

## Introduction

**Statistical significance** means a  $p$ -value less than some chosen  $\alpha$  (e.g., 0.05).

We tend to think statistical significance implies there is something more than random sampling error.

Small  $p$ -values suggest results have meaning within the study context.

This is usually true but sometimes false.

Statistical significance is not the same as **practical significance**.

## Sample Size Influences $p$ -Values

One challenge: the  $p$ -value is related to sample size.

A small difference between the hypothesized mean ( $\mu_0$ ) and sample mean ( $\bar{X}$ ) can yield a small  $p$ -value, even if the difference is *practically* insignificant.

A large sample size ( $n$ ) can cause this erroneous conclusion.

Conversely, a small  $n$  can cause the opposite, erroneous conclusion.

A large difference between  $\mu_0$  and  $\bar{X}$  can still yield a large  $p$ -value if  $n$  is small.

If  $n$  is too small, you might not have collected enough data to show the difference between the sample statistic and the hypothesized population parameter.

## Practical Significance

One aspect of practical significance is **effect size**.

Effect size relates to the practical value of the effect.

Example: emotional intelligence study

$$\mu_0 = 120$$

$$n = 130$$

$$\bar{X} = 122$$

The  $p$ -value is very close to zero.

Difference between  $\bar{X}$  (122) and  $\mu_0$  (120) is just 2 points.

Is this practically significant? What does this mean in terms of EI?

If not practically significant, statistical significance doesn't matter.

## A Practical Significance Benchmark

What makes a value practically significant?

For emotional intelligence scores, we might review the literature:

Imagine that research says a 5-point EI difference can affect a person's ability to function emotionally.

This provides a benchmark for practical significance.

The benchmark tells us that our 2-point difference isn't meaningful, regardless of the small  $p$ -value.

## Effect Size and Cohen's $d$

Effect size is a way to measure practical significance.

**Cohen's  $d$**  is a statistical method that allows us to calculate an effect size.

$$d = \left| \frac{(\bar{x} - \mu_0)}{s} \right|$$

For the EI example:

$$d = \left| \frac{(122 - 120)}{15} \right| = 0.133$$

Cohen provided a framework to categorize effects as small, medium, or large.

$d \leq 0.2$  signifies a "small" effect.

Our  $d = 0.133$  is below that threshold, so it is a "small" effect.

Any statistical significance might be the result of a large  $n$ .

$d > 0.8$  signifies a "large" effect.

Even without statistical significance,  $d \geq 0.8$  suggests a large effect.

$0.2 < d < 0.8$  signifies a "medium" effect.

This doesn't clearly suggest whether an effect is practically significant.

## Summary

A statistically significant  $p$ -value does not imply useful results.

We want useful results to help us make decisions about practical issues.