INDICES

Each bit in a bitmap corresponds to a possible item or condition, with a bit set to 1 indicating presence or true, and a bit set to 0 indicating absence or false.

record number	ID	gender	income_level
Θ	76766	m	L1
1	22222	f	L2
2	12121	f	L1
3	15151	m	L4
4	58583	f	L3

	Bitmaps for gender		
	m	10010	
	f	01101	

Bitmaps for income_level		
L1	10100	
L2	01000	
L3	00001	
L4	00010	
L5	00000	

B+ tree is a type of self-balancing tree data structure that maintains data sorted and allows searches, sequential access, insertions, and deletions in logarithmic time. It is an extension of the B-tree and is extensively used in databases and filesystems for indexing. B+ tree is Balanced; Order (n): Defined such that each node (except root) can have at most n children (pointers) and at least $\lceil \frac{n}{2} \rceil$ children; **Internal nodes hold** between $\left\lceil \frac{n}{2} \right\rceil - 1$ and n-1 keys (values); Leaf nodes hold between $\lceil \frac{n-1}{2} \rceil$ and n-1 keys, but also store all data values corresponding to the keys; Leaf Nodes Linked: Leaf nodes are linked together, making range queries and sequential access very efficient.

· Insert (kev. data):

- Insert key in the appropriate leaf node in sorted order;
- If the node overflows (more than n-1 keys), split it, add the middle key to the parent, and adjust pointers;
- 1. Leaf split: 1 to $\left\lceil \frac{n}{2} \right\rceil$ and $\left\lceil \frac{n}{2} \right\rceil + 1$ to n as two leafs. Promote the lowest from the 2nd one.
- 2. Node split: 1 to $\left\lceil \frac{n+1}{2} \right\rceil 1$ and $\left\lceil \frac{n}{2} \right\rceil + 1$ to n. $\left\lceil n + \frac{1}{2} \right\rceil$ gets moved up.
- If a split propagates to the root and causes the root to overflow, split the root and create a new root. Note: root can contain less than $\lceil \frac{n}{2} \rceil - 1$ keys.

· Delete (kev):

- · Remove the key from the leaf node.
- If the node underflows (fewer than $\lceil \frac{n}{2} \rceil 1$ keys), keys and pointers are redistributed or nodes are merged to maintain minimum

Adjustments may propagate up to ensure all properties are maintained.

Hash indices are a type of database index that uses a hash function to compute the location (hash value) of data items for quick retrieval. They are particularly efficient for equality searches that match exact values

Hash Function: A hash function takes a key (a data item's attribute used for indexing) and converts it into a hash value. This hash value determines the position in the hash table where the corresponding record's pointer is stored. Hash Table: The hash table stores pointers to the actual data records in the database. Each entry in the hash table corresponds to a potential hash value generated by the hash function.

ALGORITHMS

Nested Loop Join: A nested loop join is a database join operation where each tuple of the outer table is compared against every tuple of the inner table to find all pairs of tuples which satisfy the join condition. This method is simple but can be inefficient for large datasets due to its high computational cost.

Simplified version (to get the idea) for each tuple tr in r: (for each tuple ts in s: test pair

Block transfer cost: $\boldsymbol{n}_r \cdot \boldsymbol{b}_s + \boldsymbol{b}_r$ block transfers would be required, where b_r – blocks in relation r, same for s. Only ${\bf 2}$ seeks are required.

BLOCK-NESTED JOIN

Block Nested Loop Join: A block nested loop join is an optimized version of the nested loop join that reads and holds a block of rows from the outer table in memory and then loops through the inner table, reducing the number of disk accesses and improving performance over a standard nested loop join, especially when indices are not available.

Simplified version (to get the idea)
for each block Br of r: for each block Bs of s:
 for each tuple tr in r: (for each tuple ts in s: test pair

Block transfer cost: $\left\lceil \frac{b_r}{(M-2)} \right\rceil \cdot b_s + b_r, \ b_r$ – blocks in relation $r,\ M$ – available blocks in memory buffer. Total of $2 \cdot \left\lceil \frac{b_r}{(M-2)} \right\rceil$ seeks.

Merge Join: A merge join is a database join operation where both the outer and inner tables are first sorted on the join key, and then

merged together by sequentially scanning through both tables to find matching pairs. This method is highly efficient when the tables are already sorted or can be sorted quickly, minimizes random disk access. Merge-join method is efficient; the number of block transfers is equal to the sum of the number of blocks in both files, $b_r + b_s$. Assuming that b_b buffer blocks are allocated to each relation, the number of disk seeks required would be $\left| \frac{b_r}{b_b} \right| + \left| \frac{b_s}{b_b} \right|$ disk seeks

- 1. Sort Both Tables: If not already sorted, the outer table and the inner table are sorted based on the join keys.
- 2. Merge: Once both tables are sorted, the algorithm performs a merging operation similar to that used in merge sort:
 - a. Begin with the first record of each table.
 - b. Compare the join keys of the current records from both tables.
 - i. If the keys match, join the records and move to the next record in both tables.
 - ii. If the join key of the outer table is smaller, move to the next record in the outer table.
 - iii. If the join key of the inner table is smaller, move to the next record in the inner table.
 - c. Continue this process until all records in either table have been examined.
- 3. Output the Joined Rows;

Hash Join: A hash join is a database join operation that builds an inmemory hash table using the join key from the smaller, often called the build table, and then probes this hash table using the join key from the larger, or probe table, to find matching pairs. This technique is very efficient for large datasets where indexes are not present, as it reduces the need for nested loops

- h is a hash function mapping Join Attrs values to $\{0,1,...,n_h\}$, where JoinAttrs denotes the common attributes of r and s used in the nat-
- + $r_0, r_1, ..., r_{n_h}$ denote partitions of r tuples, each initially empty. Each
- $\begin{aligned} & \text{tuple } t_r \in r^\text{n} \text{ is put in partition } r_i, \text{ where } i = h(t_r[\text{JoinAttrs}]). \\ & \bullet s_0, s_1, ..., s_{n_h} \text{ denote partitions of s tuples, each initially empty. Each} \end{aligned}$ tuple $t_s \in s$ is put in partition s_i , where $i = h(t_s[\text{JoinAttrs}])$.

Cost of block transfers: $3(b_r + b_s) + 4n_h$. The hash join thus requires $2\left(\left\lceil \frac{b_r}{b_b}\right\rceil + \left\lceil \frac{b_s}{b_b}\right\rceil\right) + 2n_h \text{ seeks.}$

b. blocks are allocated for the input buffer and each output buffer.

- 1. Build Phase:
 - a. Choose the smaller table (to minimize memory usage) as the
 - b. Create an in-memory hash table. For each record in the build table, compute a hash on the join key and insert the record into the hash table using this hash value as an index.
- a. Take each record from the larger table, which is often referred to as the "probe table."
- b. Compute the hash on the join key (same hash function used in the build phase).
- c. Use this hash value to look up in the hash table built from the
- d. If the bucket (determined by the hash) contains any entries, check each entry to see if the join key actually matches the join key of the record from the probe table (since hash functions can lead to collisions).
- 3. Output the Joined Rows

RELATIONAL-ALGEBRA

Equivalence rules

1.
$$\begin{split} \sigma_{\theta_1 \wedge \theta_2}(E) &= \sigma_{\theta_1} \Big(\sigma_{\theta_2}(E) \Big) \\ 2. &\qquad \qquad \sigma_{\theta_1} \Big(\sigma_{\theta_2}(E) \Big) &= \sigma_{\theta_2} \Big(\sigma_{\theta_1}(E) \Big) \\ 3. &\qquad \qquad \Pi_{L_1} \Big(\Pi_{L_2} \Big(\dots \Big(\Pi_{L_n}(E) \Big) \dots \Big) \Big) = \Pi_{L_1}(E) \end{split}$$

- only the last one matters.
- 4. Selections can be combined with Cartesian products and theta

$$\sigma_{\theta}(E_1 \times E_2) = E_1 \bigotimes_{\theta} E_2$$

$$\begin{split} \sigma_{\theta_1}\!\left(E_1 \bigotimes_{\theta_2} E_2\right) &= E_1 \bigotimes_{\theta_1} \wedge \theta_2 E_2 \\ E_1 \bigotimes_{\theta} E_2 &= E_2 \bigotimes_{\theta} E_1 \end{split}$$

6. Join associativity:

$$\begin{split} &(E_1 \bigotimes E_2) \bigotimes E_3 = E_1 \bigotimes (E_2 \bigotimes E_3) \\ &\left(E_1 \bigotimes_{\theta_1} E_2\right) \bigotimes_{\theta_2 \wedge \theta_3} E_3 = E_1 \bigotimes_{\theta_1 \wedge \theta_3} \left(E_2 \bigotimes_{\theta_2} E_3\right) \end{split}$$

7. Selection distribution:

$$\sigma_{\theta_1} \left(E_1 \bigotimes_{\theta} E_2 \right) = \left(\sigma_{\theta_0}(E_1) \right) \bigotimes_{\theta} E_2$$

$$\sigma_{\theta_1 \wedge \theta_2} \bigg(E_1 \bigotimes_{\theta} E_2 \bigg) = \Big(\sigma_{\theta_1}(E) 1 \Big) \big) \bigotimes_{\theta} \Big(\sigma_{\theta_2}(E_2) \Big)$$

8. Projection distribution:

$$\Pi_{L_1 \cup L_2} \bigg(E_1 \bigotimes_{\theta} E_2 \bigg) = \bigg(\Pi_{L_1} (E_1) \bigotimes_{\theta} \Big(\Pi_{L_2} (E_2) \Big) \bigg)$$

 $\Pi_{L_1 \cup L_2} \bigg(E_1 \bigotimes_a E_2 \bigg) = \Pi_{L_1 \cup L_2} \bigg(\Big(\Pi_{L_1 \cup L_3} (E_1) \Big) \bigotimes_{\theta} \Big(\Pi_{L_2 \cup L_4} (E_2) \Big) \bigg)$

9. Union and intersection commmutativity:

$$E_1 \cup E_2 = E_2 \cup E_1$$

$$E_1 \cap E_2 = E_2 \cap E_1$$

10. Set union and intersection are associative:

$$(E_1 \cup E_2) \cup E_3 = E_1 \cup (E_2 \cup E_3)$$

 $(E_1 \cap E_2) \cap E_3 = E_1 \cap (E_2 \cap E_3)$

11. The selection operation distributes over the union, intersection, and

$$\sigma_P(E_1-E_2)=\sigma_P(E_1)-E_2=\sigma_P(E_1)-\sigma_P(E_2)$$

12. The projection operation distributes over the union operation:

$$\Pi_L(E_1\cup E_2)=(\Pi_L(E_1))\cup(\Pi_L(E_2))$$

CONCURRENCY

CONFLICT

We say that I and J conflict if they are operations by **different trans**actions on the same data item, and at least one of these instructions is a write operation. For example:

- $I = \operatorname{read}(\mathbf{Q})$, $J = \operatorname{read}(\mathbf{Q})$ Not a conflict;
- I = read(Q), J = write(Q) Conflict;
 I = write(Q), J = read(Q) Conflict;
- I = write(Q), J = write(Q) Conflict.

CONFLICT-SERIALIZABILITY

If a schedule S can be transformed into a schedule S^\prime by a series of swaps of non-conflicting instructions, we say that S and S' are conflict equivalent. We can swap only adjacent operations

The concept of conflict equivalence leads to the concept of conflict serializability. We say that a schedule S is **conflict serializable** if it is conflict equivalent to a serial schedule.

Simple and efficient method for determining the conflict seriazability of a schedule. Consider a schedule S. We construct a directed graph. called a precedence graph, from S. The set of vertices consists of all the transactions participating in the schedule. The set of edges consists of all edges $T_i \to T_j$ for which one of three conditions holds:

- 1. T_i executes write(Q) before T_i executes read(Q).
- 2. T_i executes read(Q) before T_i executes write(Q).
- T_i executes write(Q) before T_i executes write(Q).

If the precedence graph for S has a cycle, then schedule S is not conflict serializable. If the graph contains no cycles, then the schedule S is conflict serializable.

STANDARD ISOLATION LEVELS

- · Serializable usually ensures serializable execution.
- · Repeatable read allows only committed data to be read and further requires that, between two reads of a data item by a transaction, no other transaction is allowed to update it. However, the transaction may not be serializable
- · Read committed allows only committed data to be read, but does not require re- peatable reads.
- · Read uncommitted allows uncommitted data to be read. Lowest isolation level allowed by SQL.

PROTOCOLS

We say that a schedule S is legal under a given locking protocol if S is a possible schedule for a set of transactions that follows the rules of the locking protocol. We say that a locking protocol ensures conflict serializability if and only if all legal schedules are conflict serializable; in other words, for all legal schedules the associated \rightarrow relation is acyclic.

 $\mbox{\bf Recoverable}$ schedule is one where, for each pair of transactions T_i and T_i such that T_i reads a data item previously written by T_i , the commit operation of T_i appears before the commit operation of T_j .

 ${f Cascadeless}$ schedule is one where, for each pair of transactions T_i and T_i such that T_i reads a data item previously written by T_i , the commit operation of T_i appears before the read operation of T_i . Every cascade-

Shared Lock – If a transaction T_i has obtained a shared-mode lock (denoted by S) on item O, then Ti can read, but cannot write, Q.

Exclusive Lock - If a transaction Ti has obtained an exclusive-mode lock (denoted by X) on item Q, then Ti can both read and write Q.

2-PHASED LOCK PROTOCOL

The Two-Phase Locking (2PL) Protocol is a concurrency control method used in database systems to ensure serializability of transactions. The protocol involves two distinct phases: Locking Phase (Growing Phase): A transaction may acquire locks but cannot release any locks. During this phase, the transaction continues to lock all the resources (data items) it needs to execute.

Unlocking Phase (Shrinking Phase): The transaction releases locks and cannot acquire any new ones. Once a transaction starts releasing locks, it moves into this phase until all locks are released.

PROBLEMS OF LOCKS

Deadlock is a condition where two or more tasks are each waiting for the other to release a resource, or more than two tasks are waiting for resources in a circular chain.

Starvation (also known as indefinite blocking) occurs when a process or thread is perpetually denied necessary resources to process its work. Unlike deadlock, where everything halts, starvation only affects some $while \ others \ progress.$

TIMESTAMP-BASED

Timestamp Assignment: Each transaction is given a unique timestamp when it starts. This timestamp determines the transaction's temporal order relative to others. Read Rule: A transaction can read an object if the last write occurred by a transaction with an earlier or the same timestamp. Write Rule: A transaction can write to an object if the last read and the last write occurred by transactions with earlier or the same timestamps

Assumes that conflicts are rare and checks for them only at the end of a transaction. Working Phase: Transactions execute without acquiring locks, recording all data reads and writes. Validation Phase: Before committing, each transaction must validate that no other transactions have modified the data it accessed. Commit Phase: If the validation is successful, the transaction commits and applies its changes. If not, it rolls back and may be restarted.

LOGS

WAL PRINCIPLE

Write Ahead Logging - Any change to data (update, delete, insert) must be recorded in the log before the actual data is written to the disk. This ensures that if the system crashes before the data pages are saved, the changes can still be reconstructed from the log records during recovery.

RECOVERY ALGORITHM

In the redo phase, the system replays updates of all transactions by scanning the log forward from the last checkpoint. The specific steps taken while scanning the log are as follows

- 1. The list of transactions to be rolled back, undo-list, is initially set to the list L in the < checkpoint L > log record.
- 2. Whenever a normal log record of the form $< T_i, X_j, V_1, V_2>$, or a redo- only log record of the form $< T_i, X_j, V_2 >$ is encountered, the operation is redone; that is, the value V_2 is written to data item X_j .
- 3. Whenever a log record of the form $< T_i \text{ start} > \text{is found}, T_i \text{ is added}$
- 4. Whenever a log record of the form $< T_i \ {\rm abort} > {\rm or} < T_i \ {\rm commit} >$ is found, ${\cal T}_i$ is removed from undo-list.

At the end of the redo phase, undo-list contains the list of all transactions that are incomplete, that is, they neither committed nor completed rollback before the crash.

In the undo phase, the system rolls back all transactions in the undolist. It performs rollback by scanning the log backward from the end:

- 1. Whenever it finds a log record belonging to a transaction in the undo-list, it performs undo actions just as if the log record had been found during the rollback of a failed transaction.
- 2. When the system finds a $< T_i$ start $> \log$ record for a transaction T_i in undo- list, it writes a $< T_i$ abort $> \log$ record to the log and removes ${\cal T}_i$ from undo- list.
- 3. The undo phase terminates once undo-list becomes empty, that is, the system has found $< T_i \ {\rm start} > \log \ {\rm records}$ for all transactions that were initially in undo-list.

LOG TYPES

- $< T_i, X_j, V_1, V_2 >$ an update log record, indicating that transaction T_i has performed a write on data item X_j . X_j had value V_1 before the write and has value V_2 after the write;
- $< T_i \text{ start} > -T_i \text{ has started};$
- < T_i commit > T_i has committed;
- $< T_i$ abort > T_i has aborted;
- < checkpoint $\{T_0,T_1,...,T_n\}$ > a checkpoint with a list of active transactions at the moment of checkpoint.

Pieņemsim, ka ir divas relācijas \boldsymbol{r}_1 un \boldsymbol{r}_2 ar atbilstošiem atribūtiem $r_1(A,B)$ un $r_2(B,C,D,E).$ Relācijā r_1 ir 51105 raksti, relācijā r_2 ir 320251raksti. Pieņemsim, ka vienā blokā ietilpst27relācijas r_1 raks sti un 25 relācijas r_2 raksti. Relācijas tiek joinotas $(r_1 \bowtie r_2)$ izmantojot block nested-loop join algoritmu. Cik bloki ir minimālais atmiņas apjoms M (skaitlis!), lai būtu nepieciešams ne vairāk kā

- 1. 130000 bloku pārraides (transfers) no diska
- 2. 25000 bloku pārraides (transfers) no diska

$$T = \left\lceil \frac{b_r}{M-2} \right\rceil \cdot b_s + b_r \Longrightarrow M \approx \left\lceil \frac{b_s b_r}{T-b_r} \right\rceil + 2$$

$$b_{r_1} = \left\lceil \frac{51105}{27} \right\rceil = 1893; b_{r_2} = \left\lceil \frac{320251}{25} \right\rceil = 12811$$

TASK

Pieņemsim, ka ir divas relācijas r_1 un r_2 ar atbilstošiem atribūtiem $r_1(A,B)$ un $r_2(B,C,D,E).$ Relācijā r_1 ir 75435 raksti, relācijai r_2 ir 11456raksti. Pieņemsim, ka vienā blokā ietilpst22relācijas r_1 raksti un 35 relācijas r_2 raksti. Pieņemsim, ka ir pie
ejami ${\bf 5}$ atmiņas bloki konkrētā algoritma izpildei. Viena bloka pārraidei no diska nepieciešamas 0.001 ms, bloka meklēšanai – 0.1 ms. Uzrakstīt aprēķina formulas un savus pieņēmumus, kā arī aprēķināt skaitliski, cik minimāli laika (ms) nepieciešams, lai izrēķinātu $r_1 \bowtie r_2$, izmantojot $\mathit{block\ join}$ un nested-loop join. Neņemiet vērā laiku, ko prasa gala rezultāta ierakstīšana diskā un neņemt vērā procesora laiku, kas patērēts šai operācijai. Ņemt vērā tikai bloku meklēšanas un lasīšanas laikus.

$$\begin{split} |r_1| &= 75435; |r_2| = 11456 \\ b_{r_1} &= 22; b_{r_2} = 35 \\ B &= 5; T_{\rm disk} = 0.001; T_{\rm seek} = 0.1 \end{split}$$

BLOCK IOIN METHOD

1. Apply formulas for block transfers and seeks.

NESTED-LOOP JOIN METHOD

1. Apply the formula for block transfers and 2 seeks (only 2).