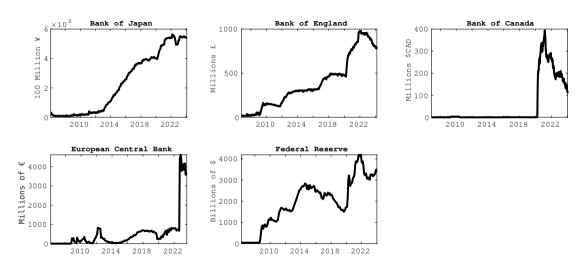
Interest rates, bank liquidity and credit frictions

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Sky-rocketing banking sector liquidity



Shows central bank reserve balances / deposit facility use

Background Model Model dynamics and policy 2/16

Bank liquidity and the credit channel

Increasing banking sector liquidity and UMPs have had an unclear affect on bank lending

Central banks injected huge amounts of liquidity, but banks often increase excess reserves rather than increase lending:

- ► 2008–2009 excess reserves in US ↑ while lending standards were tightened (source: SLOOS)
- ► 2010–2012 lots of liquidity in eurozone banking sector without increasing lending in stressed economies

Aim of Paper

Build a model to rationalise some of this evidence

- ► The ambiguous link between liquidity and lending
- ► Small business lending frictions

Use this to study:

- ► Role of monetary policy (interest rates, interest rate corridors, and UMPs)
- ► Interaction between liquidity and credit frictions

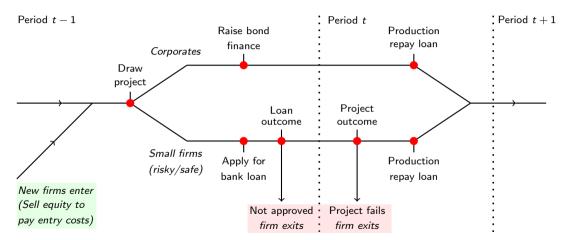
Model Overview

New Keynesian (Calvo) model + frictional bank lending:

- Households are standard
- ► Follow Swarbrick (2023) Stiglitz & Weiss (1981) information problem (see also, e.g., Ikeda 2020)
- ► Some firms have private information
- \blacktriangleright Each period draw either risky/safe projects (risk of productivity ω^i)
- ightharpoonup Expected productivity the same ightharpoonup $1 = \omega_t^s = p_t \omega_t^r$
- Banks can separate borrowers using loan approval
- ▶ When risk is high, banks can ration credit and hold excess reserves (paying CB deposit rate)

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Firms



Banks and lending 1/2

- ► Separate borrowers using loan approval
 - ► Abstract from collateral and loan size
 - lacktriangle Loan terms are repayment rate au_t^i and approval rate ax_t^i

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Banks and lending 1/2

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$$R_{t+1}^s - \tau_t^s \ge 0 \tag{1}$$

Risky incentive compatibility (IC) constraint binds

$$\underbrace{\mathbf{x}_{t}^{r} p_{t+1} \left(R_{t+1}^{r} - \tau_{t}^{r} \right)}_{\text{reluce shooting righty leap.}} \geq \underbrace{\mathbf{x}_{t}^{s} p_{t+1} \left(R_{t+1}^{r} - \tau_{t}^{s} \right)}_{\text{Surplus shooting righty leap.}} \tag{2}$$

Surplus choosing risky loan Surplus choosing safe loan

▶ The other not-always-binding IC/IR constraints imply: $x_t^r \ge x_t^s$

Banks and lending 2/2

▶ Consider IR and IC with no aggregate uncertainty (and using $p_t R_t^r = R_t^s$):

$$\tau_{t}^{s} = R_{t+1}^{s}$$

$$x_{t}^{r} p_{t+1} \left(R_{t+1}^{r} - \tau_{t}^{s} \right) = x_{t}^{s} p_{t+1} \left(R_{t+1}^{r} - \tau_{t}^{s} \right)$$

$$\Rightarrow \quad \tau_{t}^{r} = R_{t+1}^{r} \underbrace{-\frac{x_{t}^{s}}{x_{t}^{r}} \left(1 - p_{t+1} \right) R_{t+1}^{r}}_{\text{Information rents}}$$
(4)

Banks and lending 2/2

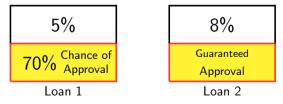
► Consider IR and IC with no aggregate uncertainty (and using $p_t R_t^r = R_t^s$):

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(4)

▶ Illustrative numbers – safe projects 5% return, risky projects 15% when successful:



Background Model Model dynamics and policy 8/16

Banks and lending 2/2

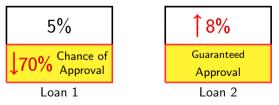
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▶ Illustrative numbers – safe projects 5% return, risky projects 15% when successful:



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Banks first-order conditions

Solution to the problem yields:

$$\mathbb{E}_{t}\left[\frac{\Lambda_{t,t+1}}{\Pi_{t,t+1}}\left(\rho_{t+1}R_{t+1}^{r}-R_{t}^{opp}\right)\right]=\varphi_{t}^{r}\frac{1}{1-\lambda}-\psi_{t}\frac{1}{1-\lambda}$$
(5)

$$\mathbb{E}_{t}\left[\frac{\Lambda_{t,t+1}}{\Pi_{t,t+1}}\left(\left(\lambda+\left(1-\lambda\right)\rho_{t+1}\right)R_{t+1}^{s}-R_{t}^{opp}\right)\right]=\varphi_{t}^{r}-\varphi_{t}^{s}$$
(6)

And

$$\varphi_t^s, \varphi_t^r, \psi_t \ge 0 \tag{7}$$

$$0 \le x_t^s \le x_t^r \le 1 \tag{8}$$

$$\varphi_t^s x_t^s = \varphi_t^r (1 - x_t^r) = \psi_t (x_t^r - x_t^s) = 0 \tag{9}$$

 R_t^{opp} is opportunity cost of funds (depends on interbank rate, interest on reserve balances etc)

Background

Model

Model dynamics and policy

Credit rationing

Consider the equilibrium with $\varphi_t^s = 0$ $(x_t^s > 0)$ and $\varphi_t^r > 0$ $(x_t^r = 1)$

- lacktriangle Credit rationing can occur if $\psi_t=0$ (no pooling), so $x_t^s<1$
- ► First-order conditions become

$$\psi_t = \mathbb{E}_t \left[\frac{\Lambda_{t,t+1}}{\Pi_{t,t+1}} \left(\left[\lambda - (1-\lambda) \left(1 - \rho_{t+1} \right) \right] R_{t+1}^s - \lambda R_t^{opp} \right) \right] \ge 0 \tag{10}$$

Credit rationing more likely if:

- ► More risk $1 p_{t+1} \uparrow$
- ▶ Lower return on capital $R_{t+1}^s \downarrow$
- ► Higher opportunity cost of funds R_t^{opp}

Implies thresholds beyond which banks ration credit

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Monetary policy

Standard Taylor rule

$$r_t^{mro} = \bar{r} + \gamma_\pi \left(\pi_{t-1,t} - \pi^* \right) + \gamma_y \left(y_t - \bar{y} \right) \tag{12}$$

- ▶ Think of this as the central bank setting the main refinancing rate at regular full -allotment auctions
- ▶ Interest rate on HH deposits $R_t = R_t^{mro}$ in equilbrium

Central bank also has two standing facilities

- ▶ Deposit facility paying R_t^{df} (excess reserves)
- ► Lending facility charging R_t^{lf}

We also allow the bank to conduct QE through purchasing assets from HHs — more on this if time

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Interest rates

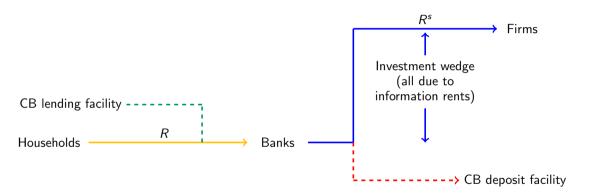
Benchmark - no liquidity risk, efficient financial markets



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Interest rates

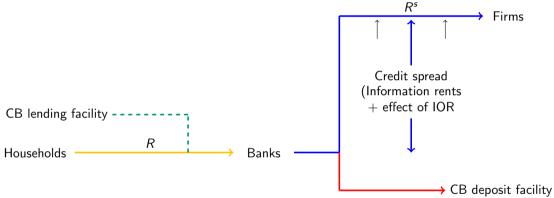
Benchmark - credit frictions, no liquidity risk, no excess liquidity



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Interest rates

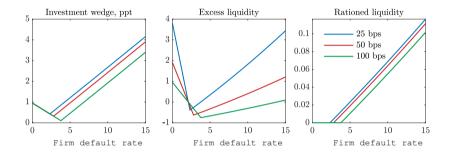
Benchmark – credit frictions, <u>with</u> excess liquidity, no liquidity risk



Note: interest rate corridor only matters when banks hold excess reserves

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Comparative statics – role of corridor



Result: changes in interest on reserves only affect economy through the effect on credit rationing.



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Example implementation:

Central Bank

Liabilities Assets

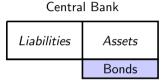
Bank

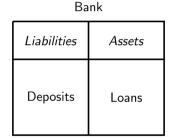
Liabilities	Assets
Deposits	Loans

e.g., Pension fund

Liabilities	Assets
Pension liabilities	Bonds

Example implementation:



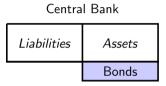


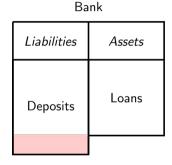
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Liabilities Assets

Pension Bonds
liabilities Deposits

Example implementation:





e.g., Pension fund

Liabilities Assets

Pension Bonds
liabilities Deposits

Example implementation:

Central Bank

Liabilities	Assets
Reserves	Bonds

Bank

Liabilities	Assets
Deposits	Loans
	Reserves

e.g., Pension fund

Liabilities	Assets
Pension liabilities	Bonds
	Deposits

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Example implementation:

Central Bank

Liabilities Assets

Reserves Bonds

Bank

Liabilities Assets

Deposits Loans

Reserves

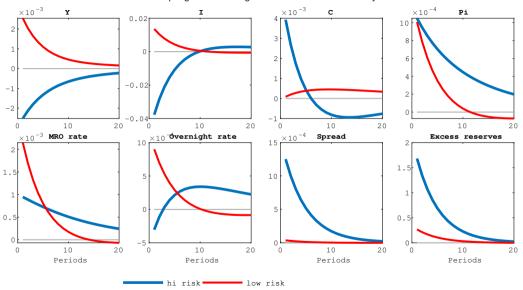
e.g., Pension fund

Liabilities	Assets
Pension liabilities	Bonds
	Deposits

- ► Lowers the return on bank assets
- $lackbox{}{}\Rightarrow$ money markets only clear at a lower overnight rate
- Overnight rate moves towards the floor (interest on reserves)

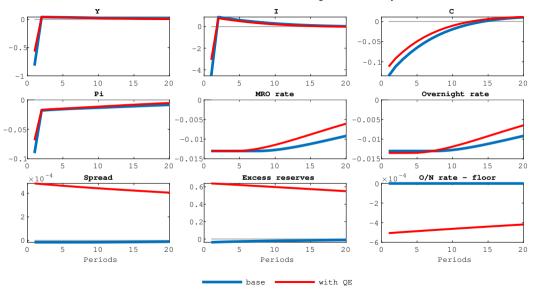
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QE programme -- high risk vs. low risk economy



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Demand shock with/without QE -- high risk economy



References I

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