

# Lists Stacks & Queues

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## 1 Lists

- Comparisons
- Amortized Analysis

## 2 Stacks

- Intro
- Array implementation
- Linked-list implementation
- Parenthesis checking

# Comparisons

- Is a **linear data structure**.
- A List is a collection where the elements are **ordered** and therefore each element has an index which is the position in the list. Allows duplicates.
- A Set is an **unordered** collection in which no two elements are identical.
- A Bag is an **unordered** collection in which can have duplicates.

	Linked List	Array based
Access	$\Theta(n)$	$\Theta(1)$
Insertion	$O(n)$	$O(1)$
Deletion	$O(n)$	$O(n)$

# Amortized Analysis

- In **Amortized analysis**, the time taken to execute a sequence is averaged over all the operations executed.
- Even though one of the operations in the sequence might take a long time, the average time taken over all operations is small.
- This is not the same as the average case.
- This guarantees the average performance of each operation in the worst-case.

- It's a list structure where all operations occur on one end of the list, known as the **top of the stack**.
- To add an element is called a **push** operation.
- To remove an element is called a **pop** operation.
- To get the element at the **top of the stack** is called a **top** operation.

# Array implementation

- Requires a means of handling **array overflow**, i.e. double size of array when full.
- `push()` has an **amortized** complexity of  $O(1)$  in the worst case.
- `top()` does not alter the stack at all and simply gives the top element, this is  $O(1)$  in the worst case.
- `pop()` only alters the last element, nothing is shifted and therefore has complexity  $O(1)$  in the worst case.

# Linked-list implementation

- `push()` has a complexity of  $O(1)$  in the worst case, this is **NOT** **amortized** due to the lack of array overflow requirement.
- `top()` has  $O(1)$  complexity in the worst case.
- `pop()` has  $O(1)$  complexity in the worst case.

# Parenthesis checking

- Stacks can be used to determine if parenthesis match correctly or not. e.g.  $[a(b + c)da/c + e]/b$
- Use a stack to push the left side of the parenthesis and when the right side has been found, pop the parenthesis.
- When an item is popped, it is compared to the found parenthesis and if they are of the same type, then it's matching.



# The End