

Rigid Body Kinematics II – Problem 4

The no-slip wheel at B has an angular velocity of 6 rad/s and an angular acceleration of 4 rad/s² (both CCW) as shown. Determine the angular velocity and acceleration of bars BC and CD as well as the acceleration of point C at this instant.

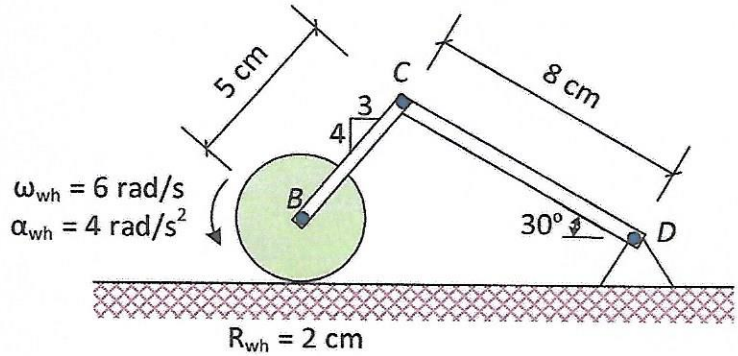
CLASSIFY MOTION

WHEEL B – GPM

BAR BC – GPM

BAR CD – RAFA

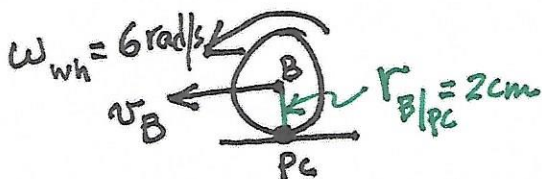
RELATIVE VELOCITY EQN:



$$\vec{v}_C = \vec{v}_B + \vec{v}_{C/B}$$

KINEMATIC DIAGRAM:

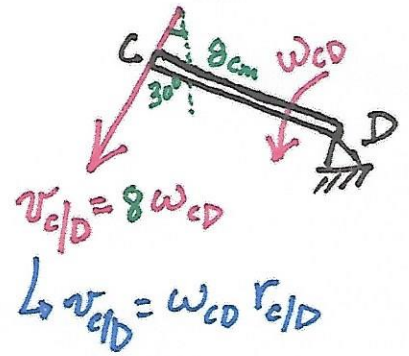
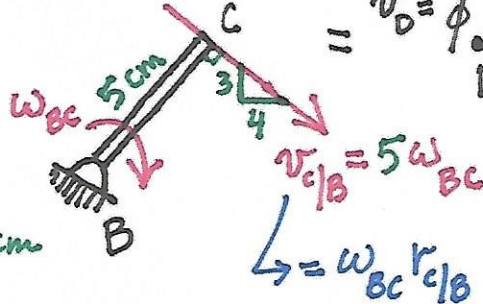
$$v_B = 12 \text{ cm/s} \leftarrow B$$



$$\text{No Slip Wheel} \Rightarrow v_B = \omega_{wh} r_{B/P_c} = 6 \frac{\text{rad}}{\text{s}} (2 \text{ cm}) = 12 \text{ cm/s} \leftarrow$$

$$\vec{v}_{C/B} = \vec{v}_D + \vec{v}_{C/D}$$

$$= v_D \phi +$$



$$v_{C/D} = 8 \omega_{CD}$$

$$v_{C/D} = \omega_{CD} r_{C/D}$$

$$\rightarrow x : -12 + 5 \omega_{BC} \left(\frac{4}{5} \right) = 0 - 8 \omega_{CD} \sin 30$$

$$-12 + 4 \omega_{BC} = -4 \omega_{CD} \text{ --- (1)}$$

$$\uparrow y : 0 - 5 \omega_{BC} \left(\frac{3}{5} \right) = 0 - 8 \omega_{CD} \cos 30$$

$$-3 \omega_{BC} = -6.9282 \omega_{CD} \text{ --- (2)}$$

2 Eqs
2 unk. ✓

Solve Eqs (1) & (2) to find ω_{BC} and ω_{CD}

$$\omega_{BC} = 2.09 \text{ rad/s} \leftarrow$$

$$\omega_{CD} = 0.907 \text{ rad/s} \leftarrow$$