Stat 250: Stat Principles and Practices Sampling Distributions

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Terminology

Ex: Interest lies in average height of S250 students.

- population: all S250 students
- ullet parameter: pop. mean height, μ
- sample: 100 students chosen
- $\overline{\,\cdot\,}$ statistic: sample mean height, $ar{x}$

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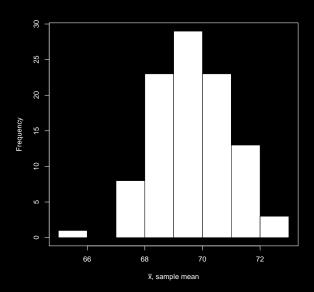
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random sample: each observation has same chance of being selected from the population.

Sampling Distribution

The sampling distribution of a sample statistic from a sample of size *n* is the probability distribution of the sample statistic.

Heights of S250 students, n = 2



Normal Sampling Distributions

	Population	Sampling distr
mean	μ	$\mu_{ar{x}}$
variance	σ^2	$\sigma_{ar{x}}^2$
	$X \sim N(\mu, \ \sigma)$	$ar{X} \sim N(\mu, \ \sigma/\sqrt{n})$
	$X \sim (\mu, \ \sigma)$	$ ar{X} \sim AN(\mu, \ \sigma/\sqrt{n}) $

Central Limit Theorem

If we obtain a random sample of size n from a population with mean μ and variance σ^2 , then for sufficiently large n the sampling distribution is approximately normal:

$$AN\left(\mu, \frac{\sigma}{\sqrt{n}}\right).$$