## RS Force-Ladder Tilt for $\cos \theta_W(\mu)$ (No Empirical Inputs)

## Internal Note — Recognition Science

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Goal. Provide a parameter–free, monotone map for the weak mixing angle  $\cos \theta_W(\mu)$  used by the internal Z/W anchor, derived solely from the ledger gap series and the RS recognition energy. This removes all empirical low–energy inputs from the tilt curve while preserving the Z/W consistency identity that fixes the absolute unit s.

Construction. Let  $\varphi = \frac{1+\sqrt{5}}{2}$  and  $g_m = \frac{(-1)^{m+1}}{m\,\varphi^m}$ . Define the recognition length  $\lambda_{\rm rec} = \sqrt{\hbar G/(\pi c^3)}$  and  $E_{\rm rec} = \hbar c/\lambda_{\rm rec}$ . For a physical scale  $\mu$  (GeV), set

$$x(\mu) = \frac{\ln((\mu \, \text{GeV}) \times 10^9 \, \text{eV/GeV} / E_{\text{rec}})}{2 \, \ln \varphi}.$$

Define complementary ladder proxies via a smoothed alternating sum

$$a_Y(x) = \sum_{m \ge 1} g_m \tanh\left(\frac{x}{m}\right), \qquad a_2(x) = \sum_{m \ge 1} g_m \tanh\left(-\frac{x}{m}\right),$$

and map them to positive quantities  $\hat{\alpha}_1 = e^{a_Y}$  and  $\hat{\alpha}_2 = e^{a_2}$ . Using the GUT group factor  $g'^2 = \frac{3}{5}g_1^2$ , we set

$$\cos \theta_W^{\rm RS}(\mu) = \frac{\sqrt{\hat{\alpha}_2(\mu)}}{\sqrt{\frac{3}{5}\,\hat{\alpha}_1(\mu) + \hat{\alpha}_2(\mu)}}.$$

This map is smooth, monotone on the relevant interval (tens-hundreds of GeV), and contains no empirical inputs.

Use in the anchor. The internal Z/W anchor solves

$$F(\mu) = \frac{m_Z^{(\varphi)}}{m_W^{(\varphi)}} \cos \theta_W^{\text{RS}}(\mu) - 1 = 0, \qquad s = \frac{\mu_*}{m_W^{(\varphi)}}.$$

With  $m_W^{(\varphi)}$  and  $m_Z^{(\varphi)}$  the dimensionless ladder outputs, this determines the global absolute unit s internally. All sector absolutes follow as  $m_i = s m_i^{(\varphi)}$ .

## Remarks.

• The tanh smoothing implements a stable, scale-equivariant interpolation across ladder steps, with rapid convergence from the harmonic-geometric decay of  $|g_m|$ .

- The recognition energy  $E_{\rm rec}$  provides a natural RS reference; reporting  $s/E_{\rm rec}$  yields a dimensionless bridge constant.
- A full force-invariants derivation can replace the proxy exponents  $a_Y, a_2$ ; the present form is a minimal, parameter-free realization consistent with the ledger structure.