

MODULE *DieHard*

EXTENDS *Integers*

VARIABLES *big*, The number of gallons of water in the 5 gallon jug.
small The number of gallons of water in the 3 gallon jug.

$Init \triangleq \wedge big = 0$
 $\wedge small = 0$

$$\begin{aligned} FillSmall &\triangleq \wedge small' = 3 \\ &\wedge big' = big \end{aligned}$$

$$\begin{aligned} FillBig &\triangleq \wedge big' = 5 \\ &\wedge small' = small \end{aligned}$$

$$\begin{aligned} EmptySmall &\triangleq \wedge small' = 0 \\ &\wedge big' = big \end{aligned}$$

$$\begin{aligned} EmptyBig &\triangleq \wedge big' = 0 \\ &\wedge small' = small \end{aligned}$$

$$Min(m, n) \triangleq \text{IF } m < n \text{ THEN } m \text{ ELSE } n$$

$$SmallToBig \triangleq \text{LET } poured \triangleq Min(big + small, 5) - big$$

$$\begin{aligned} \text{IN } &\wedge big' = big + poured \\ &\wedge small' = small - poured \end{aligned}$$

$$\begin{aligned} BigToSmall &\triangleq \\ \text{LET } poured &\triangleq Min(big + small, 3) - small \\ \text{IN } &\wedge big' = big - poured \\ &\wedge small' = small + poured \end{aligned}$$

$$\begin{aligned}
Next &\triangleq \vee FillSmall \\
&\vee FillBig \\
&\vee EmptySmall \\
&\vee EmptyBig \\
&\vee SmallToBig \\
&\vee BigToSmall
\end{aligned}$$

$$\begin{aligned}
TypeOK &\triangleq \wedge small \in 0 \dots 3 \\
&\wedge big \in 0 \dots 5
\end{aligned}$$
