

Formula Sheet – 3rd Exam

DC Circuits

Definitions of quantities:

Voltage: V (SI unit: volt)

Current: I (Amp = C/s)

Resistance: R (Ohm, Ω)

Resistance & Resistivity:

$$R = \rho \frac{L(\text{length})}{A(\text{area})}$$

Ohm's Law: $V = IR$

$$\text{Electric Power: } P = IV = I^2 R = \frac{V^2}{R}$$

Resistors in Series: $R_{\text{total}} = R_1 + R_2 + \dots$

Resistors in Parallel: $\frac{1}{R_{\text{total}}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$

Capacitors in series: $\frac{1}{C_{\text{total}}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$

Capacitors in Parallel: $C_{\text{total}} = C_1 + C_2 + \dots$

Time constant of RC circuits: $\tau = RC$

Magnetic Force

$$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m} / \text{A}$$

On Charge: $\vec{F} = q\vec{v} \times \vec{B}$

magnitude: $F = |q|vB \sin \theta$

On Current: $\vec{F} = I\vec{L} \times \vec{B}$

magnitude: $F = ILB \sin \theta$

Between two parallel current-carrying wires of length L and separation r :

$$\text{magnitude: } F = \frac{\mu_0 L I_1 I_2}{2\pi r}$$

Magnetic Torque on an N-turn loop:

$$\tau = NIAB \sin \theta$$

Magnetic Fields generated by currents

In an N-turn circular loop of radius R :

$$B = N \frac{\mu_0 I}{2R} \text{ (at the center of the loop)}$$

In an infinitely long straight wire:

$$B = \frac{\mu_0 I}{2\pi r} \text{ (at distance } r \text{ from the wire)}$$

In an N-turn solenoid with length L :

$$B = \mu_0 \left(\frac{N}{L} \right) I = \mu_0 n I \text{ (in the solenoid)}$$

Magnetic Induction

Magnetic Flux:

$$\Phi_m = \vec{B} \cdot \vec{A} = BA \cos \theta \text{ (SI unit: Weber)}$$

Faraday's Law of Induction:

$$V_{\text{ind}} = \mathcal{E} = -N \frac{\Delta \Phi_m}{\Delta t}$$

Equations of Transformers:

$$\frac{N_p}{V_p} = \frac{N_s}{V_s} \text{ or } \frac{N_p}{N_s} = \frac{V_p}{V_s}$$

Electric Generator:

$$V_{\text{ind}} = \mathcal{E} = NAB\omega \sin(\omega t)$$

Inductance, L (SI unit: Henry):

$$V_{\text{ind}} = -N \frac{\Delta \Phi_m}{\Delta t} = -L \frac{\Delta I}{\Delta t}$$

Inductance of an N-turn solenoid with length l and cross-sectional area A :

$$L = \mu_0 n^2 A l, \quad n = \frac{N}{l}$$

Time constant of RL circuit: $\tau = \frac{L}{R}$

Energy stored in Magnetic Fields

In an inductor:

$$U = \frac{LI^2}{2}$$

Energy density (energy per unit volume) of magnetic fields:

$$u_B = \frac{B^2}{2\mu_0}$$

Modern Physics

Planck's Constant: $h = 6.63 \times 10^{-34} \text{ J} \cdot \text{s}$

Energy of "one" photon:

$$E = hf; f = \text{frequency of light}$$

Energy of electrons in a hydrogen-like atom:

$$E = (-13.6 \text{ eV}) \frac{Z^2}{n^2}; 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J};$$

Z = Atomic Number

Quantum #'s: given the principle quantum $n =$

$$l = 0, 1, \dots, n-1; m_l = -l, -l+1, \dots, 0, \dots, l-1, l$$

$$m_s = \pm 1/2$$