

20220312 박준혁

1.1 $s \text{ lparen} \rightarrow s \text{ mparen}$

By rule induction on the judgment $s \text{ lparen}$.

case $\frac{}{\epsilon \text{ lparen}} L\epsilon ps$ where $s = \epsilon$

$\epsilon \text{ mparen}$

by rule $M\epsilon ps$

case $\frac{s_1 \text{ lparen} \quad s_2 \text{ lparen}}{(s_1) s_2 \text{ lparen}} Lseq$ where $s = (s_1) s_2$

$s_1 \text{ mparen}$

induction hypothesis on $s_1 \text{ lparen}$

$s_2 \text{ mparen}$

induction hypothesis on $s_2 \text{ lparen}$

$(s_1) \text{ mparen}$

by the rule $Mpar$

$(s_1) s_2 \text{ mparen}$

by the rule $Mseq$

1.2 $s \text{ tparen}$ and $s' \text{ tparen} \rightarrow ss' \text{ tparen}$

\leftrightarrow if $s' \text{ tparen}$, $s \text{ tparen}$ implies $ss' \text{ tparen}$

By rule induction on the judgment $s' \text{ tparen}$

case $\frac{}{\epsilon \text{ tparen}} T\epsilon ps$ where $s' = \epsilon$

$s \text{ tparen}$

assumption

$ss' = s\epsilon = s$

by definition of epsilon

$ss' \text{ tparen}$

by assumption

case $\frac{s_1 \text{ tparen} \quad s_2 \text{ tparen}}{s_1 (s_2) \text{ tparen}} Tseq$ where $s' = s_1 (s_2)$

$s \text{ tparen}$

assumption

$s \text{ tparen}$ implies $s s_1 \text{ tparen}$

induction hypothesis on $s_1 \text{ tparen}$

$s s_1 \text{ tparen}$

from assumption

$ss' = ss_1 (s_2)$

assumption

$s s_1 (s_2) \text{ tparen}$

by rule $Tseq$ ($s_1 = s s_1$, $s_2 = s_2$)

1.3 $s \text{ mparen} \rightarrow s \text{ tparen}$

By rule induction on the judgment $s \text{ mparen}$

case $\frac{}{\epsilon \text{ mparen}} M_{eps}$ where $s = \epsilon$

$\epsilon \text{ tparen}$

by Rule Teps

case $\frac{s' \text{ mparen}}{(s') \text{ mparen}} M_{par}$ where $s = (s')$

$s' \text{ tparen}$

induction hypothesis on $s' \text{ mparen}$

$\epsilon \text{ tparen}$

by Rule Teps

$(s') \text{ tparen}$

by Rule Tseq ($s_1=e$, $s_2=s'$) and

$e(s_2) = (s_2)$

case $\frac{s_1 \text{ mparen} \quad s_2 \text{ mparen}}{s_1 \ s_2 \text{ mparen}} M_{seq}$ where $s = s_1 \ s_2$

$s_1 \text{ tparen}$

induction hypothesis on $s_1 \text{ mparen}$

$s_2 \text{ tparen}$

induction hypothesis on $s_2 \text{ mparen}$

$s_1 s_2 \text{ tparen}$

by lemma 1.2