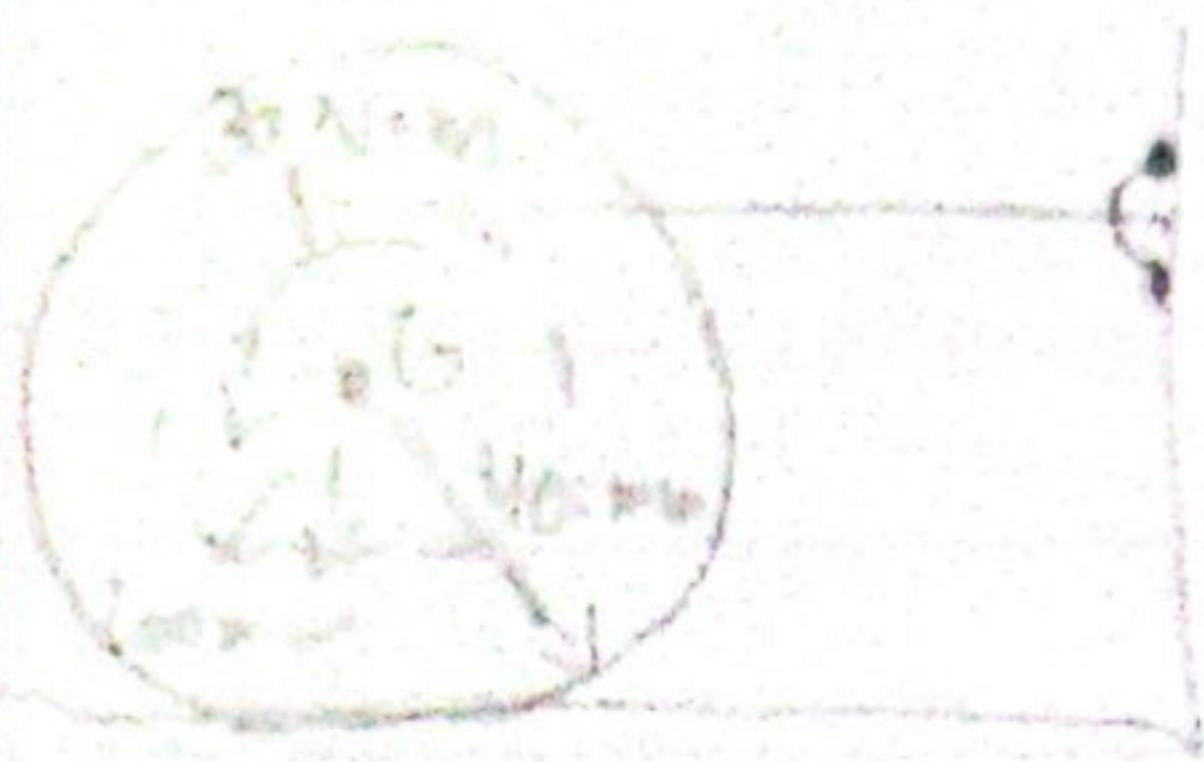
$(v_0 \neq \omega r)$, two objects move
over each other

$$F_f = \mu s N$$

F if no, then use this



Force acceleration II: problem



Radius of gyration $R = 0.25 \text{ m}$

$$\Rightarrow I_G = mR^2$$

Two objects moving
over each other
 $F_F = \mu_{\text{kin}} N$

Frictional assumption to start
the problem, always assume no slip

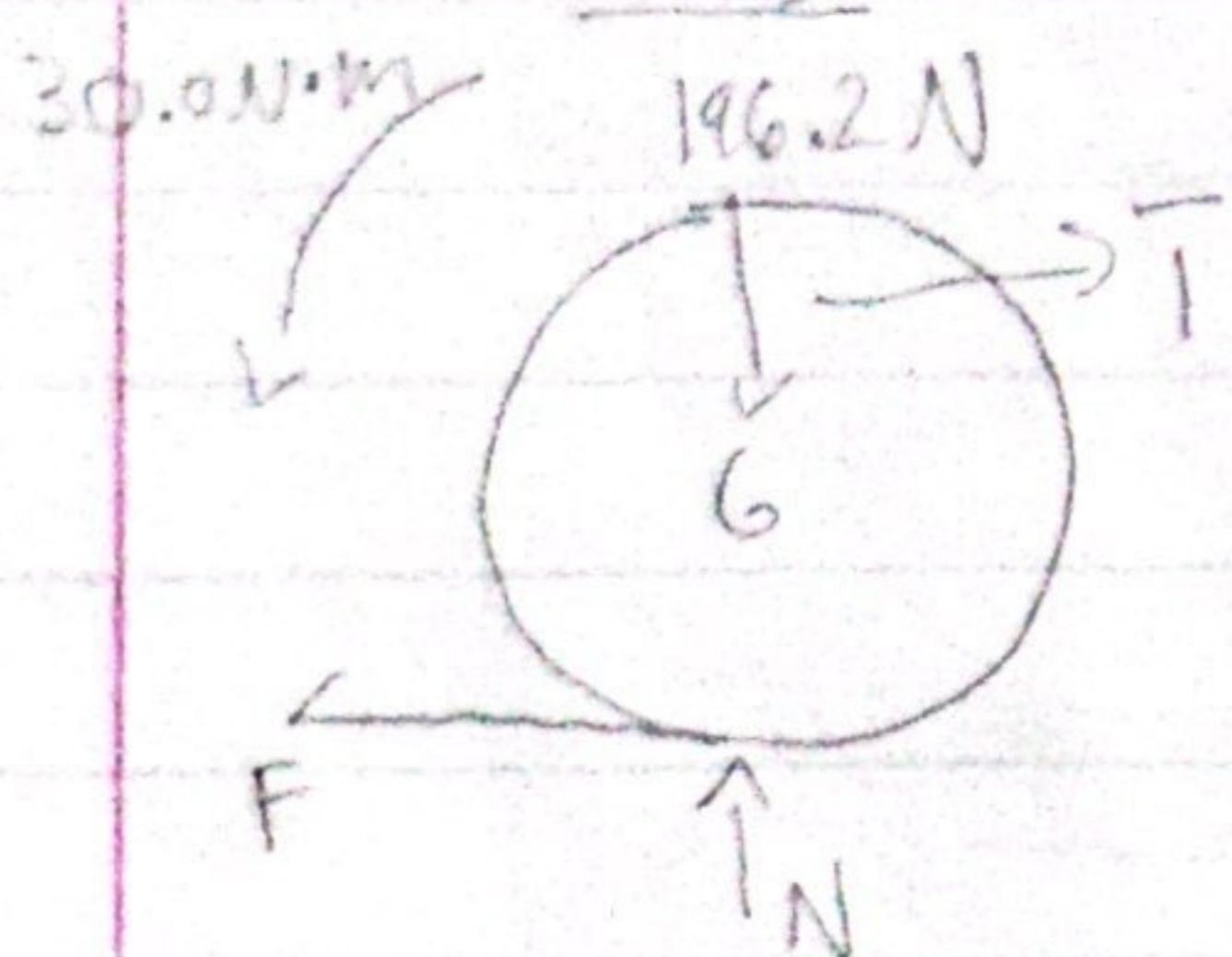
Classify motion:

$$m = 20 \text{ kg}$$

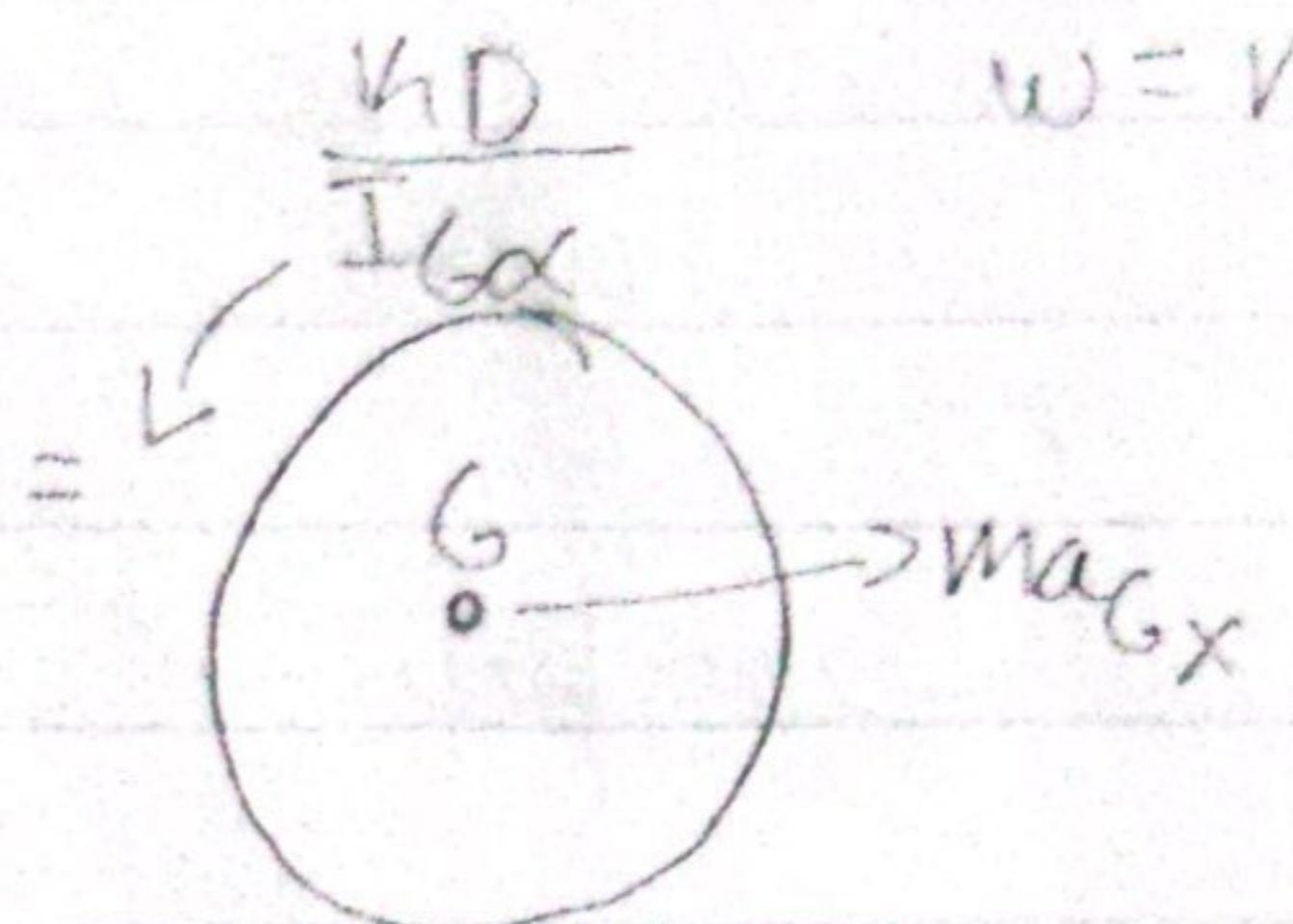
$$I_G = mR^2 = (20)(0.25)^2 = 1.25$$

$$w = Mg = (20)(9.81) = 196.2$$

FBD



FD



$$\rightarrow \sum F_x: -F + T = Ma_Gx = 20 a_Gx$$

must be slipping $\therefore F = \mu_{\text{kin}} N = 0.1(196.2) = 19.62 \text{ N}$
at ground

Statics:

1)

$$\sum F_x = 0$$

2)

$$\sum F_y = 0$$

$$\sum M_G = 0$$

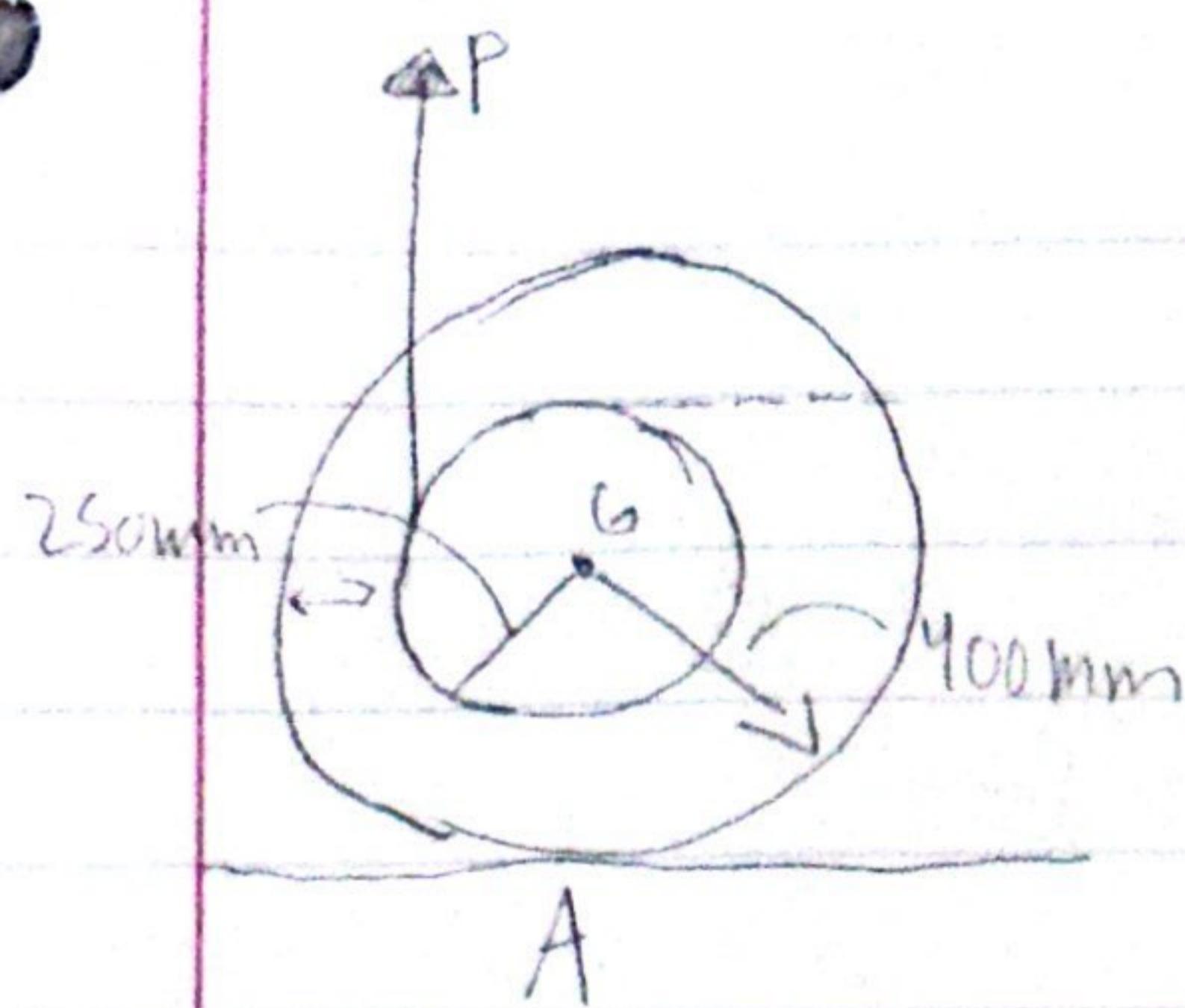
Dynamics:

$$\sum F_x = ma_Gx$$

$$\sum F_y = ma_Gy$$

$$\sum M_G = I_{G,d}$$

force acceleration III : problem 1



$$m = 10 \text{ kg}$$

radius of gyration $R_G = 0.3 \text{ m}$ $d_1 = 0.25 \text{ m}$

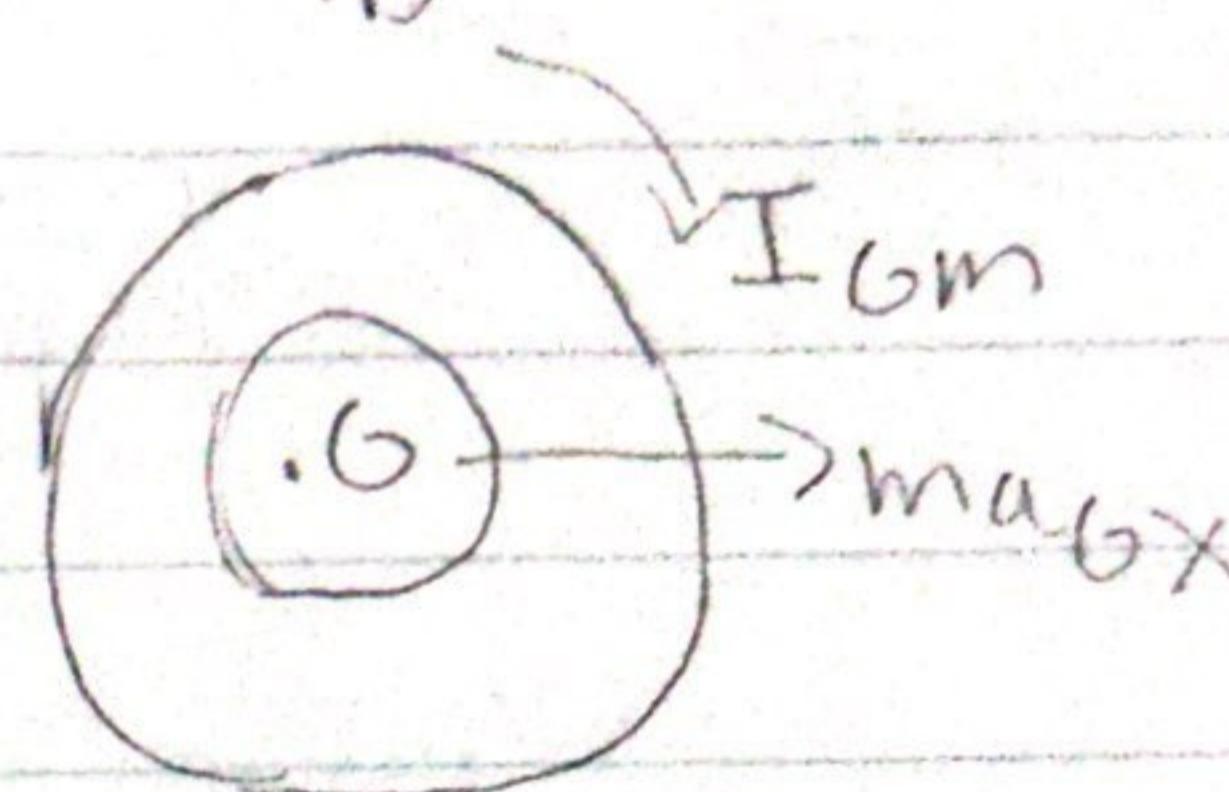
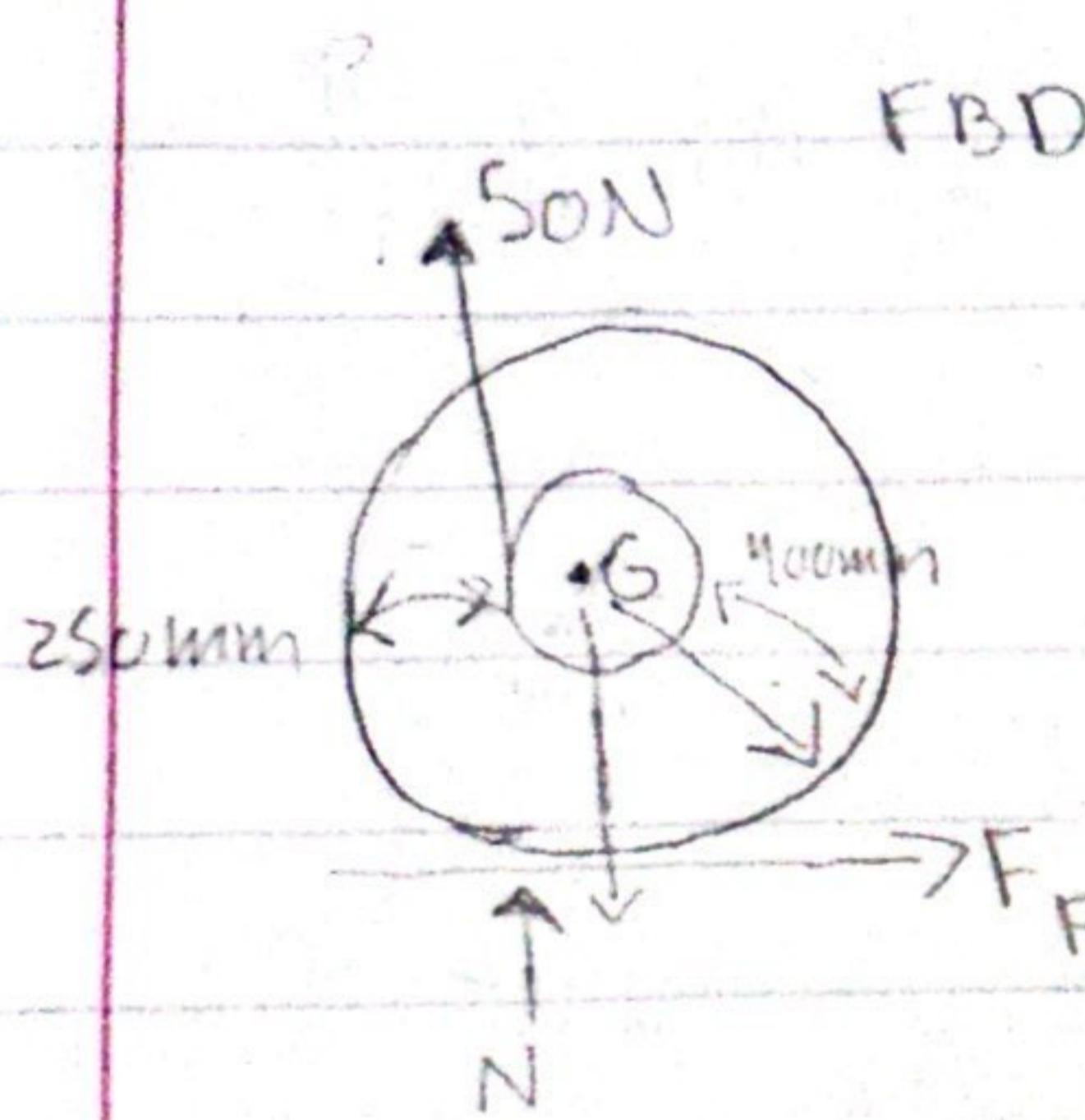
$$\mu_2 = 0.2 \quad \mu_m = 0.15 \quad P = 50 \text{ N} \quad d_2 = 0.4 \text{ m}$$

$$1 \text{ rpm}$$

$$I_G = mr^2 = (10 \text{ kg})(0.3)^2 = 0.9 \text{ kg m}^2$$

$$w = mg = (10)(9.81) = 98.1 \text{ N}$$

$$a_0 = \omega r = (9.81)(0.4) = 3.92 \text{ m/s}^2$$



$$1) \uparrow \sum F_y \Rightarrow 50 - 98.1 + N = 0 \quad N = 48.1$$

$$2) \rightarrow \sum F_x \Rightarrow F = ma_{6x} = 10a_{6x} = 10(0.4\alpha)$$

$$3) \sum M_G \Rightarrow -50(0.25) + F(0.4) = -0.9\alpha$$

$$\text{assume no slip} \quad F = 4\alpha$$

$$a_{6x} = \alpha r = 0.4\alpha \quad -50(0.25) + (0.4\alpha)(0.4) = -0.9\alpha$$

$$\alpha = 5.01 \text{ rad/s}^2$$

$$a_{6x} = 0.4\alpha = 2.0 \text{ m/s}^2 \quad F = 10a_{6x} = 20.0 \text{ N}$$

$$F_{\max} = \mu_2 N = 0.2(48.1 \text{ N}) = 9.62 \text{ N}$$

$F > F_{\max} \therefore$ slipping

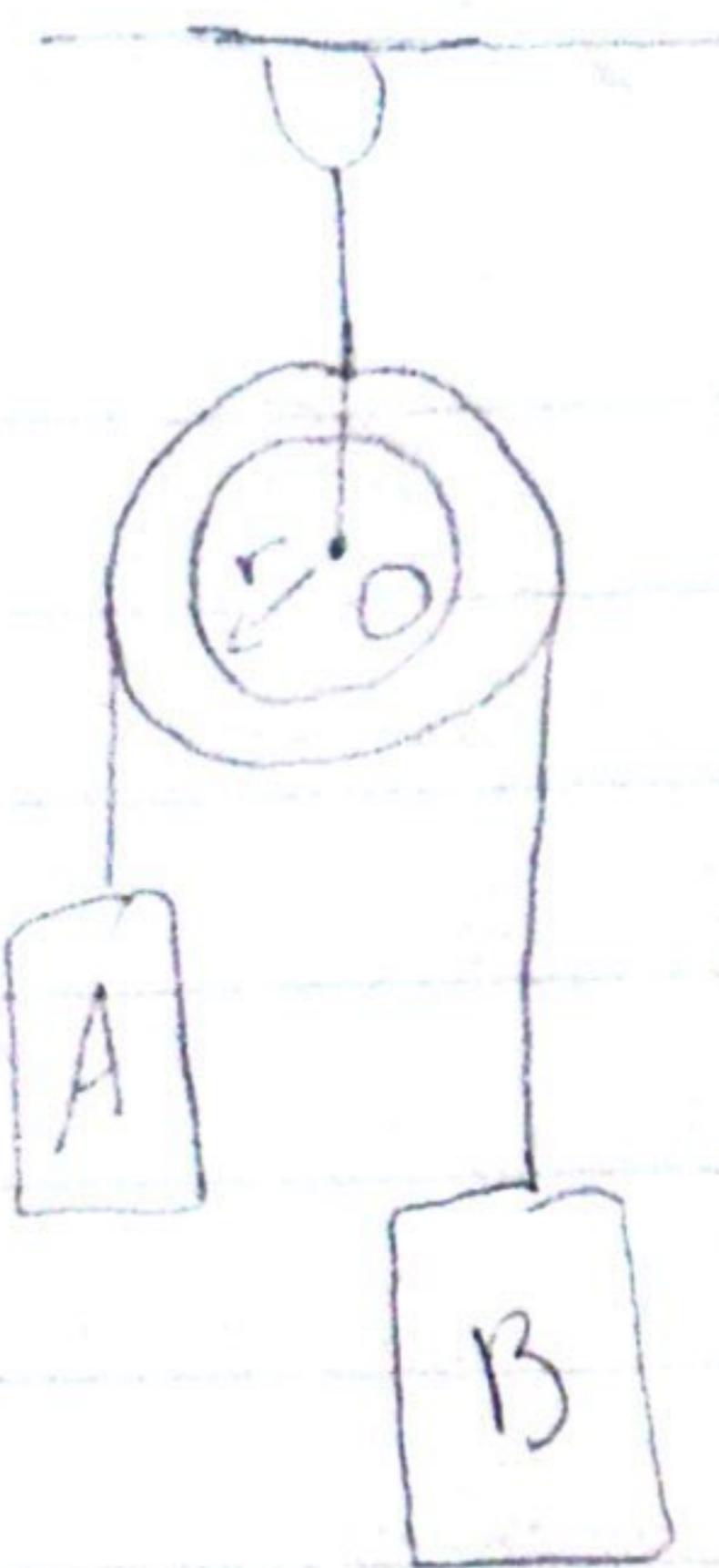
$$F = \mu_m N = 0.15(48.1 \text{ N}) = 7.21 \text{ N}$$

$$-50(0.25) + F(0.4) = -0.9\alpha$$

$$-50(0.25) + 7.21(0.4) = -0.9\alpha$$

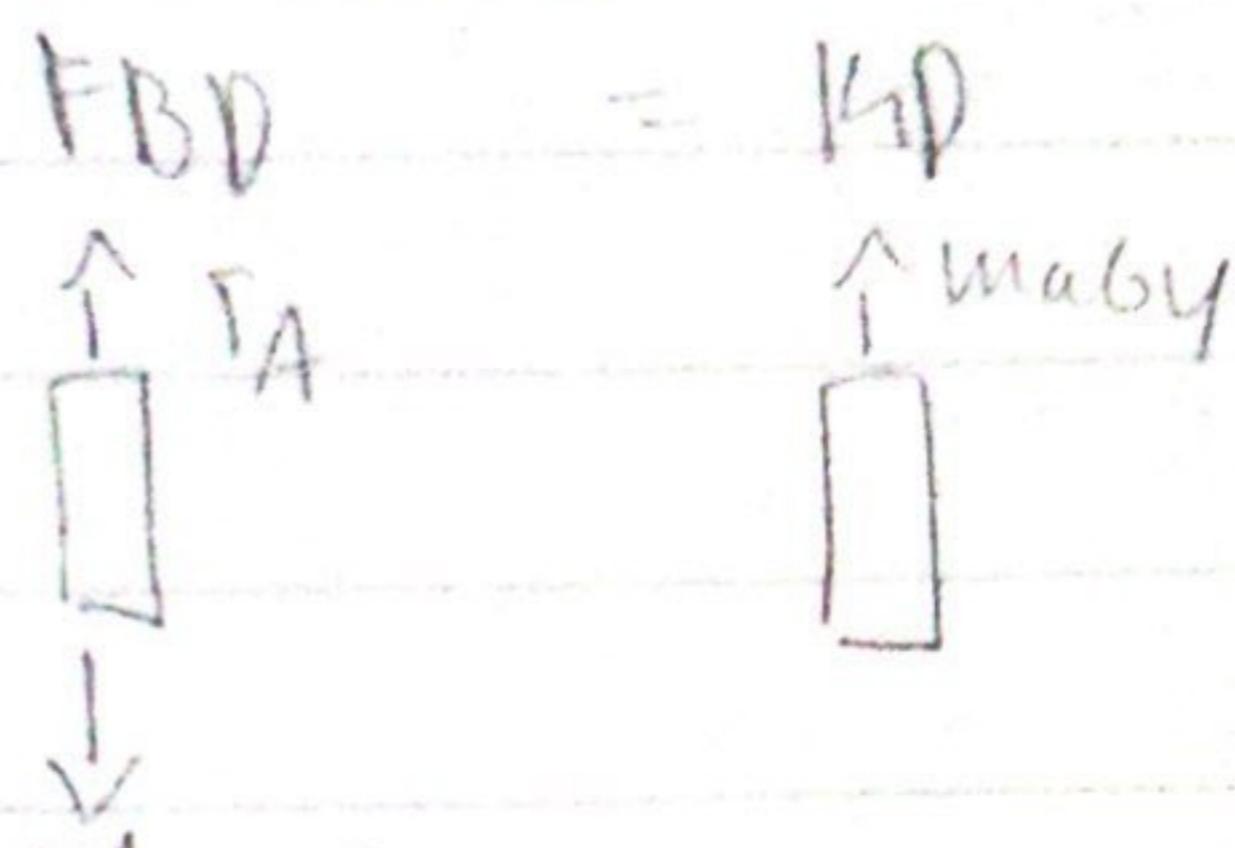
$$\boxed{\alpha = 10.68 \text{ rad/s}^2}$$

Force acceleration



$$\begin{aligned}m_A &= 5 \text{ kg} \\m_B &= 10 \text{ kg} \\m_{\text{pulley}} &= 3 \text{ kg} \\r &= 0.15 \text{ m}\end{aligned}$$

Block A:



$$\alpha = \arctan r$$

$$\uparrow \sum F_y = m_A g_y$$

$$T_A - W_A = m_A g_y \quad \alpha$$

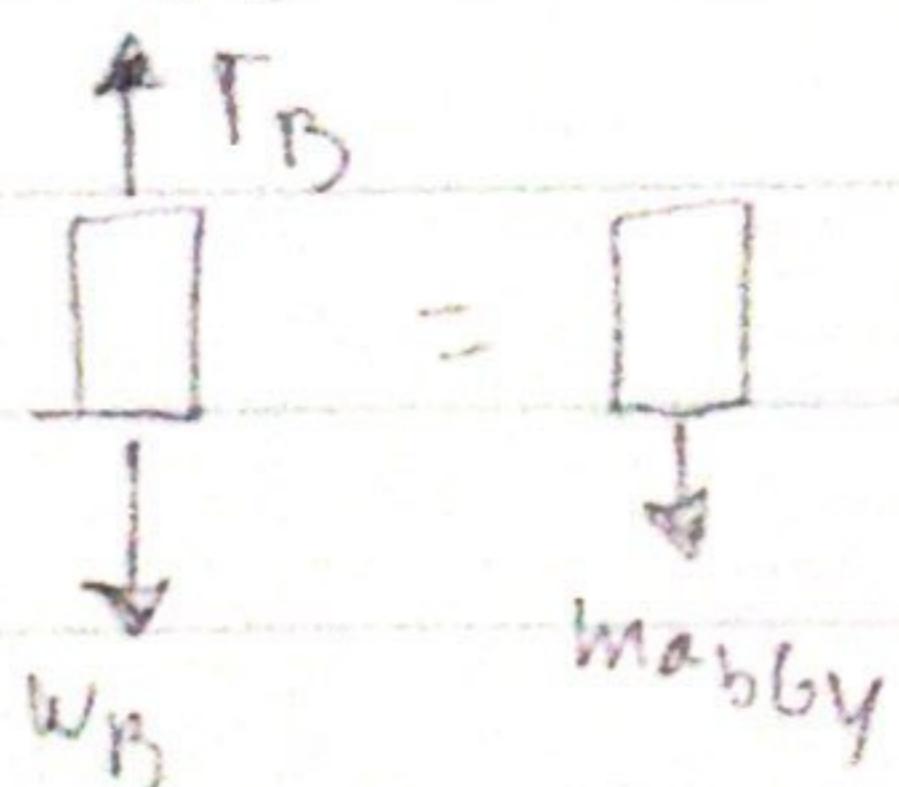
$$T_A - (5 \text{ kg})(9.81) = 5 \text{ kg} \alpha$$

$$T_A - 49 = (5 \text{ kg})(0.15 \text{ m}) \alpha$$

$$\textcircled{1} \quad T_A = 0.75 \alpha + 49$$

Block B:

$$\text{FBD} \quad \text{FD} \quad \uparrow \sum F_y = m_B g_y$$



$$T_B - W_B = -m_B g_y$$

$$T_B - (10 \text{ kg})(9.81) = -(10 \text{ kg}) \alpha$$

$$T_B - 98 = -(10 \text{ kg}) \alpha (0.15 \text{ m})$$

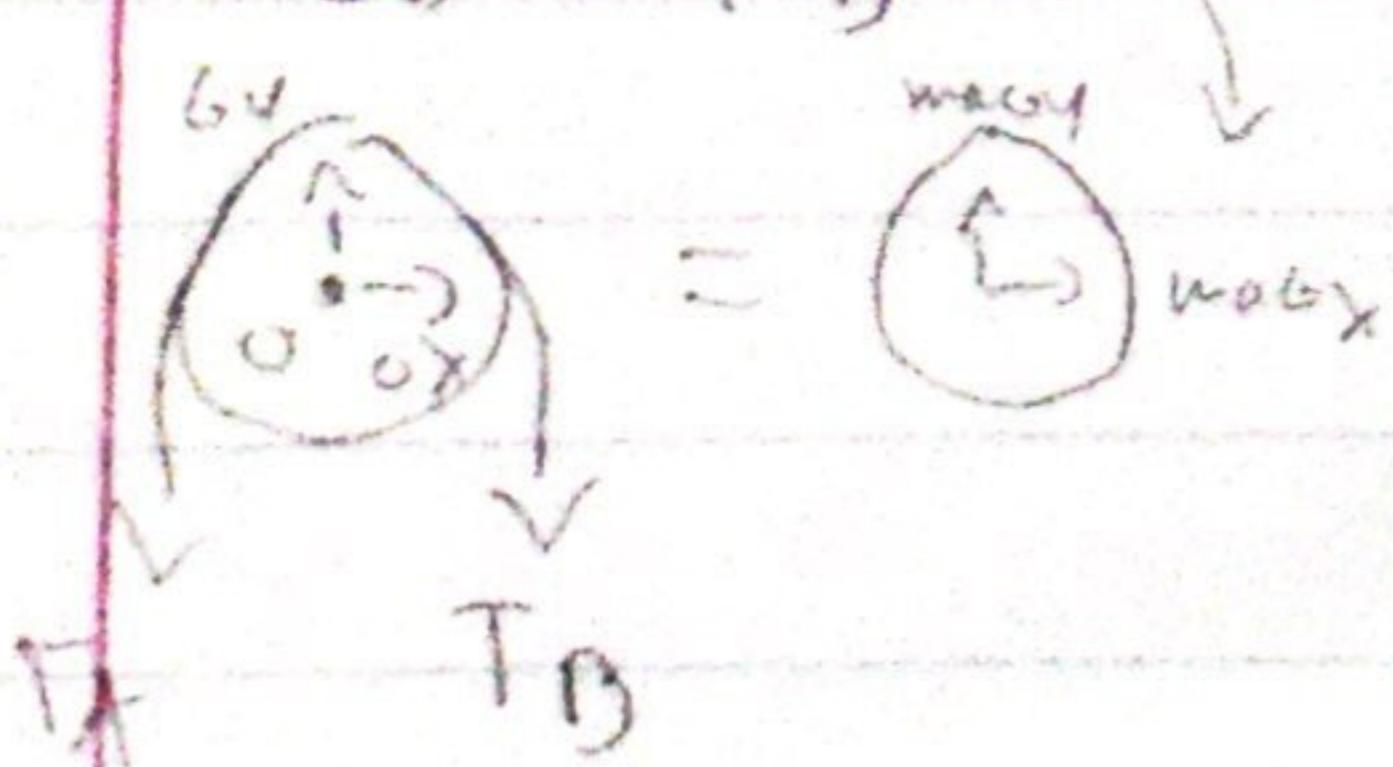
$$T_B = -1.5 \alpha + 98$$

$$I_0 = \frac{1}{2} m r^2$$
$$\frac{1}{2} (3)(0.15)^2$$

Drum

$$\vec{\sum M}_0 = I_0 \alpha \quad T_B (0.15 \text{ m}) - T_A (0.15 \text{ m}) = I_0 \alpha$$

$$\text{FBD} = \text{FD} \quad I_0 \alpha$$



$$T_B - T_A = \frac{1}{2} (3)(0.15) \alpha$$

$$T_B - T_A = 0.225 \alpha$$

$$T_B - T_A = 0.225 \alpha$$

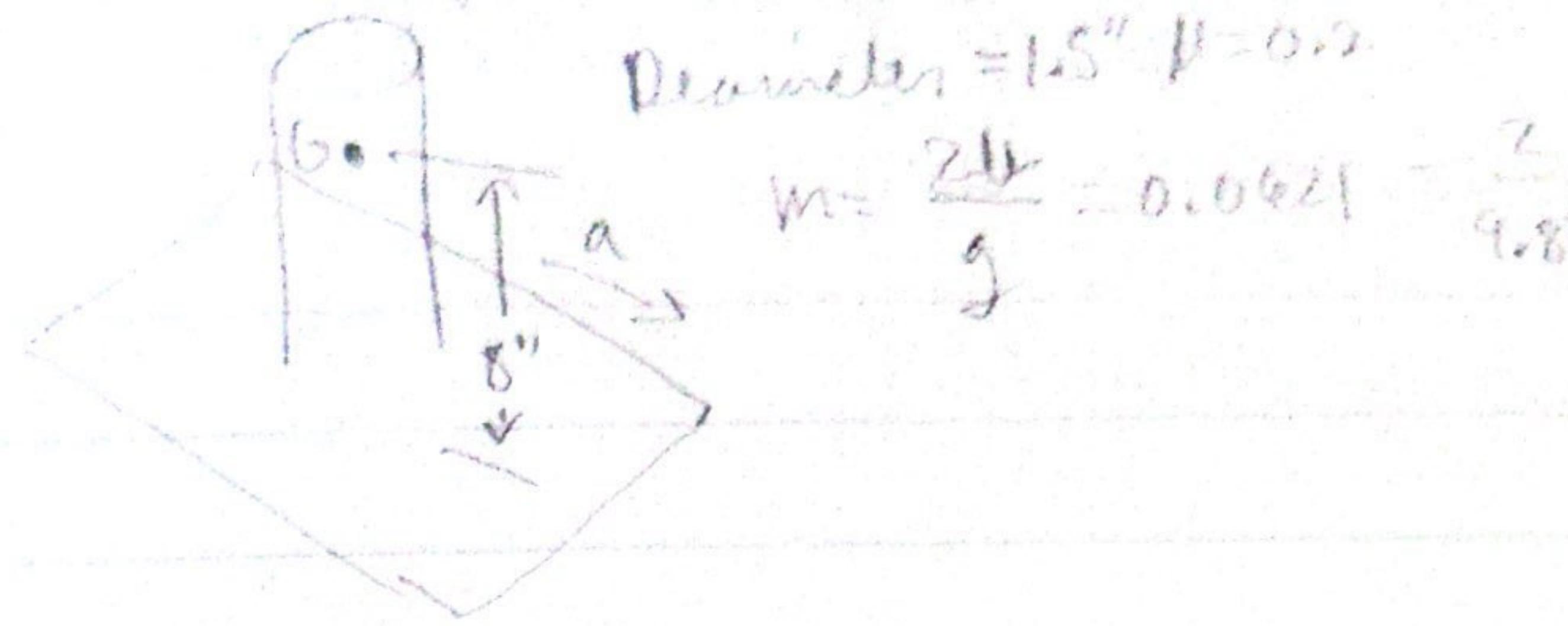
$$-1.5 \alpha + 98 - (0.75 \alpha + 49) = 0.225 \alpha$$

$$\textcircled{2} \quad \alpha = 19.798$$

$$\alpha = \omega r = \omega = (19.798)(0.15 \text{ m})$$

$$\omega = 2.97 \text{ rad/s}$$

Force acceleration I - Problem 1:

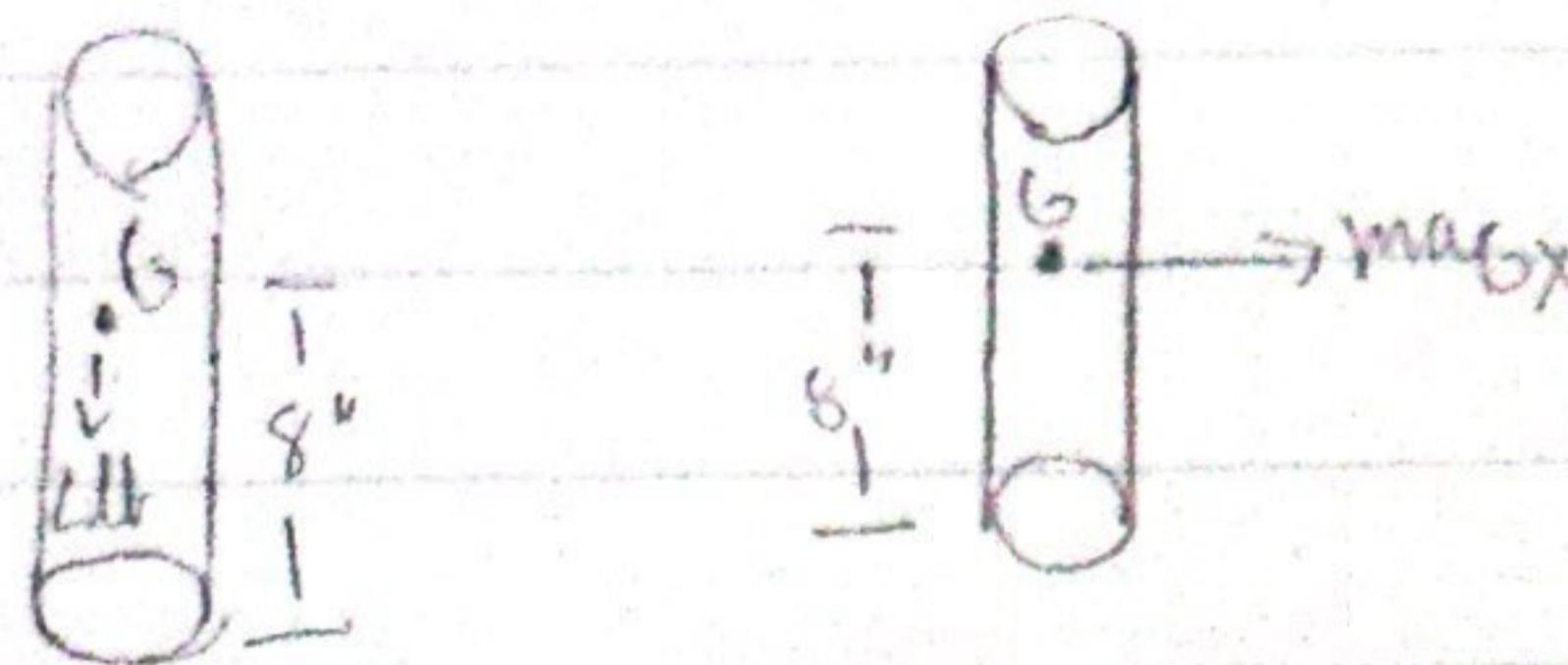


$$\text{Diameter} = 1.5" \quad \mu = 0.2$$

$$m = \frac{\pi}{4} \times 1.5^2 \times 8 = 0.0621 \times 9.81$$

$$\text{FBD} = \text{FD}$$

$$\rightarrow \sum F_x = ma_{6x} = 0.0621 a_{6x}$$



$$\uparrow \sum F_y = ma_{6y} = N - 2 = 0$$

$$N = 2 \text{ lbs}$$

$$F \uparrow \quad N \leftarrow$$

$$\text{L} \sum M_G = I_{6x} \Rightarrow \Theta F - 2x = 0$$

$$F = \mu_2 N = 0.2(2) = 0.4 \text{ lb}$$

$$\Theta F - 2x = 0 \Rightarrow 0.4 - 2x = 0 \quad x = 1.6" > 0.75"$$

assume tipping

$$x = 0.75$$

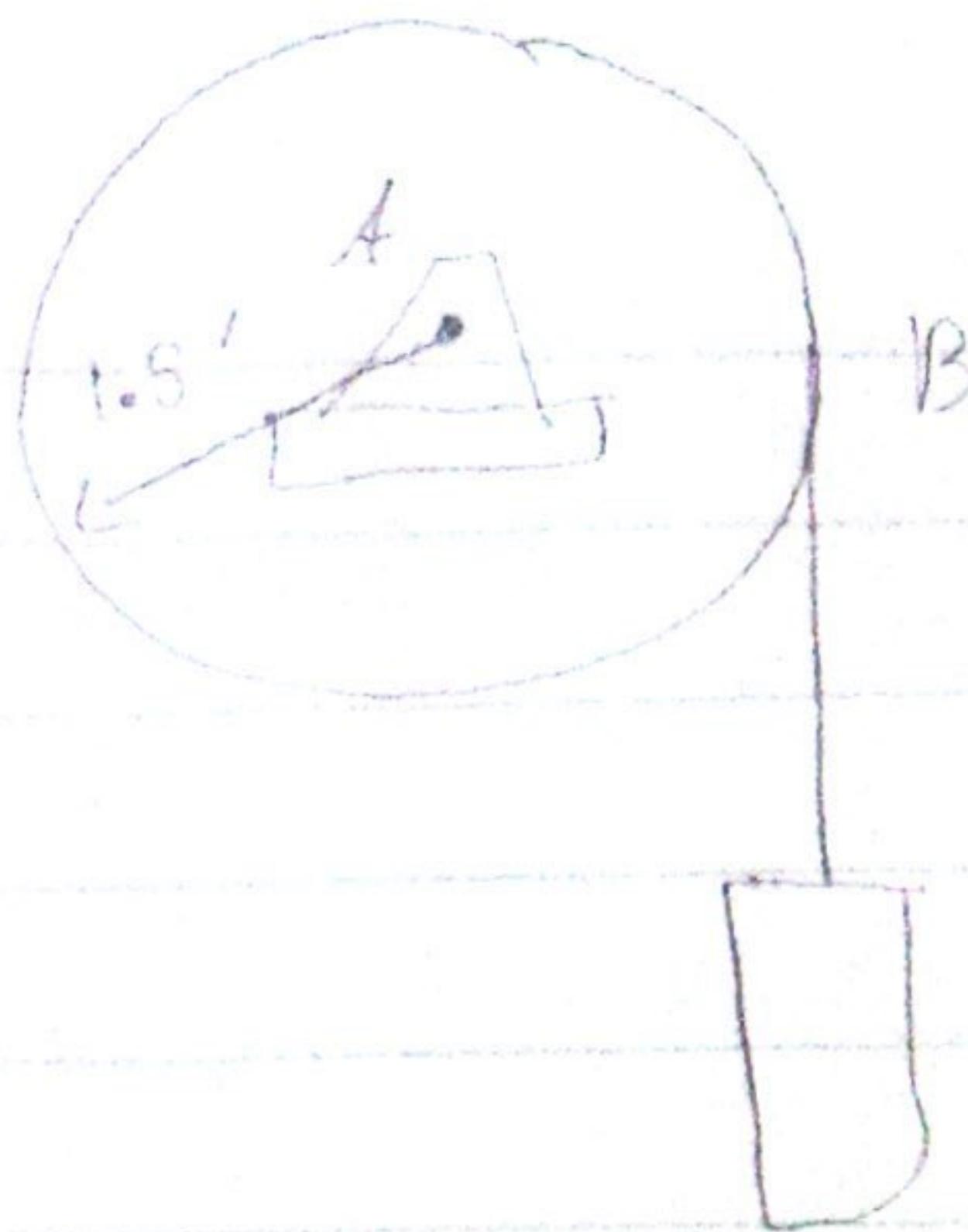
$$\Theta F = 2x \quad \Theta F = 2(0.75) \quad F = 0.0621 a_{6x}$$

$$F = 0.1875$$

$$0.1875 = 0.0621 a_{6x}$$

$$a_{6x\max} = 3.02 \text{ ft/s}^2$$

Force acceleration:



$$m_{drum} \cdot 2\pi r = \frac{20}{32.2} = 0.6211$$

$$I_G = 0.8\pi r^2, (0.6211)(0.8^2) = 0.397$$

$$m_B = 12\text{lb} = \frac{12}{32.2} = 0.3726$$

Properties:

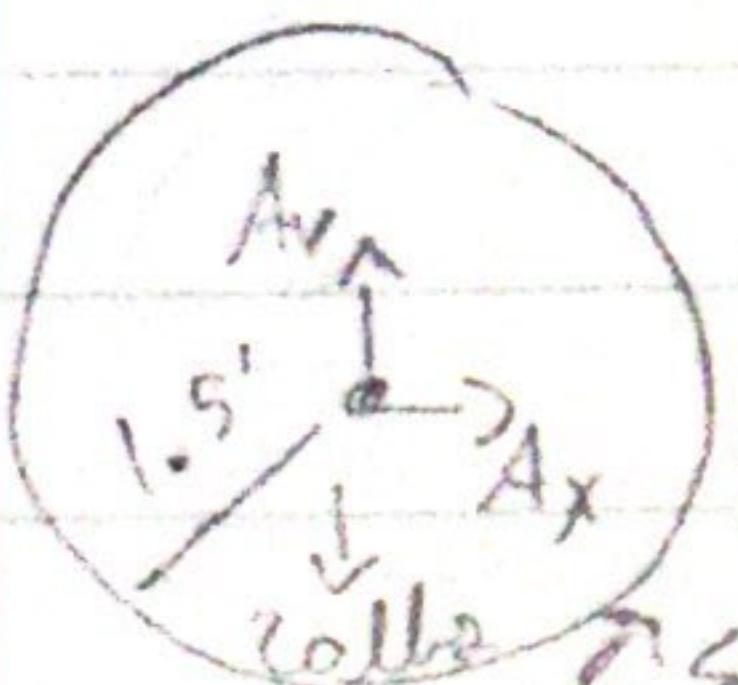
$$I_G = mR^2$$

$$m_d = \frac{20}{32.2} = 0.621 \quad w_B = 12\text{lb/s}$$

$$w_d = 2\pi R/s, \quad R = 0.8\text{ft}$$

$$m_B = \frac{12}{32.2} = 0.373$$

FBD Wheel:



$$\sum F_x = Ax = 0$$

$$\sum F_y = Ay - 20 - T = 0$$

$$\sum M = 1.5T = I_{Gd}$$

$$Ay - 20 = T \quad 3(1.5)(Ay - 20) = 0.397\alpha$$

$$1.5T = 0.397\alpha$$

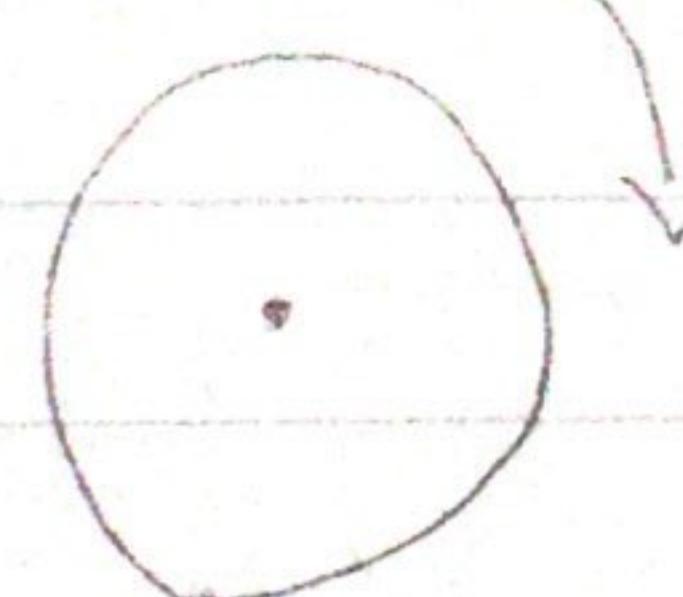
Motion:

Drum: Roto

Block: Translation

1D Wheel

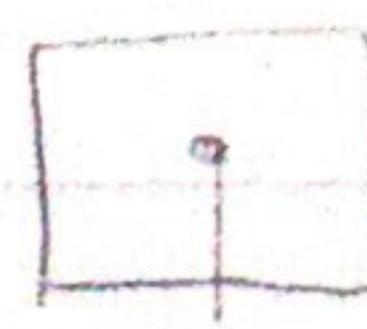
$$I_{Gd}$$



FBD Block:



1D Block



$$m_{block} g_{block}$$

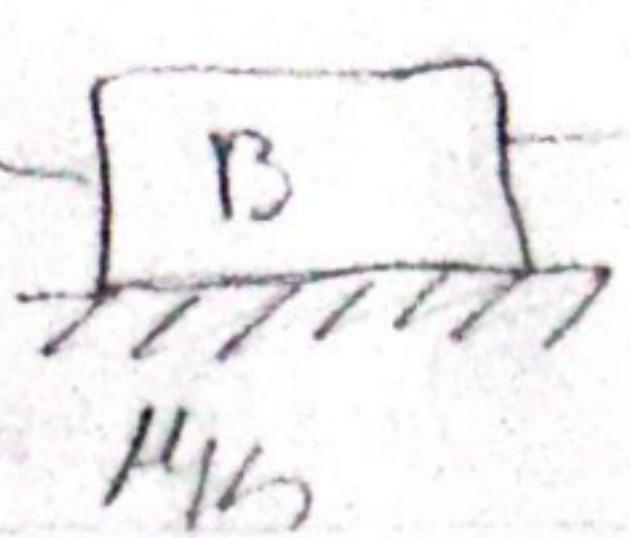
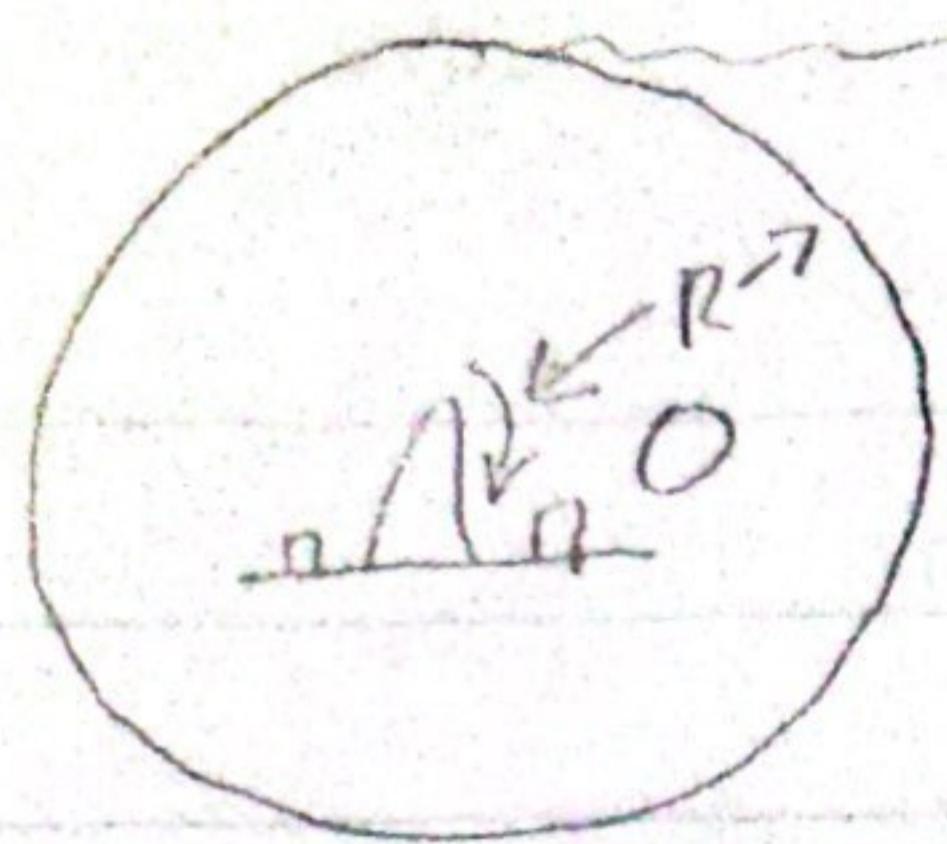
$$\sum F_y = T - 12 = m_{block} g_{block}$$

$$Ay - 20 - 12 = 0.393 a_{Gx}$$

$$Ay - 8 = 0.373 \times 1.5\alpha$$

$$\frac{Ay - 8}{0.56} = 0.56\alpha \quad \frac{Ay - 14.28}{0.56} = \alpha$$

$$\frac{Ay - 8}{0.56} = \alpha$$



$m_p = 20 \text{ kg}$
 $R_p = 0.5$
 $m_{\text{rock}} = 5 \text{ kg}$
 $P = 100 \text{ N}$
 $\mu_{\text{fr}} = 0.15$

$$\begin{aligned}
 \sum F_x &= m_B a & P - T - \mu_{\text{fr}} m_B g &= m_B a \\
 100 - T - (0.15 \times 5 \times 9.81) &= 5a \\
 100 - T - 7.3575 &= 5a \\
 92.6425 - T &= 5a \text{ eqn 1}
 \end{aligned}$$

$$\sum M_O = I_O \alpha$$

$$T R = I_O \alpha$$

$$I_O = \frac{1}{2} m_B R^2$$

$$T(0.5) = \left(\frac{1}{2} \times 20 \times (0.5)^2 \right) \alpha = 0.5T = (2.5)\alpha \quad T = 5\alpha$$

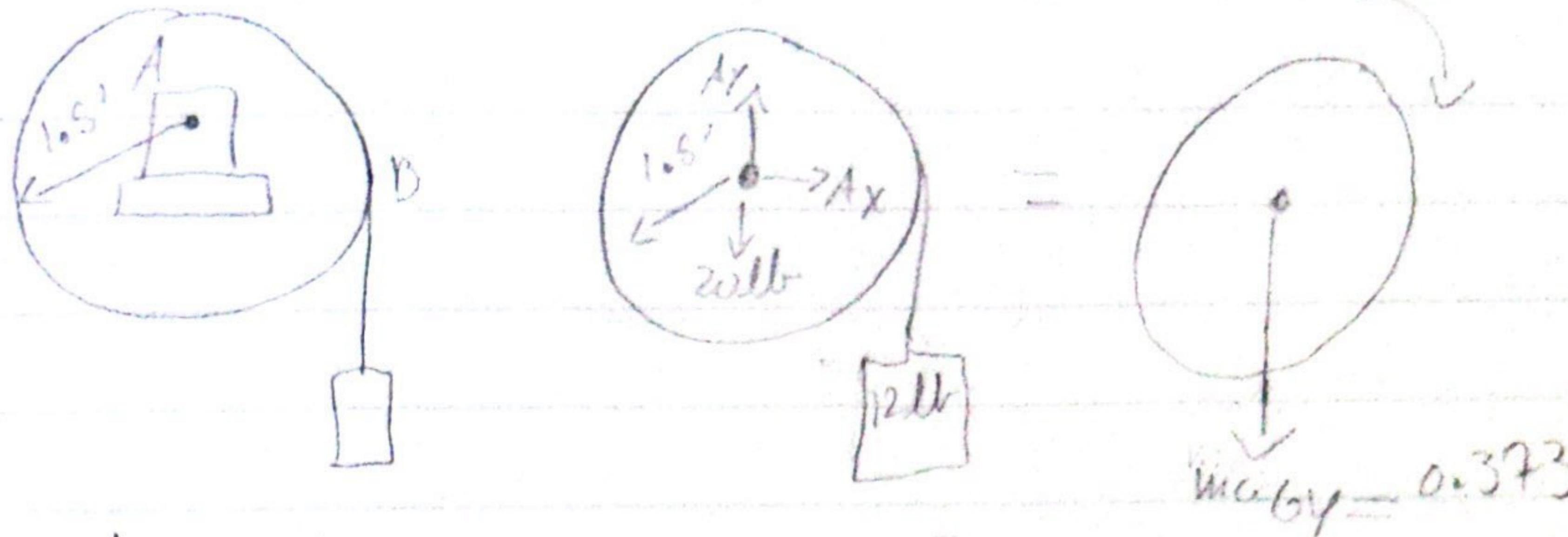
$$T = 5 \left(\frac{a}{0.5} \right) = 10a = T \text{ eqn 2}$$

$$92.6425 - 10a = 5a \quad 92.6425 = 15a \quad a = \frac{92.6425}{15} = \boxed{6.175 \text{ m/s}^2}$$

$$T = 10a = 10(6.175) = \boxed{61.76 \text{ N}}$$

Force acceleration I: problem 3

$$FBD = HD \underline{I}_{col}$$



$$W_0 = 20\text{W}$$

$$F = 12 \text{ lb} \quad \underline{12 \text{ lb}} = M_p(32.2)$$

$$h = 0.8 ft$$

$$F = ma \quad M_B = 0.373$$

$$M_D = \frac{20}{32.2} = 0.62$$

$$T_G = m k^2$$

$$I_6 = 10.621(0.8)^2 = \boxed{P_2 397.44}$$

$$+\triangleright \sum F_y = ma_y \quad \{ \sum M_g = I_{Gx} \cdot \ddot{\theta} = 1.5T = -0.397a$$

$$Ax = 0$$

$$\uparrow \sum F_y = M_B a_{Gy}$$

$$\sum \Sigma F_y = m a_y$$

$$T-12 = 0.37364$$

$$Ay - 20 - \bar{I} = 0$$

$$a_B = 1.5d \quad a_B = a_{Gy}$$

$$T-12 = -(0.373)64$$

$$a_{xy} = 1.5a$$

$$a_T = \alpha V \text{ a block} = a_B = \alpha g y = 1.5 \alpha$$

$$T-12 = (0.373)(1.5d) \quad T + 0.56d = 12$$

$$Ay - w - t = 6 \Rightarrow -t - Ay = 20$$

$$1.5 \Gamma = 0.397 \alpha$$

$$1.5T - 0.397a = 0$$

$$T = 3.85 \text{ lbs} \quad a = 14.55 \text{ in/sec}^2 \quad A_y = 23.85 \text{ in}^2$$

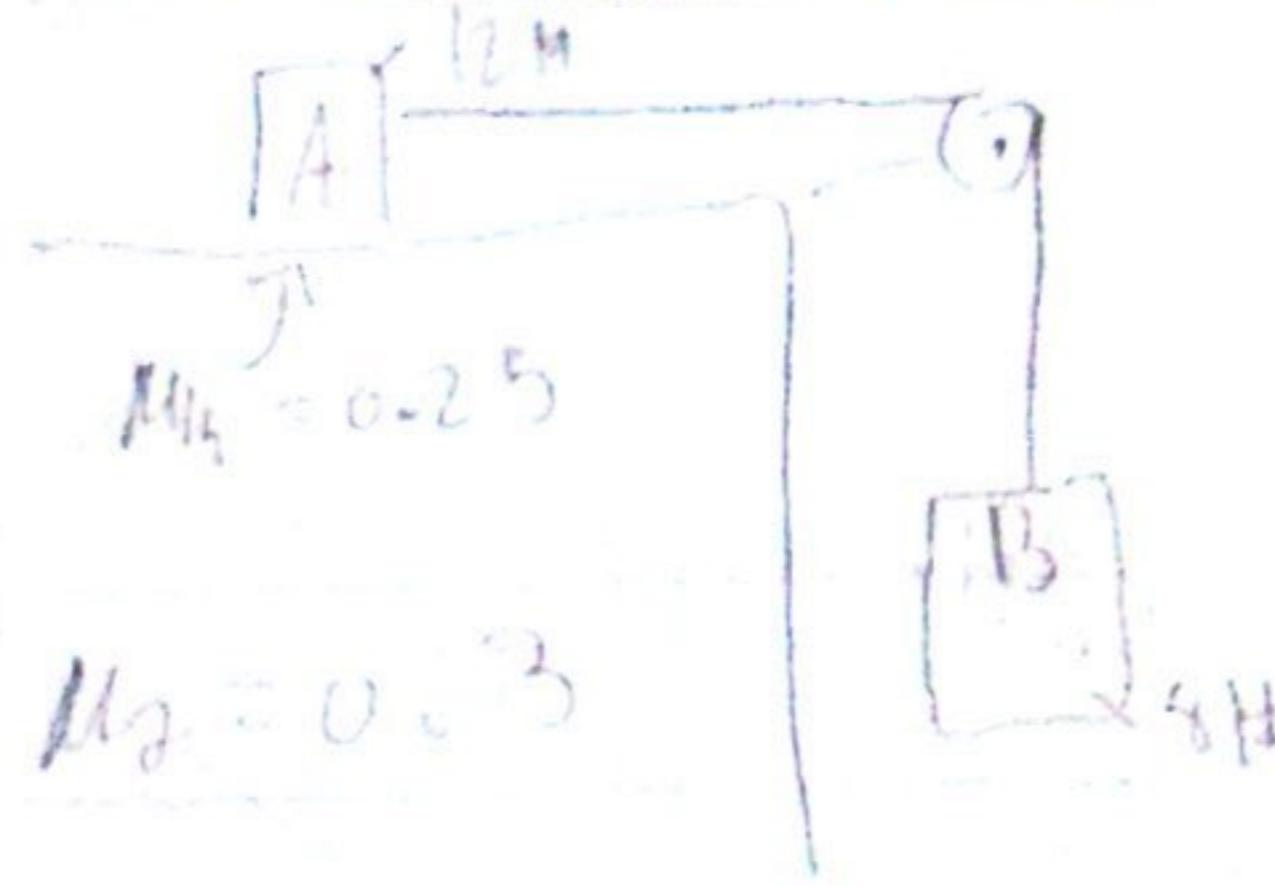
$$\Sigma M_G = I_{Gd}$$

$$1.5(12) = -0.397 + a$$

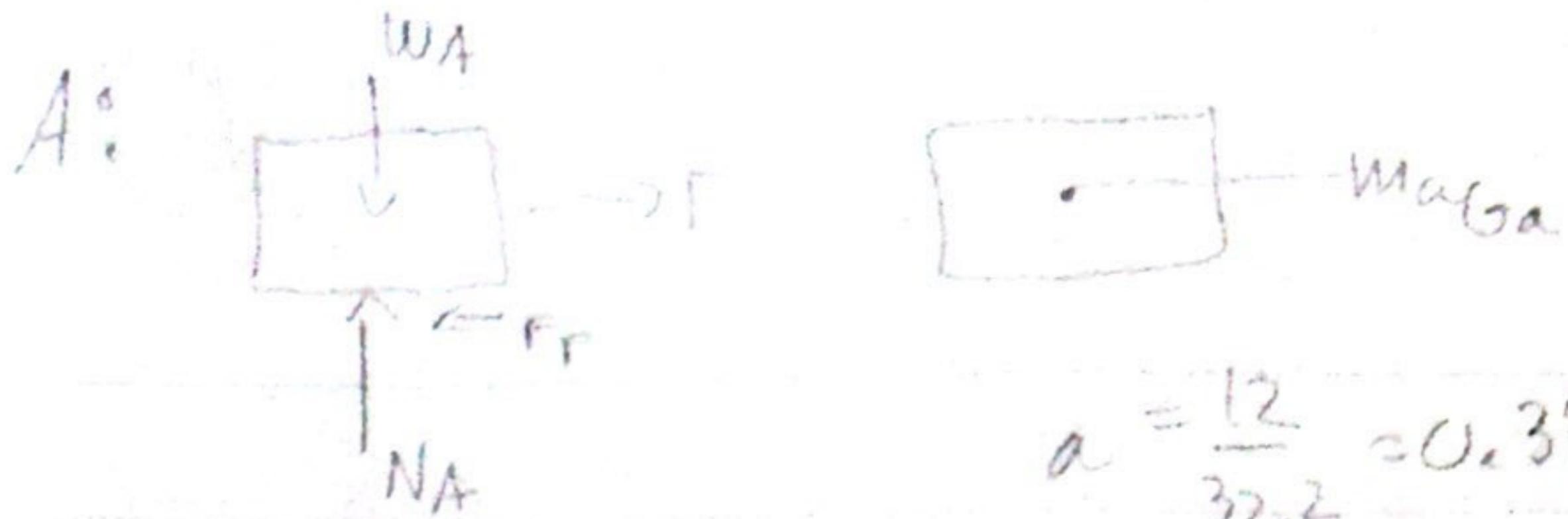
$$\alpha = 45.3 \text{ nm}^2$$

$$\begin{bmatrix} 1 & 0.56 & 0.7 \end{bmatrix} \begin{Bmatrix} \alpha \\ \beta \\ \gamma \end{Bmatrix} = \begin{Bmatrix} 12 \\ 20 \\ 0 \end{Bmatrix}$$

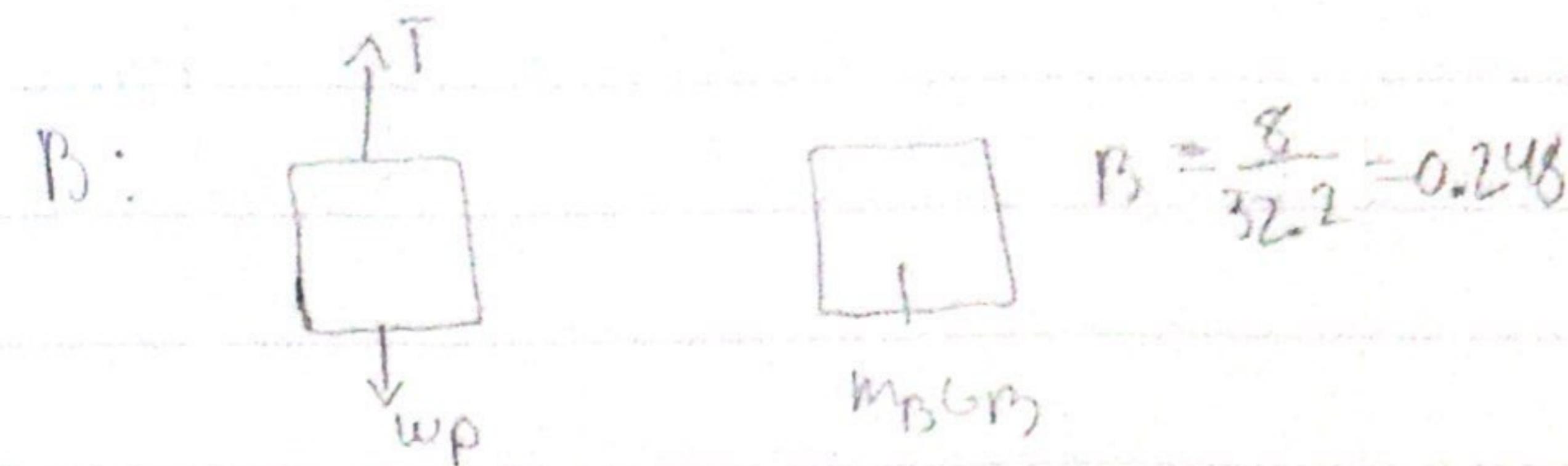
Force acceleration:



FBD $\Rightarrow 14 \text{ N}$



$$a = \frac{12}{32.2} = 0.373$$



$$B = \frac{8}{32.2} = 0.248$$

$$A: \sum x \Rightarrow T - F_f = m_A a \quad (1)$$

$$B: \sum x \Rightarrow 0$$

$$\sum y \Rightarrow N_A - w_A = 0$$

$$\sum y \Rightarrow T - 8 \text{ N} = m_B a_B$$

$$F_f = \mu N_A = 0.25(12)$$

$$\frac{T-8}{-0.248} = a \quad (2)$$

$$F_f = 3 \text{ N}$$

$$\sum x \Rightarrow T - F_f = m_A a \quad T - 3 = 0.373 \left(\frac{T-8}{-0.248} \right) \frac{0.373}{-0.248} = 1.504 \left(\frac{T-8}{-0.248} \right)$$

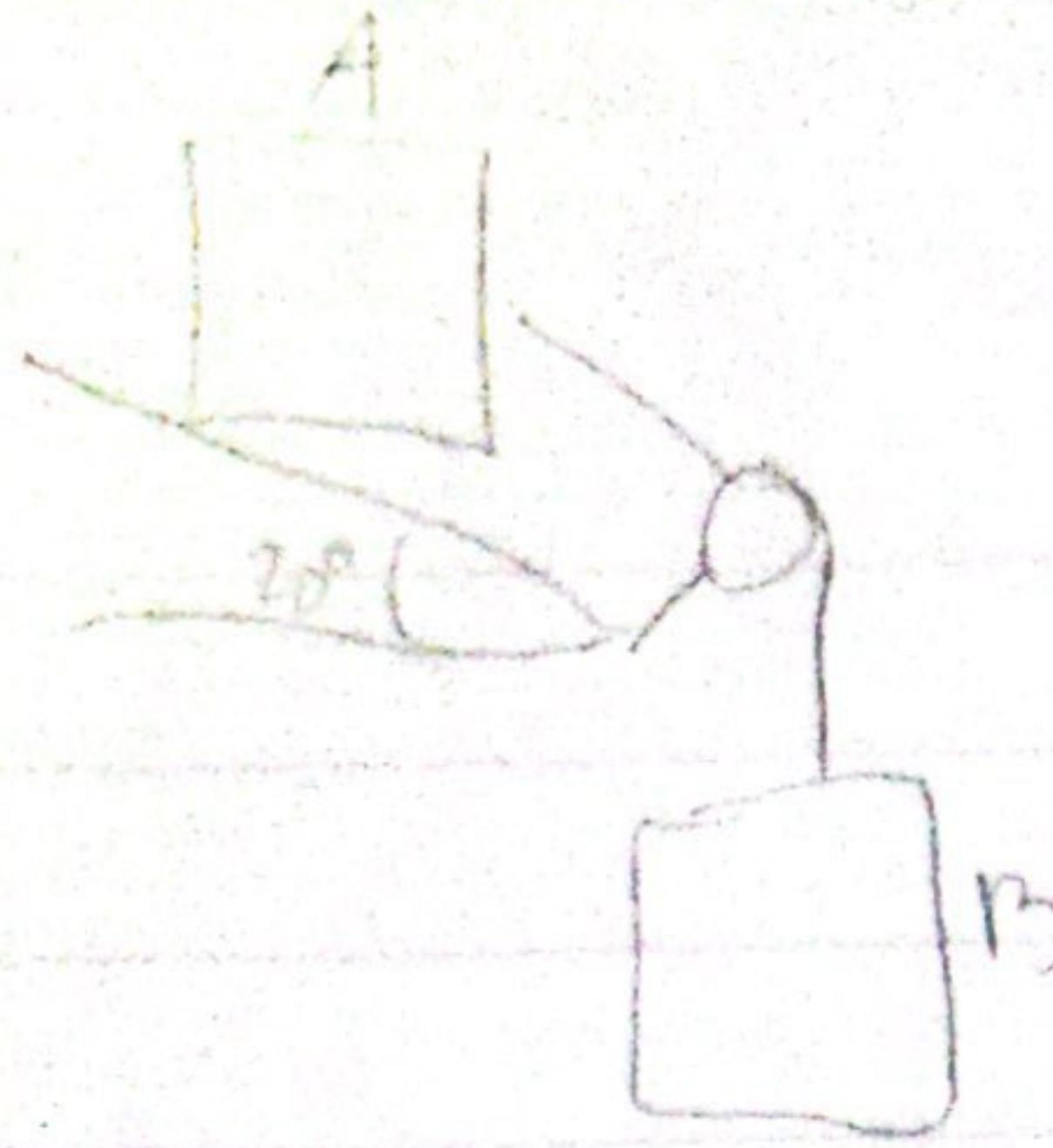
$$1.504T - 1.504 \times 8$$

$$2.504T = 15.03$$

$$1.504T - 12.032$$

$$T = 6 \text{ N}$$

Force acceleration:



Classify motion:

Blocks A & B: Translation

Properties:

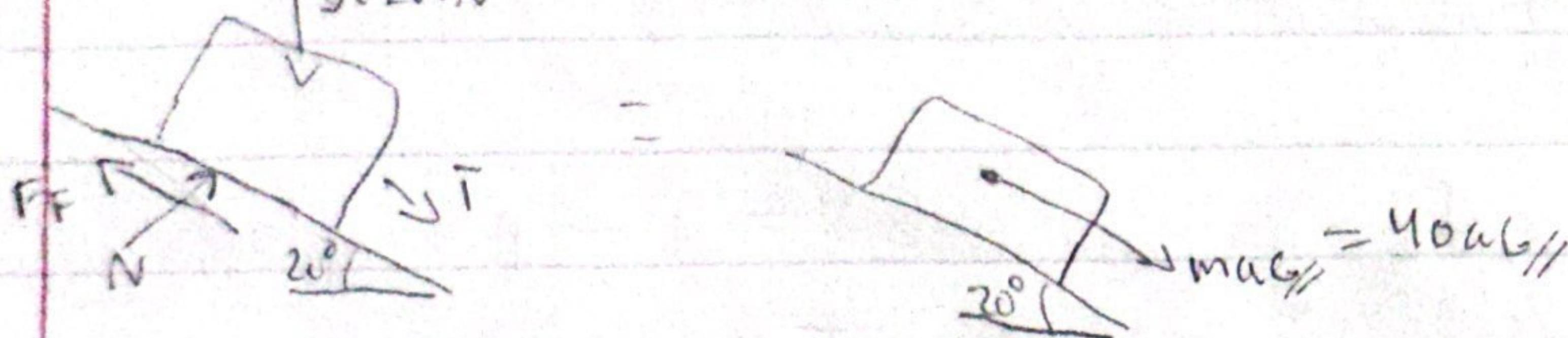
$$m_A = 40 \text{ kg} \quad W_A = 40(9.8) = 392.4 \text{ N}$$

$$m_B = 30 \text{ kg} \quad W_B = 30(9.8) = 294.3 \text{ N}$$

$$\mu_s = 0.2 \quad \mu_k = 0.15$$

$$FBD = \text{FD}$$

392.4 N



A:

$$F_F = \mu_k N = 0.15 N = 0.15(369) = 55.4 \text{ N}$$

$$\sum \text{EF}_\perp = m_A g_\perp = N - 392.4 \cos 20^\circ = \phi = N = 369 \text{ N}$$

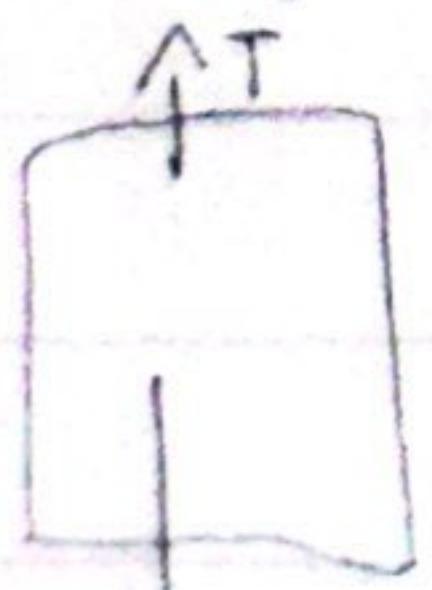
$$\sum \text{EF}_\parallel = m_A g_\parallel \Rightarrow T - F_F + 392.4 \sin 20^\circ = 40 a_G_\parallel$$

$$T - 55.4 \text{ N} + 392.4 \sin 20^\circ = 40 a_G_\parallel$$

$$(1) T - 40 a_G_\parallel = -78.86$$

B:

$$FBD = \text{FD}$$



294.3 N

$$(2) \sum F_y = m_B g \Rightarrow 294.3 - T = 30 a_Y$$

kinematic: $a_{G\parallel} = a_Y$

$$(1) T - 40 a_{G\parallel} = -78.86$$

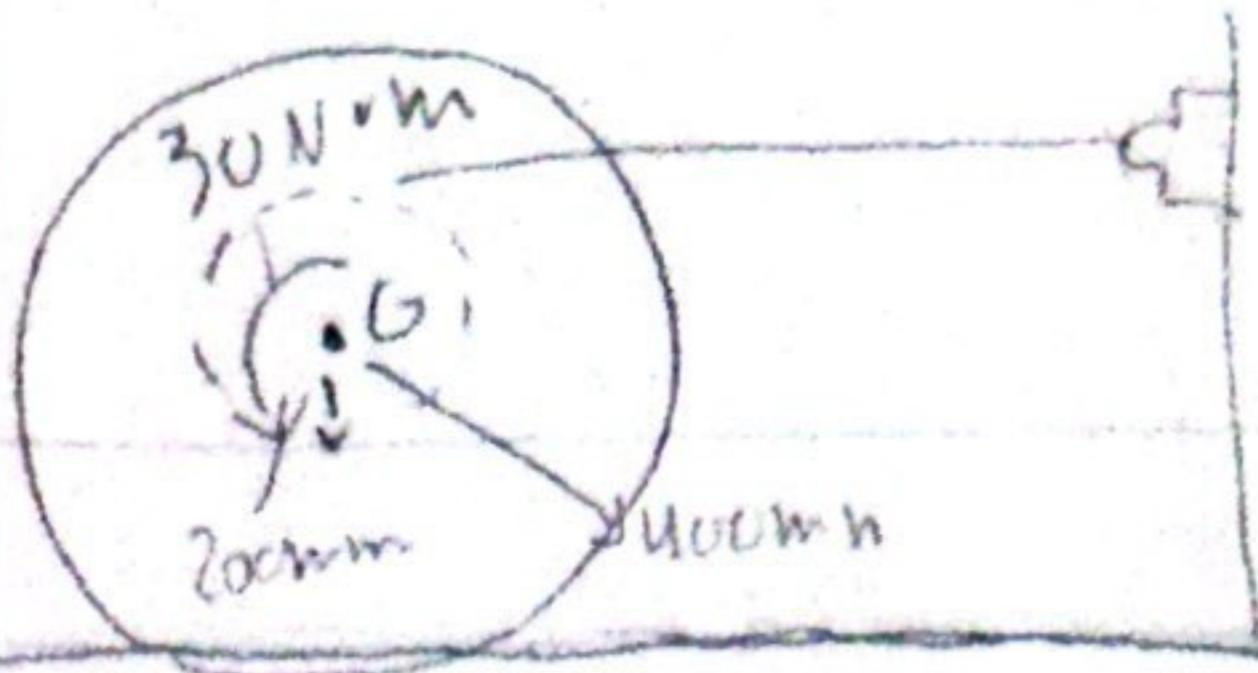
$$(2) T + 30 a_{G\parallel} = 294.3$$

$$\boxed{T = 134 \text{ N} \quad a_{G\parallel} = 5.32}$$

Force acceleration:

$$M=20 \text{ kg} \quad r_{0j}=250 \text{ mm} \quad \mu_D=0.1$$

$$C=30 \text{ mm}$$



Classify motion

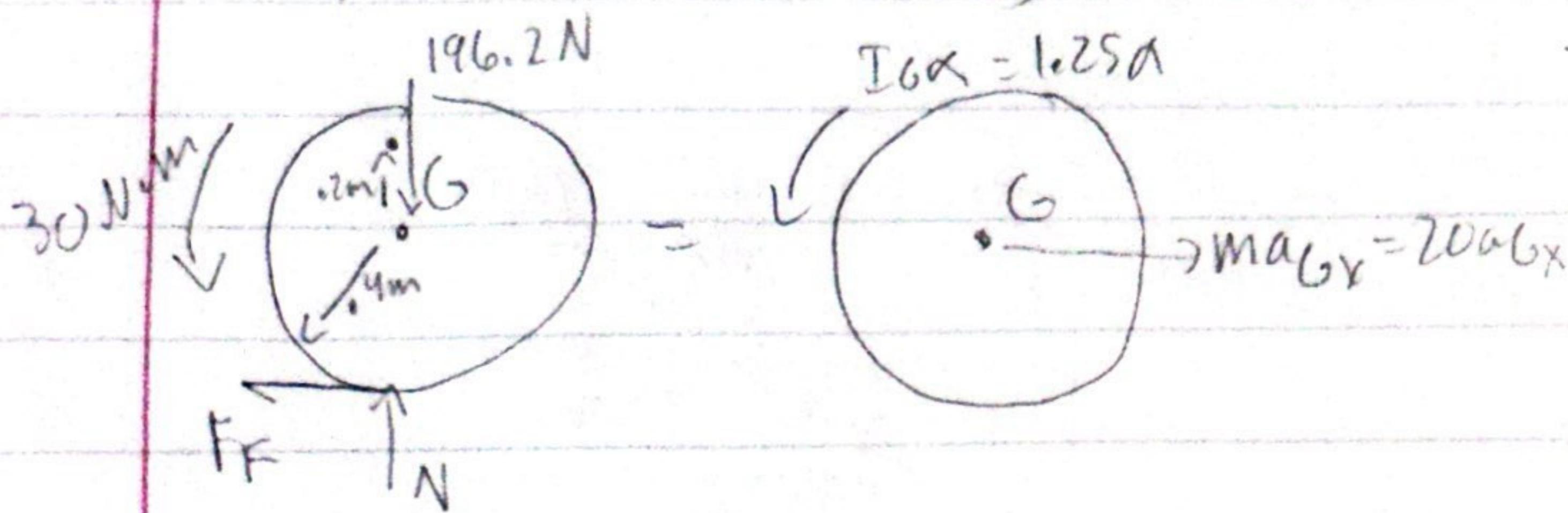
6pm

Properties

$$m=20 \text{ kg} \quad W=20(9.81)=196.2 \text{ N}$$

$$I_G = m r_0^2 = 20(0.25^2) = 1.25 \text{ kg} \cdot \text{m}^2$$

FBD = ID



$$\uparrow \sum F_y = m a_Gy \Rightarrow N - 196.2 = 0 \Rightarrow N = 196.2$$

$$\rightarrow \sum F_x = m a_Gx \Rightarrow T - F_F = 20 a_Gx \quad (1)$$

$$\uparrow \sum M_G = I_G \alpha \Rightarrow 30 - F_F(0.4) - T(0.2) = 1.25 \alpha$$

$$2 \text{ Eqn 4 unknowns must solve } F_F = \mu m N = 0.1(196.2) = \boxed{F_F = 19.26 \text{ N}}$$

$$a_Gx = \alpha r \quad a_Gx = \alpha r = 0.2 \alpha$$

$$\textcircled{1}: T - 19.26 = 20(0.2 \alpha)$$

$$T - 19.26 = 4 \alpha \Rightarrow T = 19.26 + 4 \alpha$$

$$\textcircled{2}: 30 - 19.26(0.4) - T(0.2) = 1.25 \alpha$$

$$30 - 7.68 - 0.2 T = 1.25 \alpha \Rightarrow 22.32 - 0.2(19.26 + 4 \alpha) = 1.25 \alpha$$

$$T = 55.21 \quad \frac{1}{2} \alpha = 8.89$$

$$22.32 - 0.2(19.26 + 4 \alpha) = 1.25 \alpha$$

$$22.32 - 3.852 - 0.8 \alpha = 1.25 \alpha \Rightarrow 18.468 = 2.05 \alpha$$

$$\alpha = \frac{18.468}{2.05} = 9.0088$$

$$T = 19.26 + 4(9.0088) = 55.2951$$