

Coulombs Law  $F_1$  on  $2 = F_2$  on  $1 = \frac{K|q_1||q_2|}{r^2}$

The forces are repulsive for two like charges, attractive for two opposite charges.

The net force on a charge is the sum of the forces from all other charges.

The unit of charge is the coulomb (C).

The electrostatic constant is  $K = 9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$ .

Fundamental charges are protons and electrons, with charge  $\pm e$ , where  $e = 1.60 \times 10^{-19} \text{ C}$ .

The amount of charge is  $q = (N_p - N_e)e$ .

An electric field is identified and measured in terms of the force on a probe charge  $q$ :  $\vec{E} = \frac{\vec{F}_{\text{on } q}}{q}$

The electric field of a point charge is  $\vec{E} = \frac{1}{4\pi\epsilon_0 r^2} \frac{q}{r} \hat{r}$ , where permittivity constant  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N} \cdot \text{m}^2)$

The principle of superposition:  $\vec{E} = \vec{E}_1 + \vec{E}_2 + \vec{E}_3 + \dots$

A linear charge density  $\lambda = \frac{q}{L}$ , a surface charge density  $\sigma = \frac{q}{A}$

The electric field exerts a force on a charged particle:  $\vec{F} = q\vec{E}$

The electric dipole moment is  $\vec{p} = (qs, \text{from negative to positive})$

The electric field exerts a torque on a dipole:  $\tau = pE \sin \theta$

Field on axis:  $\vec{E} = \frac{1}{4\pi\epsilon_0 r^3} 2\vec{p}$

Field in bisecting plane:  $\vec{E} = -\frac{1}{4\pi\epsilon_0 r^3} \frac{\vec{p}}{r}$

Field of an infinite line of charge with linear charge density  $\lambda$ :  $\vec{E} = \left( \frac{1}{4\pi\epsilon_0 r} \frac{2\lambda}{r}, \text{perpendicular to line} \right)$

Field of an infinite plane of charge with surface charge density  $\sigma$ :  $\vec{E} = \left( \frac{\sigma}{2\epsilon_0}, \text{perpendicular to plane} \right)$

Field of a sphere of charge is the same as a point charge outside of the sphere.

The electric field inside an ideal capacitor is a uniform electric field:  $\vec{E} = \left( \frac{\sigma}{\epsilon_0}, \text{from positive to negative} \right)$

For any closed surface enclosing net charge  $Q_{in}$ , the net electric flux through the surface is  $\Phi_e = \oint \vec{E} \cdot d\vec{A} = \frac{Q_{in}}{\epsilon_0}$

Flux is the amount of electric field passing through a surface of area  $A$ :  $\Phi_e = \vec{E} \cdot \vec{A}$

The electric potential of a point charge  $q$ :  $V = \frac{1}{4\pi\epsilon_0 r} \frac{q}{r}$

The principle of superposition:  $V = V_1 + V_2 + V_3 + \dots$

A charged particle has potential energy  $U = qV$  at a point where source charges have created an electric potential  $V$ .

The electric force is a conservative force, so the mechanical energy is conserved for a charged particle in an electric potential:  $K_f + qV_f = K_i + qV_i$  The potential energy of two point charges separated by distance  $r$  is  $U_{q_1+q_2} = \frac{Kq_1q_2}{r} = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r}$

The potential energy in an electric field of an electric dipole with dipole moment  $\vec{p}$  is  $U_{dipole} = -pE \cos \theta = -\vec{p} \cdot \vec{E}$

The electric potential of a sphere of charge  $Q$  is the same as a point charge if  $r \geq R$ .

The potential difference between plates of parallel-plate capacitor:  $E = \frac{\Delta V_C}{d}$

Electric potential: 1 V = 1 J/C. Electric field: 1 V/m = 1 N/C

$V$  and  $\vec{E}$  are related by  $\Delta V = V_f - V_i = - \int_{s_i}^{s_f} E_s ds$

$$E_s = -\frac{dV}{ds}$$

The sum of all potential differences around a closed path is zero:  $\sum (\Delta V)_i = 0$

The capacitance of two conductors charged to  $\pm Q$  is  $C = \frac{Q}{\Delta V_C}$

A parallel-plate capacitor has  $C = \frac{\epsilon_0 A}{d}$

Filling the space between the plates with a dielectric of dielectric constant  $k$  increases the capacitance to  $C = kC_0$ .

The energy stored in a capacitor is  $u_C = \frac{1}{2}C(\Delta V_C)^2$

This energy is stored in the electric field at density  $u_E = \frac{1}{2}k\epsilon_0 E^2$

Series capacitors  $C_{eq} = \left( \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots \right)^{-1}$

Parallel capacitors  $C_{eq} = C_1 + C_2 + C_3 + \dots$

Material	Dielectric constant $k$	Dielectric strength $E_{max} (10^2) \text{ V/m}$
Vacuum	1	
Air (1 atm)	1.0006	3
Teflon	2.1	60
Polystyrene plastic	2.6	24
Mylar	3.1	7
Paper	3.7	16
Pyrex glass	4.7	14
Pure water (20°C)	80	
Titanium dioxide	110	6
Strontium titanate	300	8