

STAT345: Homework 8

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Problem 1

a

$$Z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$$

$$Z = \frac{19.8889 - 20}{0.75 / \sqrt{10}}$$

$$Z = -0.4684387308$$

$$p-value = 1 - 0.68439$$

$$p-value = 0.31561$$

I do not reject the null hypothesis.

b

$$Z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$$

$$Z = \frac{19.8889 - 20}{0.75 / \sqrt{10}}$$

$$Z = -0.4684387308$$

$$p-value = 2(1 - 0.68439)$$

$$p-value = 0.63122$$

I still do not reject the null hypothesis.

Problem 2

a

$$\bar{x} = 98.224$$

$$s = 0.5577335$$

$$t_{n-1, \frac{\alpha}{2}} = 2.064$$

$$t_0 = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$$

$$t_0 = \frac{98.224 - 98.6}{0.5577335 / 5}$$

$$t_0 = -3.3707855096$$

The null hypothesis is incorrect. $\mu_0 \neq 98.6$.

b

$$\bar{x} = 98.224$$

$$s = 0.5577335$$

$$t_{n-1, \frac{\alpha}{2}} = 2.064$$

$$t_0 = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$$

$$t_0 = \frac{98.224 - 98.6}{0.5577335/\sqrt{5}}$$

$$t_0 = -3.3707855096$$

The null hypothesis is incorrect. $\mu_0 < 98.6$.

Problem 3

a

$$\mu = 1.5 \quad \bar{x} = 1.4975 \quad \sigma = 0.01 \quad Z = -1.25$$

The diameter is not less than 1.5.

b

$$p-value = 1 - \phi(z) \quad p-value = 1 - 0.06681 \quad p-value = 0.93319$$

Problem 4

$$\hat{p} = 0.6 \quad p_0 = 0.5 \quad z_0 = \frac{\hat{p} - p_0}{\sqrt{p_0(1-p_0)/n}} \quad z_0 = \frac{0.6 - 0.5}{\sqrt{0.5(1-0.5)/500}} \quad z_0 = 4.472135956 \quad \text{Yes}$$

more than half of the voters support term limits for politicians.