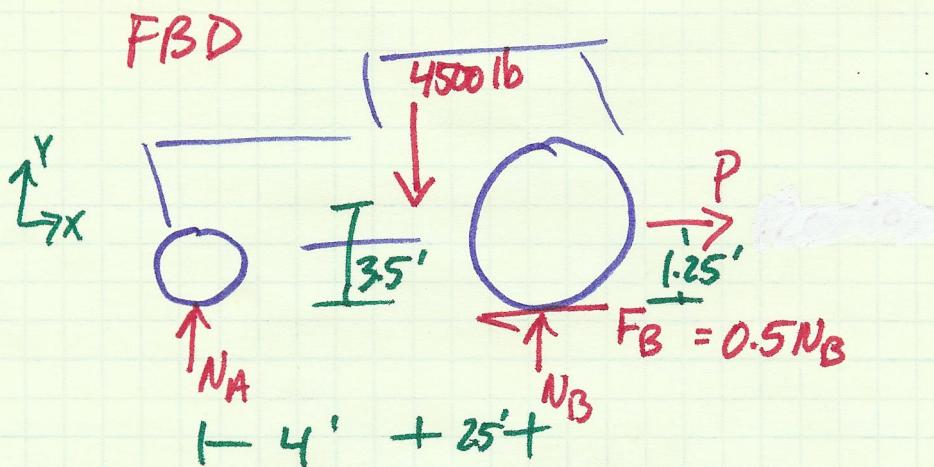
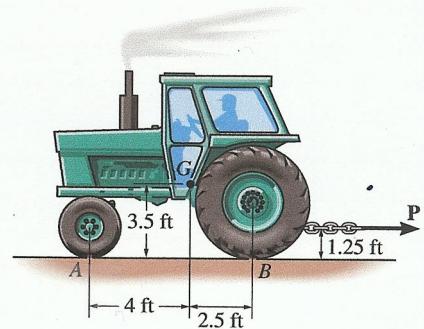


The tractor has a weight of 4500 lb with center of gravity at G . The driving traction is developed at the rear wheels B , while the front wheels at A are free to roll. If the coefficient of static friction between the wheels at B and the ground is $\mu_s = 0.5$, determine if it is possible to pull at $P = 1200$ lb without causing the wheels at B to slip or the front wheels at A to lift off the ground.

SOLUTION



ASSUME SLIPPING

$$\nabla \sum M_A = 0$$

$$4(4500) - 6.5N_B + 1.25P = 0$$

$$\rightarrow \sum F_x = 0$$

$$P - 0.5N_B = 0$$

$$P = 1532 \text{ lb} \quad N_B = 3060 \text{ lb}$$

\checkmark $> 1200 \text{ lb}$

ASSUME TIPPING

$$\nabla \sum M_B = 0$$

$$-4500(2.5) + 1.25P = 0$$

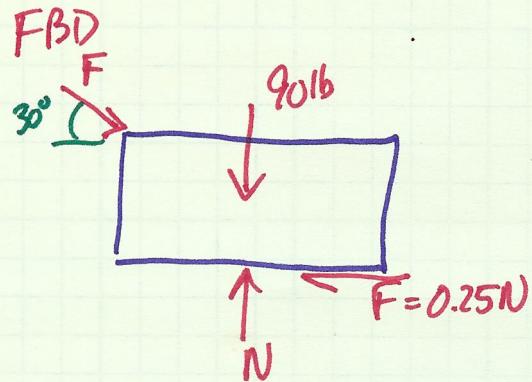
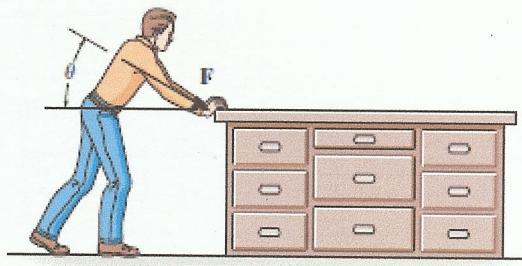
$$P = 9000 \text{ lb} > 1200 \text{ lb}$$

\checkmark

YES, POSSIBLE TO PULL 1200 lb w/o Tipping or Slipping

8-17.

The uniform dresser has a weight of 90 lb and rests on a tile floor for which $\mu_s = 0.25$. If the man pushes on it in the direction $\theta = 30^\circ$, determine the smallest magnitude of force F needed to move the dresser. Also, if the man has a weight of 150 lb, determine the smallest coefficient of static friction between his shoes and the floor so that he does not slip.



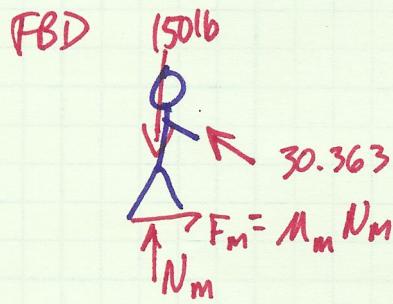
$$\uparrow \sum F_y = 0$$

$$-F_{s,n} \sin 30 + N - 90 = 0$$

$$\rightarrow \sum F_x = 0$$

$$F \cos 30 - 0.25N = 0$$

$$F = 30.363 \text{ lb} \quad N = 105.1 \text{ lb}$$



$$\uparrow \sum F_y = 0$$

$$N_m - 150 + 30.363 \sin 30 = 0$$

$$N_m = 134.82$$

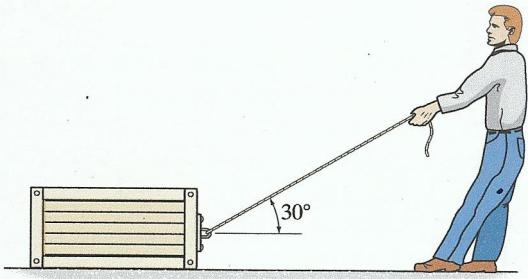
$$\rightarrow \sum F_x = 0$$

$$F_m - 30.363 \cos 30 = 0$$

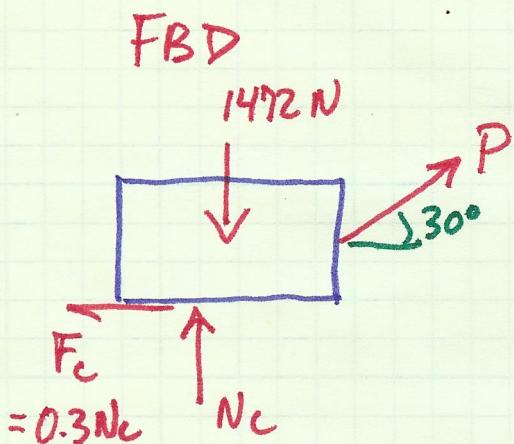
$$m_m (134.82) - 30.363 \cos 30 = 0$$

$$\underline{m_m = 0.195}$$

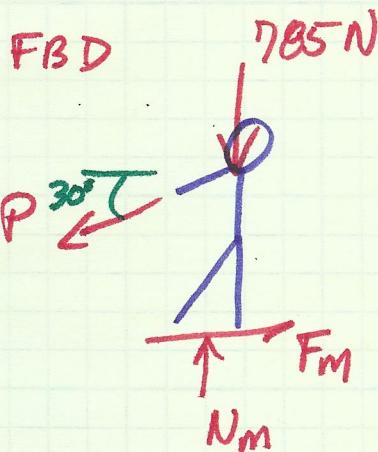
The coefficient of static friction between the 150-kg crate and the ground is $\mu_s = 0.3$, while the coefficient of static friction between the 80-kg man's shoes and the ground is $\mu'_s = 0.4$. Determine if the man can move the crate.



SOLUTION



$\sum F_y = 0$



$$\uparrow \sum F_y = 0$$

$$-1472 + N_c + P \sin 30^\circ = 0$$

$$\rightarrow \sum F_x = 0$$

$$P \cos 30^\circ - 0.3N_c = 0$$

$$N_c + 0.5P = 1472$$

$$-0.3N_c + 0.866P = 0$$

SOLVE

$$\begin{bmatrix} 1 & 0.5 \\ -0.3 & 0.866 \end{bmatrix} \begin{Bmatrix} N_c \\ P \end{Bmatrix} = \begin{Bmatrix} 1472 \\ 0 \end{Bmatrix}$$

$$N_c = 1254 \text{ N}$$

$$P = 434 \text{ N}$$

$$\uparrow \sum F_y = 0$$

$$N_m - 785 - 434 \sin 30^\circ = 0$$

$$N_m = 1002 \text{ N}$$

$$\rightarrow \sum F_x = 0$$

$$-434 \cos 30^\circ + F_m = 0$$

$$F_m = 376 \text{ N}$$

SINCE $F_{\max} = 0.4(1002)$
 $= 400 \text{ N}$

AND

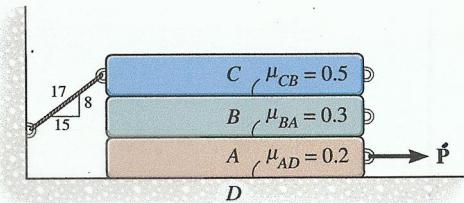
$$F_m = 376 \text{ N} < F_{\max} 400 \text{ N}$$

MAN DOES NOT SLIP

+ CAN MOVE CRATE

8-45.

The three bars have a weight of $W_A = 20 \text{ lb}$, $W_B = 40 \text{ lb}$, and $W_C = 60 \text{ lb}$, respectively. If the coefficients of static friction at the surfaces of contact are as shown, determine the smallest horizontal force P needed to move block A.



IF A + B MOVE TOGETHER, THEN SLIPPING OCCURS AT CONTACT SURFACES CB + AD. THEN $F_{CB} = \mu_{CB} N_{CB} = 0.5 N_{CB}$

$$\text{AND } F_{AD} = \mu_{AD} N_{AD} = 0.2 N_{AD}$$

$$\uparrow \sum F_y = 0 \quad N_{CB} - \frac{8}{17} T - 60 = 0$$

$$\rightarrow \sum F_x = 0 \quad 0.5 N_{CB} - T \left(\frac{15}{17} \right) = 0$$

SOLVE $T = 46.4 \text{ lb}$ $N_{CB} = 81.8 \text{ lb}$

$$\uparrow \sum F_y = 0 \quad -N_{CB} - 60 + N_{AD} = 0$$

$$\rightarrow \sum F_x = 0 \quad P - 0.5 N_{CB} - 0.2 N_{AD} = 0$$

SOLVE

$$N_{AD} = 142 \text{ lb} \quad P = 69.3 \text{ lb}$$

IF ONLY A MOVES, THEN SLIPPING OCCURS AT SURFACES BA AND AD. THEN $F_{BA} = \mu_{BA} N_{BA} = 0.3 N_{BA}$ AND

$$F_{AD} = \mu_{AD} N_{AD} = 0.2 N_{AD}$$

$$\uparrow \sum F_y = 0 \quad N_{BA} - 100 - \frac{9}{17} T = 0$$

$$\rightarrow \sum F_x = 0 \quad -\frac{15}{17} T + 0.3 N_{BA} = 0$$

SOLVE $T = 40.5 \quad N_{BA} = 119 \text{ lb}$

$$\uparrow \sum F_y = 0 \quad N_{AD} - N_{BA} - 20 = 0$$

$$\rightarrow \sum F_x = 0 \quad P - 0.3 N_{BA} - 0.2 N_{AD} = 0$$

SOLVE $P = 63.5 \text{ lb}$ $N_{AD} = 139 \text{ lb}$

CONTROLS

