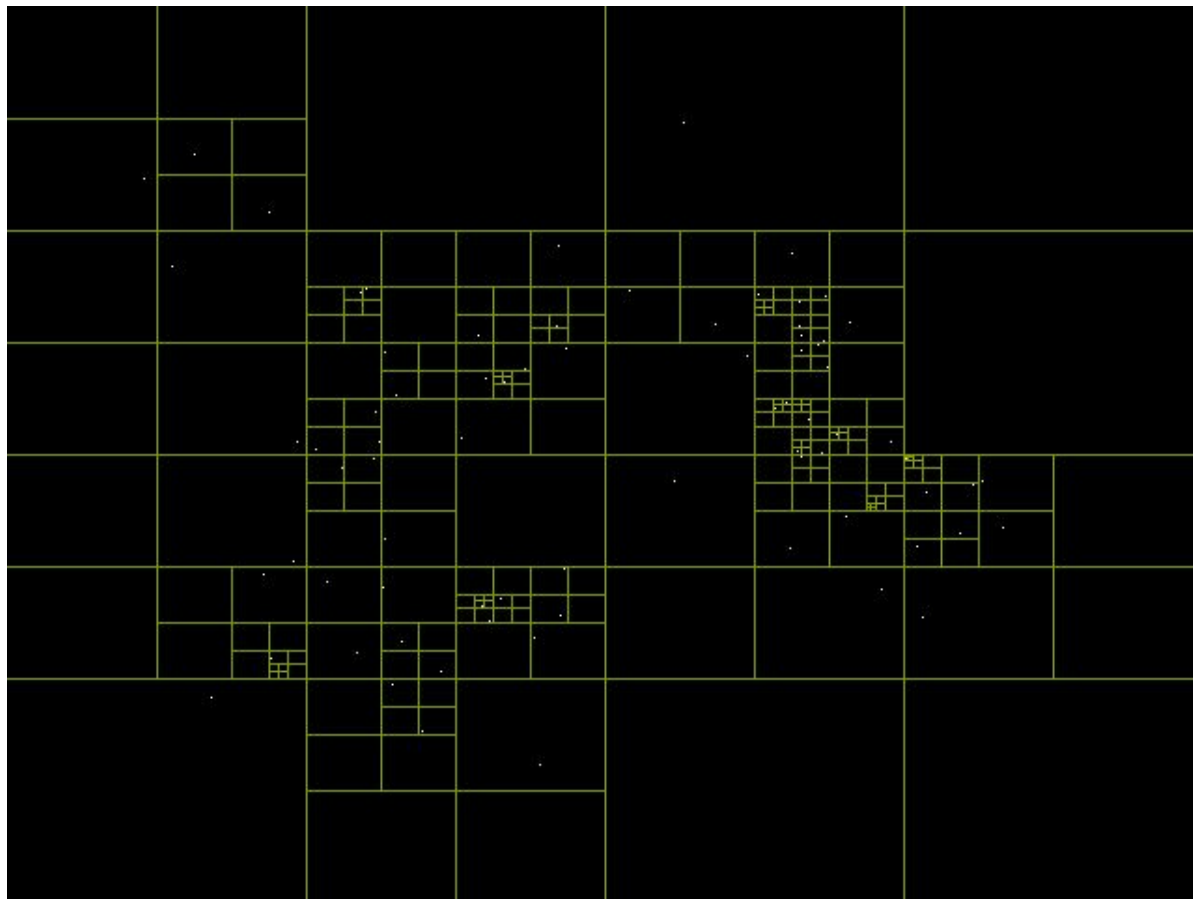



Jorge Arellano





Developed in 1987 by Leslie Greengard & Vladimir Rokhlin Jr.,  
FMM was originally developed as a fast algorithm for approximating  
the N-body problem

$$O(N^2) \quad \text{to} \quad O(N)$$



# Motivation

“Complexity Trumps Hardware.”

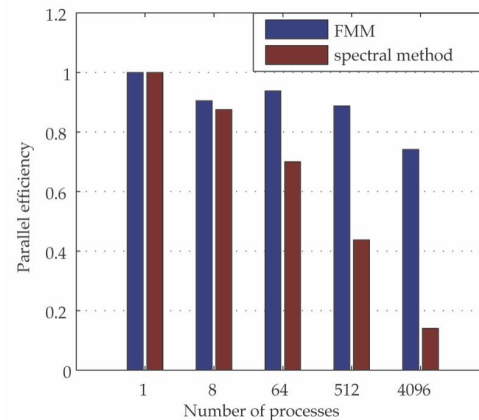
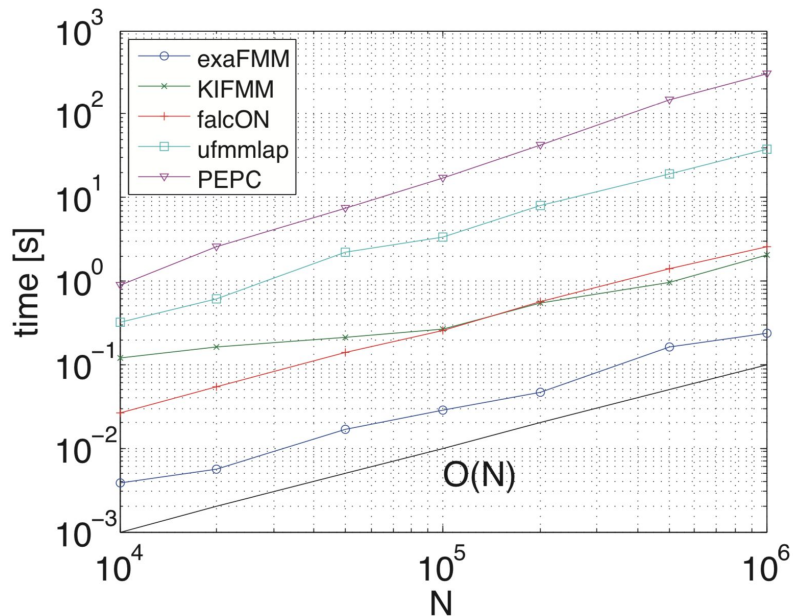
The current trend in computer architecture is moving towards multi-core processors and many-core processors where the Byte/flop ratio is decreasing with every generation.



# Simulation of Celestial Bodies

<https://youtu.be/W04TzMMpp9A>

# Benchmarks



**Figure 2.** Weak scaling from 1 to 4096 processes of two parallel application codes for fluid turbulence, one using an FMM-based solver on GPUs (one GPU per MPI process), the other an FFT-based solver on CPUs. Figure used under CC-BY license; doi:10.6084/m9.figshare.92425.



# Conclusion

FMM works!

But only useful when the problem can be parallelized

Low byte/flop (dense lin-alg) tend to have high complexity  $O(N)$  and algorithms with low complexity (FFT, Sparse Lin-alg) have high Byte/flop. FMM has an impressive combination of  $O(N)$  complexity and a Byte/flop that is even lower than matrix-matrix multiplication.

A possible alternative more PDE solvers.



# references

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