



Nodal equivalent force.

$$\{f\}_P = \int_S [N]^T \cdot \begin{Bmatrix} \phi_x \\ \phi_y \end{Bmatrix} t ds.$$

$$\begin{Bmatrix} \phi_x \\ \phi_y \end{Bmatrix} t ds = \begin{Bmatrix} -\sigma t ds \sin \beta + \tau t ds \cos \beta \\ \tau t ds \sin \beta + \sigma t ds \cos \beta \end{Bmatrix}$$

$$= \begin{Bmatrix} \tau dx - \sigma dy \\ \sigma dx + \tau dy \end{Bmatrix} t$$

$$dx = J_{11} d\xi, \quad dy = J_{12} d\xi. \quad (\text{Definition of Jacobian})$$

$$\therefore \{f_x\} = \int_{-1}^1 [N]^T (\tau J_{11} - \sigma J_{12}) t d\xi.$$

$$\{f_y\} = \int_{-1}^1 [N]^T (\sigma J_{11} + \tau J_{12}) t d\xi.$$