

A Multiplication Layer for Sequence Data



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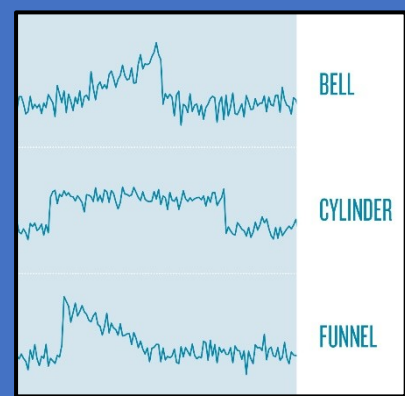
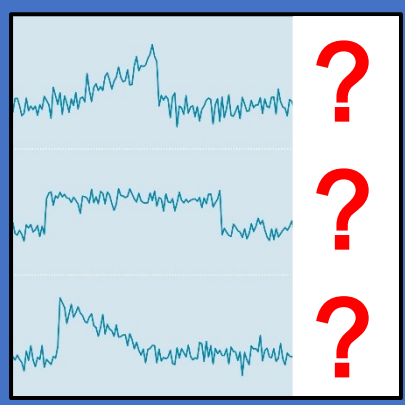
Kyushu University

START

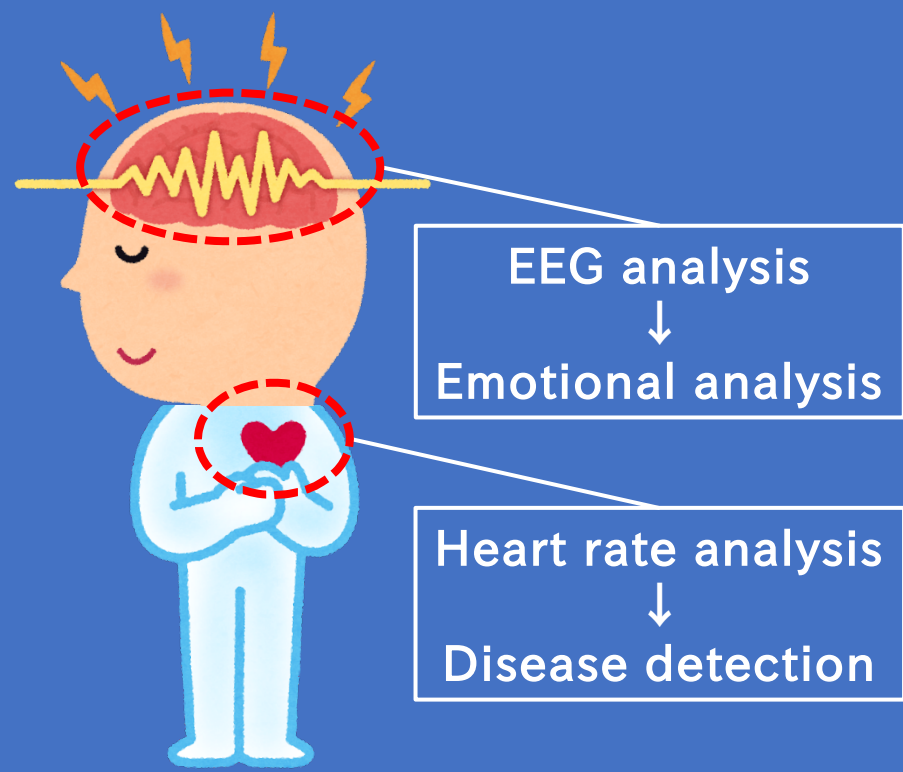
P2 What is time series classification ?

➡ Assigning labels to each observed time series

Objective

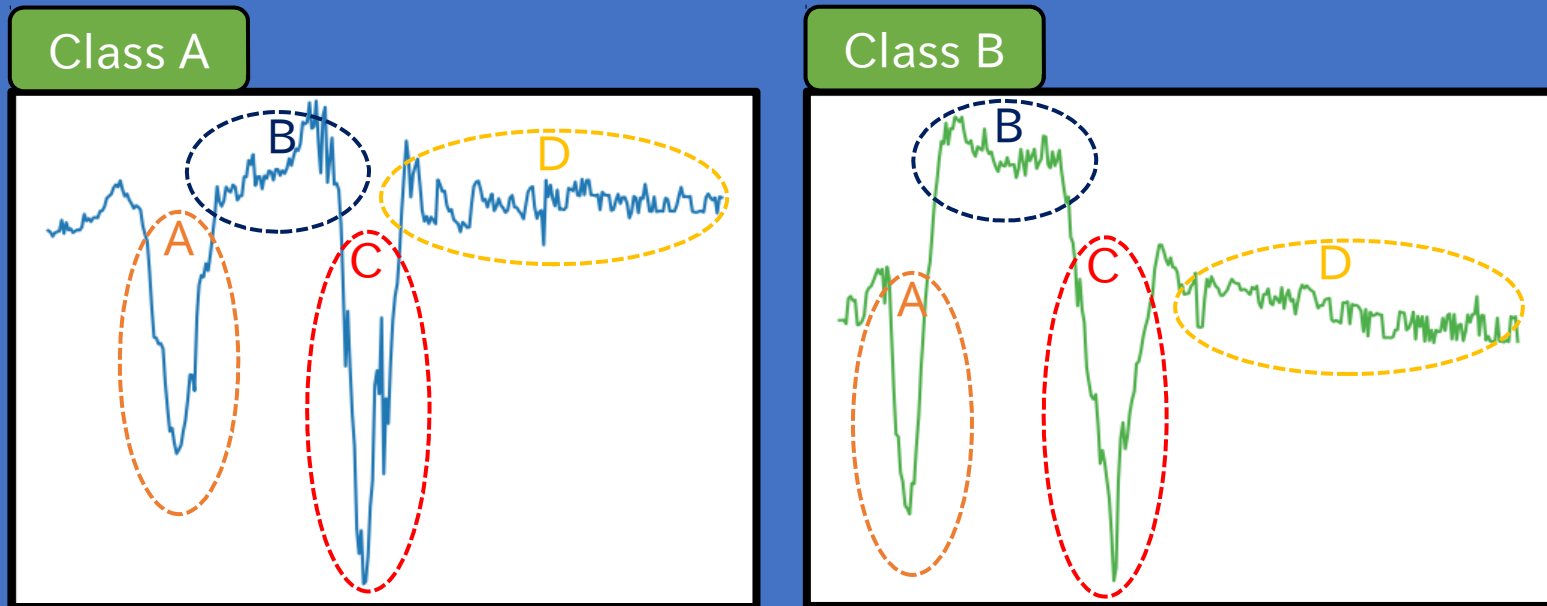


Application



P3

Where is the best feature to classify ?



Did you notice these places, right ?

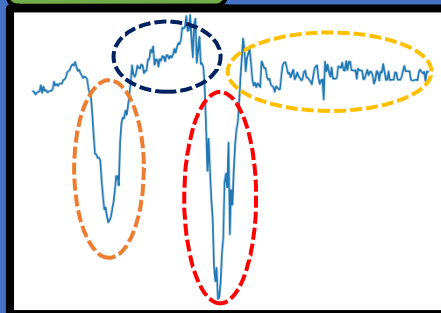
P4

The answer is ..!

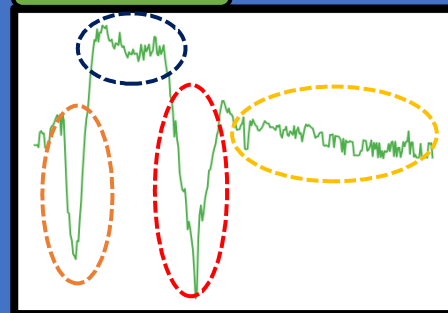
I don't know..



Class A



Class B



◆ Why?

- ✓ There are **multiple** patterns and pattern that is difficult to notice easily.
- It is hard to judge where to place weights.

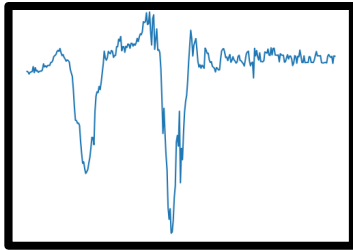


Many studies have been conducted to classify the labels

P5

How to classify ?

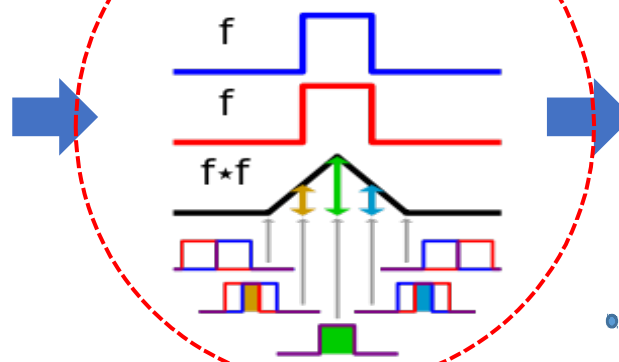
Hand crafted



Input data

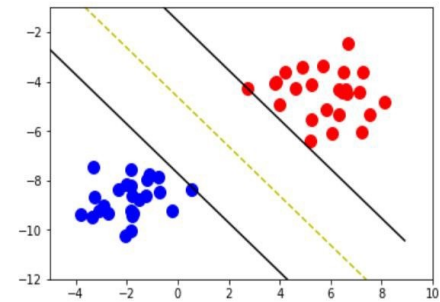
Feature extraction

Autocorrelation



Classifier

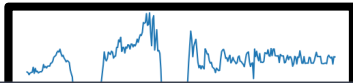
SVM



www.ibric.org/scicare/read.php?Board=seicafe000692&id=15891

<https://medium.com/deep-math-machine-learning-ai/chapter-3>

Deep learning



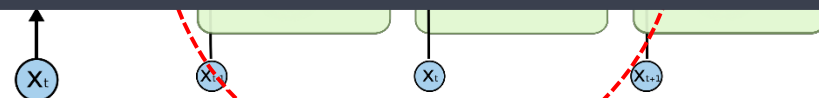
Input data

Neural Networks model

RNN

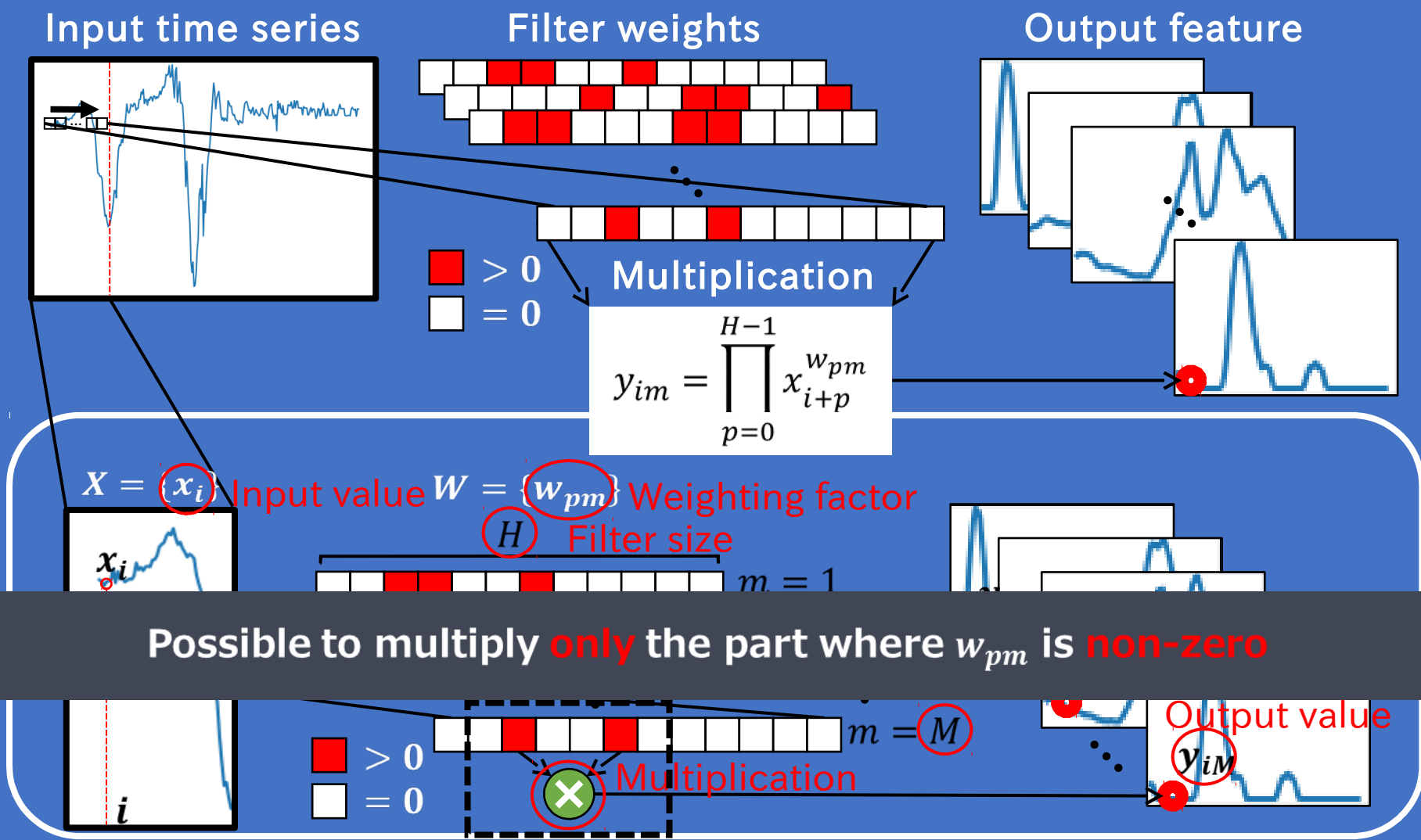
LSTM

There is no layer for autocorrelation in NN model

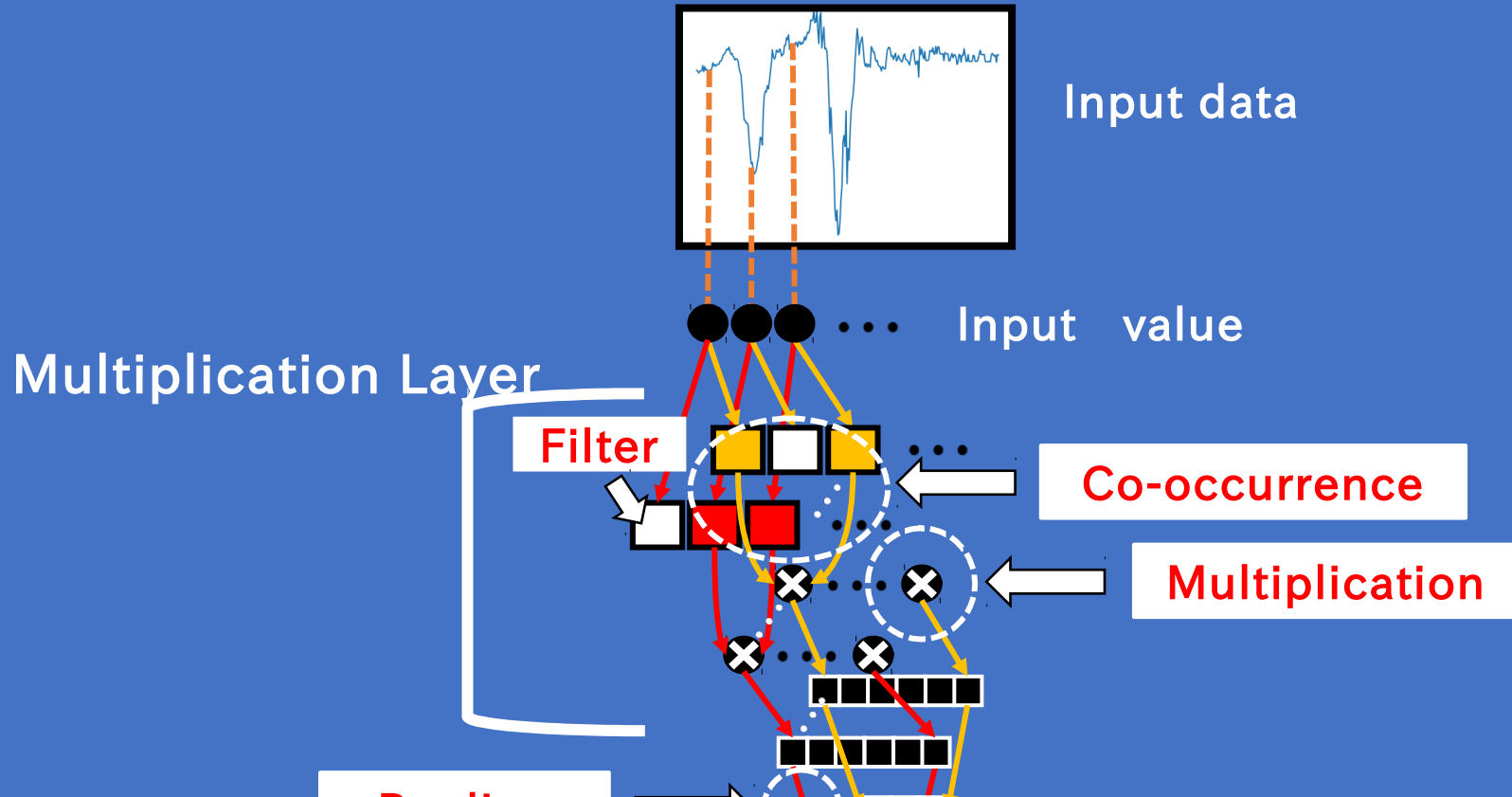


<https://qfita.com/KojiOhki/items/89cd7b69a8a6239d67ca>

P6 Let me propose multiplication layer !



P7 How to use ?



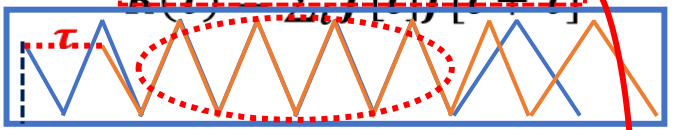
Possible to **discriminatively** extract **high-order autocorrelation** features

model
NN

P8 What it means ?

Autocorrelation

$$R(\tau) = \sum_t f[t]f[t+\tau]$$

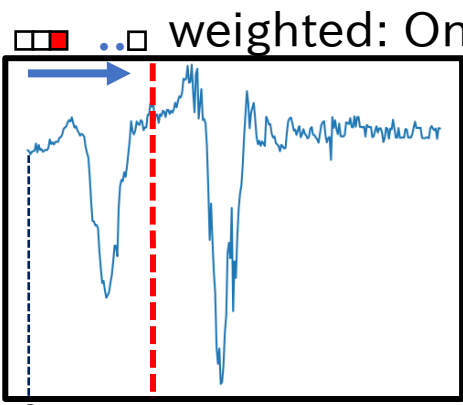
Ex) 

co-occurrence
takes place
when pattern is same

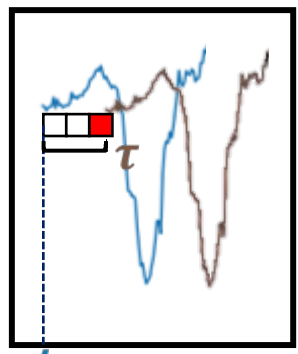
High-order autocorrelation
Lth-order autocorrelation

$$R(\tau_1, \tau_2, \dots, \tau_L)$$
$$= \sum_D f[t]f[t+\tau_1]f[t+\tau_2]\dots f[t+\tau_L]$$
$$D = \{t | t + \tau_l \in D, \forall l \in \{1, 2, \dots, L\}\}$$

Key point : we can extract autocorrelation features in any situation.



weighted: Only 3th



τ



weighted: 1,2,3th



τ_1
 τ_2
 τ_3

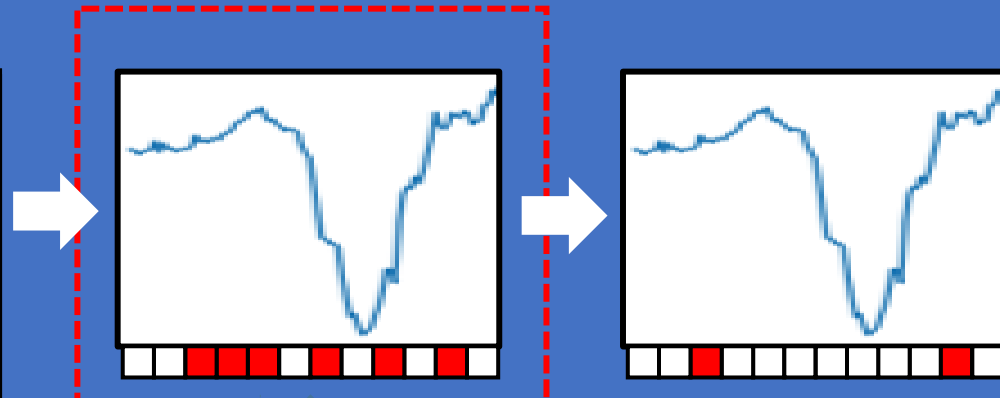
What it means ?

Constraint 1

- ✓ Let w be zero if possible

Constraint 2

✓ If all w are added, it becomes



Key point : The features can be extracted discriminatively.

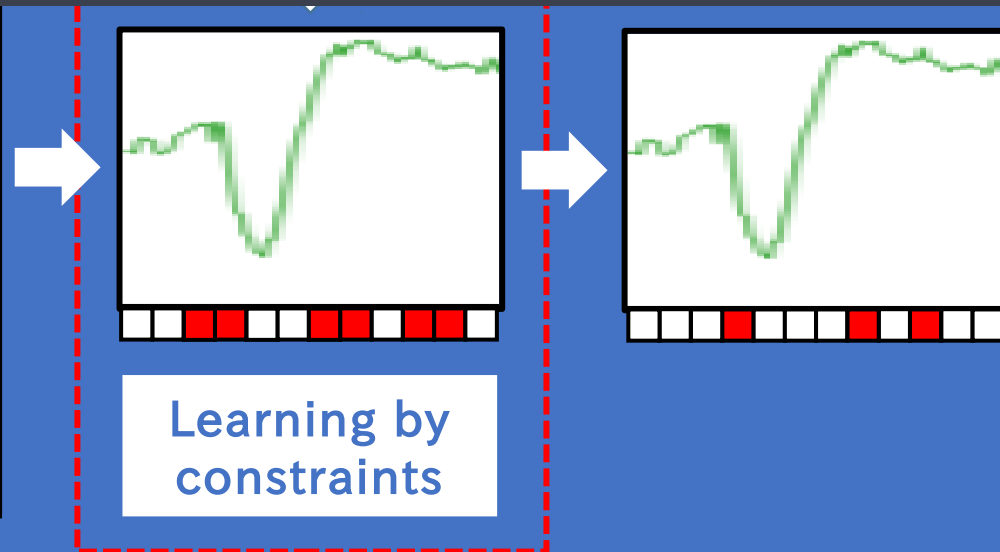
Constraint 3

- ✓ Let w have values between zero and one

+

Comparison

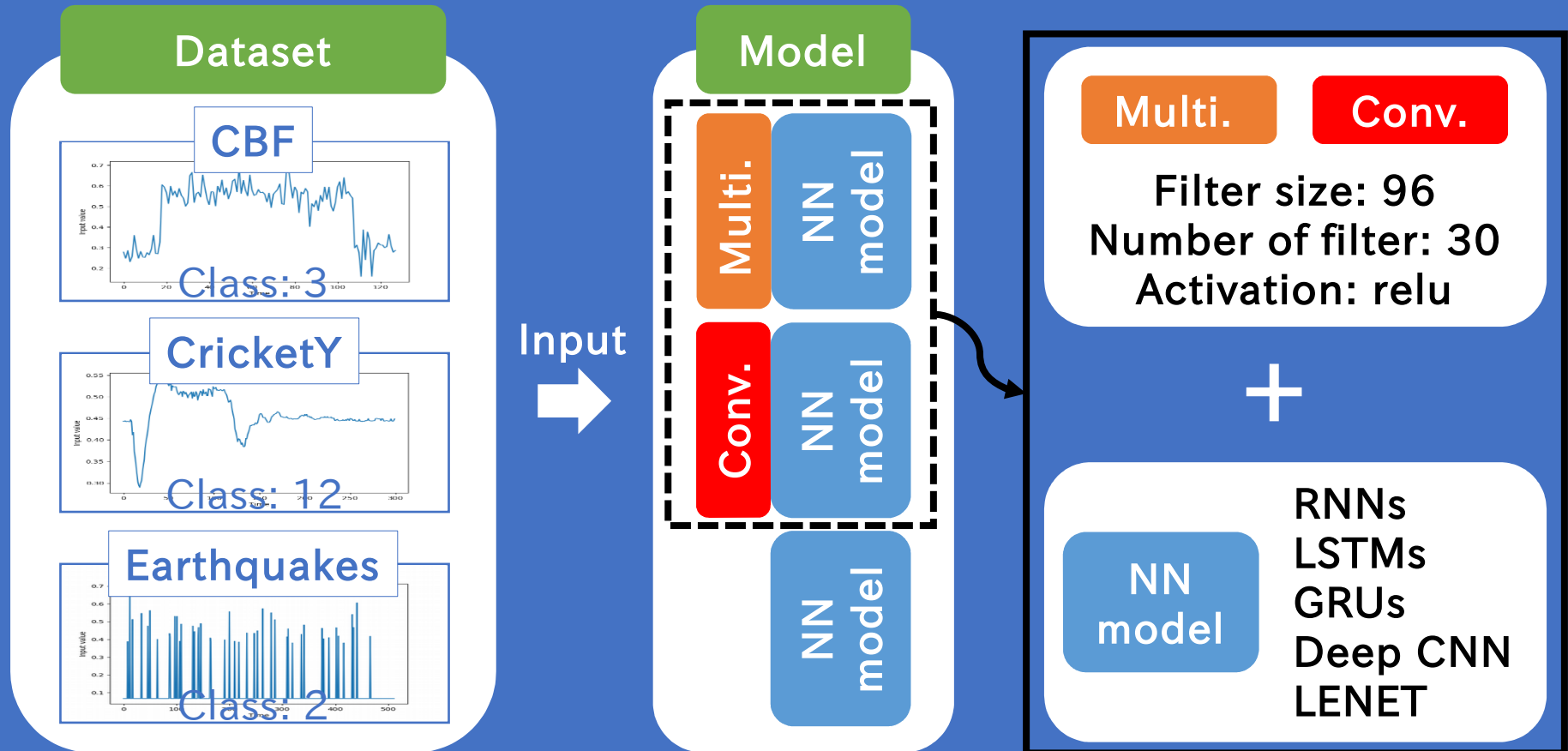
- ✓ Compare with each other class extracted features



P10

Let's check how effective the proposed layer is !

- ✓ Combining the Multi. with the **head** of NN model
- ✓ Comparing when Multi. is **absent** and **Conv.** is combined instead of Multi.



P11

Comparison of classification accuracies

Model	CBF	CricketY	Earthquakes
RNNs	0.331	0.07	0.748
LSTMs	0.939	0.144	0.784
GRUs	0.522	0.151	0.763
RNNs + Conv.	0.997	0.164	0.712
LSTMs + Conv.	0.982	0.09	0.683
GRUs + Conv.	0.983	0.09	0.698
LENET + Multi.	0.976	0.506	0.748
Deep CNN + Multi.	Big difference		0.748
RNNs + Multi.			0.748
LSTMs + Multi.			0.748
GRUs + Multi. (1)	0.971	0.636	0.741
GRUs + Multi. (2)	0.932	0.07	0.799

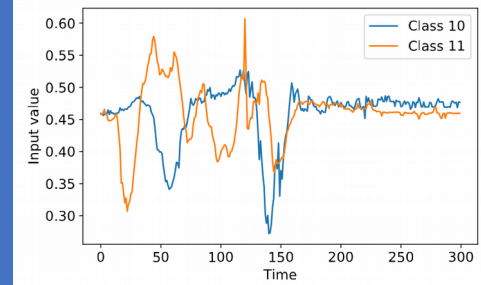
Differences in parameters

Discussion (CricketY)

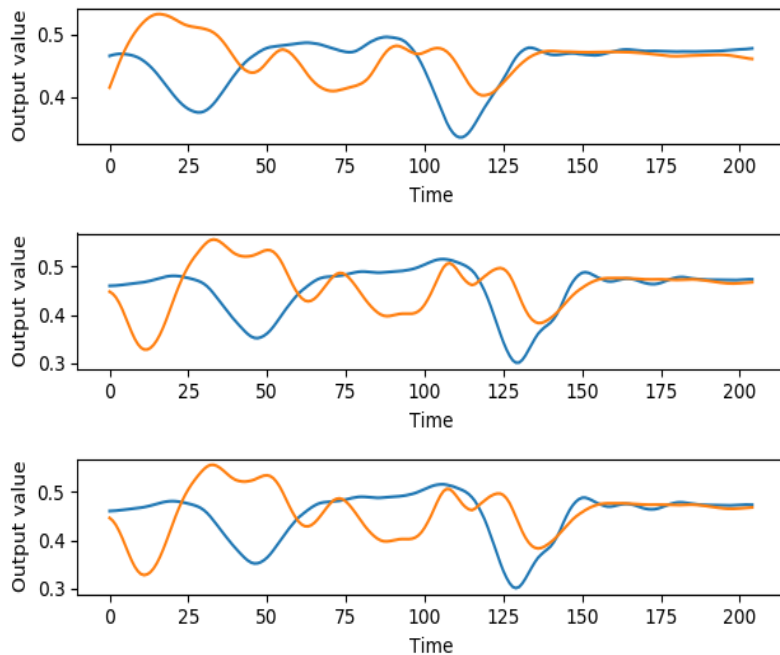
Comparing extracted features of Multi. with those of Conv.

P12

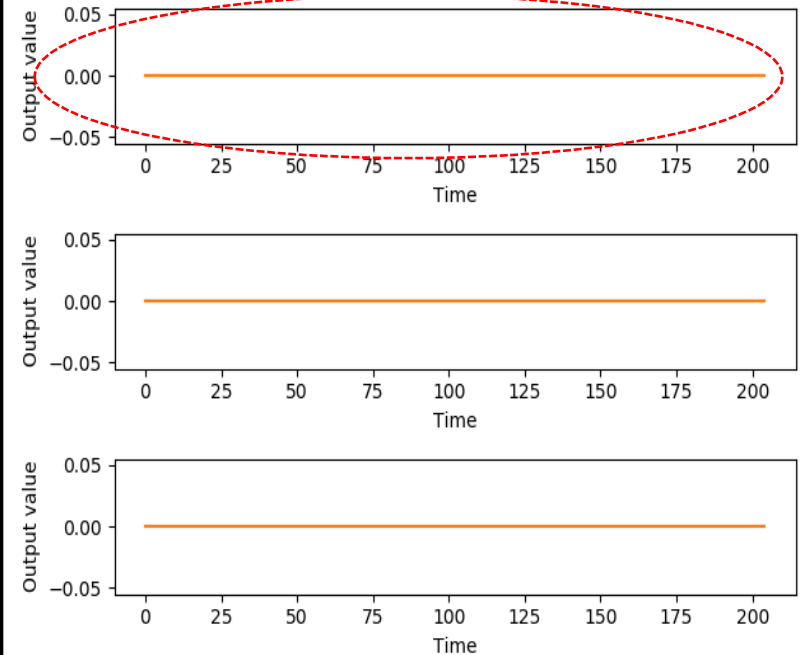
Visualization of extracted features



Multiplication layer



Convolutional layer



**Big
difference**

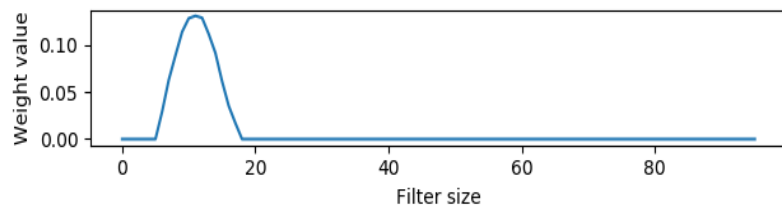
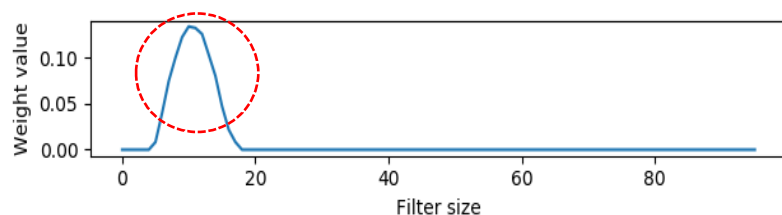
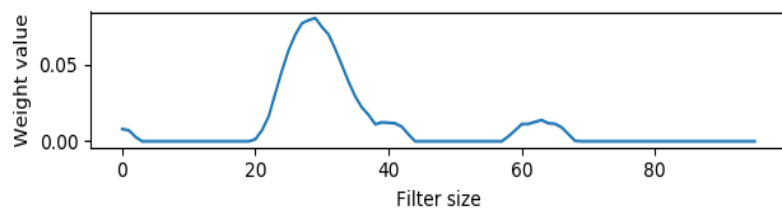
Class 10

Class 11

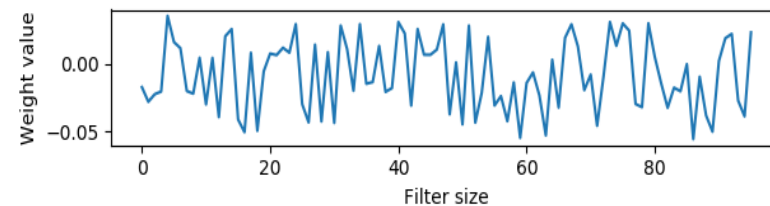
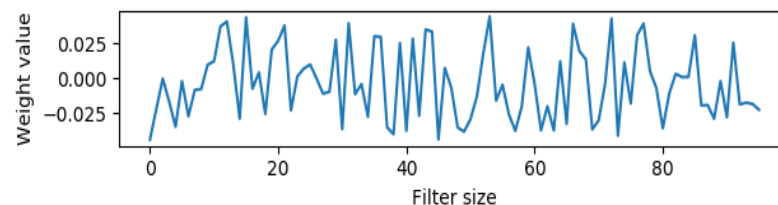
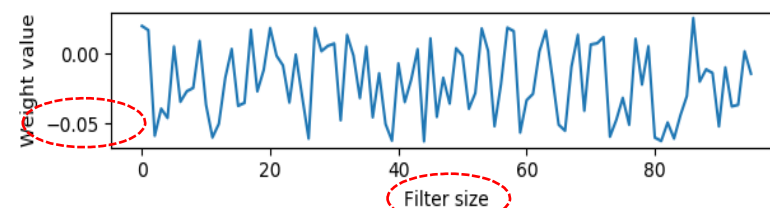
P13

Visualization of filter weights

Multiplication layer

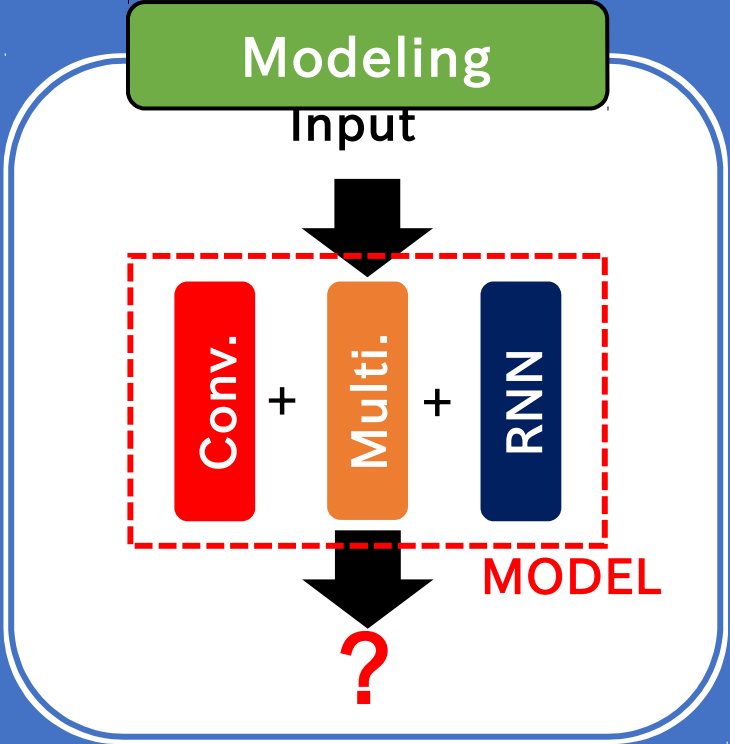
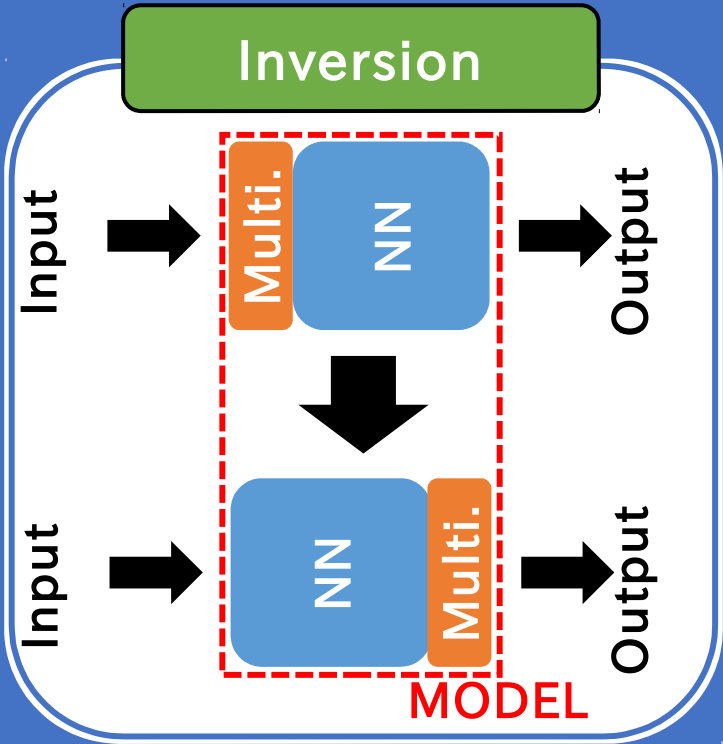


Convolutional layer



**Big
difference**

P14 I'll do this !



Thank you for your attention !



Any question~?