

Correlation and Causation

Professor Widom's Instructional Odyssey
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Correlation and Causation

Analyzing data with two (or more) measures X and Y

- Height and shoe size
- Grades and entrance exam scores
- Education level and starting salary
- Temperature and cold drink sales

➤ **Correlation (informal):** The values of X and Y tend to be interdependent

➤ **Causation (informal):** X's value tends to influence Y's value

Why Do We Care?

- Discoveries in the medical domain
 - Patients with problem X also tend to have problem Y
 - Taking drug X tends to make symptom Y subside
- Discoveries in the political domain
 - Voters who approve of X tend to also approve of Y
 - Voter turnout is weather-dependent
- Discoveries in the advertising domain
 - Larger fonts tend to result in more click-throughs
 - More online purchases are made in the evening

Which are correlation and which are causation?

Categorical versus Numeric Values

- **Categorical values:** unordered categories
 - color, weather, major
- **Numeric values:** ordered values
 - height, price, time, age, exam score
 - May be discrete or continuous
- **Ordinal values:** categories that can be ordered
 - movie rating, letter grade, education level
 - But differences may not be on a meaningful scale

Assume ordered for now

Positive Correlation

Two measures X and Y

When X is higher Y tends to be higher

When X is lower Y tends to be lower

When Y is higher X tends to be higher

When Y is lower X tends to be lower

Examples

X = height, Y = shoe size

X = grades, Y = entrance exam scores

Notation (mine): $X \approx Y$

Positive Correlation by Causation

Two measures X and Y

X being higher causes Y to be higher

X being lower causes Y to be lower

Examples

X = education, Y = starting salary

X = temperature, Y = cold drink sales

Notation (mine): $X \rightarrow Y$

Correlation due to Hidden Causation

Correlation can be the result of causation from a hidden “confounding variable”

$A \approx B$ because there's a hidden C such that
 $C \rightarrow A$ and $C \rightarrow B$

Homeless population \approx crime rate

Confounding variable: unemployment

Forgetfulness \approx poor eyesight

Confounding variable: age

Negative Correlation by Causation

Two measures X and Y

X being higher causes Y to be lower

X being lower causes Y to be higher

Examples

X = latitude, Y = temperature

X = car weight, Y = gas mileage

X = class absences, Y = final grade

Negative Correlation without Causation

Two measures X and Y

When X is higher Y tends to be lower

When X is lower Y tends to be higher

When Y is higher X tends to be lower

When Y is lower X tends to be higher

Examples

X = cold drink sales, Y = hot tea sales

X = years of schooling, Y = years in jail

Confounding variables?

Is There Such a Thing as Pure Correlation?

Correlation without causation: usually a confounding variable lurking somewhere

X = height, Y = shoe size

X = grades, Y = entrance exam scores

What about the “surprising correlations”?

Bottom Line

- 1) Want to know when things are correlated
- 2) But should not assume one causes the other
“Correlation does not imply causation”

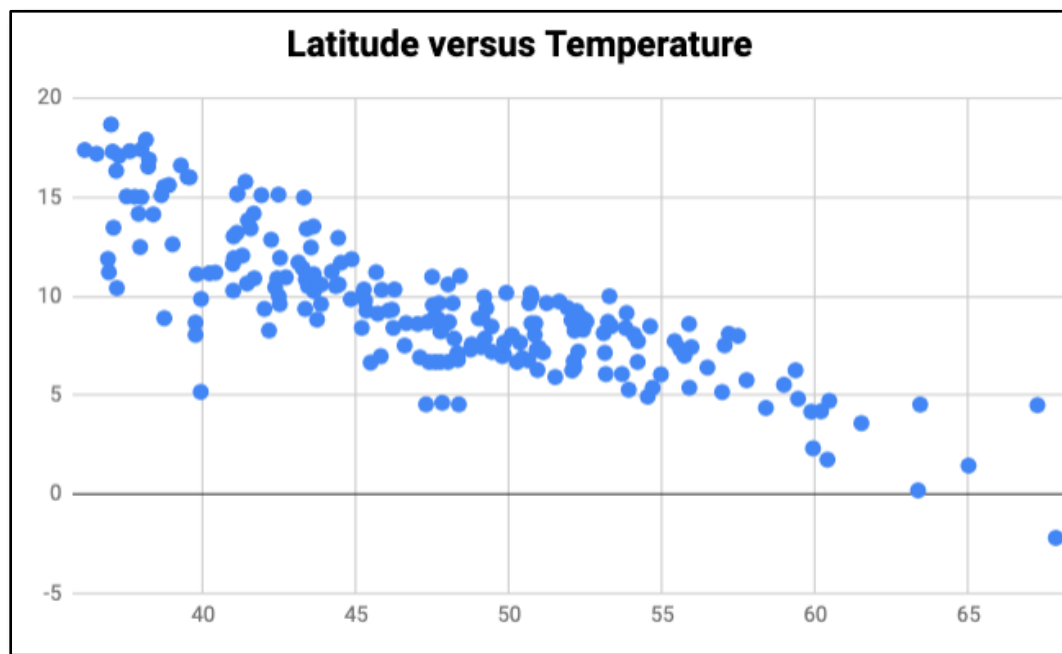
Next:

- Determining correlation
- Determining if there's causation



Determining Correlation

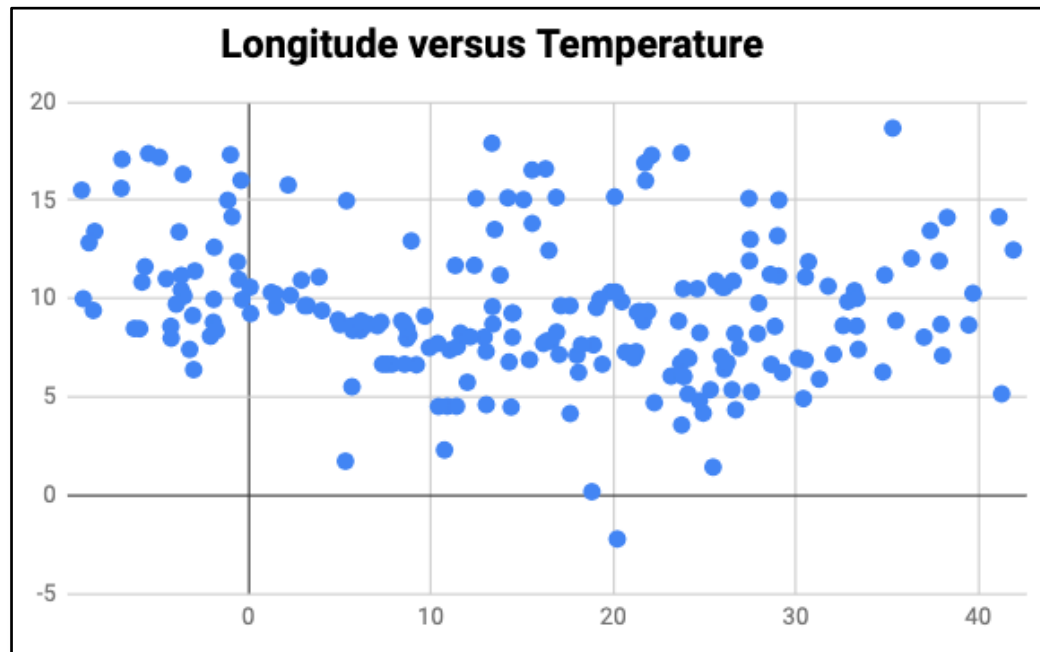
X and Y both ordered: scatterplot, r-values



Significant negative correlation, $r = -0.82$

Determining Correlation

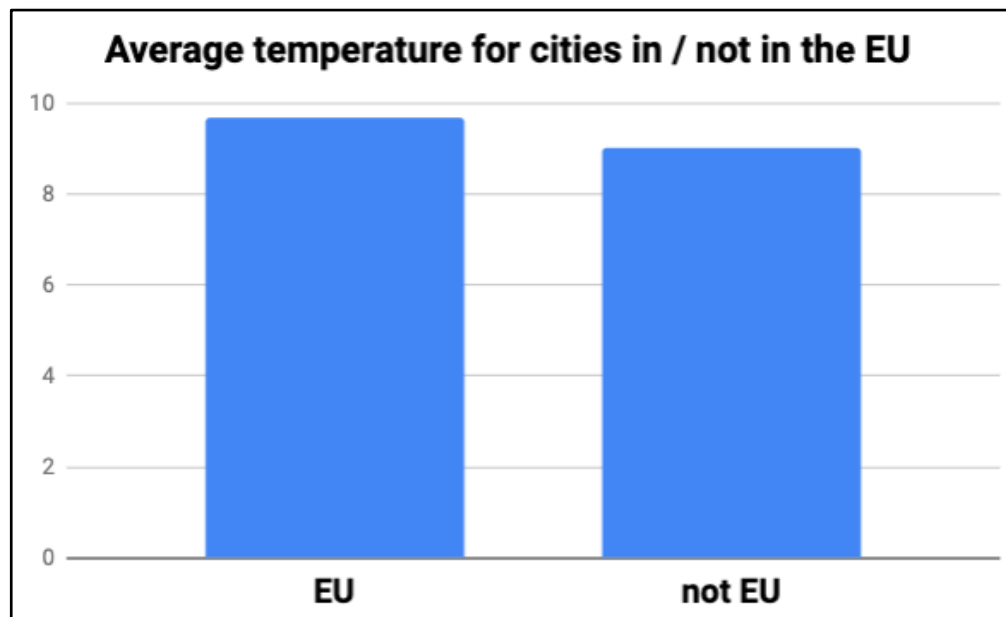
X and Y both ordered: scatterplot, r-values



Little correlation, $r = -0.17$

Determining Correlation

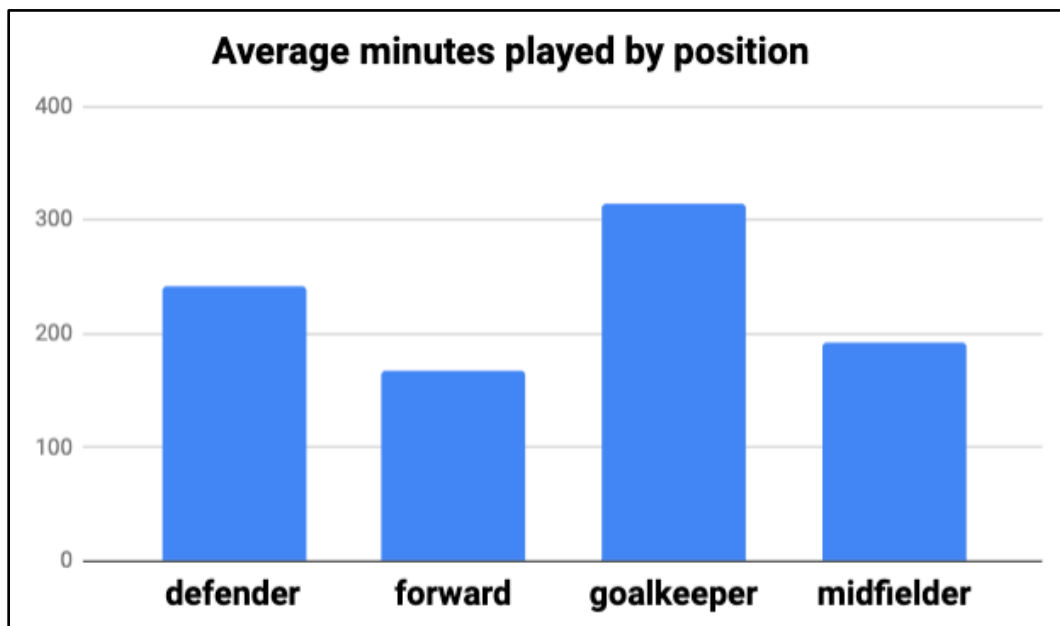
X categorical, Y ordered: bar graph



Similar averages → little correlation

Determining Correlation

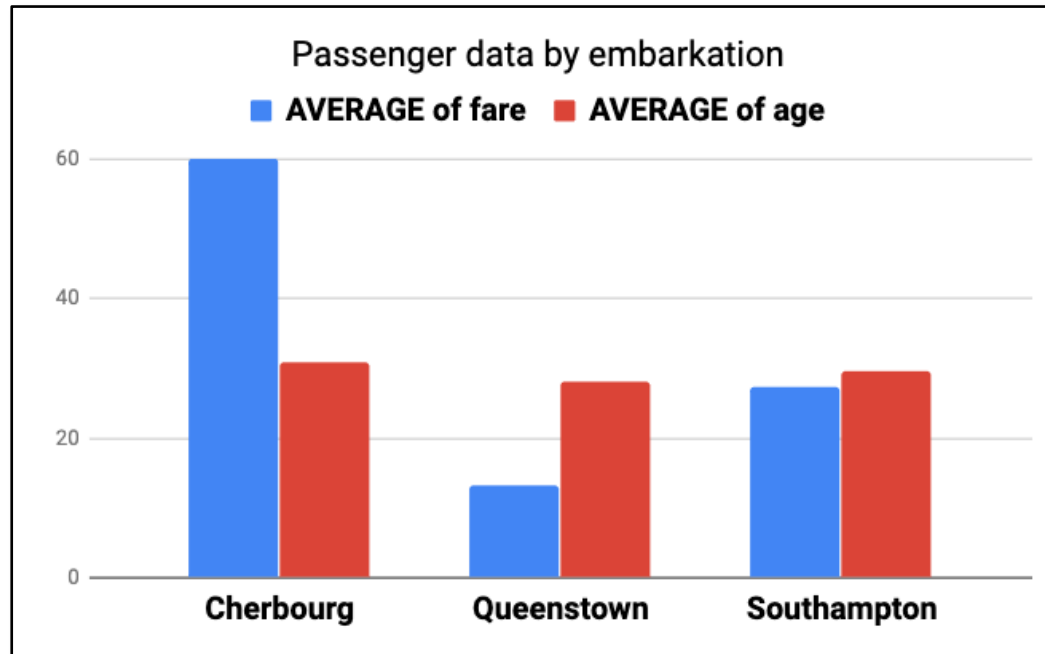
X categorical, Y ordered: bar graph



Different averages → correlation

Determining Correlation

X categorical, Y ordered: bar graph



Different averages → correlation
Similar averages → little correlation

Determining Correlation

X and Y both categorical: table

	EU	Not EU
Cold	12	5
Cool	63	29
Warm	44	18
Hot	31	11

(Ignore that temperature category is ordinal)

Without correlation expect similarly divided values

Determining Correlation

X and Y both categorical: table

	EU	% of row	Not EU	% of row
Cold	12	71%	5	29%
Cool	63	68%	29	32%
Warm	31	74%	11	26%
Hot	44	71%	18	29%

Without correlation expect similarly divided values

Determining Correlation

X and Y both categorical: table

	EU	% of row	Not EU	% of row
Cold	12	71%	5	29%
Cool	63	68%	29	32%
Warm	31	74%	11	26%
Hot	44	71%	18	29%

If % of row is similar in each of the columns, values are **uncorrelated**

If % of row varies significantly in any of the columns, values are **correlated**

Determining Correlation

X and Y both categorical: table

	EU	% of column	Not EU	% of column
Cold	12	8%	5	8%
Cool	63	42%	29	46%
Warm	31	21%	11	17%
Hot	44	29%	18	29%

If % of *column* is similar in each of the *rows*, values are **uncorrelated**

If % of *column* varies significantly in any of the *rows*, values are **correlated**

Your Turn

Are Position and Passes-per-Minute correlated?
(for purpose of exercise treat ppm as categories)

	Low ppm	Med ppm	High ppm
Defender	94	46	48
Midfielder	79	44	105
Forward	116	15	12

Your Turn

Are Position and Passes-per-Minute correlated?

	Low ppm	% of row	% of col	Med ppm	% of row	% of col	High ppm	% of row	% of col
Defender	94			46			48		
Midfielder	79			44			105		
Forward	116			15			12		

If % of row/column are similar in each of the columns/rows, values are uncorrelated

If % of row/column vary significantly in any of columns/rows, values are correlated

Your Turn Extra (Titanic)

Are Class and Survival correlated?

	Died	Survived
First class	80	136
Second class	97	87
Third class	372	119

Your Turn Extra (Titanic)

Are Class and Survival correlated?

	Died	% of row	% of col	Survived	% of row	% of col
First class	80			136		
Second class	97			87		
Third class	372			119		

If % of row/column are similar in each of the columns/rows, values are uncorrelated

If % of row/column vary significantly in any of columns/rows, values are correlated

Your Turn Extra #2 (Titanic)

Are Age-group and Gender correlated?

	Female	Male
Children	108	182
Adults	152	286
Seniors	54	109

Your Turn Extra #2 (Titanic)

Are Age-group and Gender correlated?

	Female	% of row	% of col	Male	% of row	% of col
Children	108			182		
Adults	152			286		
Seniors	54			109		

If % of row/column are similar in each of the columns/rows, values are uncorrelated

If % of row/column vary significantly in any of columns/rows, values are correlated

Determining Causation

Typically not possible based on data analysis alone

- 1) “Hill’s Criteria”
- 2) Run experiments



Hill's Criteria (slightly adapted)

Strength - of correlation between X and Y

Consistency - of correlation across different datasets

Specificity - no other likely explanation for correlation

Temporality - Y occurs after X

Plausibility - there's a reason for causation

Coherence - consistent with related theories

Experimental Validation

To determine if $X \rightarrow Y$

- Create “experimental group” with X =value
- Create “control group” with different X values
- *Ensure no other distinctions between two groups*
- See if experimental vs. control $\approx Y$

Works for things like drug therapy, advertising font size

Less useful for things like weather, crime rate, forgetfulness

Historical Example

Smoking and Lung Cancer, 1950's

- Strong correlation observed between smoking and lung cancer
- Tobacco proponents implicated confounding variables (e.g., pollution, occupation, genetic predisposition)
- Experimental validation not feasible
- Large-scale data analysis (Big Data!) concluded causation, both using Hill's criteria and eliminating proposed confounding variables

Bottom Line

- 1) Can measure when things are correlated
- 2) But should not assume one causes the other
“Correlation does not imply causation”



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