

MACHINE LEARNING OUTLINE

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Pseudocode for finding the derivative of some node with respect to some weight w_k :

```
if w_k is in links:
    return links[w_k].previousActivation
else:
    out = 0
    for link in links:
        selfDer = derivative of this with respect to link
        out += selfDer * (derivative of link with respect to w_k)
    return out
```

Anatomy of an error node:

Method 1 (vector norm):

$$y = \sqrt{\sum (e_i - o_i)^2}$$
$$\frac{\partial y}{\partial w_k} = \frac{-\sum (e_i - o_i) \frac{\partial o_i}{\partial w_k}}{y}$$

Method 2 (easy derivative):

$$y = \sum (e_i - o_i)^2$$
$$\frac{\partial y}{\partial w_k} = -2 \sum (e_i - o_i) \frac{\partial o_i}{\partial w_k}$$

Anatomy of a regular node:

Sigmoid S :

$$S(x) = \frac{1}{1 + e^{-x}}$$
$$S'(x) = S(x)(1 - S(x))$$

Sum f :

$$f(\vec{b}) = \sum v_i w_i + b$$
$$\frac{\partial f(\vec{b})}{\partial w_k} = \sum w_i \frac{\partial v_i}{\partial w_k}$$

(If w_k is within its list of weights, the derivative will instead be equal to v_i)

Full equation:

$$y = S(f(\vec{b}))$$
$$\frac{\partial y}{\partial s} = S'(f(\vec{b}))(f'(\vec{b}))$$

With inputs v_n , weights w_i and bias b . Partial derivative taken with respect to later weight s .