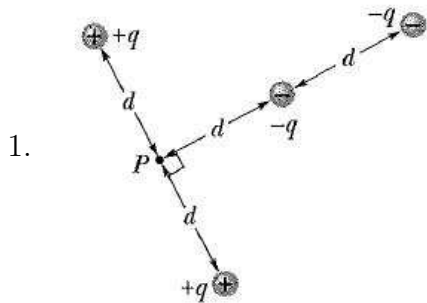


Part 1. Write your answers to each of the multiple-choice problems below on the designated lines. Use only **CAPITAL LETTERS** for your responses. If you change your answer, strike out the old answer and write your new answer next to it. Write clearly. (2 pts each problem, 30 pts total)

- | | | | |
|------|------|-------|-------|
| 1) E | 5) A | 9) D | 13) B |
| 2) A | 6) E | 10) C | 14) A |
| 3) B | 7) D | 11) B | 15) E |
| 4) A | 8) C | 12) A | |

Part 2. Select **THREE** problems as mandatory, any other extra will give you bonus points. You must show **EACH STEP** in your solution **AND the UNITS** for the full credit consideration. **If you will write only the numbers I will not give you any credit.** (70 pts total as a minimum)



What is the net electric potential at point P due to the four particles if $V = 0$ at infinity, $q = 5.00 \text{ fC}$, and $d = 4.00 \text{ cm}$?

Solution:

$$V = \frac{q}{4\pi\epsilon_0} = \left(-\frac{1}{2d} - \frac{1}{d} + \frac{1}{d} + \frac{1}{d} \right) = \frac{q}{8\pi\epsilon_0 d} = 5.62 \cdot 10^{-4} \text{ V}$$

2. Two particles are fixed to an x axis: particle 1 of charge $q_1 = 2.1 \cdot 10^{-8} \text{ C}$ at $x = 20 \text{ cm}$ and particle 2 of charge $q_2 = -4.00q_1$ at $x = 70 \text{ cm}$. At what coordinate on the axis is the net electric field produced by the particles equal to zero?

Solution:

At points between the charges, the individual electric fields are in the same direction and do not cancel. Since charge $q_2 = -4.00q_1$ located at $x_2 = 70 \text{ cm}$ has a greater magnitude than $q_1 = 2.1 \cdot 10^{-8} \text{ C}$ located at $x_1 = 20 \text{ cm}$, a point of zero field must be closer to q_1 than to q_2 . It must be to the left of q_1 .

Let x be the coordinate of P, the point where the field vanishes. Then, the total electric field at P is given by

$$E = \frac{1}{4\pi\epsilon_0} \left(\frac{|q_1|}{(x - x_2)^2} - \frac{|q_2|}{(x - x_1)^2} \right)$$

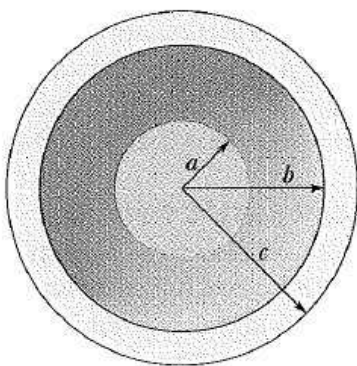
If the field is to vanish, then

$$\frac{|q_1|}{(x - x_2)^2} = \frac{|q_2|}{(x - x_1)^2}$$

$$\frac{|q_2|}{|q_1|} = \frac{(x - x_2)^2}{(x - x_1)^2}$$

From here $x = -30 \text{ cm}$.

3.



A solid sphere of radius $a = 2.00$ cm is concentric with a spherical conducting shell of inner radius $b = 2a$ and outer radius $c = 2.4a$. The sphere has a net uniform charge $q_1 = +5.00$ fC; the shell has a net charge $q_2 = -q_1$. What is the magnitude of the electric field at radial distances (a) $r = 0$, (b) $r = a/2$, (c) $r = a$, (d) $r = 1.50a$, (e) $r = 2.30a$, and (f) $r = 3.50a$?

Solution:

At all points where there is an electric field, it is radially outward. For each part of the problem, use a Gaussian surface in the form of a sphere that is concentric with the sphere of charge and passes through the point where the electric field is to be found.

For $r < a$, the charge enclosed by the Gaussian surface is $q_1(r/a)^3$. Gauss law yields

$$4\pi r^2 E = \left(\frac{q_1}{\epsilon_0}\right) \left(\frac{r}{a}\right)^3$$

$$E = \frac{q_1 r}{4\pi \epsilon_0 a^3}$$

(a)

For $r = 0$, the above equation implies $E = 0$.

(b)

For $r = a/2$, we have

$$E = \frac{q_1 a/2}{4\pi \epsilon_0 a^3} = 5.62 \cdot 10^{-2} \text{ N/C}$$

(c)

For $r = a$, we have

$$E = \frac{q_1}{4\pi \epsilon_0 a^2} = 0.112 \text{ N/C}$$

In the case where $a < r < b$, the charge enclosed by the Gaussian surface is q_1 , so Gauss law leads to

$$4\pi r^2 E = \frac{q_1}{\epsilon_0}$$

$$E = \frac{q_1}{4\pi \epsilon_0 r^2}$$

(d)

For $r = 1.50a$, we have

$$E = \frac{q_1}{4\pi \epsilon_0 r^2} = 0.0499 \text{ N/C}$$

(e)

In the region $b < r < c$, since the shell is conducting, the electric field is zero. Thus, for $r = 2.30a$, we have $E = 0$.

(f)

For $r > c$, the charge enclosed by the Gaussian surface is zero. Gauss law yields

$$4\pi r^2 E = 0$$

Thus, $E = 0$ at $r = 3.50a$.

4. Two electrons are fixed 2.0 cm apart. Another electron is shot from infinity and stops midway between the two. What is its initial speed?

Solution:

We use conservation of energy, taking the potential energy to be zero when the moving electron is far away from the fixed electrons. The final potential energy is then

$$U_f = \frac{2e^2}{4\pi\epsilon_0 d},$$

where d is half the distance between the fixed electrons. The initial kinetic energy is

$$K_i = \frac{1}{2}mv^2,$$

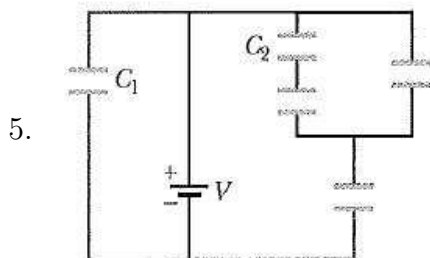
where m is the mass of an electron and v is the initial speed of the moving electron. The final kinetic energy is zero. Thus,

$$K_i = U_f$$

$$\frac{1}{2}mv^2 = \frac{2e^2}{4\pi\epsilon_0 d}$$

Hence,

$$v = \sqrt{\frac{4e^2}{4\pi\epsilon_0 dm}} = \sqrt{\frac{9 \cdot 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2 \cdot 4 \cdot (1.6 \cdot 10^{-19} \text{ C})^2}{0.01 \text{ m} \cdot 9.11 \cdot 10^{-31} \text{ kg}}} = 320 \text{ m/s}$$



The battery has a potential difference of $V = 10.0 \text{ V}$ and the five capacitors each have a capacitance of $10.0 \mu\text{F}$. What is the charge on (a) capacitor 1 and (b) capacitor 2?

Solution:

(a)

The potential difference across C_1 is $V_1 = 10.0 \text{ V}$. Thus,

$$q_1 = C_1 V_1 = 10 \mu\text{F} \cdot 10 \text{ V} = 1 \cdot 10^{-4} \text{ C}$$

(b)

We first consider the three-capacitor combination consisting of C_2 and its two closest neighbors, each of capacitance C . The equivalent capacitance of this combination is

$$C_{eq} = C + \frac{C_2 C}{C + C_2} = 1.5C$$

Also, the voltage drop across this combination is

$$V = \frac{C V_1}{C + C_{eq}} = \frac{C V_1}{C + 1.5C} = 0.4 V_1$$

Since this voltage difference is divided equally between C_2 and the one connected in series with it, the voltage difference across C_2 satisfies $V_2 = V/2 = V_1/5$. Thus

$$q_2 = C_2 V_2 = 10 \mu\text{F} \cdot \left(\frac{10 \text{ V}}{5}\right) = 2 \cdot 10^{-5} \text{ C}$$