


Number Representation

Big Idea: Bits can represent anything

N bits $\rightarrow 2^N$ representations

Number Bases: Decimal, Octal, Hexadecimal, etc...

Converting other bases from base 10: "leftover algorithm"

ex) $73_3 \rightarrow$ base 4?

$$1) 4^5 = 1024 \rightarrow \text{fits } 0 \rightarrow \text{leftover } 73$$

$$2) 4^4 = 256 \rightarrow \text{fits } 0 \rightarrow \text{leftover } 73$$

$$3) 4^3 = 64 \rightarrow \text{fits } 1 \rightarrow \text{leftover } 9$$

$$4) 4^2 = 16 \rightarrow \text{fits } 0 \rightarrow \text{leftover } 9$$

$$\dots \rightarrow 0 \times 4^5 + 0 \times 4^4 + 1 \times 4^3 + 0 \times 4^2 + 2 \times 4^1 + 1 \times 4^0$$

$$\rightarrow 73_{10} = 001021_4$$

Common bases: Decimal, Binary, Hexadecimal

Notation: No prefix, $0b\dots$, $0x\dots$

Binary \leftrightarrow Hexadecimal Conversion: Use the table!

Why it works: each 4 binary digits corresponds to 1 hex digit.

Units: Byte (8 bits, 2 hex), Nibble (4 bits, 1 hex)

Integer Representation: Signed & Unsigned

Unsigned: N bits $\rightarrow [0, 2^N - 1]$

↳ Overflow/Negative Overflow (not enough digits!)

Signed: Sign-Magnitude \rightarrow leftmost bit is the sign.

↳ $[-2^{N-1} + 1, 2^{N-1} - 1]$, counting in bits is weird.

Signed: One's Complement \rightarrow negative, then flip the bits.

↳ always increasing, but overflow on the edges.

Signed: Two's Complement \rightarrow shift all negatives to left 1.

↳ fixes double representation of zero

↳ Another definition: MSB is now negative

Signed: Bias Notation \rightarrow shift everything to prevent overflow

↳ "standard bias" centers at zero, math is hard.

Pointers, Arrays, & Strings

* In C, false is only \emptyset or null pointers (all else is true)

"Memory is just a huge array" \rightarrow each value has address

Pointer: the value is an address of another variable

\hookrightarrow if p holds x's address, "p is a pointer to x"

ex) int *p; int x = 3;

$p = \&x;$ $\leftarrow (\&)$ is the "address of" operator

print(*p); $\leftarrow (*)$ is the dereference (prints 3)

$*p = 5;$ \leftarrow able to write on the address

C passes by values, but pointers can give references!

ex) void addOne(int *p) {

$*p = *p + 1;$ \leftarrow changes the content that

}

p points to, not p

The NULL pointer: pointer to all \emptyset s, no r/w

\hookrightarrow guard pointers with if(!p){...}

Pointer to Structs: $(\ast \text{ptr}).x \Leftrightarrow \text{ptr} \rightarrow x$

Arrays: `int arr[2];` $\text{arr}[\text{num}]$ is actually pointer
 $\text{arr}[i] \Leftrightarrow *(\text{arr} + i)$!! (i automatically scales with type)
↳ $\text{pointer} + n == \text{pointer} + n \times (\text{sizeOf}(*\text{pointer}))$

A pointer to a pointer is a "handle" (`int **h`)
↳ this allows manipulation of pointer values out of scope!

Arrays lose its size information when passed

Strings: array of chars that ends with '\0'

Memory Management

"word size": # of bytes in an address

Endianness: little endian = LSB is stored first

big endian = MSB is stored first

"word alignment": 4-byte boundaries for multiple-byte data

↳ uses padding for structs/small types to enforce alignment

`sizeof()`: gives size in bytes (of type or variable)

C Program Address Space: 4 regions

- 1) Stack: local variable, grows down
- 2) Heap: requested via malloc(), grows up
- 3) (Static) Data: variables declared outside main
- 4) Text (code): program executable loaded, does not change

Global vars → Data, Local vars → Stack, auto freed

Stack: a new frame is allocated every time a function is called

↳ frame stores: return address, arguments, local variable space

The stack pointer tracks the last frame relevant

→ locally declared variable are lost when function closes

↳ Don't return a pointer to something on the stack??

Heap: "Dynamic" memory that can be allocated, resized, and freed

↳ Huge pool of memory, but not allocated contiguously

malloc(): allocates raw memory, uninitialized from heap

free(): frees memory from heap

realloc(): resizes previously allocated heap block to new size

- void * malloc(size_t n) → unsigned int for byte counting
 ↳ returns a general pointer ↳ might return NULL if out of memory
 ! Always check for NULL malloc returns !

To allocate a struct:

SomeStruct * sp = (SomeStruct *) malloc(sizeof(SS));

To allocate an array of 20 ints:

int *ptr = (int *) malloc(sizeof(int) * 20);

↳ this depends on the architecture!

- free(void *ptr) → the exact pointer returned by (re)alloc()
 ↳ always should be manually called for each allocation
- realloc(void *ptr, size_t size) → new size wanted
 ↳ returns a new address of the memory block
 (the data might have been copied to a new memory space!)

Memory leak: failure to free() allocated memory

Use after free: referencing a pointer after free()

Double-free: trying to free() a memory already freed
 (realloc() can produce dangling references if multiple pointers point to the same memory)

Function Pointers

`int (*fn)(void*, void*) = &foo;`

↳ `(*fn)(x, y)` calls the function

Generics

General-purpose code that updates blocks regardless of types

ex) `malloc` returns a `void` pointer to be casted

Invalid to dereference a `void` pointer!

Generic memory copying: `memcpy()`, `memmove()`

↳ copy does not check overlap, move always makes a temp array.

a `char` is always 1 byte → use to store a general length array

ex) `swap_ends (void* arr, size_t nelems, size_t nbytes) {`
 `swap (arr, (char*)arr + (nelems - 1) * nbytes, nbytes)`
}

↳ pointer arithmetic
in 1 increments!

Floating Points

Binary Point: boundary between integer and fractional part

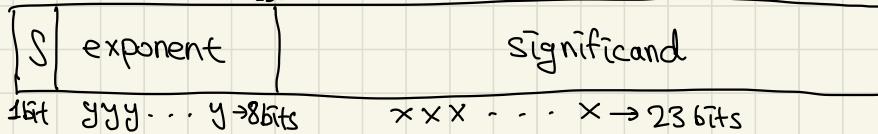
$\begin{array}{c} X \quad X \\ \downarrow \quad \downarrow \\ 2^1 \quad 2^0 \end{array} \cdot \begin{array}{c} Y \quad Y \\ \downarrow \quad \downarrow \\ 2^{-1} \quad 2^{-2} \end{array}$ a "fixed binary point" has a predetermined # of integer and fractional bit.

Floating Point: some of the bits carry the binary point location!

Scientific Notation: no leading zeroes \rightarrow change to base 2

Ex) $1.01 \times 2^{\text{exponent}}$ \rightarrow when normalized, first digit is 1!

\hookrightarrow Normalized format: $1.\underset{31 \text{ bit}}{XXX\dots} \times 2^{\underset{23 \text{ bits}}{yyy}}$ $\xrightarrow{\text{IEEE 754}}$



\hookrightarrow Over/Underflow if the exponent is too big/small

How to store the exponent \rightarrow bias notation! (exp -127)

$\Rightarrow (-1)^S \times (1 + \text{Significand}) \times 2^{(\text{Exponent} - 127)}$

Special Numbers: $\pm \infty \rightarrow$ most positive exponent reserved for ∞

0 \rightarrow all zeroes in exponent & significand

Max exponent, nonzero significand \rightarrow NaN representation

exponent 0, nonzero significand \rightarrow De Normed numbers

RISC-V

Assembly: set of instructions, operators & operands

Instruction Set Architecture (ISA) ex) RISC-V, x86, ...

Reduced Instruction Set Computer (RISC): small, simple, fast

One line of assembly code \Rightarrow One instruction

No type, bits in registers get interpreted by operators

Registers are inside the processor, interaction is very fast

RISC-V has 32 registers that are 32 bits wide

\hookrightarrow 32 bits is 1 word, 32 = word size (4 bytes)

x0 is special and is always 0. (editing is impossible)

RISC Syntax: opname rd, rs1, rs2

ex) add x1 x2 x3 \Leftrightarrow $a = b + c$ (in C)

Using temporary registers is possible, but might want to minimize

Immediates: numerical constants! ex) addi x3 x4 0

\hookrightarrow the last operand must be a number instead of a register

RISC-V Data Transfer

How do we load from and store to memory?

↳ interacting w/ memory is slow... (later on improvement)

lw (Load word "from") rd, [byte offset] (rs)
← data flow → pointer to array

sw (Store word "to") rd, [byte offset] (rs)

* rs + (byte offset) must be a multiple of 4 for integers!

lb, sb : load and store byte into the low byte position,
and extends the leftmost bit to the rest of the word
→ LSB

↳ endianness matters in this case! (lbu for unsigned, no extend)

lbu extends all zeroes for "unsigned byte"

RISC-V Procedures

When calling a function...

- ① Put arguments
- ② Transfer control to function
- ③ Acquire storage
- ④ Do the function
- ⑤ Store the return value
- ⑥ Transfer control to callee

Calling Conventions: what registers do what job

a0-a7: argument registers (a0-a1 are return registers as well)

ra: return address to return to point of origin

s0-s1,s2-s11: saved registers

Instruction Support for Functions:

Every line of code also lives in memory like data.

When a function is called, the next line's address is stored to ra.

PC jumps to the address stored in the j call.
↑^{jump}

After the function terminates, it returns via jr ra.
↑^{jump to register}

* jal (jump and link) removes hardcoded line numbers!

↳ jal rd, FunctionLabel saves next line's address to rd and jumps to
the address associated with the FunctionLabel

↳ jr ra is also aliased as "ret"

(jalr rd,rs,imm can manually set PC to imm(rs))

When a function is called, old register values are stored and
then restored just before returning \Rightarrow use stack !!

push the sp for space, pop the sp to free stack space

Nested Calls?? → clobbers values in $a0-a7$ & ra
↳ the nested function will overwrite the old return address!
→ save ra to the stack, too

Register Convention: rules for what registers may be altered

- 1) Preserved across function calls: sp, gp, tp, S0-S11
- 2) Not preserved: $a0-a7$, ra, $t0-t6$ ↳ the callee is responsible for preserving these

RISC-V Instruction Format

PC (Program Counter) is a pointer for instruction count

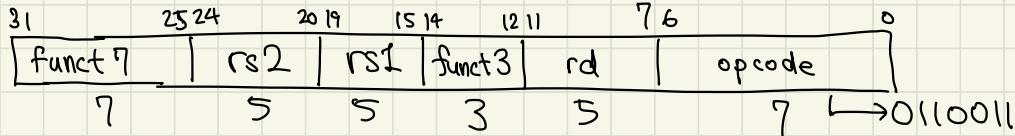
Assembly code \Rightarrow Machine Code (binary)

Most data are in words (32-bit), RISC-V uses 32-bit.

Fields in an instruction tells something meaningful

6 Key Instruction Formats: R, I, S, B, U, J

R-Format: opname rd, rs1, rs2 (add, sll, ...)



Opcode "partially" specifies the instruction, and funct3&7 describes specifics of which version of the instruction to run

ex) add $\times 4$ $\times 3$ $\times 2$

f1	r2	r1	f3	rd	op
00000000	00010	00011	000	00100	0110011

(0 0 2 1 8 2 3 3)₁₆

I-Format: opname rd, rs1, imm (addi, slli, ...)

31	20 19	15 14	12 11	7 6	0
imm[11:0]	rs1	funct3	rd	opcode	

12 5 3 5 7 \hookrightarrow 0010011

$[-2^{10}, 2^{10}]$, CPU sign extends before operating
shift operations use only 5 bits for shamt (shift amount)

↳ the leftover bits tells logical / arithmetic

I-Format (Load): loadop rd, imm(rs1)

31	offset	20 19	15 14	12 11	7 6	0
imm[11:0]	rs1	funct3	rd	opcode		

12 5 3 5 7 \hookrightarrow 0000011

funct3 specifies how much to load in what format (lw, lb, ...)

S-Format: storeop rs2, imm(rs1) \rightarrow no change in register!

31	25 24	20 19	15 14	12 11	7 6	0
imm[11:5]	rs2	rs1	funct3	imm[4:0]	opcode	

7 5 5 3 5 7 \hookrightarrow 0100011

the immediate is split into two parts (RISC-V prioritizes keeping register fields in place more than immediates)

Program Counter (PC): pointer to place in code

↪ +4 after most lines, updated to a label for jumps

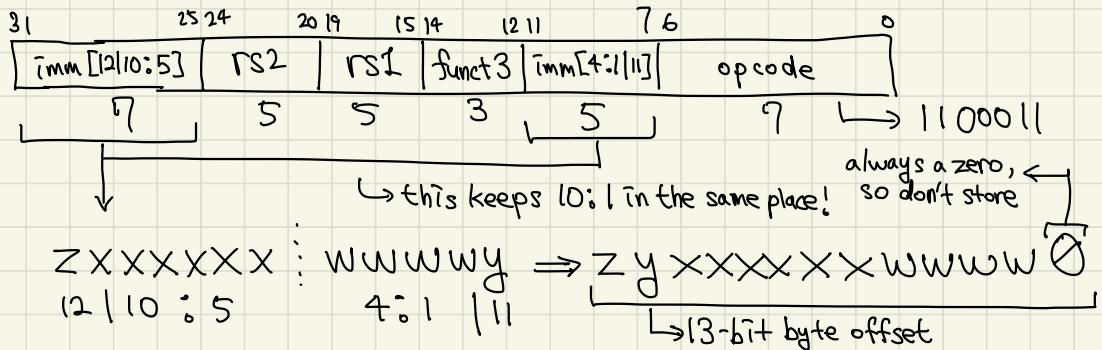
PC-Relative Addressing: $PC = PC + (\text{byte offset})$

↪ this enables Position Independent Code (no hard coding)

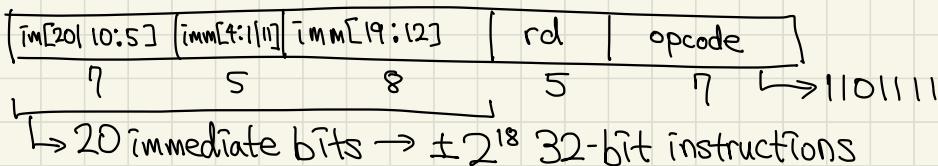
B-Format: branch op rs1, rs2, Label

↪ Label only gets 12 bits → In units of 2 bytes (half-words)

→ PC relative offsets support [-4096, 4095]



J-Format: jal rd, Label



U-Format: opname rd, immed

↪ "upper immediate"

$\text{imm}[31:12]$		rd		opcode
---------------------	--	----	--	--------

$$\hookrightarrow \text{imm} = \text{imm} \ll 12$$

lui rd, immed : load immed to upper 20 bits, clear rest

\hookrightarrow then use addi to load the lower 12 bits!

(li pseudo instruction handles $\text{lui} + \text{addi}$ implicitly)

Edge Case: addi sign extends and decrements next bit

\hookrightarrow if 12-bit immediate is negative, add 1 to upper immediate!

$\text{auipc rd, imm} \rightarrow \text{rd} = \text{PC} + (\text{immed} \ll 12)$

($\text{auipc rd, } 0$ stores the current address to rd!)

$\text{jalr rd, rs1, imm} \rightarrow \text{PC} = \text{rs1} + \text{imm}, \text{rd} = \text{PC} + 4$

\hookrightarrow this is just an I-Format instruction (imm not $\times 2$)

$\Rightarrow \text{lui} + \text{jalr}$ can access all 32-bit address

CALL

How to translate high-level code to machine code?

Compiler: High Level Language \rightarrow Assembly Code

\hookrightarrow output may include pseudo instructions ($\text{mv}, \text{li}, \text{ji}, \dots$)

Assembler: Assembly Code → Machine Language Module
↳ object code & information for linking & debugging
replaces pseudo instructions with real instructions!

Directives inform how to build object files!
↳ .text, .data, .globl, .string, .word

Object File Format:

- 1) Header: size & position of other parts of the file
- 2) Text Segment: machine code
- 3) Data Segment: static data in machine code
- 4) Symbol Table: store undetermined absolute addresses
- 5) Relocation Information: store labels for other files to reference for the linker to resolve (To-do list)
- 6) Debugging Information

Linker: Object files → executable machine code
↳ enables separate compilation of files!
Patches text and data segments, then resolve references
↳ through relocation table

PC-relative addressing don't need relocation!!

External function reference & static data needs relocation

Static vs Dynamic Linking: self-contained vs only references

DLLs saves space but sacrifices runtime overhead

Upgrading libraries is much more reasonable in DLL

Loader: executable code → running program

Synchronous Digital Systems

Synchronous: All operations coordinated by a central clock

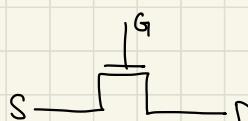
Digital: All values are discretized to 0s or 1s.

Switches: open when 0, closed when 1 (asserted)

AND gate: $Z \equiv A \text{ and } B$ (Z is on only when $A=1$ and $B=1$)

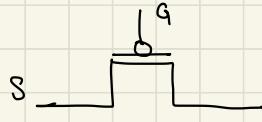
OR gate: $Z \equiv A \text{ or } B$ (Z is on when $A=1$ or $B=1$)

Transistor: MOS transistors act as voltage-controlled switches

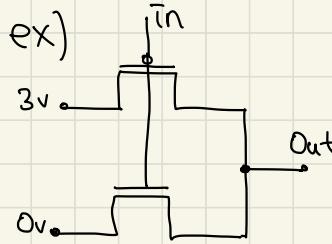


n-channel: open when G is low, closed when G is high

$S \rightarrow D$ flows when G is high enough

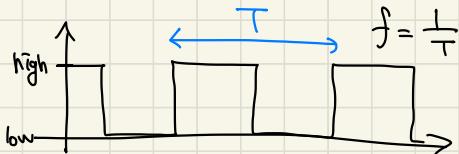


P-channel: closed when G is low, closed when G is high
 S \rightarrow D flows when G is low enough



Relationship between in and out?

in	out
0V	3V
3V	0V



Signals & Waveforms (clock)

↪ Assume transmission is effectively instant

↪ Implies that a wire has only one value at a time

Circuit Delay: Transistors take time to calculate outputs!

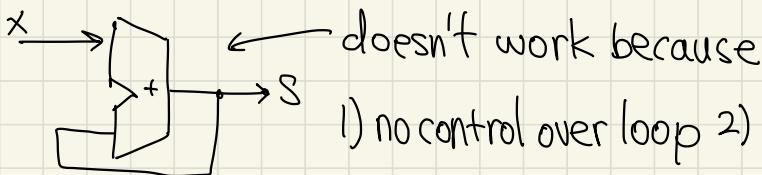
↪ only look at the value after the propagation delay

Types of Circuits: ① Combinational Logic Circuit ② State Elements

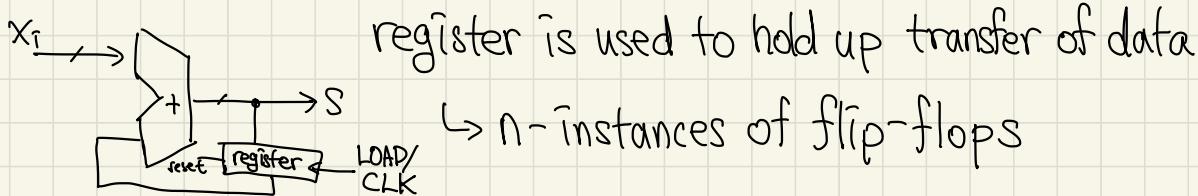
↪ state elements can store information for future calculations!

States

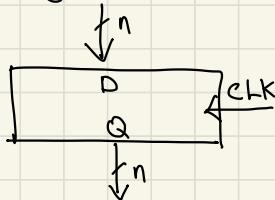
Accumulator: $x_i \rightarrow \boxed{\text{sum}} \rightarrow S$



- doesn't work because
- 1) no control over loop 2) no initialization



Register:



a rising edge-triggered flip-flop samples the input d and outputs to q on a rising edge

* there is a "clk-to-q delay" and a "hold time"

If input X is not synced with clk, the register may capture a wrong value temporarily, but it is fixed eventually.

$\Rightarrow \text{Max delay} = \text{CLK to Q delay} + \text{Logic delay} + \text{Setup time}$

Finite State Machine: states and transition function

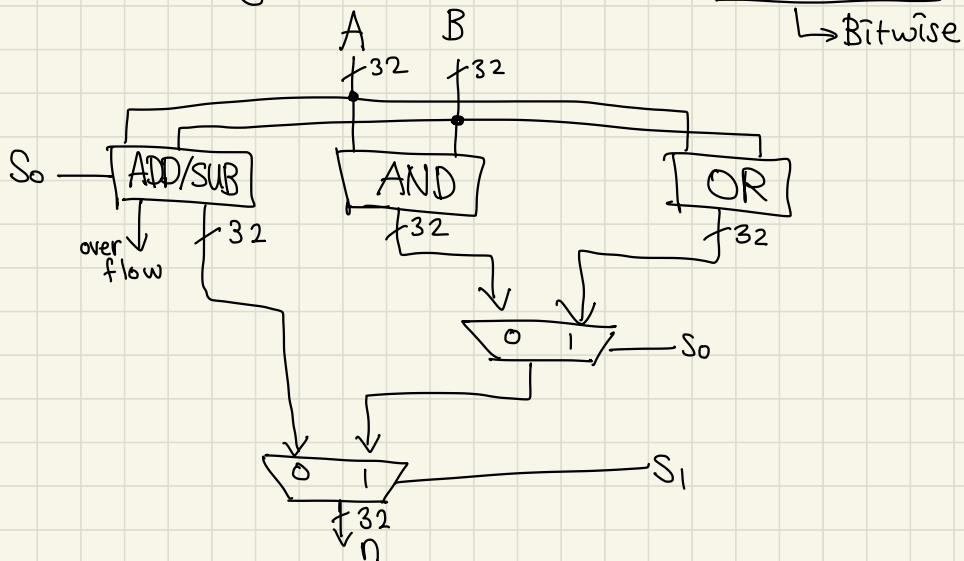
↳ each transition has an input and an output

* FSM can be mapped to hardware with a CL and register!

Combinatorial Logic Block

Multiplexor: signal chooses which input gets outputted

Arithmetic Logic Unit: ADD, SUB, AND, OR



Adder/Subtractor Design: Truth Table or Cascade Layer?

↪ Truth table needs 2^{65} rows...

a ₀	b ₀	S ₀	C ₁
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

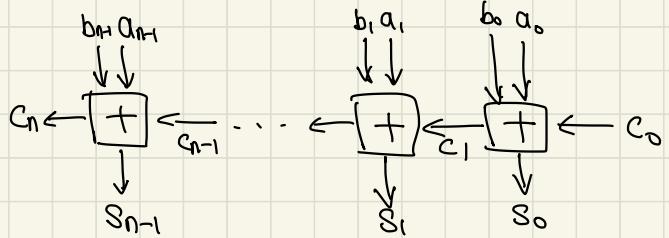
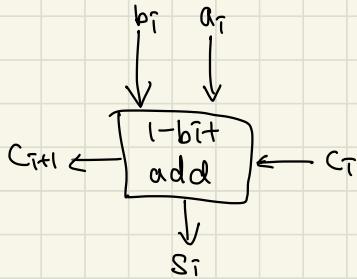
For LSB (without carry input)

$$S_0 = a_0 \text{ XOR } b_0, C_1 = a_0 \text{ AND } b_0$$

Every other row will have a carry bit as an input

$$\hookrightarrow S_i = \text{XOR}(a_i, b_i, c_i), C_{i+1} = \text{MAJ}(a_i, b_i, c_i) = a_i b_i + a_i c_i + b_i c_i$$

The 1-bit Adder \longrightarrow N-bit Adder



\rightarrow Is $C_n=1$ necessarily an overflow? Yes, for unsigned.

\hookrightarrow what about signed numbers? Only when $C_n \text{ XOR } C_{n-1}$??

Subtractor: Realize that $A - B = A + (-B)$

\hookrightarrow All bits in B are XORed with 1, then $C_0 = 1 \Rightarrow (-B)$

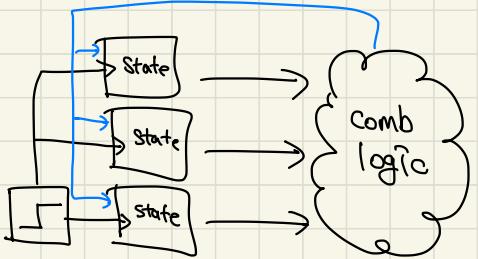
\Rightarrow The SUB signal is connected to XORs to B and C_0 !!

RISC-V Datapath

Processor $\xrightarrow{\text{Datapath: the logic of the hardware}}$ Control: the choicemaking decisions

One-Instruction-Per-Cycle RISC-V Machine

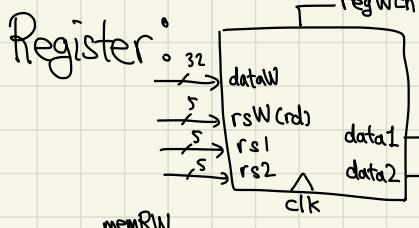
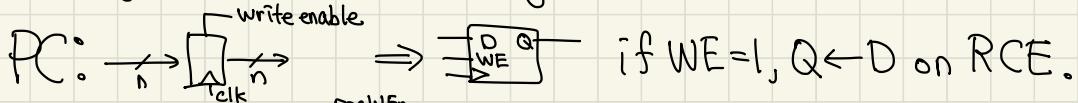
\hookrightarrow composed of combinational logic blocks & state elements



current output of state elements are input to CL, and its outputs affect the state elements on the next clock cycle

States required by RISC-V ISA: PC, Reg[], IMEM, DMEM

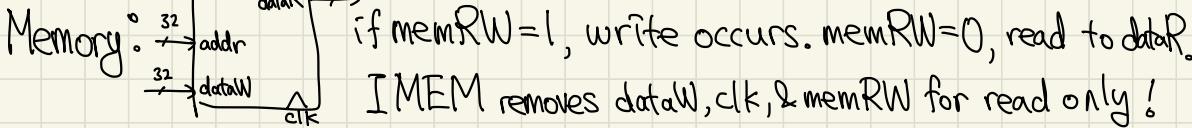
* Every RISC-V instruction changes some state element!



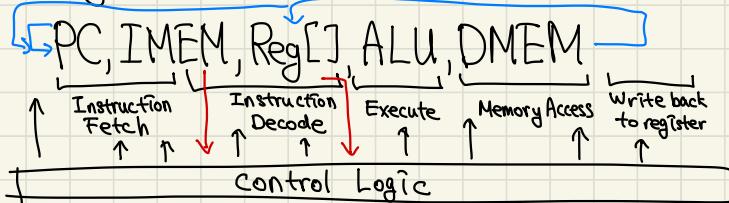
Registers are accessed via their 5-bit

register numbers: R[rs1], R[rs2], R[rd]

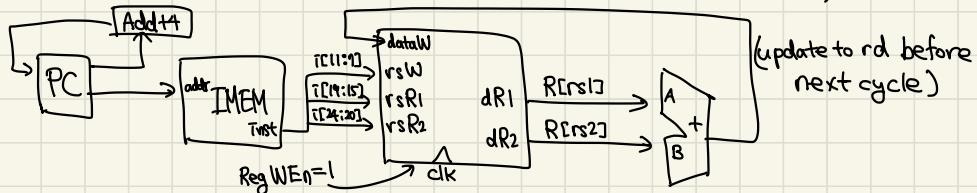
write operations put dataW into R[rd]!



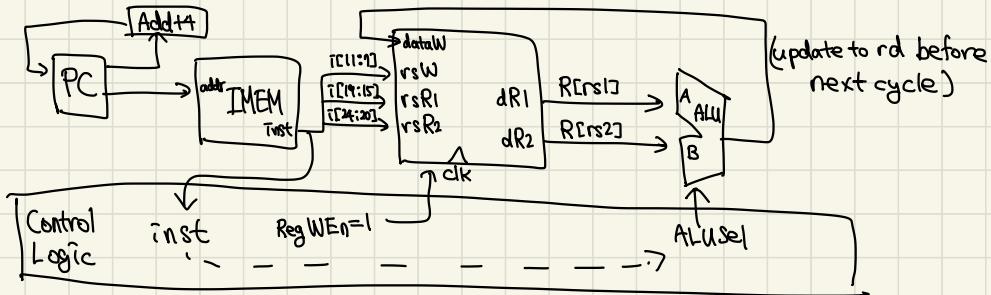
5 Stages of Instruction Execution:



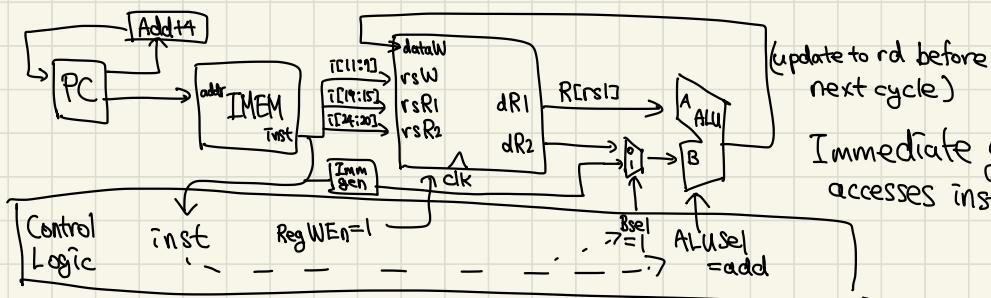
Implementing add: $R[rd] = R[rs1] + R[rs2]$, $PC += 4$



Implement sub: only differ in one bit in func[7], inst[30]!

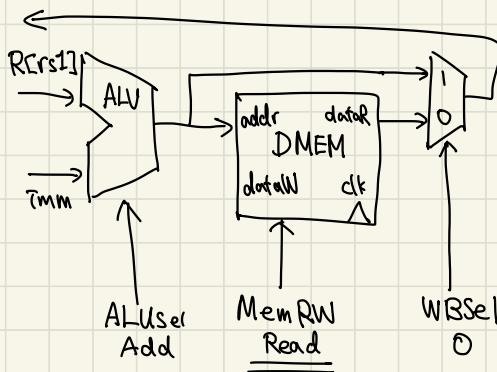


Implement addi: how to take the immediate?

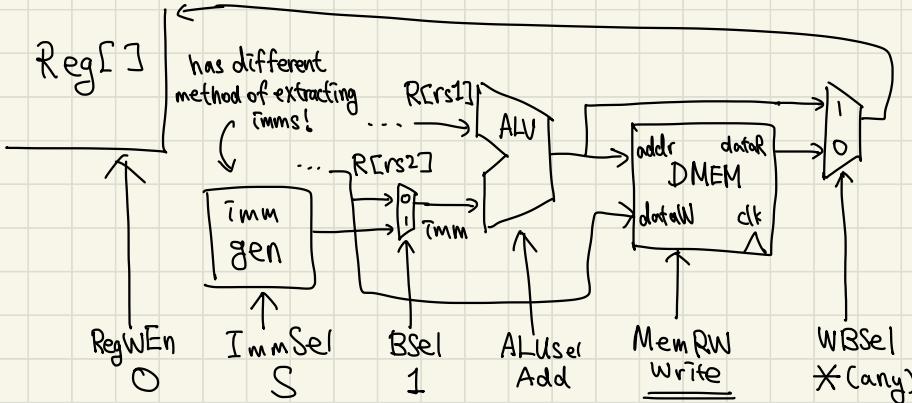


Imm Gen: copy to 12 bits, then smear the most upper bit

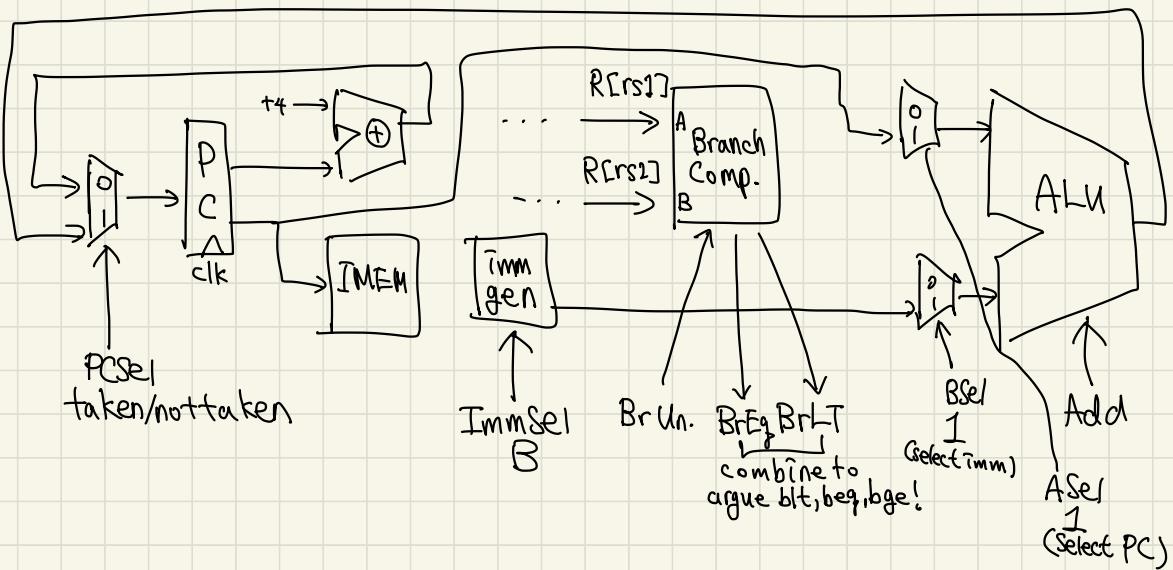
Implement Load: actually similar to addi! with DMEM access now



Implement Store : Saves to $R[rs2]$ in memory!



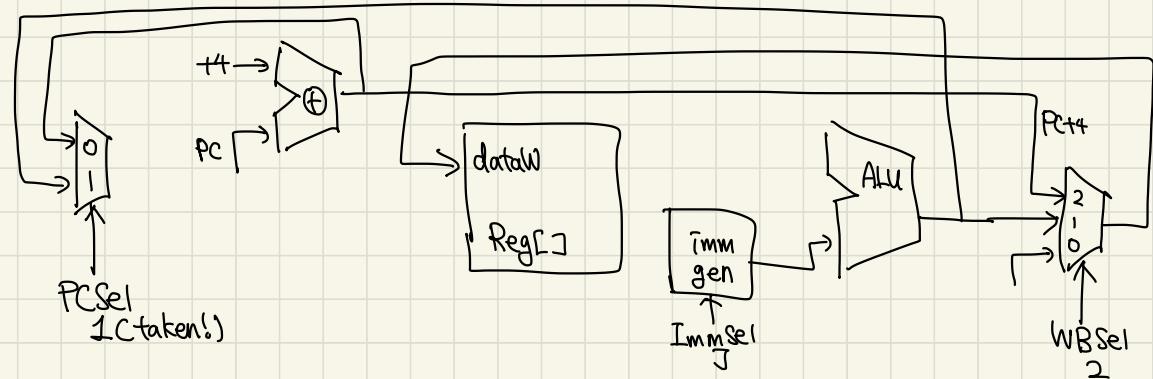
Implement Branches : new imm. format, pc conditionally changes!



Imm. Gen. for B-Types : MUX for $\text{imm}[1]$ $\begin{cases} S: \text{instr}[31] \\ B: \text{instr}[7] \end{cases}$

MUX for $\text{imm}[0]$ $\begin{cases} S: \text{instr}[7] \\ B: 0 \text{ (implicit)} \end{cases}$

Implement jal : update PC, and save ra to $R[rd]$



Implement $jalr$: almost same, but starts from $R[rs1]$ (absolute)

↳ just use the I-format, but MUX selects $R[rs1]$ instead of pc

Implement U-Format: Change the Imm.Gen accordingly

$LUI \rightarrow R[rd] = imm$, so ALU just selects the Blne!

$AUIPC \rightarrow R[rd] = PC + imm$, so ALU just does it.

Datapath Control

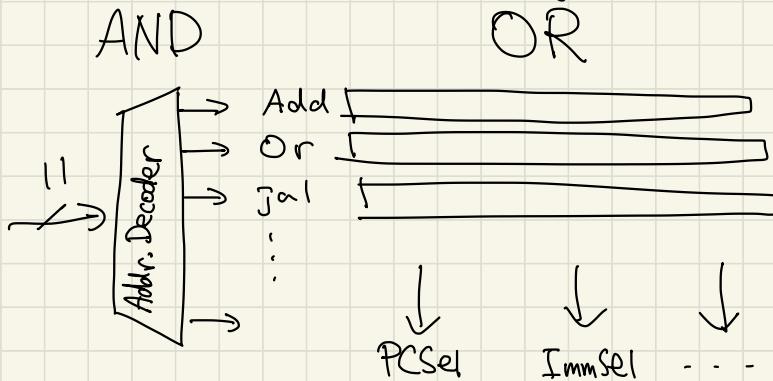
Somehow, we need to extract control logic from instr. bits

Critical Path: $t_{c-q} + [t_{IMEM} + t_{Reg} + t_{mux} + t_{ALU} + t_{DMEM} + t_{mux}] + t_{setup}$

Two ways to realize control: ROM or Comb. Logic

In RISCV32, we only need 11 bits, $inst[30, 14:12, 6:2] + BrEq, LT!$

ROM Controller: One-hot encoding for all instructions



Pipelining

"How do we improve our datapath performance?"

↳ what does it mean to improve performance?

① Program Execution Time → Time / program

② Throughput

③ Energy per Task → Energy / program

$$\frac{\text{Time}}{\text{Program}} = \frac{\text{Instruction Program}}{\text{Cycle Instruction}} \cdot \frac{\text{Time Cycle}}{\text{Critical Path}} \rightarrow \text{Execution depends on all 3!}$$

↓
 PL, compiler,
 algorithm, etc.

$$\frac{\text{Energy}}{\text{Program}} = \frac{\text{Instruction}}{\text{Program}} \cdot \frac{\text{Energy}}{\text{Instruction}}$$

CV^2; hardware

capacitance supply voltage

reducing supply voltage is hard

- Pipelining: make an assembly line-like structure
- ↳ Latency (single task speed) is unchanged, but throughput increases!
 - ↳ max speedup = # of stages, limited by the slowest stage
 - ⇒ We can apply this to our RISC-V datapath with registers!
 - ↳ clock now tells stage time, not instruction time

However, there are some things to be careful about...

- * the register is actually accessed twice (decoding & write back)
 - ↳ the rd is not what we originally meant → send it during WB!
- * the control logic needs to be pipelined (either the instruction or control)

Pipelining: Hazards

Structural Hazards: two instructions need the same resource

- ① Instructions take turns (incurs "stall time")
- ② Add more hardware
- ③ Design ISA to avoid conflict (RISC-V!)

Data Hazards: register values don't get updated instantly!

- ↳ Three solutions: ① Stalling ② Forwarding ③ Code Scheduling

- ① Stalling: insert noop (no instruction) intentionally to delay instructions
 - ↳ the compiler needs to know about the pipeline!

② Forwarding: communicate the computed value earlier than WB

↳ needs extra hardware to implement instantaneous "shouting"

↳ extra wire & extra logic to find whether forwarding is needed

ex) wire the output of ALU to A input of ALU for immediate usage

If the forwarding is still too slow, we need stalling. (A sel now has ↗)

ex) value from lw is wired to the A input of ALU ← more choices

③ Scheduling: use a no-op slot to execute an unrelated instruction

Control Hazards: branches aren't taken instantaneously!

↳ If we take a branch, cancel some future instructions as no-op

↳ To cancel, force all Write controls to 0 (nothing is updated)

Branch prediction can increase performance on average

More pipeline depth \Rightarrow Faster, but more potentials for hazards!

Superscalar: Multiple execution units in parallel \Rightarrow CPI < 1!

$$\hookrightarrow \text{CPI} = \frac{\text{Time}}{\text{Program}} \div \left(\frac{\text{Instructions}}{\text{Program}} \cdot \frac{\text{Time}}{\text{Cycle}} \right)$$

Caching

Binary Prefix: kilobyte = 1024 bytes, in SI Units, 1000 bytes.

↪ Hard Disk & Telecommunications use SI, all else "binary prefixes"

$$\text{kibi} \rightarrow 2^{10}, \text{mebi} \rightarrow 2^{20}, \text{gibi} \rightarrow 2^{30}, \dots \Rightarrow 2^x = 2^y \cdot 2^{10x}$$

Cache: Middle memory between processor and main memory ^(DRAM)

↪ Secondary memory (disk / flash) is even farther away

* closer to processor \Rightarrow smaller, faster, expensive, and subset

* Cache stores instructions and data most relevant to program

Locality: Temporal & Spatial locality gives direction on what to save

\Rightarrow recently accessed data can be stored close to processor!

\Rightarrow move blocks nearby the referenced data together!

Direct Mapped Caches: memory address mapped to one block in cache

↪ Each block can hold an 2^x number of bytes \rightarrow shift arithmetic!

\Rightarrow In address: tag index offset, where $h \underbrace{\overline{1111}}_{\leftarrow w} \underbrace{\overline{1111}}_{\leftarrow 2^2} \underbrace{\overline{0000}}_{\leftarrow 2^3}$.

(think of the index & offset like row & column coordinates

where # of bytes of index & offset are $\log(h), \log(w)$!)

\Rightarrow tag length = addr length - offset - index *

Memory Access with Cache: If hit, send. If miss, fetch block.

↪ Cache never writes to memory, only copies it!

Cache miss, block replacement: wrong data, so fetch and overwrite

Cache Temperature: Cold ← Warming → Warm Hot → for performance

Miss penalty: time lost by missing a cache and replacing it

Valid Bit: 0 → cache miss/garbage 1 → cache hit if addr.=tag

↪ when initializing a program, set all valid bits to 0

How to handle writing?

↪ Write-through updates both cache and memory

↪ Write-back allows inconsistency and updates when replaced
(being "stale")

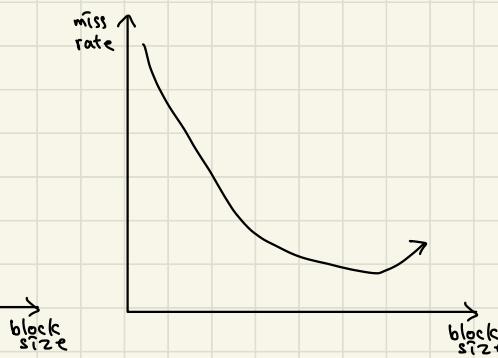
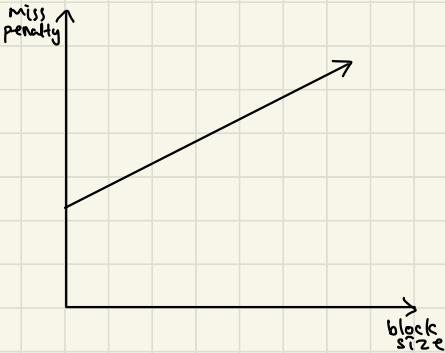
(also need to add a "dirty" bit to remind inconsistency)

⇒ Trade-off between performance and complexity

Is large block size good? There is also a trade-off.

↪ Spatial locality ∝ block size, but also larger miss penalty

↪ an extremely large block size will need to discard data too often (ping-pong effect)



Types of Misses:

- 1) Compulsory Miss: First time, so it must be empty
- 2) Non-compulsory Miss: All other misses

Fully Associative Cache: put data on any row, but need to compare against all rows when reading from cache \Rightarrow infeasible hardware

Set-Associative Cache: A middle-ground for associativity

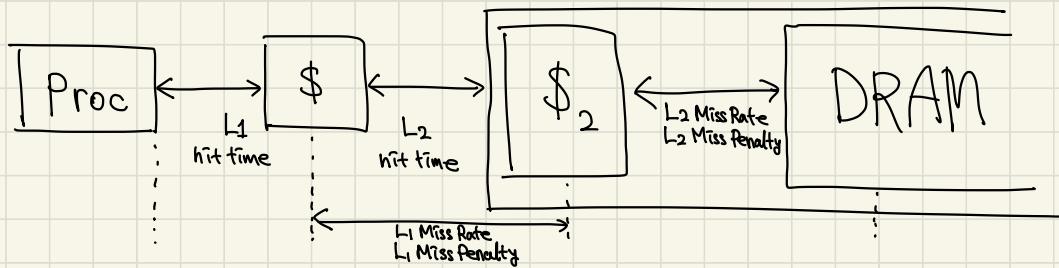
\hookrightarrow Each set acts like a fully associative cache, but the set itself is directly mapped to the index value \Rightarrow much more lenient!

Block Replacement Policy: If all valid bits are on in the same set, which to replace with?

ex) Least Recently Used (LRU), FIFO, Random, etc.

Average Memory Access Time = Hit Time + Miss Penalty × Miss Rate

↳ How do we improve the miss penalty? Second Level Cache!!



$$AMAT = L_1 \text{HitTime} + L_1 \text{MissRate} \times L_1 \text{MissPenalty}$$

$$L_1 \text{MissPenalty} = L_2 \text{HitTime} + L_2 \text{MissRate} \times L_2 \text{MissPenalty}$$

$$\Rightarrow AMAT = L_1 \text{HitTime} + L_1 \text{MissRate} \times (L_2 \text{HitTime} + L_2 \text{MissRate} \times L_2 \text{MissPenalty})$$

→ hardware limit for clock speed

How to improve miss rate? Larger cache, or increase associativity

Parallelism

Single Instruction/Single Data Stream: What we did upto now

Single Instruction/Multiple Data Stream (SIMD): parallel operations!

Multiple Instruction/Multiple Data Stream (MIMD): multicore/WSC

MISD is not relevant anymore (Why would you do this...)

		Software	
		single	multiple
Hardware	single		
	multiple		

SIMD Architectures: Data-Level Parallelism (DLP)

ex) vector element-wise multiplication in a single cycle

Advanced Digital Media Boost: MultiMedia eXtension (MMX)

→ developed to wider registers for more parallelism (512b)

XMM registers: eight 128-bit data registers (packed!)

↳ allows four single-precision operations in parallel

(Intel uses 16 bits for a word, 32 for float, and 64 for double)

SIMD Array Processing: for every 4 members in array ...

Intrinsics: C functions & procedures that can choose SSE instructions

↳ How to do this in RISC-V? → add SIMD instructions!

Thread-Level Parallelism

ex) CPU with two cores: two processors executing their own instructions

↳ Separate: Datapath (PC, Reg, ALU), L1 & L2 cache

↳ Not separate: Memory (DRAM), L3 cache (not required)

Thread: A single stream of instruction, a program can fork into multiple threads. Single core can execute each thread via time sharing.

Each thread has: a dedicated PC, registers, and access to shared memory

Hardware thread: ones running on cores, Software thread: all else

↳ Multiplex sw thread onto hw threads for efficiency!

Removing a sw thread from hw: Interrupt, save registers & PC

Load a sw thread to hw: Initialize a core with loaded registers & PC

Multithreading: is swapping threads while stalled worth it?

↳ Two copies of PC & registers → executes like two threads!

→ More Logical CPUs than Physical CPUs! (Hyperthreading)

OpenMP

Parallel Loops: #pragma omp parallel for

↳ code must be resilient to indeterminism in order!

Fork-Join Model: forks and executes simultaneously, then joins

Race Condition: result depends on the parallelized operation order

Synchronization: Limit access to shared resource to 1 actor at a time

↳ use a "lock" to signify possession of a variable by a thread

→ However, there can be a race condition for lock possession!

Hardware Synchronization → atomic read/write! no interruption in btwn

Atomic Memory Operation: performs operation in place, old value to rd

↳ This enables abstraction to declare a critical block of code

Deadlock: a system state in which no progress is possible

OpenMP timing: double omp_get_time(void) → wall clock time

Shared Memory Multiprocessor: Single memory space shared by all

↳ each processor has their own private cache → incoherent values?

Cache Coherency: notify other processors when a write or miss happens

↳ a shared block is consistent with memory

↳ a modified block is changed, no other cache has a copy, memory out-of-date

↳ an exclusive block is same as modified except memory is up-to-date

↳ an owner block, other caches can have a copy (shared state),
the owner must respond to a snoop request with data.

False sharing: two caches claim that they have the valid block

↳ Introduces a Coherence Miss!

Distributed Computing

- "Many different programs working together to achieve common goal"
- Concurrency is hard: no shared memory / state, locks are hard.
- Failure handling is hard: "zombie processes" keeps running in one crash
- Communication is hard: transmission delay, message expectation?
- Split into independent subtasks, minimize communication!

Manager-Worker Framework: One manager only assigns work to others

- ↳ needs agreement on what instructions are supposed to mean
- ↳ manager doesn't do work to prevent stalling giving out instructions

MapReduce: Abstraction for jobs involving mapping and reduction

- ↳ transform via mapping, then group elements by keys for reduction

Virtual Memory

"Give each process the illusion of using their own memory"

- Physical vs Virtual Addresses, OS translating between

Naïve approach: 1-to-1 mapping table for each address

Pages: Map ranges of contiguous memory → saves table columns!

↳ store only the top bits necessary to tell pages → page numbers

ex) Virtual page 0x12345 has address 0x12345000 ~ 0x12345FFF

→ In real life, only physical page numbers are stored, and VPNs are indices.

Page tables also lives in memory → every load/store is two mem access! *

↳ ① Fetch PPN from page table ② Access actual data in memory

Parameters: Page size, VM size, PM size ⇒ affects # of bits

VPN bits = VM bits - offset bits, and so forth.

Size of Page Table: # of entries × size of each entry

What if physical memory < virtual memory? → use disk memory!

↳ accessing data not in memory causes a page fault, evicting another data in memory and updating the page table ↳ PPN is garbage

How to allocate pages? → Demand paging: only load upon request

Writing Data: ① write through ② write back (like cache)

↳ ALL VMs uses write-back (disk is too slow), use dirty bit

⇒ Gives illusion of larger memory and demands isolation btwn programs

... sometimes, multiple program might need the same memory
→ just direct both programs to the same physical page.

A Read-Only bit can be used to protect certain pages!

→ only one TLB per core

Translation Lookaside Buffer(TLB): "Caches" for page tables.

↪ Fully associative, just remembers the last few pages accessed

TLB Reach = # of TLB entries \times Page size (immediate resolve!)

* When the OS context-switches, it must invalidate the TLB (flush!)

⇒ Three cases: ① TLB hit ② Page Table hit ③ Disk access

↳ if TLB or Page Table faults, update it on the way back!

VM + Caches: Physically Indexed, Physically Tagged (PIPT)

