

# Multiproduct intermediaries

JPE, 2021

Andrew Rhodes, Makoto Wanabe, Jidong Zhou

February 9, 2026

# Outline

1 Introduction

2 Model

3 Discussion

# Motivation

- Many intermediaries sell *multiple products* (retailers, malls, platforms, TV platforms).
- A core strategic decision: product assortment and exclusivity.
- Two forces reshape this decision: direct-to-consumer (DTC) sales and exclusivity agreements.
- Existing theory offers little guidance on optimal assortment choices.

# Motivation

- **Question:** how can a multiproduct intermediary create value and earn profits?
- Standard models: profits require lower prices or better search.
- **Key result:** a multiproduct intermediary can earn strictly positive profits *without reducing prices or search costs*.
- Profits arise from assortment choice and cross-product search incentives.

# Related Literature

## Intermediaries

- Search / matching efficiency (Rubinstein–Wolinsky, 1987; Gehrig, 1993; Spulber, 1996)
- Certification, asymmetric information (Biglaiser, 1993; Lizzeri, 1999)

⇒ **This paper:** intermediaries earn profits even without improving search efficiency.

## Bundling

- Classic bundling mechanisms (Stigler, 1968; Adams–Yellen, 1976; McAfee et al., 1989)

⇒ **This paper:** focuses on which products are bundled via endogenous assortment choice.

## Multiproduct search

- Consumer search with exogenous product ranges (McAfee, 1995; Shelegia, 2012; Zhou, 2014; Rhodes, 2015)

⇒ **This paper:** endogenous product range choice with upstream manufacturers and vertical structure.

# Setting

## • Products / Manufacturers

- Continuum of products  $i \in [0, 1]$ , marginal cost  $c_i \geq 0$
- Demand  $Q_i(p)$ , monopoly price  $p_i^m$
- Per-consumer profit and surplus:

$$\pi_i = (p_i^m - c_i)Q_i(p_i^m), \quad v_i = \int_{p_i^m}^{\infty} Q_i(p) dp$$

## • Consumers

- Unit mass, additive utility across products
- Identical preferences; heterogeneity only in search cost  $s \sim F$
- Observe availability, not prices

## • Intermediary

- Chooses assortment  $A \subset [0, 1]$ ,  $|A| \leq \bar{m}$
- TIOLI contracts  $(\tau_i, T_i)$ , exclusive or not
- Search cost  $h(|A|) \cdot s$

# Timing

## Add a simple line, that is all, shimplesh

- ① The intermediary simultaneously makes TIOI offers  $(\tau_i, T_i)$  to manufacturers, specifying exclusivity or non-exclusivity. Manufacturers accept or reject.
- ② All firms that sell to consumers set retail prices for their products.
- ③ Consumers observe availability, form rational expectations over prices, then search sequentially and purchase.

# Lemma 1 (Pricing and Contracting)

## Lemma

*In any equilibrium where product markets are active:*

- ① *All sellers of product  $i$  charge the monopoly price  $p_i = p_i^m$ .*
- ② *If product  $i$  is stocked by the intermediary, there exists an equilibrium contract with*

$$\tau_i = c_i, \quad T_i = \pi_i F(v_i),$$

*both under exclusivity and non-exclusivity.*

## Add definition of $\Omega$ !!!!!!!

**Implication:** products can be indexed by

$$(\pi_i, v_i) \in \mathbb{R}_+^2,$$

with joint distribution  $G(\pi, v)$ .



# Simple Case: Consumer Decision

**Assumptions:** exclusivity,  $h(m) = m$ ,  $\bar{m} = 1$

Intermediary stocks  $A \subset \Omega$  exclusively.

$$\text{Visit } I \iff \underbrace{\int_A v dG}_{\text{expected surplus}} \geq \underbrace{s \int_A dG}_{\text{search cost}}$$

$$\iff s \leq \hat{v} \equiv \frac{\int_A v dG}{\int_A dG}$$

*Consumers compare average surplus to their search cost.*

# Simple Case: Intermediary Problem

Consumers visiting intermediary:  $F(\hat{v})$

Net profit from product  $(\pi, v)$ :

$$\pi [F(\hat{v}) - F(v)]$$

(gains from extra consumers – lump-sum paid to manufacturer)

$$\max_{A \subset \Omega} \int_A \pi [F(\hat{v}) - F(v)] dG$$

*Low- $v$  products earn profits. High- $v$  products attract consumers.*

# Solution: Optimal Product Selection

## Reformulation

Stocking decision:

$$q(\pi, v) = 1 \iff (\pi, v) \in A$$

## Intermediary problem

$$\max_q \int_{\Omega} q(\pi, v) \left[ \underbrace{\pi(F(\hat{v}) - F(v))}_{\text{direct profit}} + \underbrace{\lambda(v - \hat{v})}_{\text{search externality}} \right] dG$$

## Optimal policy: cutoff structure

$$q(\pi, v) = 1 \iff \begin{cases} v < \hat{v} \text{ and } \pi \geq \frac{\hat{v} - v}{F(\hat{v}) - F(v)} \\ v > \hat{v} \text{ and } \pi \leq \frac{\hat{v} - v}{F(\hat{v}) - F(v)} \end{cases}$$

*High- $\pi$ , low- $v$  products make money. Low- $\pi$ , high- $v$  products attract consumers.*

**Clarify the constraint, where does it come from** 

# Solution: Optimal Product Selection

mention proposition 1?

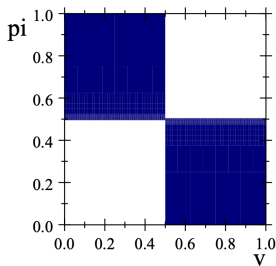


Figure 1: Optimal product range in the simple case

# Main Model

- richer environment
  - ①  $q(\pi, v) \in ((0, 0), (1, 0), (0, 1))$ , allow for  $(q^e, q^{ne})$
  - ②  $\hat{m} \leq 1$
  - ③  $h(m) \begin{smallmatrix} \leq \\ \geq \end{smallmatrix} m$
- $\rightarrow$  adds one more layer of complexity: firms also find it optimal to provide high  $\pi$ , high  $v$  goods.
- Now results endogeneously depend on  $h(m)$ ,  $\bar{m}$ , this provides scope for richer applications: exclusivity/nonexclusivity margin and capacity margin.
- **Applications:** re

# Summary

- New framework to study multiproduct intermediaries when consumers face heterogeneous demand and search frictions.
- Main result: show that a multiproduct intermediate is profitable even if it does not provide search efficiencies.
- Mechanism: bundling + effects of technology/exclusivity under more complex contracts
- Provide applications to DTCs.

# Critiques/review

- I would add critique + possible solutions; be nice and fair with them. This is to do.
- Mostly, consumers are passive agents, accept the monopoly price.
- Also, absence of price competition among I (only one; this is the most obvious critique, but their model serves the purpose of starting a conversation)-; they acknowledge this... and actually is part of their research agenda. How would this look like?
- What else?