# Basic Sorting

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## Overview I

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#### Intro

#### Time Complexity:

- worst/average/best cases
- Order andruntime complexity function
- Number of comparisons vs number of swaps

#### Space Complexity:

• Is it in place, this requires just a constant amount of memory.

#### Basis:

- Comparison (selection, insertion, bubble, merge, quick and heap sort).
- Grouping (counting, bucket and radix).

#### Stability:

 Algorithm stable if the ordering of equal items in the original array is maintained in the sorted array.

#### Selection sort

- 1 Find the minimum value in the list.
- Swap it with the value in the first position.
- Repret the steps above for the for remainder of the list (starting in the second position).

```
for i = 1 to n-1:
    pos = i
    for j=i+1 to n:
        if T[j] < T[pos]
        pos = j
        endif
    endfor
    temp = T[pos]
    T[pos] = T[i]
    T[i] = temp
endfor</pre>
```

## Analysis

- Fundamental operation: T[j] < T[pos].</li>
- Worst case: All cases the same.
- Complexity function:

$$t(n) = \sum_{i=1}^{n-1} \left(\sum_{j=i+1}^{n} (1)\right)$$

$$= \sum_{i=1}^{n-1} (n - (i+1) + 1)$$

$$= \sum_{i=1}^{n-1} (n - i)$$

$$= n(n-1) - \sum_{i=1}^{n-1} (i)$$

$$= n(n-1) - \frac{n(n-1)}{2}$$

$$= \frac{n(n-1)}{2}$$

$$= \frac{n^2}{2} - \frac{n}{2}$$



(1)

# Summary

- Basis: Comparison
- Time Complexity:
  - Number of comparisons is  $\Theta(n^2)$
  - Number of swaps is  $\Theta(n)$ .
- Space Complexity: Constant (in place).
- Stability: Not Stable

#### Bubble sort

- Scan the array, swapping any out of order neighbouring elements.
- Once the largest element is in the last position, the procedure is repeated to find the next largest, and so on.

```
for i=n to 1:
    for j=1 to i-1:
        if T[j] > T[j+1]
            SWAP(T[j],T[j+1]
        endif
    endfor
endfor
```

## **Analysis**

- Fundamental operation: T[j] > T[j+1].
- Worst case: All cases are the same.
- Complexity function:

$$t(n) = \sum_{i=1}^{n} (\sum_{j=1}^{i-1} (1))$$

$$= \sum_{i=1}^{n} (i-1)$$

$$= \sum_{i=1}^{n} (i) - \sum_{i=1}^{n} (1)$$

$$= \sum_{i=1}^{n} (i-n)$$

$$= \frac{n(n-1)}{2} - n$$

$$= \frac{n^{2}}{2} + \frac{n}{2} - n$$

$$= \frac{n^{2}}{1} - \frac{n}{2}$$

$$\Theta(n^{2})$$

(2)

# Summary

- Basis: Comparison
- Time Complexity:
  - Number of comparisons is  $\Theta(n^2)$ .
  - Number of swaps is  $\Theta(n^2)$ .
- Space Complexity: Constant (in place sorting)
- Stability: Stable

### Insertion Sort

- A list size 1 is already sorted.
- Insert the element in position 2 into the already sorted list.
- From position 3 to n repreat the steps above

```
for i=2 to n:
    temp = T[i]
    j = i-1
    while j > 0 and temp < T[j]
        T[j+1] = T[j]
        j = j-1
    endwhile
    T[j+1] = temp
endfor</pre>
```

# Summary

- Basis: Comparison
- Time Complexity:
  - Worst Case and Average Case:
    - Number of Comparisons:  $O(n^2)$
    - Number of swaps:  $O(n^2)$
  - Best case:
    - O(n).
- Space Complexity: Constant (in place)
- Stability: Stable.

# The End