

$$1) \lambda = \frac{m}{\sum_{i=1}^n t_i} = \frac{25}{5048,36} = 0,005954 \approx 9,6 \cdot 10^{-4}$$

$$2) L(\lambda) = \prod_{i=1}^n f(\lambda, x_i) = \prod_{i=1}^n \lambda^m x_i^m e^{-\frac{\lambda}{2} \sum_{i=1}^n x_i^2}$$

Aplicando o ln

$$l(\lambda) = \ln(L(\lambda)) = m \ln \lambda + m \ln x + -\frac{\lambda}{2} \sum_{i=1}^n x_i^2$$

Derivando e igualando a zero

$$\frac{\partial l(\lambda)}{\partial \lambda} = \frac{m}{\lambda} + 0 + -\frac{1}{2} \cdot \sum_{i=1}^n x_i^2 = 0$$

$$\frac{m}{\lambda} = -\frac{\sum_{i=1}^n x_i^2}{2} \rightarrow \boxed{\lambda = \frac{2m}{\sum_{i=1}^n x_i^2}}$$

$$3) L(\lambda) = \prod_{i=1}^n f(\lambda, t_i) = \prod_{i=1}^n \left[\lambda^m e^{-\lambda^2 \cdot \sum_{i=1}^n t_i} \right]$$

$$\ln(L(\lambda)) = -m \ln \lambda + -\lambda^2 \sum_{i=1}^n t_i$$

Aplicando a derivada

$$\frac{\partial}{\partial \lambda} (l(\lambda)) = -\frac{m}{\lambda} - 2\lambda \cdot \sum_{i=1}^n t_i = 0$$

$$\frac{m}{\lambda} = -2\lambda \cdot \sum_{i=1}^n t_i \rightarrow \lambda = \sqrt{\frac{-m}{2 \sum_{i=1}^n t_i}}$$

$$f(x) = \lambda^x (5-2\lambda)^{1-x}$$

$$L(\lambda) = \prod_{i=1}^n \left(5-2\sum_{j=1}^m x_{ij} \right)$$

$$l(\lambda) = \ln(L(\lambda)) = \sum_{i=1}^n \ln \lambda + (m-2) \sum_{i=1}^n x_{ii} \ln(5-2\lambda)$$

Desenvolvendo e igualando a zero.

$$\frac{\partial}{\partial \lambda} = \frac{\sum_{i=1}^n x_{ii}}{\lambda} + (m-2) \frac{\sum_{i=1}^n x_{ii}}{5-2\lambda} = \frac{\sum_{i=1}^n x_{ii}}{\lambda} + \frac{(-2m+4\sum_{i=1}^n x_{ii})}{5-2\lambda} = 0$$

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$$\frac{\sum_{i=1}^n x_{ii}}{\lambda} = \frac{(-2m+4\sum_{i=1}^n x_{ii})}{5-2\lambda} = 0$$

$$5-2\lambda(\sum_{i=1}^n x_{ii}) - (-2m+4\sum_{i=1}^n x_{ii}) = 0$$

$$\cancel{\lambda \cdot (5-2\lambda)}$$

$$5\sum_{i=1}^n x_{ii} - \cancel{2\lambda \sum_{i=1}^n x_{ii}} - 2m\lambda + 4\sum_{i=1}^n x_{ii} = 0$$

$$5\sum_{i=1}^n x_{ii} - 2m\lambda + 2\sum_{i=1}^n x_{ii}\lambda = 0$$

$$5\sum_{i=1}^n x_{ii} = 2m\lambda - 2\sum_{i=1}^n x_{ii}\lambda$$

$$5\sum_{i=1}^n x_{ii} = \lambda(2m - 2\sum_{i=1}^n x_{ii})$$

$$\boxed{\lambda = \frac{5\sum_{i=1}^n x_{ii}}{2m - 2\sum_{i=1}^n x_{ii}}}$$

5) a) $\lambda = h(\tau) = \text{Taxa de falhas}$

$$\lambda = \frac{m}{\sum_{i=1}^n \tau_i} = \frac{6}{396} = 0,0151515 \approx 1,515 \cdot 10^{-2}$$

b) MTTF $= \frac{1}{\lambda} \approx 66$ mil horas de uso

c) $R = e^{-\lambda t}$ para $t = 300$ = ~~0,2000~~ $\approx 0,2000$

$$R = e^{-1,51515} = 0,25978$$