

Worksheet 1A
Internal Forces

Given: Beam with applied loads as shown.
Determine the internal forces on a transverse cross-section through points "S" and "T".

External - Entire FBD

$$6 \sum M_A = 0 = (-2 \cdot 9)(4.5) + 18 B_y - (4/5 \cdot 25)(15) + 18 B_y$$

$$B_y = \frac{21.16 k}{\uparrow}$$

$$\Rightarrow \sum F_x = 0 = A_x - (\frac{3}{5} \cdot 25)$$

$$A_x = \frac{15 k}{\rightarrow}$$

Internal C-S

$$M_T = \frac{V_T}{25k} \cdot 25k \uparrow$$

$$M_S = \frac{V_S}{25k} \cdot 25k \uparrow$$

$$N_T = \frac{V_T}{25k} \cdot 25k \leftarrow$$

$$N_S = \frac{V_S}{25k} \cdot 25k \leftarrow$$

$$\Rightarrow \sum F_x = 0 = 15 - N_S$$

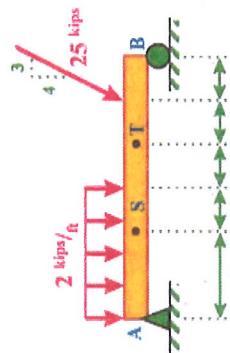
$$N_S = \frac{15 k}{\leftarrow} \text{ on AS}$$

$$\sum F_y = 0 = 16.83 - (2 \cdot 6) - V_S$$

$$V_S = \frac{4.83 k}{\downarrow} \text{ on AS}$$

$$\sum M_S = 0 = M_{S_i} + (2 \cdot 6)(3) - (16.83)(6)$$

$$M_{S_i} = \frac{65.0 kft}{\uparrow \text{ on AS}}$$



$$+ \sum F_y = 0 = A_y - (2 \cdot 9)$$

$$-(\frac{4}{5} \cdot 25) + 21.16$$

$$A_y = \frac{16.83 k}{\uparrow}$$

$$\text{Internal C-T} \quad \uparrow$$

$$M_T = \frac{V_T}{25k} \cdot 25k \uparrow$$

$$M_S = \frac{V_S}{25k} \cdot 25k \uparrow$$

$$N_T = \frac{V_T}{25k} \cdot 25k \leftarrow$$

$$N_S = \frac{V_S}{25k} \cdot 25k \leftarrow$$

$$\Rightarrow \sum F_x = 0 = -V_T - N_T - N_S$$

$$N_T = \frac{V_T}{25k} \cdot 25k \uparrow$$

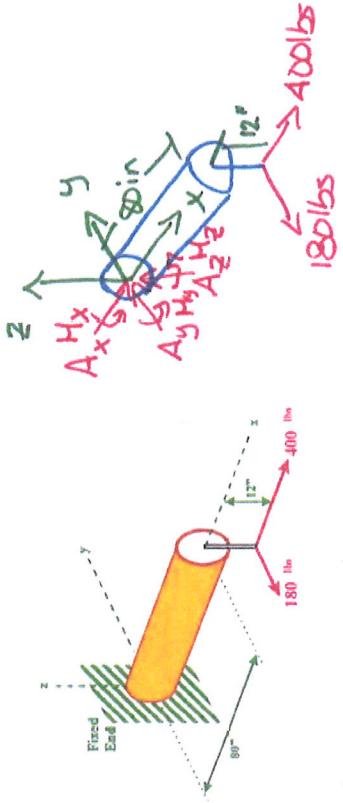
$$N_S = \frac{V_S}{25k} \cdot 25k \leftarrow$$

$$\sum F_y = 0 = -V_S - N_T - N_S$$

$$N_T = \frac{67.0 kft}{\uparrow \text{ on TB}}$$

Worksheet 1B
Internal Forces

Find the external reactions at the fixed end of the structure shown.



RHQ

$$\sum F_x = 0 = A_x + 400$$

$$A_x = -400 \text{ lbs}$$

$$\sum F_y = 0 = A_y - 180$$

$$A_y = 180 \text{ lbs}$$

$$\sum F_z = 0 = A_z$$

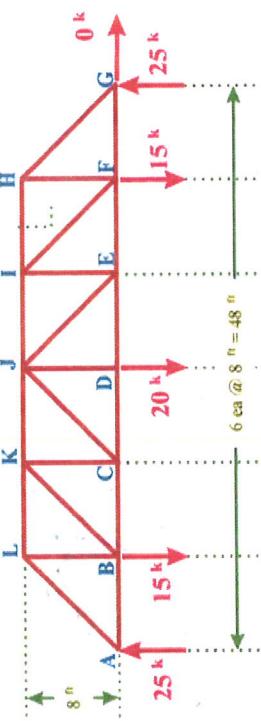
$$M_x = 2160 \text{ lb-in}$$

$$M_y = 4800 \text{ lb-in}$$

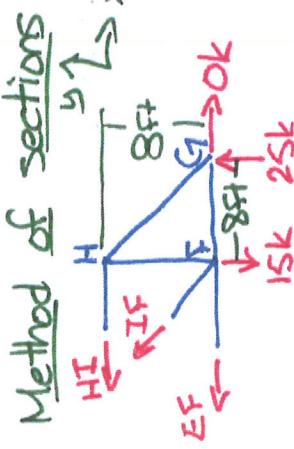
$$M_z = 14,400 \text{ lb-in}$$

Worksheet 1C
Internal Normal Forces/Stresses

Given: The cross-sectional area of all truss members below is 4 in^2 . For the loads and reactions shown:



Determine the normal stress on a transverse plane in member HI.



$$\sum M_I = 0 = -(HI)(8) - (25)(8)$$

$$HI = -25k = \underline{\underline{25k(c)}}$$

Stress

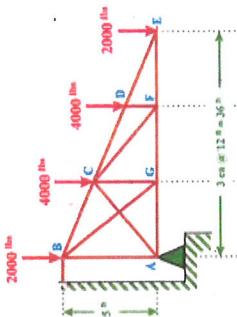
$$A = 4 \text{ in}^2$$

$$\sigma = \frac{P}{A} = \frac{25}{4} = \underline{\underline{6.25 ksi(c)}}$$

Worksheet 1D
Internal Normal Forces/Stresses

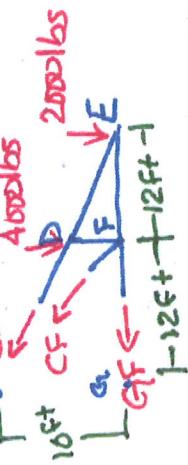
Given: Member GF of the pin-connected truss has a cross-sectional area of 7.4 in^2 .

Determine the maximum normal stress in GF.



Do we need external? No!

Method of sections



$$\sum M_G = 0 = (4000)(12) + (2000)(24) + (GF)(10)$$

$$GF = -9600 \text{ lbs} = \underline{\underline{9600 \text{ lbs}(c)}}$$

Stress

$$A = 7.4 \text{ in}^2$$

$$\sigma = \frac{P}{A} = \frac{9600}{7.4} = \underline{\underline{1297 \text{ psi}(c)}}$$