

Rigid Body Kinematics III – Problem 3

For the train wheel shown, find the acceleration of the piston at A relative to the track and the angular acceleration of the push arm AB when the velocity and acceleration of the train is $v_O = 80$ fps and $a_O = 40$ fps² and the angular velocity of the push arm AB is $\omega_{AB} = 10$ rps (CCW). Assume no slip.

CLASSIFY MOTION

PISTON A TRANS
ARM AB GPM
WHEEL GPM

NO SLIP WHEEL

$$V_O = \omega_{WH} r_{WH}, \quad \omega_{WH} = \frac{V_O}{r_{WH}} = \frac{80}{2} = 40 \text{ rps}$$

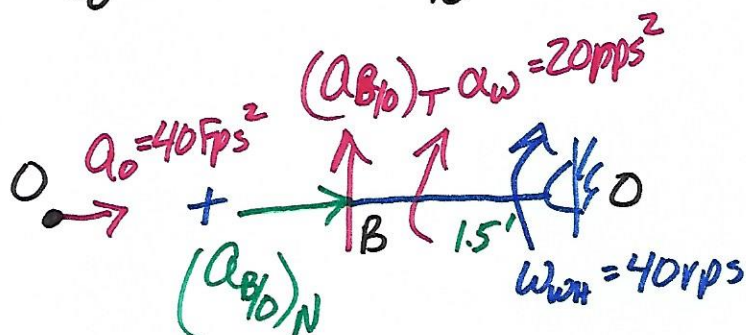
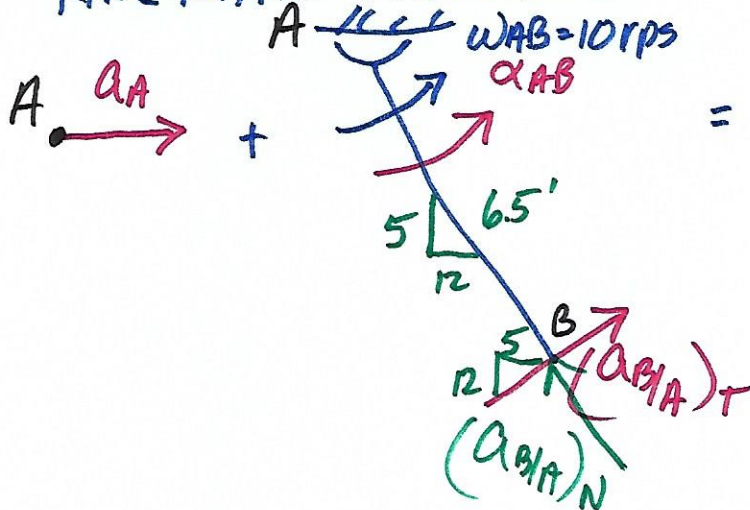
$$\omega_{WH} = 40 \text{ rps} \downarrow$$

$$a_O = \alpha_{WH} r_{WH}, \quad \alpha_{WH} = \frac{a_O}{r_{WH}} = \frac{40}{2} = 20 \text{ rps}^2 \downarrow$$

ALL ω 's KNOWN, NO NEED TO SOLVE VELOCITY PROBLEM
RELATIVE ACCELERATION EQU

$$\vec{a}_B = \vec{a}_A + \vec{a}_{B/A} = \vec{a}_O + \vec{a}_{B/O}$$

KINEMATIC DIAGRAMS



NOTES

$$(a_{B/A})_N = \omega_{AB}^2 r_{AB} = 10^2 (6.5) = 650 \text{ fps}^2$$

$$(a_{B/A})_T = \alpha_{AB} r_{AB} = 6.5 \alpha_{AB}$$

$$(a_{B/O})_N = \omega_{WH}^2 r_{B/O} = 40^2 (1.5) = 2400 \text{ fps}^2$$

$$(a_{B/O})_T = \alpha_{WH}^2 r_{B/O} = 20 (1.5) = 30 \text{ fps}^2$$

Rigid Body Kinematics III – Problem 3 (Continued)

SCALAR EQUATIONS

$$\rightarrow X \quad a_A + \frac{5}{13}(65\alpha_{AB}) - \frac{12}{13}(650) = 40 + 2400$$

$$\uparrow y \quad 0 + \frac{12}{13}(65\alpha_{AB}) + \frac{5}{13}(650) = 30$$

$$\alpha_{AB} = -36.7 = 36.7 \text{ rps}^2 \downarrow$$

$$a_A = 2948 \text{ fps}^2 \rightarrow$$