CSE-321 Assignment 5 (100 points)

gla@postech

Due at 11:59pm, April 7 (Monday)

In this assignment, you will implement the type system of TML (Typed ML) which is essentially the simply typed λ -calculus without the type void.

The abstract syntax for TML is shown below. Compared with the abstract syntax for the simply typed λ -calculus discussed in class, it includes another base type int for integers, but omits the type void which is useless in practice. \hat{n} denotes an integer n, and plus and minus are arithmetic operators on integers; eq tests two integers for equality.

The concrete syntax for TML is as follows. All entries in the right side of the definition below are arranged in the same order that their counterparts in the abstract syntax appear in the definition above:

We add two forms of syntactic sugar:

```
let x:A = e in e' for (\operatorname{fn} x:A \Rightarrow e') e
let \operatorname{rec} x:A = e in e' for (\operatorname{fn} x:A \Rightarrow e') (\operatorname{fix} x:A. e)
```

(A) is the same as A, and is used to alter the default right associativity of \rightarrow . For example, $A_1 \rightarrow A_2 \rightarrow A_3$ is equal to $A_1 \rightarrow (A_2 \rightarrow A_3)$ which is different from $(A_1 \rightarrow A_2) \rightarrow A_3$. Similarly (e) is the same as e, and is used to alter the default left associativity of applications. For example, $e_1 \ e_2 \ e_3$ is equal to $(e_1 \ e_2) \ e_3$ which is different from $e_1 \ (e_2 \ e_3)$.

The goal of this assignment is to implement the type system of TML shown in Figure 1.

Programming instruction

Download hw5.zip from the course webpage or the handin directory, and unzip it on your working directory. It will create a bunch of files on the working directory.

First see tml.ml which declares a structure Tml:

```
type var = string
type tp =
    ...
type exp =
    ...
```

Figure 1: Type system of TML

The datatypes tp and exp correspond to the syntactic categories type and expression, respectively. Read the comments in the file and make sure that you understand what each data constructor is for.

Next see typing.mli and typing.ml. The goal is to implement the function typing in the structure Typing:

```
val typing : context -> Tml.exp -> Tml.tp
```

That is, typing takes a typing context Γ of type Typing.context and an expression e of type Tml.exp, and returns a type A such that $\Gamma \vdash e : A$; it raises an exception TypeError if e does not typecheck, i.e., there is no A such that $\Gamma \vdash e : A$.

Note that you will decide the definition of type Typing.context yourself. In the stub file, Typing.context is defined as unit, but you should replace it by an appropriate type for typing contexts. After deciding the definition of Typing.context, you have to implement the function createEmptyContext which returns an empty typing context:

```
val createEmptyContext : unit -> context
```

Then try to implement the rule Var to make sure that you can retrieve an individual element (which is a type binding x:A) from a typing context.

You have to think about how to represent $\Gamma, x: A$ which is required by the rules \rightarrow I, +E, and Fix. If we wanted to maintain the invariant that variables in a typing context are all distinct, we would need α -conversion for these rules. It turns out, however, that we do not need α -conversion at all! Think about this. (Or take a wrong path and implement α -conversion, if you like.)

As another tip, if you are tempted to use (Tml.var * Tml.tp) list for Typing.context, think again. (Tml.var * Tml.tp) list is definitely a good candidate for the definition of Typing.context (and indeed a reasonably good solution), but try to come up with a better and more elegant definition.

After implementing the function typing in typing.ml, run the command make to compile the sources files.

```
gla@ubuntu:~/temp/hw5$ make
ocamlc -thread -c tml.ml -o tml.cmo
ocamlyacc parser.mly
26 shift/reduce conflicts.
ocamlc -c parser.mli
ocamlc -c parser.ml
ocamllex lexer.mll
```

```
67 states, 4625 transitions, table size 18902 bytes

ocamlc -c lexer.ml

ocamlc -thread -c typing.mli -o typing.cmi

ocamlc -thread -c typing.ml -o typing.cmo

ocamlc -thread -c inout.ml -o inout.cmo

ocamlc -thread -c eval.ml -o eval.cmo

ocamlc -thread -c loop.ml -o loop.cmo

ocamlc -thread -c hw5.ml -o hw5.cmo

ocamlc -o lib.cma -a tml.cmo parser.cmo lexer.cmo typing.cmo inout.cmo eval.cmo loop.cmo

ocamlc -o hw5 lib.cma hw5.cmo
```

There are two ways to test your code in typing.ml. First you can run hw5. At the TML prompt, enter a TML expression followed by the semicolon symbol; (The syntax of TML will be given shortly.) Each time you press the return key, a reduced expression is displayed.

```
gla@ubuntu:~/temp/hw5$ ./hw5
Tml> fn : int => x ;
Syntax error
Tml> fn x : int => x ;
(fn x : int => x) : int -> int
Tml> x;
x has no type.
```

Alternatively you can use those functions in loop.ml in the interactive mode of OCAML. (You don't actually need to read loop.ml.) At the OCAML prompt, type #load ''lib.cma';; to load the library for this assignment. Then open the structure Loop:

Submission instruction

- 1. Make sure that you can compile typing.ml by running make.
- 2. When you have your file typing.ml ready for submission, copy it to your hand-in directory on programming2.postech.ac.kr. For example, if your Hemos ID is foo, copy your typing.ml to:

/home/class/cs321/handin/foo/