

Assignment 1: Get at least 1 working benchmark done

Jordan Dehmel

Due no later than 11:59 PM on Friday, January 16, 2026

Choice of first benchmark

From a cursory glance, problem 8 (AKA `list_append_inj_1.smt2`) seems like one of the more simple ones. The following is the SMT2 code defining the problem.

```
; Injectivity of append
(declare-datatype
  list (par (a) ((nil) (cons (head a) (tail (list a))))))
(define-fun-rec
  ++
  (par (a) (((x (list a)) (y (list a))) (list a)))
  (match x
    ((nil y)
     ((cons z xs) (cons z (++ xs y))))))
(prove
  (par (a)
    (forall ((xs (list a)) (ys (list a)) (zs (list a)))
      (=> (= (++ xs zs) (++ ys zs)) (= xs ys)))))
```

Understanding the benchmark in SMT-LIB

We will take this line-by-line according to the SMT2 documentation.

Line 1: `declare-datatype`

Line 1 is

```
(declare-datatype list
  (par (a) (
    (nil)
    (cons
      (head a)
      (tail
        (list a)
      )
    )
  ))
)
```

The relevant information comes from `smt-lib` reference, page 61.

This means that `(declare-datatype list ...)` means “create an algebraic datatype `list` with the following constructors”. The `(par (a) BODY)` syntax allows parametric types with parameter `a` (Ibid, page 29).

Therefore, line 1 creates a parametric algebraic datatype called `(list a)` (over parameter `a`) which is instantiable via either a `nil` (empty list / list termination) or a `cons` (non-empty list with two data members) constructor.

Line 2: define-fun-rec

Line 2 is

```
(define-fun-rec
  ++
  (par (a) (
    (
      (x (list a))
      (y (list a))
    )
    (list a)
  ))
  (match x
    (
      (nil y)
      (
        (cons z xs)
        (cons z (++ xs y))
      )
    )
  )
)
```

The manual deals with `define-fun-rec` on page 63. This command takes the form `(define-fun-rec f ((x1 s1) ... (xn sn)) s t)`, where `f` is the name of the function (of sort `s`), `(xi si)` is the *i*-th argument named `xi` of sort `si`, and `t` is the function body. Also see page 29 for match statements.

```
(define-fun-rec                                ; Define a recursive function
  ++                                           ; Named "++"
  (par (a) (                                    ; With signature parametrized by a
    (
      (x (list a))                             ; Arg 1 named x of sort (list a)
      (y (list a))                             ; Arg 2 named y of sort (list a)
    )
    (list a)                                   ; Return sort (list a)
  ))
  (match x                                     ; Begin function body: Match on x
    (
```

```

      (nil y)                ; If x was nil, return y
    (
      (cons z xs)            ; Else, head=z tail=xs
      (cons z (++ xs y))    ; Return new list w head=z,
                           ; tail=(++ xs y)
    )
  )
)

```

In effect, this creates a function `++` which takes in two lists `a`, `b` and returns a new list containing all the elements of `a` followed by all the elements of `b`.

Line 3: prove

Line 3 is

```

(prove
  (par (a)
    (forall
      (
        (xs (list a))
        (ys (list a))
        (zs (list a))
      )
      (=>
        (= (++ xs zs) (++ ys zs))
        (= xs ys)
      )
    )
  )
)

```

In effect, this says that:

Given some type parameter `a`, for all `xs`, `ys`, `zs` of sort `(list a)`, if the appendation of `zs` onto the end of `xs` is equal to the appendation of `zs` onto the end of `ys`, it must be true that `xs` are equal to `ys`.

Translating to rust

We need to have the following:

- A generic `LinkedList<T>` structure (or enumeration) with
 1. A `nil` variant constructor to signify an empty list
 2. A head/tail variant constructor to signify a nonempty list
- A function taking in two like-typed lists `a`, `b` and returning a new list containing all items of `a` followed by all items of `b`
 - We will call this `conjoin(a, b)`

From these, we need to prove that: - For any generic type: - For any three like-typed lists `xs`, `ys`, `zs`: - `conjoin(xs, zs) == conjoin(ys, zs)` implies that `xs == ys`

A corresponding rust snippet is given below.

```

/// A module exposing an axiomitized generic linked list
pub mod linked_list {
    /// A generic linked list
    #[derive(Clone)]
    pub enum LinkedList<T> where T: Clone {
        /// The end-of-list / empty-list constructor
        Nil,
        /// A non-empty constructor which points to memory on the
        /// heap
        Cons { head: T, tail: std::rc::Rc<LinkedList<T>> },
    }

    /// Given two linked lists of similar type, return a new list
    /// containing the elements of the first (x) followed by the
    /// elements of the second (y).
    pub fn conjoin<T>(
        x: LinkedList<T>,
        y: LinkedList<T>) -> LinkedList<T> where T: Clone {
        match x {
            LinkedList::Nil => y,
            LinkedList::Cons{head, tail} => LinkedList::Cons{
                head: head,
                tail: std::rc::Rc::new(conjoin(
                    (*tail).clone(), y
                ))
            }
        }
    }

    /// Returns whether or not two lists are identical (EG of the
    /// same length and containing corresponding items)
    pub fn eq<T>(x: &LinkedList<T>, y: &LinkedList<T>)
        -> bool where T: Clone + std::cmp::PartialEq {
        match x {
            LinkedList::Nil => match y {
                LinkedList::Nil => true,
                _ => false
            },
            LinkedList::Cons{head: x_head, tail: x_tail} => match y {
                LinkedList::Nil => false,
                LinkedList::Cons{head: y_head, tail: y_tail} =>

```

```
        (x_head == y_head) && eq(x_tail, y_tail)
    }
}
}
```

Now we just need to figure out how to encode our “prove” statement in **ravencheck** syntax.

Expressing in **ravencheck**

Verification