

Electron current  $i_e$  and  $N_e = i_e \cdot \Delta t$

The drift speed  $v_d = \frac{e\tau}{m} E$ , where  $\tau$  is the mean time between collisions.

The electron current is related to the drift speed by  $i_e = n_e A v_d$ , where  $n_e$  is the electron density.

Conventional current  $I = e i_e$  and  $Q = I \Delta t$

Current density  $J = \frac{I}{A}$

An electric field  $E$  in a conductor causes a current density  $J = n_e e v_d = \sigma E$ , where the **conductivity** is  $\sigma = \frac{n_e e^2 \tau}{m}$

The resistivity is  $\rho = \frac{1}{\sigma}$

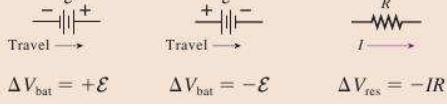
A potential difference  $\Delta V_{wire}$  between the ends of a wire creates an electric field inside the wire:  $E_{wire} = \frac{\Delta V_{wire}}{L}$

The size of the current in the wire is  $I = \frac{\Delta V_{wire}}{R}$ , where  $R = \frac{\rho L}{A}$  is the wires resistance. This is **Ohms law**.

Kirchhoffs junction law:  $\sum I_{in} = \sum I_{out}$

Kirchhoffs loop law:  $\sum (\Delta V)_i = 0$

#### Signs of $\Delta V$ for Kirchhoff's loop law



A potential difference  $\Delta V$  between the ends of a conductor with resistance  $R$  creates a current  $I = \frac{\Delta V}{R}$ .

The battery supplies energy at the rate  $P_{bat} = IV_{bat}$

The resistors dissipate energy at the rate  $P_R = I \Delta V_R = I^2 R = \frac{(\Delta V_R)^2}{R}$

Series resistors  $R_{eq} = R_1 + R_2 + R_3 + \dots$

Parallel resistors  $R_{eq} = \left( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots \right)^{-1}$

The discharge of a capacitor through a resistor satisfies:  $Q = Q_0 e^{-\frac{t}{\tau}}$  and  $I = -\frac{dQ}{dt} = \frac{Q_0}{\tau} e^{-\frac{t}{\tau}} = I_0 e^{-\frac{t}{\tau}}$ , where  $\tau = RC$  is the time constant.

| Material | Resistivity ( $\Omega \cdot m$ ) | Conductivity ( $(\Omega \cdot m)^{-1}$ ) |
|----------|----------------------------------|--|
| Aluminum | $2.8 \times 10^{-8}$             | $3.5 \times 10^7$                        |
| Copper   | $1.7 \times 10^{-8}$             | $6.0 \times 10^7$                        |
| Gold     | $2.4 \times 10^{-8}$             | $4.1 \times 10^7$                        |
| Iron     | $9.7 \times 10^{-8}$             | $1.0 \times 10^7$                        |
| Silver   | $1.6 \times 10^{-8}$             | $6.2 \times 10^7$                        |
| Tungsten | $5.6 \times 10^{-8}$             | $1.8 \times 10^7$                        |
| Nichrome | $1.5 \times 10^{-6}$             | $6.7 \times 10^5$                        |
| Carbon   | $3.5 \times 10^{-5}$             | $2.9 \times 10^4$                        |