DATA 621—Assignment no. 3

Critical Thinking Group 2 October 30, 2019

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Executive Overview

In this homework assignment, you will explore, analyze and model a data set containing information on crime for various neighborhoods of a major city. Each record has a response variable indicating whether or not the crime rate is above the median crime rate (1) or not (0).

Your objective is to build a binary logistic regression model on the training data set to predict whether the neighborhood will be at risk for high crime levels.

Below is a short description of the variables of interest in the data set:

Variable	Description
zn	proportion of residential land zoned for large lots (over 25000 square feet) (predictor variable)
indus	proportion of non-retail business acres per suburb (predictor variable)
chas	a dummy var. for whether the suburb borders the Charles River (1) or not (0) (predictor variable)
nox	nitrogen oxides concentration (parts per 10 million) (predictor variable)
rm	average number of rooms per dwelling (predictor variable)
age	proportion of owner-occupied units built prior to 1940 (predictor variable)
dis	weighted mean of distances to five Boston employment centers (predictor variable)
rad	index of accessibility to radial highways (predictor variable)
tax	full-value property-tax rate per \$10,000 (predictor variable)
ptratio	pupil-teacher ratio by town (predictor variable)
black	1000(Bk - 0.63)2 where Bk is the proportion of blacks by town (predictor variable)
lstat	lower status of the population (percent) (predictor variable)
medv	median value of owner-occupied homes in \$1000s (predictor variable)
target	whether the crime rate is above the median crime rate (1) or not (0) (response variable)

Create train and test sets using the caret machine learning package:

Only use the train data frame until the very end of the process, when we use test to evaluate how effective the model is!

```
df <- read.csv('crime-training-data_modified.csv', stringsAsFactors=FALSE)
set.seed(1804)
#80% train, 20% test split
train_ix <- createDataPartition(df$target, p=0.8, list=FALSE)
train <- df[train_ix, ]
test <- df[-train_ix, ]
rm(df)</pre>
```

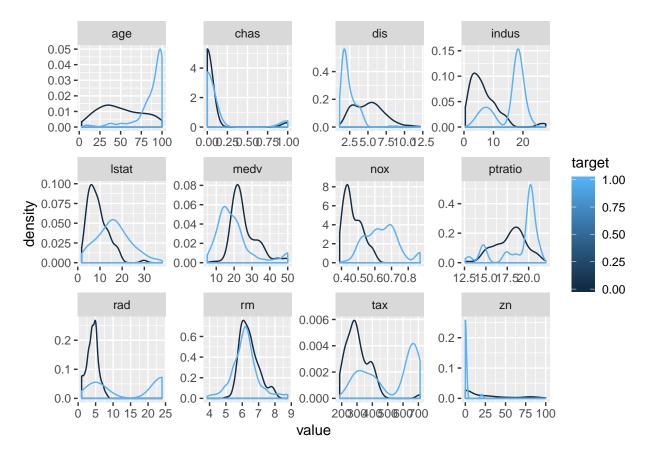
Data Exploration

Below is descriptive statistic of the variables. There are no NA values.

```
(train.summary <- data.frame(unclass(summary(train)), row.names = NULL))
                            X....indus
                                              X....chas
            X....zn
                                                                 X....nox
## 1 Min.
            : 0.00
                              : 0.46
                                       Min.
                                               :0.00000
                                                          Min.
                                                                 :0.3890
## 2 1st Qu.:
               0.00
                      1st Qu.: 5.13
                                       1st Qu.:0.00000
                                                          1st Qu.:0.4480
## 3 Median :
               0.00
                      Median: 9.90
                                       Median :0.00000
                                                          Median :0.5380
## 4 Mean
            : 11.66
                      Mean
                              :11.14
                                       Mean
                                               :0.07775
                                                          Mean
                                                                 :0.5571
## 5 3rd Qu.: 12.50
                      3rd Qu.:18.10
                                                          3rd Qu.:0.6470
                                       3rd Qu.:0.00000
            :100.00
## 6 Max.
                      Max.
                             :27.74
                                       Max.
                                              :1.00000
                                                          Max.
                                                                 :0.8710
##
           X....rm
                             X....age
                                              X....dis
                                                                X....rad
## 1 Min.
            :3.863
                             : 2.90
                                               : 1.130
                                                                : 1.000
                     Min.
                                       Min.
                                                         Min.
                     1st Qu.: 43.70
## 2 1st Qu.:5.913
                                       1st Qu.: 2.022
                                                         1st Qu.: 4.000
## 3 Median :6.226
                     Median: 78.70
                                       Median : 3.092
                                                         Median : 5.000
## 4 Mean
            :6.298
                             : 68.47
                                       Mean
                                              : 3.748
                                                         Mean
                                                                : 9.729
                     Mean
                     3rd Qu.: 94.60
## 5 3rd Qu.:6.635
                                       3rd Qu.: 5.212
                                                         3rd Qu.:24.000
## 6 Max.
            :8.780
                     Max.
                             :100.00
                                       Max.
                                              :12.127
                                                         Max.
                                                                :24.000
##
           X....tax
                          X...ptratio
                                           X....lstat
                                                            X....medv
## 1 Min.
            :187.0
                             :12.60
                                             : 1.73
                                                              : 5.00
                                                       Min.
                     Min.
                                      Min.
## 2 1st Qu.:281.0
                     1st Qu.:17.00
                                      1st Qu.: 6.75
                                                       1st Qu.:17.00
## 3 Median :345.0
                     Median :18.90
                                      Median :11.32
                                                       Median :21.50
## 4 Mean
            :412.6
                     Mean
                             :18.41
                                      Mean
                                            :12.63
                                                       Mean
                                                              :22.81
## 5 3rd Qu.:666.0
                     3rd Qu.:20.20
                                      3rd Qu.:17.09
                                                       3rd Qu.:26.20
## 6 Max.
            :711.0
                             :22.00
                                             :37.97
                                                              :50.00
                     Max.
                                      Max.
                                                       Max.
##
          X....target
            :0.0000
## 1 Min.
## 2 1st Qu.:0.0000
## 3 Median :0.0000
## 4 Mean
            :0.4987
## 5 3rd Qu.:1.0000
## 6 Max.
            :1.0000
```

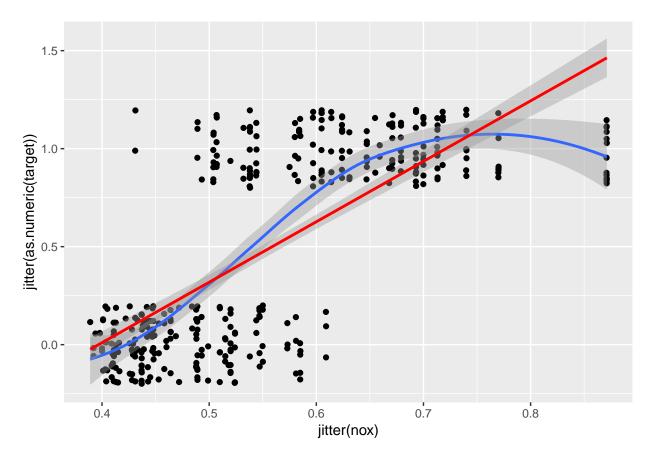
There don't seem to be any outliers or missing data, so we will proceed directly to examining the variables. First, histograms of each variable for each target class:

```
train %>%
  gather(-target, key='variable', value='value') %>%
  ggplot(aes(x=value, group=target, color=target)) +
   facet_wrap(~ variable, scales='free') +
   geom_density()
```



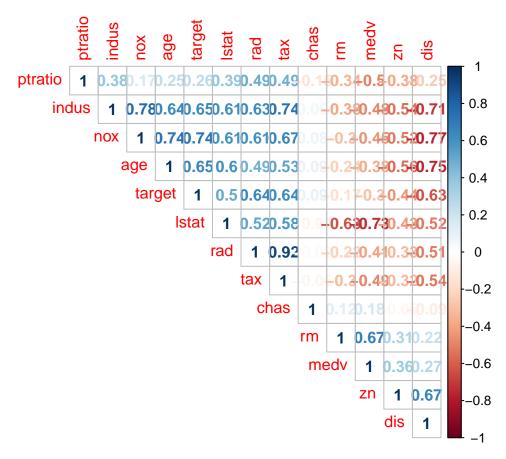
Most variables have distinct shapes for each target class. chas and zn are quite skewed, and do not appear terribly informative. indus and tax have two peaks for target = 1, indicating there are two separate processes at work there.

```
ggplot(train, aes(x=jitter(nox), y=jitter(as.numeric(target)))) +
  geom_point() +
  geom_smooth() +
  geom_smooth(method='lm', color='red')
```



It is to be expected that many of these variables will be correlated with each other:

corrplot(cor(train), type='upper', method='number', order='hclust')



Obviously, the concentration of industry is strongly and positively correlated with nitrogen oxide concentration $\rho=0.78$). Parent-teacher ratio is negatively correlated with median property values ($\rho=-0.5$), and positively correlated with property taxes ($\rho=0.49$). What these and other variables are really getting at is *economic class*. Each measures a different phenomenon, but can be conceived of as operationalizing one thing. This suggests PCA may be useful on this dataset.

Checking for interactions

Given the high correlation between the variables, it may be the case that there are numerous interactions that can improve our modeling. In this section, we attempt to determine if this is the case. We will group numeric variables by membership in quartile, and examine line plots.

```
calc_percentile <- function(x){
  trunc(rank(x)) / length(x)
}</pre>
```

Data Preparation

Modeling

Function to calculate McFadden's pseudo- R^2 for logistic models:

```
calc_r2 <- function(model) {
  1 - model$deviance / model$null.deviance
}</pre>
```

M_0 : Dummy model

Baseline model, which just predicts the class proportion, which is nearly balanced between the two classes. If we are having trouble improving on this model, we know we are doing something wrong.

This dummy model has an accuracy of about 0.50, sensitivity of 1, and specificity of 0. Since it has zero predictive power, we know that it has a pseudo- R^2 of 0.

```
m 0 <- glm(target ~ 1, train, family=binomial())</pre>
pred_0 <- factor(round(predict(m_0, train, type='response')), levels=c('0', '1'))</pre>
confusionMatrix(data=pred_0, reference=factor(train$target, levels=c('0', '1')))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
                    1
##
            0 187 186
##
##
##
                  Accuracy : 0.5013
                    95% CI: (0.4494, 0.5532)
##
##
       No Information Rate: 0.5013
##
       P-Value [Acc > NIR] : 0.5207
##
##
                     Kappa: 0
##
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 1.0000
##
               Specificity: 0.0000
            Pos Pred Value: 0.5013
##
            Neg Pred Value :
##
                Prevalence: 0.5013
##
##
            Detection Rate: 0.5013
##
      Detection Prevalence: 1.0000
         Balanced Accuracy: 0.5000
##
##
          'Positive' Class : 0
##
##
```

M_1 : Full model

0 173 19

The next simplest model uses all available data, without transformations or interactions or polynomials:

```
m_1 <- glm(target ~ zn + indus + chas + nox + rm + age + dis + rad + tax + ptratio + lstat + medv, train
pred_1 <- factor(round(predict(m_1, train, type='response')), levels=c('0', '1'))
calc_r2(m_1)

## [1] 0.7216759

confusionMatrix(data=pred_1, reference=factor(train$target, levels=c('0', '1')))

## Confusion Matrix and Statistics
##
## Reference
## Prediction 0 1</pre>
```

```
##
            1 14 167
##
##
                  Accuracy: 0.9115
                    95% CI: (0.878, 0.9383)
##
##
       No Information Rate: 0.5013
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.823
##
##
   Mcnemar's Test P-Value: 0.4862
##
               Sensitivity: 0.9251
##
##
               Specificity: 0.8978
            Pos Pred Value: 0.9010
##
##
            Neg Pred Value: 0.9227
##
                Prevalence: 0.5013
##
            Detection Rate: 0.4638
##
      Detection Prevalence: 0.5147
##
         Balanced Accuracy: 0.9115
##
##
          'Positive' Class : 0
##
```

M_2 : Stepwise variable selection with interactions

We know that variable interaction is probably likely. We can automatically test all interactions using stepwise selection:

```
##
## Call:
  glm(formula = target ~ zn + indus + chas + nox + rm + age + dis +
       rad + tax + ptratio + lstat + medv + ptratio:lstat + chas:tax +
##
      nox:age + rm:lstat + rm:age + age:medv + nox:ptratio + dis:tax +
       indus:tax + tax:medv + indus:dis + age:lstat, family = binomial(),
##
       data = train)
##
## Deviance Residuals:
       Min
                   10
                         Median
                                       3Q
                                                Max
## -1.70636 -0.00332
                        0.00000
                                  0.00000
                                            2.57482
##
## Coefficients:
##
                   Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                  2.503e+00 8.456e+01
                                       0.030 0.976389
                 -4.539e-01 1.865e-01
                                       -2.433 0.014958 *
## zn
## indus
                 -2.261e+00
                             8.363e-01
                                        -2.703 0.006862 **
## chas
                 -6.926e+03 4.370e+05
                                       -0.016 0.987355
## nox
                  3.607e+02 1.952e+02
                                        1.848 0.064661 .
## rm
                 -2.264e+01 7.012e+00
                                       -3.228 0.001247 **
## age
                 -2.219e+00 5.930e-01
                                        -3.742 0.000182 ***
                -1.474e+01 5.996e+00 -2.459 0.013933 *
## dis
```

```
## tax
                 -3.465e-01
                             1.186e-01
                                        -2.922 0.003473 **
                             4.858e+00
## ptratio
                  8.824e+00
                                          1.817 0.069279
                 -1.399e+00
## 1stat
                             2.456e+00
                                        -0.570 0.568786
## medv
                  9.272e-01
                             7.603e-01
                                          1.220 0.222642
## ptratio:lstat 2.242e-01
                            1.271e-01
                                          1.764 0.077731
## chas:tax
                  2.502e+01
                             1.578e+03
                                          0.016 0.987343
## nox:age
                  1.362e+00
                             5.341e-01
                                          2.549 0.010789 *
## rm:lstat
                 -5.908e-01
                             2.796e-01
                                        -2.113 0.034585 *
## rm:age
                  3.657e-01
                             9.577e-02
                                          3.819 0.000134 ***
## age:medv
                 -3.075e-02
                             9.117e-03
                                        -3.372 0.000745 ***
## nox:ptratio
                 -1.843e+01
                             9.957e+00
                                        -1.851 0.064239
                  5.026e-02
                             1.892e-02
                                          2.656 0.007913 **
## dis:tax
## indus:tax
                  5.110e-03
                             1.884e-03
                                          2.713 0.006672 **
## tax:medv
                  4.637e-03
                             1.871e-03
                                          2.477 0.013231 *
## indus:dis
                  1.913e-01
                             1.284e-01
                                          1.490 0.136209
                  7.722e-03 3.927e-03
                                          1.966 0.049257 *
## age:lstat
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 517.085
                               on 372
                                       degrees of freedom
## Residual deviance: 50.534
                               on 348
                                       degrees of freedom
## AIC: 100.53
## Number of Fisher Scoring iterations: 25
However, this model is probably overfit. By common heuristic, we have enough data for:
min(table(train$target)) / 15
```

3.639 0.000274 ***

```
## [1] 12.4
```

rad

i.e., 12 variables.

M_3 : Adjusting for multiple significance tests

2.495e+00

6.857e-01

To correct for this overfitting, we will use the p.adjust function to revise our p-values, and then use those that remain significant at p = 0.05 for the next model:

```
m_2_p <- summary(m_2)$coefficients[,4]
sort(p.adjust(m_2_p))</pre>
```

```
##
                                                     age:medv
          rm:age
                            age
                                           rad
                                                                          rm
##
     0.003352611
                    0.004375544
                                   0.006294925
                                                  0.016389911
                                                                 0.026180977
##
                          indus
                                     indus:tax
                                                      dis:tax
                                                                     nox:age
             tax
##
     0.069463666
                    0.126774120
                                   0.126774120
                                                  0.134529104
                                                                 0.172628530
##
                                                                   age:1stat
               zn
                            dis
                                      tax:medv
                                                     rm:lstat
##
     0.198464177
                    0.198464177
                                   0.198464177
                                                  0.415017379
                                                                 0.541826029
##
                        ptratio ptratio:lstat
                                                 nox:ptratio
                                                                   indus:dis
##
     0.642394932
                    0.642394932
                                   0.642394932
                                                  0.642394932
                                                                 0.817253780
##
     (Intercept)
                           chas
                                         lstat
                                                         medv
                                                                    chas:tax
     1.00000000
                    1.00000000
                                   1.00000000
                                                  1.00000000
                                                                 1.00000000
```

Using the top values (including any variable as well as interaction effect:

```
m_3 <- glm(target ~ age*rm + rad + age*medv, train, family=binomial())</pre>
pred_3 <- factor(round(predict(m_3, train, type='response')), levels=c('0', '1'))</pre>
confusionMatrix(data=pred_3, reference=factor(train$target, levels=c('0', '1')))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
                    1
##
            0 160 22
##
            1 27 164
##
##
                  Accuracy : 0.8686
                    95% CI : (0.8301, 0.9012)
##
##
       No Information Rate: 0.5013
       P-Value [Acc > NIR] : <2e-16
##
##
##
                      Kappa: 0.7373
##
    Mcnemar's Test P-Value: 0.5677
##
##
##
               Sensitivity: 0.8556
##
               Specificity: 0.8817
            Pos Pred Value: 0.8791
##
##
            Neg Pred Value: 0.8586
##
                Prevalence: 0.5013
##
            Detection Rate: 0.4290
##
      Detection Prevalence: 0.4879
##
         Balanced Accuracy: 0.8687
##
##
          'Positive' Class : 0
##
calc_r2(m_3)
```

[1] 0.609916

The psuedo- R^2 is naturally much less than the overfit M_2 . Presumably, it will be better fit to the hold-out sample, however. We do see theat sensitivity, specificity, and pos/neg predictive value are actually still pretty strong. As expected and required, all variables are extremely significant.

```
summary(m_3)
```

```
##
## Call:
  glm(formula = target ~ age * rm + rad + age * medv, family = binomial(),
       data = train)
##
##
##
  Deviance Residuals:
                      Median
##
       Min
                 1Q
                                    3Q
                                            Max
##
   -1.9933
            -0.3056
                     -0.0112
                                0.0131
                                         3.9635
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 29.933949
                            9.484583
                                       3.156 0.001599 **
                            0.116138 -3.372 0.000747 ***
## age
               -0.391606
## rm
               -9.166313
                            2.215904 -4.137 3.52e-05 ***
```

```
## rad
               0.572715
                           0.131517
                                     4.355 1.33e-05 ***
                                     4.365 1.27e-05 ***
## medv
               0.767617
                           0.175859
                           0.026477
## age:rm
               0.108631
                                     4.103 4.08e-05 ***
               -0.008883
                           0.002072 -4.288 1.80e-05 ***
## age:medv
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 517.09 on 372
                                     degrees of freedom
## Residual deviance: 201.71
                             on 366
                                     degrees of freedom
## AIC: 215.71
##
## Number of Fisher Scoring iterations: 8
```

M_4 : Previous model + a few more predictors

We noted above that we have data for up to 12 variables in this model, so I will include the first 12 significant variables of the p-value adjustment:

```
m_4 <- glm(target ~ age*rm + rad + age*medv +
             indus*tax + dis*tax + nox*age + zn, train, family=binomial())
pred_4 <- factor(round(predict(m_4, train, type='response')), levels=c('0', '1'))</pre>
confusionMatrix(data=pred_4, reference=factor(train$target, levels=c('0', '1')))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
               0
##
            0 174 14
##
            1 13 172
##
##
                  Accuracy : 0.9276
##
                    95% CI: (0.8964, 0.9518)
##
       No Information Rate: 0.5013
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.8552
##
    Mcnemar's Test P-Value : 1
##
##
##
               Sensitivity: 0.9305
##
               Specificity: 0.9247
            Pos Pred Value: 0.9255
##
##
            Neg Pred Value: 0.9297
##
                Prevalence: 0.5013
##
            Detection Rate: 0.4665
##
      Detection Prevalence: 0.5040
##
         Balanced Accuracy: 0.9276
##
          'Positive' Class : 0
##
##
calc_r2(m_4)
```

[1] 0.7624825

Despite adding all these variables, we see that the confusion matrix evaluations are not that much higher. Psuedo- R^2 did take a nice bump, though. Nonetheless, it is possible that this model does not fit the hold out sample as well as M_3 .

```
summary(m_4)
##
## Call:
  glm(formula = target ~ age * rm + rad + age * medv + indus *
       tax + dis * tax + nox * age + zn, family = binomial(), data = train)
##
## Deviance Residuals:
                         Median
                                       3Q
                   1Q
                                                 Max
## -1.99998 -0.17796
                        0.00000
                                  0.00012
                                            2.94942
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) 36.3490667 16.0747814
                                       2.261 0.023744 *
                                      -3.427 0.000611 ***
## age
               -0.7613783
                           0.2221787
               -8.3921084
                           2.5514316
                                      -3.289 0.001005 **
## rm
## rad
                1.0682193
                           0.2427743
                                       4.400 1.08e-05 ***
## medv
                0.8831142
                           0.2527643
                                       3.494 0.000476 ***
## indus
               -0.3370128
                           0.1593284
                                      -2.115 0.034412 *
## tax
               -0.0572609
                           0.0206903
                                      -2.768 0.005648 **
## dis
               -2.7775922 1.4321662
                                      -1.939 0.052448
## nox
                0.9108840 17.1773095
                                       0.053 0.957709
               -0.2092179 0.0602181
                                      -3.474 0.000512 ***
## zn
## age:rm
                0.1058911 0.0318826
                                       3.321 0.000896 ***
## age:medv
               -0.0105802
                           0.0029532
                                      -3.583 0.000340 ***
## indus:tax
                0.0008713
                           0.0004702
                                       1.853 0.063907 .
                                       2.676 0.007452 **
## tax:dis
                0.0122552
                           0.0045798
## age:nox
                0.7561247
                           0.2713618
                                       2.786 0.005330 **
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 517.09 on 372
                                      degrees of freedom
## Residual deviance: 122.82 on 358 degrees of freedom
## AIC: 152.82
## Number of Fisher Scoring iterations: 10
M_5: PCA
pca <- prcomp(train[,1:12], retx=TRUE, center=TRUE, scale=TRUE)</pre>
summary(pca)
## Importance of components:
                             PC1
                                    PC2
                                            PC3
                                                    PC4
                                                            PC5
                                                                    PC6
##
## Standard deviation
                          2.4660 1.2794 1.04731 0.9172 0.88763 0.63278
## Proportion of Variance 0.5067 0.1364 0.09141 0.0701 0.06566 0.03337
## Cumulative Proportion 0.5067 0.6431 0.73455 0.8047 0.87031 0.90368
##
                                              PC9
                              PC7
                                      PC8
                                                      PC10
                                                              PC11
                          0.53845 0.52925 0.45673 0.42813 0.36816 0.24159
## Standard deviation
```

```
## Proportion of Variance 0.02416 0.02334 0.01738 0.01527 0.01129 0.00486 ## Cumulative Proportion 0.92784 0.95118 0.96857 0.98384 0.99514 1.00000
```

The first five account for 87 percent of variation, so we will use those for modeling:

```
pca_df <- as.data.frame(cbind(train$target, pca$x[,1:5]))
colnames(pca_df) <- c('target', 'PC1', 'PC2', 'PC3', 'PC4', 'PC5')
m_5 <- glm(target ~ ., pca_df, family=binomial())
pred_5 <- factor(round(predict(m_5, pca_df, type='response')), levels=c('0', '1'))
confusionMatrix(data=pred_5, reference=factor(train$target, levels=c('0', '1')))</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
              0 1
##
            0 162 36
            1 25 150
##
##
##
                  Accuracy : 0.8365
                    95% CI: (0.7949, 0.8725)
##
##
       No Information Rate: 0.5013
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.6729
##
##
   Mcnemar's Test P-Value: 0.2004
##
##
               Sensitivity: 0.8663
##
               Specificity: 0.8065
            Pos Pred Value: 0.8182
##
##
            Neg Pred Value: 0.8571
                Prevalence: 0.5013
##
##
            Detection Rate: 0.4343
      Detection Prevalence: 0.5308
##
##
         Balanced Accuracy: 0.8364
##
##
          'Positive' Class : 0
##
```

[1] 0.5806149

calc_r2(m_5)

This model has similar confusion matrix evaluation values as some models above, though it's psuedo- \mathbb{R}^2 value is a bit low.

The results of this exercise with PCA seem to suggests there are three seperate 'clusters' of phenomenon that affect crime level, at least at a statistically significant level. All three are negative related.

```
summary(m_5)
```

```
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.33271
                         0.26973
                                  1.233 0.2174
## PC1
              -1.18169
                          0.13143 -8.991 < 2e-16 ***
## PC2
              -0.90733
                          0.15730 -5.768 8.01e-09 ***
## PC3
              -0.62027
                          0.24223 - 2.561
                                           0.0104 *
              -0.02799
                          0.18400 -0.152
                                           0.8791
## PC4
## PC5
              -0.15736
                          0.20946 -0.751
                                           0.4525
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 517.09 on 372 degrees of freedom
## Residual deviance: 216.86 on 367 degrees of freedom
## AIC: 228.86
##
## Number of Fisher Scoring iterations: 6
```

Evaluating the Models on the Test Set

```
# Don't run until the very end
# confusionMatrix(data=predict(model, test), reference=test$target)
# Evaluate on F1 score
# For PCA prediction:
# pred_xx <- factor(round(predict(m_5, as.data.frame(predict(pca, newdata=test)), type='response')), le</pre>
```

Analysis of Final Model