

Single slit of width a :

A bright central maximum of width $w = \frac{2\lambda L}{a}$ is flanked by weaker secondary maxima.

Dark fringes are located at angles such that $a \sin \theta_p = p\lambda$, $p=1,2,3,\dots$

If $\lambda/a \ll 1$, then from the small-angle approximation $\theta_p = \frac{p\lambda}{a}$, $y_p = \frac{p\lambda L}{a}$

Circular aperture of diameter D :

A bright central maximum of diameter $w = \frac{2.44\lambda L}{D}$ is surrounded by circular secondary maxima.

The first dark fringe is located at $\theta_1 = \frac{1.22\lambda}{D}$, $y_1 = \frac{1.22\lambda L}{D}$

Double slit with separation d .

Equally spaced bright fringes are located at $\theta_m = \frac{m\lambda}{d}$, $y_m = \frac{m\lambda L}{d}$, $m=0,1,2,3,\dots$

The fringe spacing is $\Delta y = \frac{\lambda L}{d}$

Diffraction grating with slit spacing d :

Very bright and narrow fringes are located at angles and positions $d \sin \theta_m = m\lambda$, $y_m = L \tan \theta_m$

Law of reflection: $\theta_r = \theta_i$

Plane mirrors: A virtual image is formed at P' with $s' = s$.

Snells law of refraction: $n_i \sin \theta_i = n_r \sin \theta_r$

Index of refraction is $n = \frac{c}{v}$

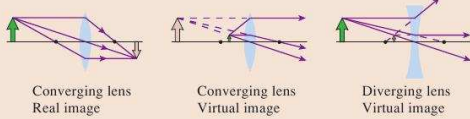
If $n_r < n_i$, **total internal reflection** occurs when the angle of incidence $\theta_i \geq \theta_c = \sin^{-1}(n_r/n_i)$.

Spherical surface: Object and image distances are related by: $\frac{n_1}{s} + \frac{n_2}{s'} = \frac{n_2 - n_1}{R}$

Plane surface: $\left| \frac{s'}{s} \right| = \frac{n_2}{n_1}$

Ray tracing

3 special rays in 3 basic situations:



Magnification $m = -\frac{s'}{s}$
 m is + for an upright image, - for inverted.
 The height ratio is $h'/h = |m|$.

Thin lenses

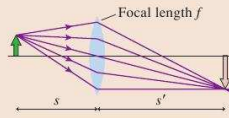
The image and object distances are related by

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f}$$

where the focal length is given by the lens maker's equation:

$$\frac{1}{f} = (n - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

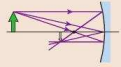
R + for surface convex toward object - for concave
 f + for a converging lens - for diverging
 s' + for a real image - for virtual



Spherical mirrors

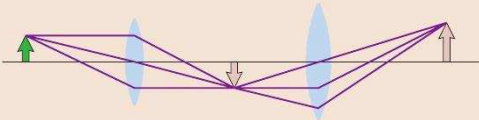
The image and object distances are related by

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f}$$



R, f + for concave mirror - for convex
 s' + for a real image - for virtual
 Focal length $f = R/2$

Lens Combinations



The image of the first lens acts as the object for the second lens.

Lens **power:** $P = \frac{1}{f}$ diopters, $1 \text{ D} = 1 \text{ m}^{-1}$

Vision

Refraction at the cornea is responsible for most of the focusing. The lens provides fine-tuning by changing its shape (**accommodation**).



In normal vision, the eye can focus from a far point (FP) at ∞ (relaxed eye) to a near point (NP) at $\approx 25 \text{ cm}$ (maximum accommodation).

- **Hyperopia** (farsightedness) is corrected with a converging lens.
- **Myopia** (nearsightedness) is corrected with a diverging lens.